



iBRAIN

Deep Hyperalignment

Muhammad Yousefnezhad, Daoqiang Zhang

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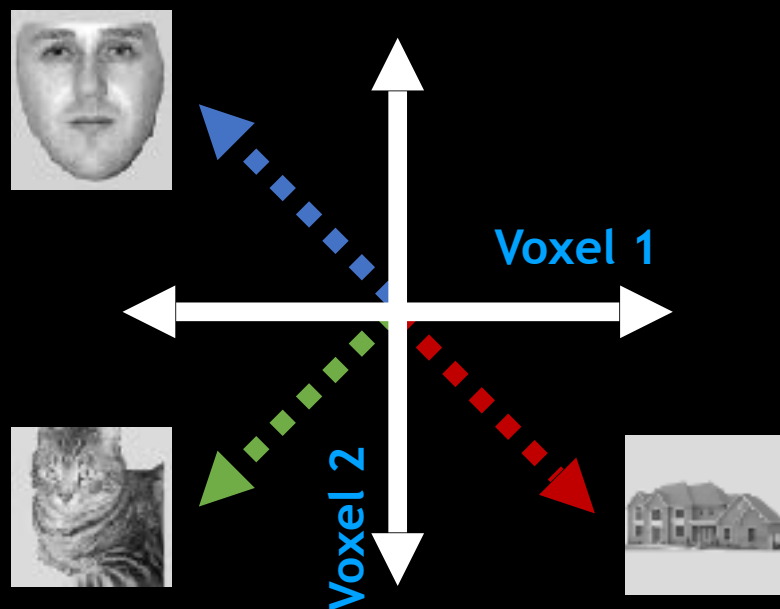
Dec 2017

Hyperalignment

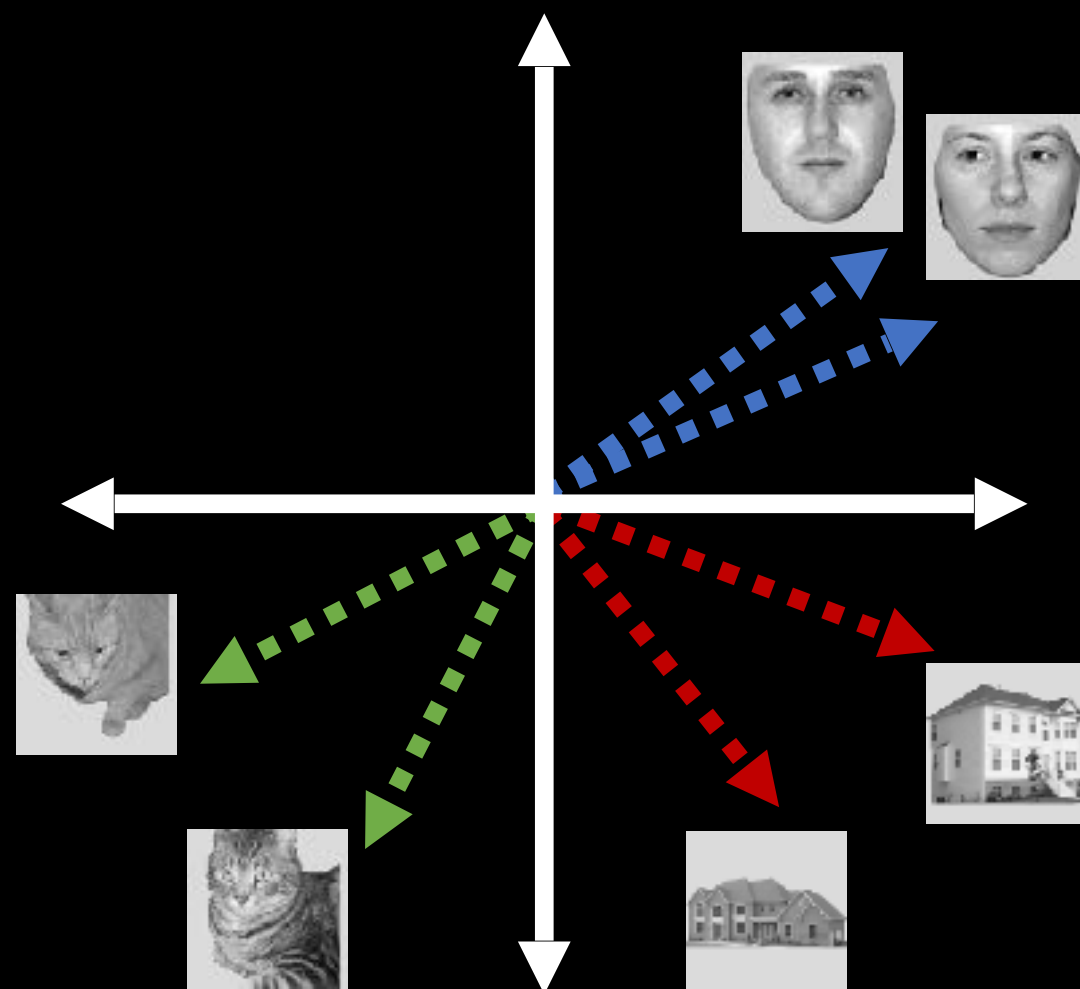
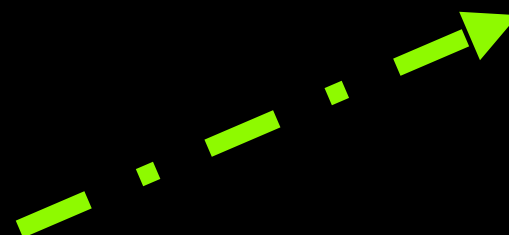
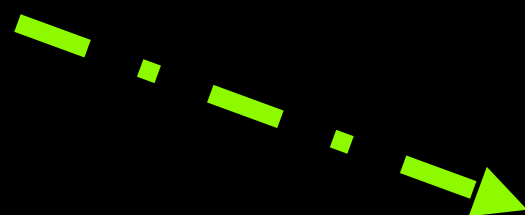
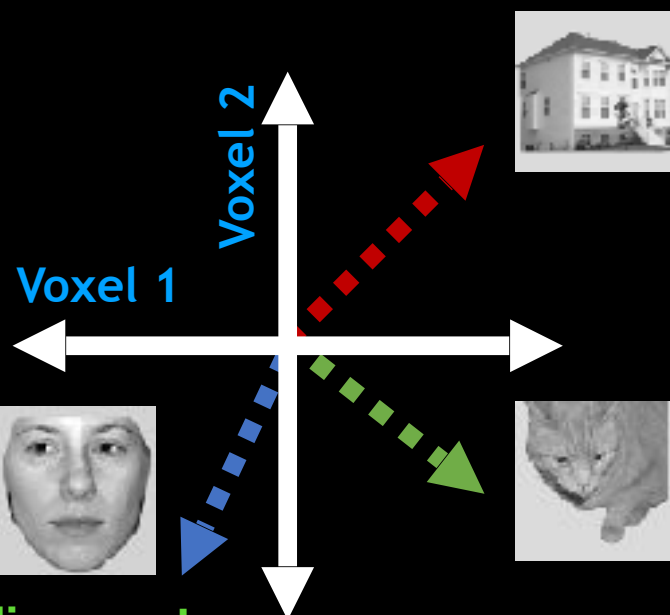
Individual Brain Patterns

Common Space (G)

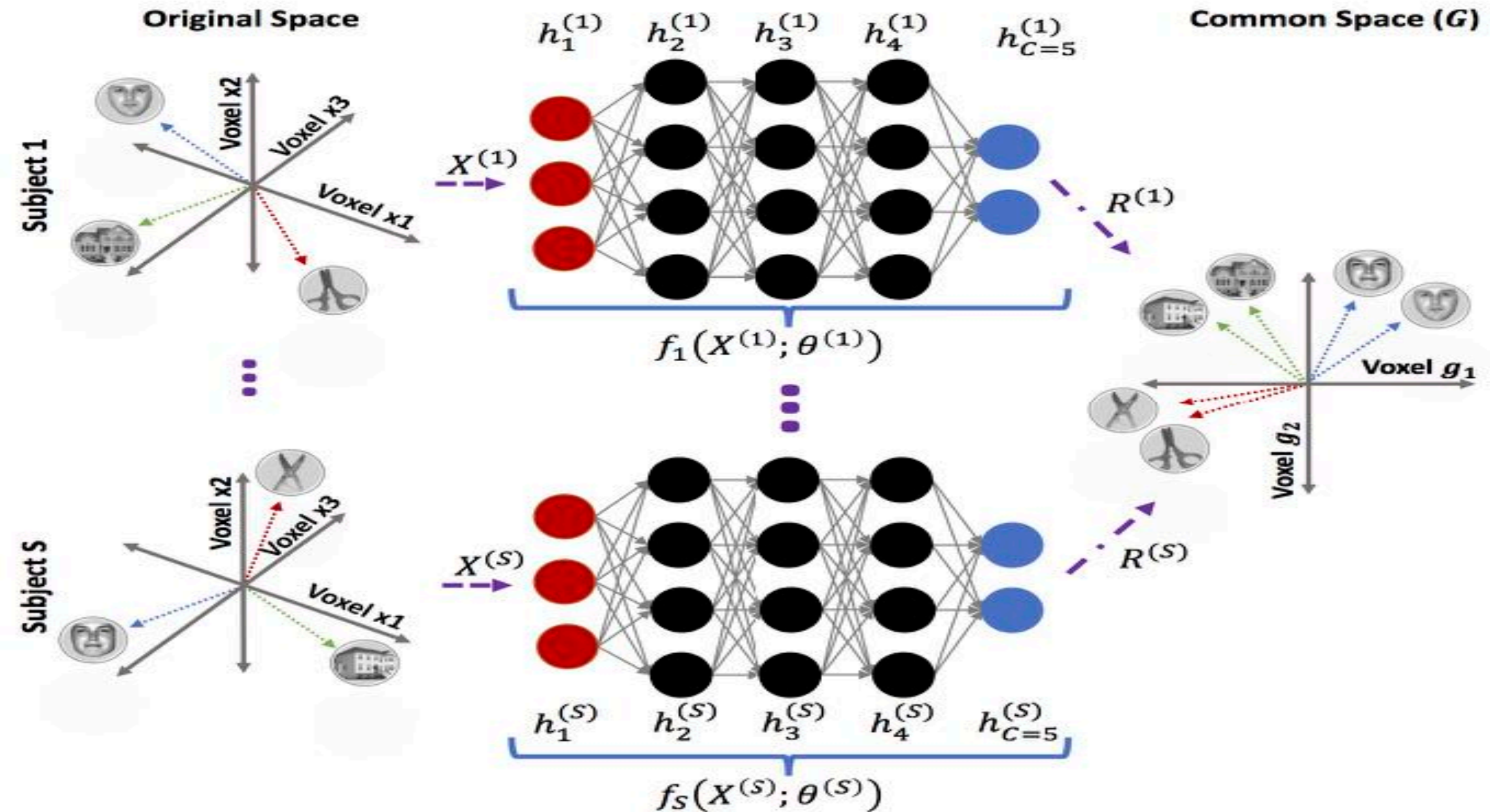
Subject 1



Subject S



Main Idea



DHA: Objective Function

★ We want to optimize following function:

$$\min_{\mathbf{G}, \mathbf{R}^{(i)}, \theta^{(i)}} \sum_{i=1}^S \left\| \mathbf{G} - f_i(\mathbf{X}^{(i)}; \theta^{(i)}) \mathbf{R}^{(i)} \right\|_F^2 \quad \text{s.t.} \quad \mathbf{G}^\top \mathbf{G} = \mathbf{I}$$

$$\mathbf{G} = \frac{1}{S} \sum_{j=1}^S f_j(\mathbf{X}^{(j)}; \theta^{(j)}) \mathbf{R}^{(j)}$$

where the deep network is defined as follows:

$$f_\ell(\mathbf{X}^{(\ell)}; \theta^{(\ell)}) = \text{mat}\left(\mathbf{h}_C^{(\ell)}, T, V_{new}\right)$$

$$\mathbf{h}_m^{(\ell)} = \mathbf{g}\left(\mathbf{W}_m^{(\ell)} \mathbf{h}_{m-1}^{(\ell)} + \mathbf{b}_m^{(\ell)}\right), \quad \text{where} \quad \mathbf{h}_1^{(\ell)} = \text{vec}(\mathbf{X}^{(\ell)}) \quad \text{and} \quad m = 2:C$$

DHA: Optimization

★ *rank-m SVD*

$$f_{\ell}(\mathbf{X}^{(\ell)}; \theta^{(\ell)}) \stackrel{SVD}{=} \mathbf{\Omega}^{(\ell)} \mathbf{\Sigma}^{(\ell)} (\mathbf{\Psi}^{(\ell)})^{\top}, \quad \ell = 1:S$$

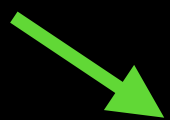
★ *Projection Matrix*

$$\begin{aligned} \mathbf{P}^{(\ell)} &= f_{\ell}(\mathbf{X}^{(\ell)}; \theta^{(\ell)}) \left(\left(f_{\ell}(\mathbf{X}^{(\ell)}; \theta^{(\ell)}) \right)^{\top} f_{\ell}(\mathbf{X}^{(\ell)}; \theta^{(\ell)}) + \epsilon \mathbf{I} \right)^{-1} \left(f_{\ell}(\mathbf{X}^{(\ell)}; \theta^{(\ell)}) \right)^{\top} \\ &= \mathbf{\Omega}^{(\ell)} (\mathbf{\Sigma}^{(\ell)})^{\top} \left(\mathbf{\Sigma}^{(\ell)} (\mathbf{\Sigma}^{(\ell)})^{\top} + \epsilon \mathbf{I} \right)^{-1} \mathbf{\Sigma}^{(\ell)} (\mathbf{\Omega}^{(\ell)})^{\top} = \mathbf{\Omega}^{(\ell)} \mathbf{D}^{(\ell)} \left(\mathbf{\Omega}^{(\ell)} \mathbf{D}^{(\ell)} \right)^{\top} \end{aligned}$$

where $\mathbf{D}^{(\ell)} (\mathbf{D}^{(\ell)})^{\top} = (\mathbf{\Sigma}^{(\ell)})^{\top} \left(\mathbf{\Sigma}^{(\ell)} (\mathbf{\Sigma}^{(\ell)})^{\top} + \epsilon \mathbf{I} \right)^{-1} \mathbf{\Sigma}^{(\ell)}.$

★ *Sum of Projection Matrices*

$$\mathbf{A} = \sum_{i=1}^S \mathbf{P}^{(i)} = \widetilde{\mathbf{A}} \widetilde{\mathbf{A}}^{\top}, \quad \text{where} \quad \widetilde{\mathbf{A}} \in \mathbb{R}^{T \times mS} = [\mathbf{\Omega}^{(1)} \mathbf{D}^{(1)} \dots \mathbf{\Omega}^{(S)} \mathbf{D}^{(S)}].$$



Cholesky Decomposition

DHA: Optimization

★ *Objective Function can be reformulated as follows:*

$$\min_{\mathbf{G}, \mathbf{R}^{(i)}, \theta^{(i)}} \sum_{i=1}^S \left\| \mathbf{G} - f_i(\mathbf{X}^{(i)}; \theta^{(i)}) \mathbf{R}^{(i)} \right\| \equiv \max_{\mathbf{G}} \left(\text{tr}(\mathbf{G}^\top \mathbf{A} \mathbf{G}) \right).$$

★ *So, we have:*

$$\mathbf{A} \mathbf{G} = \mathbf{G} \mathbf{\Lambda}, \text{ where } \mathbf{\Lambda} = \{\lambda_1 \dots \lambda_T\}$$

$$\widetilde{\mathbf{A}} = \mathbf{G} \widetilde{\mathbf{\Sigma}} \widetilde{\mathbf{\Psi}}^\top \longrightarrow \text{Incremental PCA}$$

★ *DHA mappings can be calculated as follows:*

$$\mathbf{R}^{(\ell)} = \left(\left(f_\ell(\mathbf{X}^{(\ell)}; \theta^{(\ell)}) \right)^\top f_\ell(\mathbf{X}^{(\ell)}; \theta^{(\ell)}) + \epsilon \mathbf{I} \right)^{-1} \left(f_\ell(\mathbf{X}^{(\ell)}; \theta^{(\ell)}) \right)^\top \mathbf{G}.$$

DHA: Optimization

- ★ *In order to use back-propagation algorithm for seeking an optimized parameters for the deep network, we also have:*

$$\frac{\partial \mathbf{Z}}{\partial f_{\ell}(\mathbf{X}^{(\ell)}; \theta^{(\ell)})} = 2\mathbf{R}^{(\ell)}\mathbf{G}^{\top} - 2\mathbf{R}^{(\ell)}(\mathbf{R}^{(\ell)})^{\top} \left(f_{\ell}(\mathbf{X}^{(\ell)}; \theta^{(\ell)}) \right)^{\top}.$$

where

$$\mathbf{Z} = \sum_{\ell=1}^T \lambda_{\ell}$$

Datasets

Table S2: The datasets.

Title	ID	S	K	T	V	X	Y	Z	Scanner	TR	TE
Mixed-gambles task	DS005	48	2	240	450	53	63	52	S 3T	2	30
Visual Object Recognition	DS105	71	8	121	1963	79	95	79	G 3T	2.5	30
Word and Object Processing	DS107	98	4	164	932	53	63	52	S 3T	2	28
Auditory and Visual Oddball	DS116	102	2	170	2532	53	63	40	P 3T	2	25
Multi-subject, multi-modal	DS117	171	2	210	524	64	61	33	S 3T	2	30
Forrest Gump	DS113	20	10	451	2400	160	160	36	S 7T	2.3	22
Raiders of the Lost Ark	N/A	10	7	924	980	78	78	54	S 3T	3	30

S is the number of subject; K denotes the number of stimulus categories; T is the number of scans in unites of TRs (Time of Repetition); V denotes the number of voxels in ROI; X, Y, Z are the size of 3D images; Scanners include S=Siemens, G = General Electric, and P = Philips in 3 Tesla or 7 Tesla; TR is Time of Repetition in millisecond; TE denotes Echo Time in second; Please see *openfmri.org* for more information.

Simple Tasks Analysis

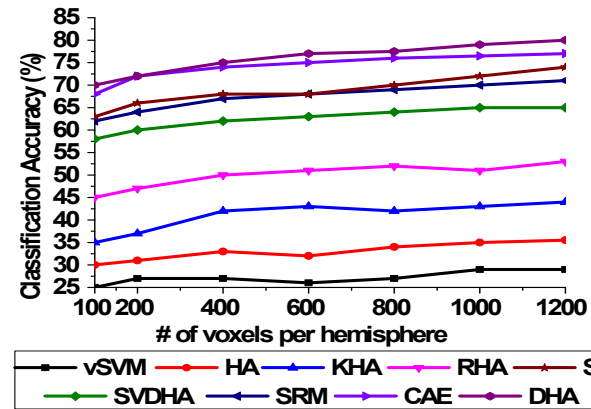
Table 1: Accuracy of HA methods in post-alignment classification by using simple task datasets

↓Algorithms, Datasets→	DS005	DS105	DS107	DS116	DS117
ν -SVM [17]	71.65±0.97	22.89±1.02	38.84±0.82	67.26±1.99	73.32±1.67
HA [1]	81.27±0.59	30.03±0.87	43.01±0.56	74.23±1.40	77.93±0.29
RHA [2]	83.06±0.36	32.62±0.52	46.82±0.37	78.71±0.76	84.22±0.44
KHA [3]	85.29±0.49	37.14±0.91	52.69±0.69	78.03±0.89	83.32±0.41
SVD-HA [4]	90.82±1.23	40.21±0.83	59.54±0.99	81.56±0.54	95.62±0.83
SRM [5]	91.26±0.34	48.77±0.94	64.11±0.37	83.31±0.73	95.01±0.64
SL [9]	90.21±0.61	49.86±0.4	64.07±0.98	82.32±0.28	94.96±0.24
CAE [6]	94.25±0.76	54.52±0.80	72.16±0.43	91.49±0.67	95.92±0.67
DHA	97.92±0.82	60.39±0.68	73.05±0.63	90.28±0.71	97.99±0.94

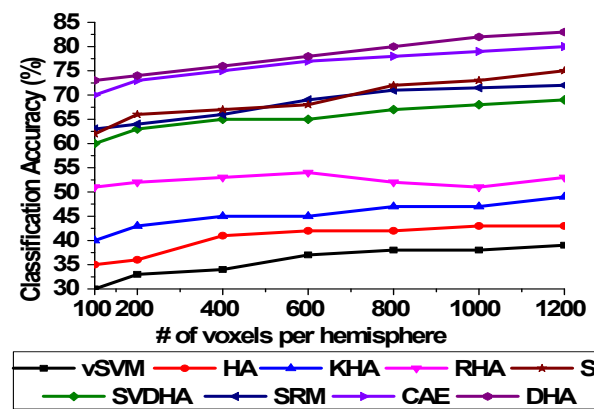
Table 2: Area under the ROC curve (AUC) of different HA methods in post-alignment classification by using simple task datasets

↓Algorithms, Datasets→	DS005	DS105	DS107	DS116	DS117
ν -SVM [17]	68.37±1.01	21.76±0.91	36.84±1.45	62.49±1.34	70.17±0.59
HA [1]	70.32±0.92	28.91±1.03	40.21±0.33	70.67±0.97	76.14±0.49
RHA [2]	82.22±0.42	30.35±0.39	43.63±0.61	76.34±0.45	81.54±0.92
KHA [3]	80.91±0.21	36.23±0.57	50.41±0.92	75.28±0.94	80.92±0.28
SVD-HA [4]	88.54±0.71	37.61±0.62	57.54±0.31	78.66±0.82	92.14±0.42
SRM [5]	90.23±0.74	44.48±0.75	62.41±0.72	79.20±0.98	93.65±0.93
SL [9]	89.79±0.25	47.32±0.92	61.84±0.32	80.63±0.81	93.26±0.72
CAE [6]	91.24±0.61	52.16±0.63	72.33±0.79	87.53±0.72	91.49±0.33
DHA	96.91±0.82	59.57±0.32	70.23±0.92	89.93±0.24	96.13±0.32

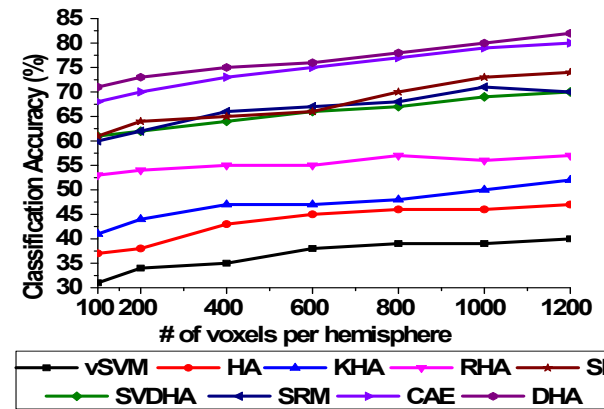
Complex Tasks Analysis



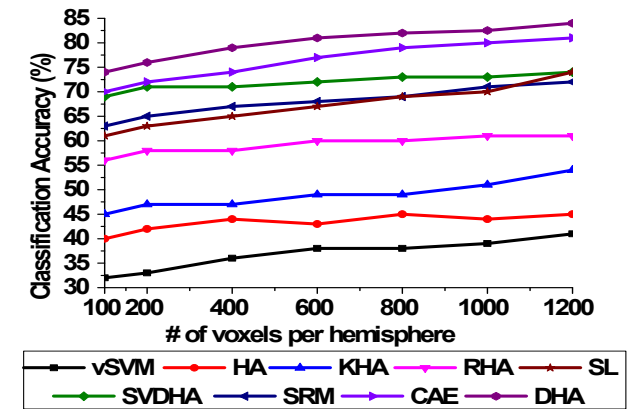
(a) Forrest Gump
(TRs = 100)



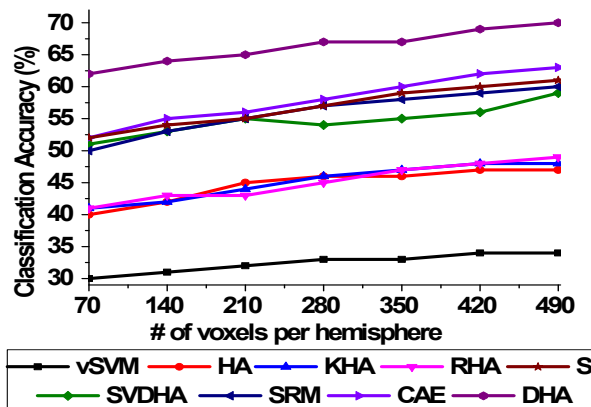
(b) Forrest Gump
(TRs = 400)



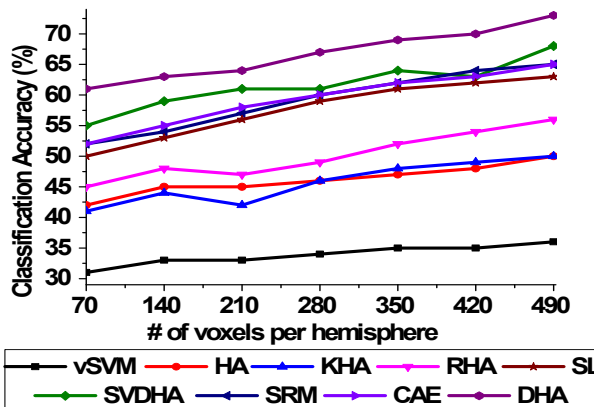
(c) Forrest Gump
(TRs = 800)



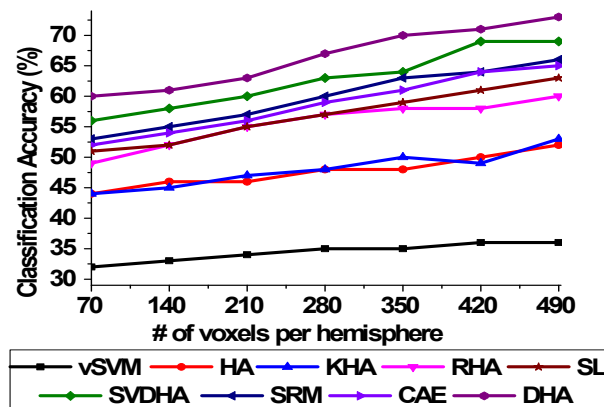
(d) Forrest Gump
(TRs = 2000)



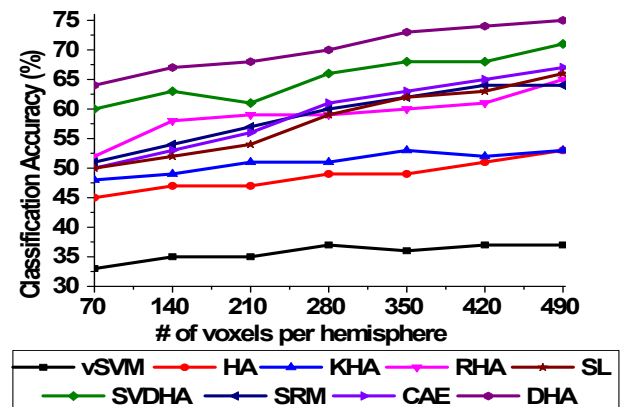
(e) Raiders
(TRs = 100)



(f) Raiders
(TRs = 400)



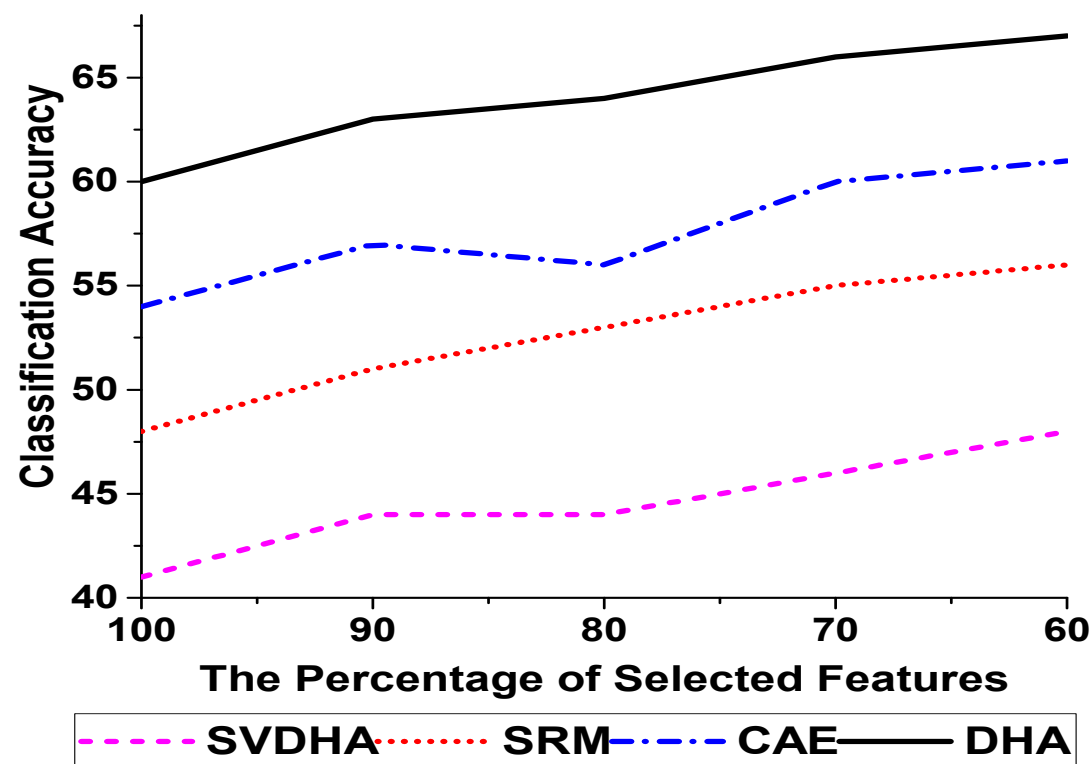
(g) Raiders
(TRs = 800)



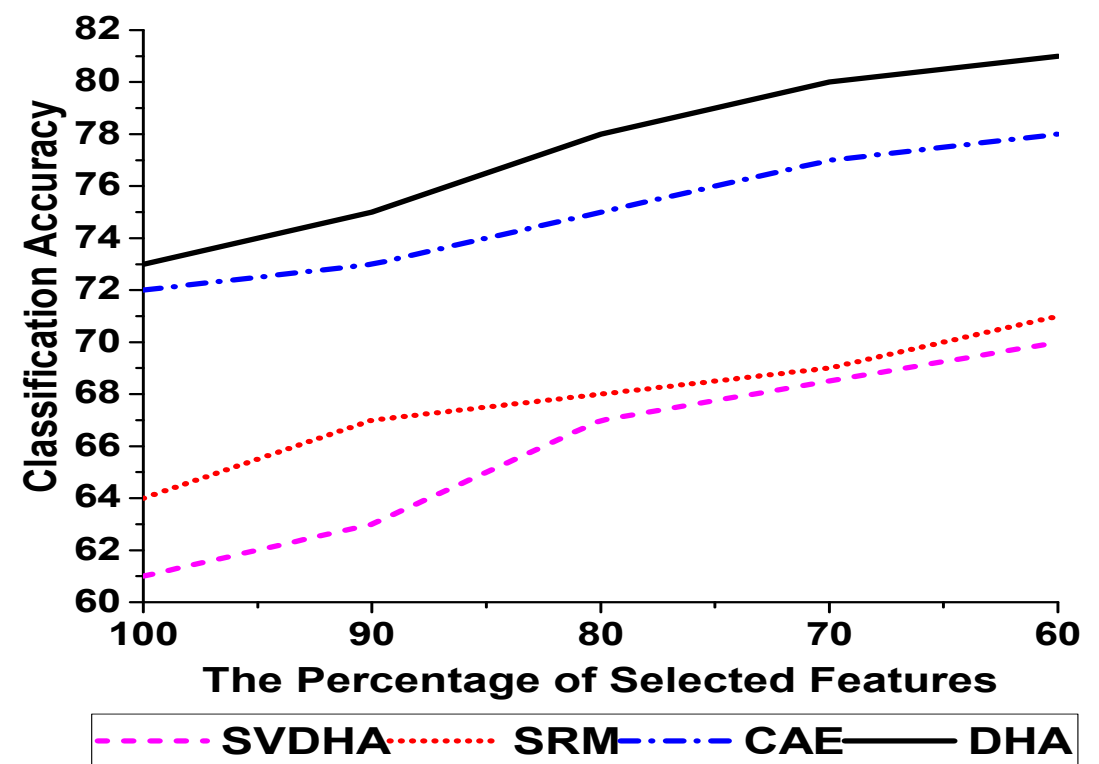
(h) Raiders
(TRs = 2000)

Figure 1: Comparison of different HA algorithms on complex task datasets by using ranked voxels.

Classification analysis by using feature selection

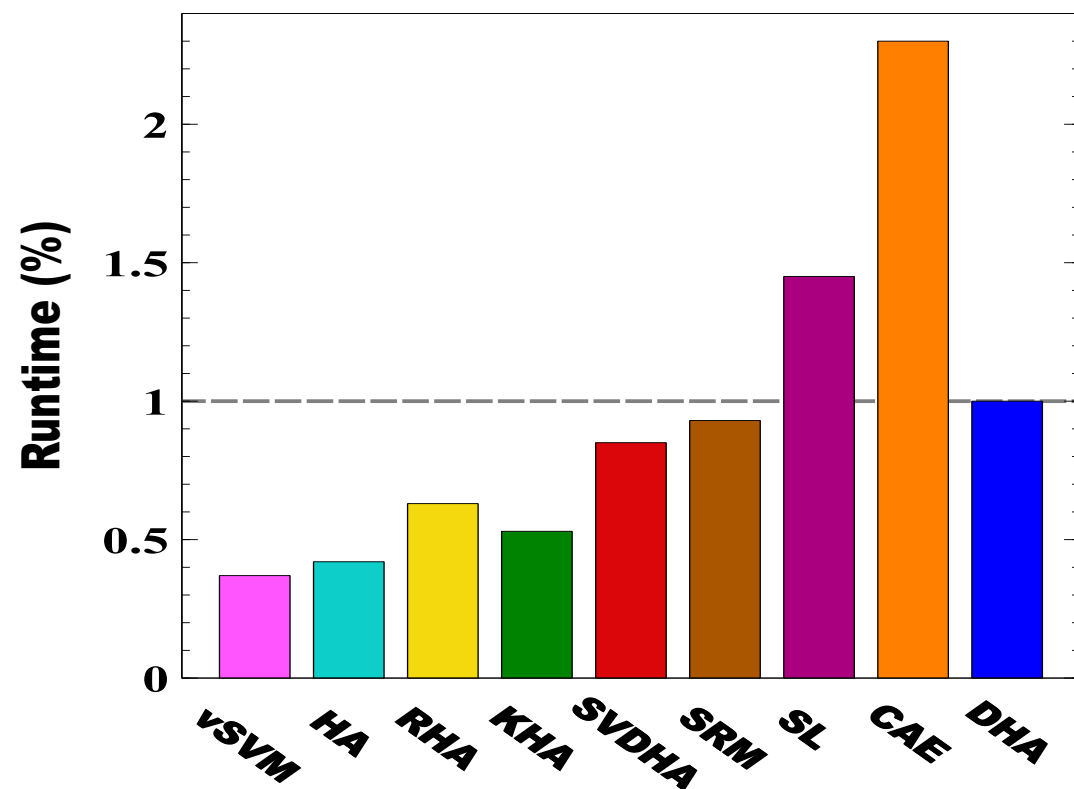


(A) DS105

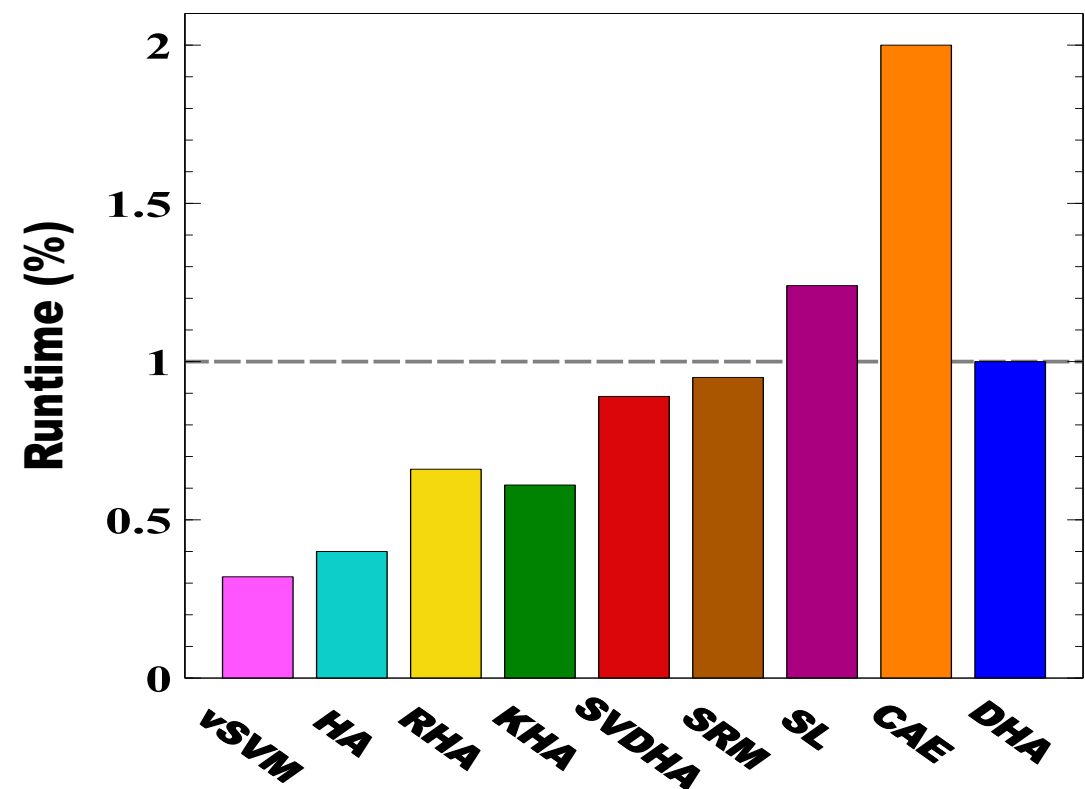


(B) DS107

Runtime Analysis



(A) DS105



(B) DS107

Future Works

- ★ This paper extended a **deep approach** for **hyperalignment** methods in order to provide accurate functional alignment in multi-subject fMRI analysis.
- ★ Deep Hyperalignment (DHA) can handle fMRI datasets with **nonlinearity**, **high-dimensionality (broad ROI)**, and **a large number of subjects**. Further, its **time complexity** fairly scales with data size and the **training data is not referenced** when DHA computes the functional alignment for a new subject.
- ★ In the future, we will plan to employ DHA for improving the performance of other techniques in fMRI analysis, e.g. **Representational Similarity Analysis (RSA)**.

Thank You!

Q & A

For more details, contact:

myousefnezhad@nuaa.edu.cn

myousefnezhad@outlook.com

dqzhang@nuaa.edu.cn

<http://ibrain.nuaa.edu.cn>

<https://myousefnezhad.github.io/>