

Lesson Plan
SI Session #13
September 5, 2017

SI Leader: Eason Chang

Course: Math 18

Academic Quarter: Summer Session 2 2017

Instructor: Professor Drimbe

Topics Covered: Basis & Span, Eigenvalues, Eigenvectors



Opener Activity:

5:05pm - 5:10pm

Basis and Span

$$S = \left\{ \begin{pmatrix} 1 \\ 2 \end{pmatrix}, \begin{pmatrix} 0 \\ 1 \end{pmatrix}, \begin{pmatrix} 2 \\ -1 \end{pmatrix} \right\}.$$

Then $\text{span}(S) = \mathbb{R}^2$. (**Exercise**). In fact, any two of the elements of S span \mathbb{R}^2 . (**Exercise**). So we can throw out any one of them, for example, the second one, obtaining the set

$$\widehat{S} = \left\{ \begin{pmatrix} 1 \\ 2 \end{pmatrix}, \begin{pmatrix} 2 \\ -1 \end{pmatrix} \right\}.$$

And this smaller set \widehat{S} also spans \mathbb{R}^2 . (There are two other possibilities for subsets of S that also span \mathbb{R}^2 .) But we can't discard an element of \widehat{S} and still span \mathbb{R}^2 with the remaining one vector.

(Why not? Suppose we discard the second vector of \widehat{S} , leaving us with the set

$$\widetilde{S} = \left\{ \begin{pmatrix} 1 \\ 2 \end{pmatrix} \right\}.$$

Now $\text{span}(\widetilde{S})$ consists of all scalar multiples of this single vector (a line through $\mathbf{0}$). But anything not on this line, for instance the vector

$$\mathbf{v} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

is not in the span. So \widetilde{S} does not span \mathbb{R}^2 .)

Activity 1

5:10pm - 5:30pm

Practice problem 1a:

3. (a) If a 4 x 5 matrix A has rank 2, find $\text{dimRow}(A)$.

(b) If a 5 x 6 matrix A has rank 3, find $\text{Rank } A^T$.

(c) If A is a 7 x 9 matrix, what is the largest possible rank of A ?

Solutions for Practice Problem 1a:

- a) 2
- b) 3
- c) 7

Practice Problem 1b:

2. Find a basis for Row A , Nul A and for Col A , where

$$A = \begin{bmatrix} 1 & 0 & -1 \\ 2 & 1 & -1 \\ 1 & 1 & 2 \end{bmatrix}.$$

Practice Problem 1b Solutions:

$$\text{Nul } A = \{0\}$$

$$\text{Col } A = \{ (1,2,1), (0,1,1), (-1,-1,2) \}$$

$$\text{Row } A = \{ (1,0,0), (0,1,0), (0,0,1) \}$$

$$\text{Rank } A = 3$$

Activity 2

5:30pm - 5:45pm

Practice Problem 2a:

1. Consider the matrices $A = \begin{bmatrix} 2 & 3 & -1 \\ 1 & 1 & 0 \\ 1 & -3 & 1 \end{bmatrix}$ and $B = \begin{bmatrix} 1 & 0 & -1 \\ 1 & 2 & 0 \\ 1 & -1 & -1 \end{bmatrix}$.

(a) Find $\det A$ and $\det B$.

(b) Find $\det A^{-1}$ and $\det A^2 B$.

(c) Is $A^3 B^3$ invertible?

Solution to Practice Problem 2a:

a)

$$\text{Det } A = 3$$

$$\text{Det } B = 1$$

b)

$$\text{Det } A^{-1} = 1/3$$

c)

$$\text{Det } A^2 B = 9$$

c)

$$\det A^3 B^3 = 27$$

Closure- Survey/ Feedback

5:45pm- 5:50pm

- Wrap-up:

- Please share with the group one thing you gained understanding of through the session today.

- Make a note to yourself/ write down anything you need to review/ do more practice problems on.

- Survey/ Feedback:

1. How fun was the session? (1-10)

2. How useful was the session? (1-10)

3. Would you come back? (yes or no)

4. Optional: Comments (pace of the activity), questions, concerns, suggestions, feedback on the back or wherever

Please recommend SI to your friends/ peers if you found the session useful! Thanks for coming and have a great day :)

PLANNING THE SI SESSION

SI Leader:

Session Date & Day of Week:

Course:

Course Instructor:

Warm-up/ Opening: (2-4 min.)	Content to cover:	Collaborative Learning Technique	Strategy to be used:

Please provide a **DETAILED BREAKDOWN** of warm-up activity **OR** attach corresponding document(s)

Cool-down/ Closing: (2-4 min.)	Content to cover:	Collaborative Learning Technique	Strategy to be used:

Please provide a **DETAILED BREAKDOWN** of cool-down activity **OR** attach corresponding document(s)

Workout: (44-46 min.)	Content to cover:	Collaborative Learning Technique(s)	Strategy(ies) to be used:

Please provide a **DETAILED BREAKDOWN** of workout activity **OR** attach corresponding document(s)