Supplementary Material: Catastrophes, connectivity, and Allee effects in the design of marine reserve networks

Easton R. White, 1,2* Marissa L. Baskett, 2,3, Alan Hastings 2,3,4

¹Department of Biology, University of Vermont, Burlington, VT, USA ²Center for Population Biology, University of California, Davis, CA, USA, ³Department of Environmental Science and Policy, University of California, Davis, CA, USA ⁴Santa Fe Institute, Sante Fe, NM, USA

*To whom correspondence should be addressed: E-mail: eastonrwhite@gmail.com

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Data and code for all the figures and tables can be found at (https://github.com/eastonwhite/MPA-disturbances). All the analyses were run in R.

Appendix S1 n-patch model description

To extend the model described in the main manuscript to an n-patch scenario, we use the Beverton-Holt structure within each patch and model spatially-explicit dispersal (i.e. resulting connectivity between patches) and disturbances. We focus on a coastline system (a simple one-dimensional landscape) where d_{ij} is the distance between patches i and j. We use geometric decay for the dispersal kernel, with a dispersal shape parameter δ , where increasing δ decreases dispersal. The probability of dispersal is then

$$P(\text{dispersal from patch i to patch j}) = \text{Geometric}(\delta, d_{ij}).$$
 (S1)

For disturbances, we model the probability of disturbance, M_i , in each patch as a binomial process with probability p_i :

$$M_i(t) \sim \text{Binomial}(1, p_i).$$
 (S2)

The spatial extent of the disturbance is a stochastic process giving the disturbance size (x), which affects patches near the disturbance. If a disturbance in patch i is larger than the distance between patches i and j, d_{ij} , then patch j will also be affected by the disturbance:

$$P(\text{disturbance in patch j} \mid \text{disturbance in patch i}) = \begin{cases} 1 & \text{if } d_{ij} < x \\ 0 & \text{if otherwise.} \end{cases}$$
 (S3)

With this n-patch model, we can relax the assumption of a "scorched earth" between patches by setting the fishing rate in non-reserves to be F < 1. This allows us to study the effect of fishing pressure outside reserves on the effectiveness of the marine reserve network.

Appendix S2 Additional figures

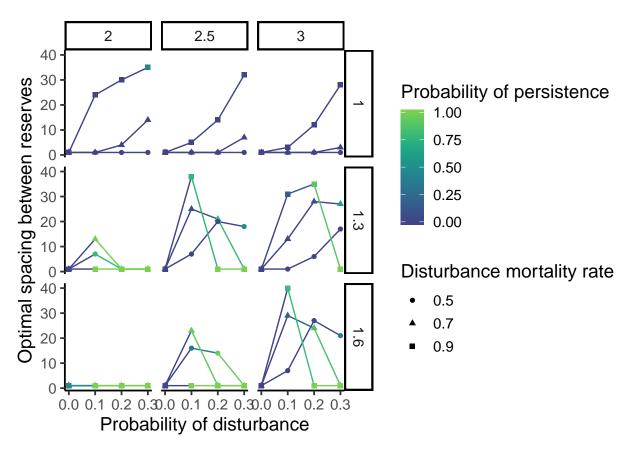


Figure S1: Optimal spacing for varying Allee and r values along with different disturbance parameters.

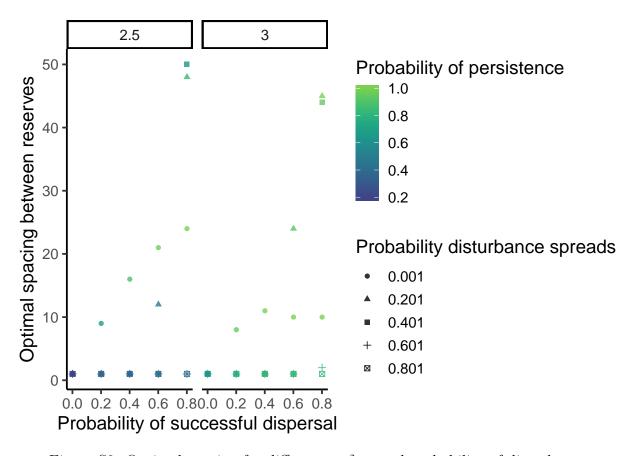


Figure S2: Optimal spacing for different $\gamma,\,\delta,\,{\bf r},$ and probability of disturbance.

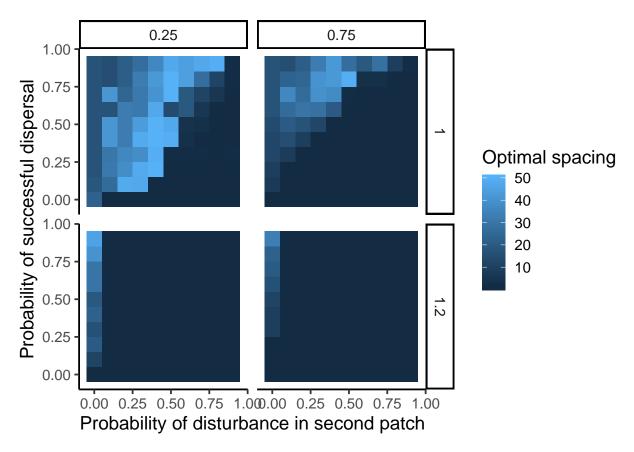


Figure S3: Optimal spacing for all the dispersal parameters and the probability of disturbance.

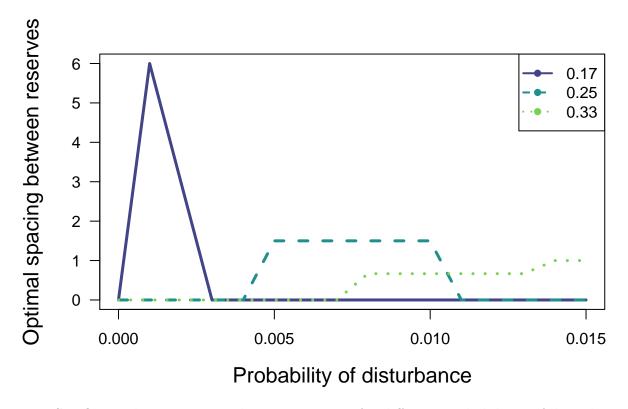


Figure S4: Optimal mean spacing between reserves for different probabilities of disturbance and fraction of coasline in reserves. The specific parameters used here include: $\delta = 0.7$, $\omega = 1.2$, r = 3, and $\mu = 0.9$.