

# Damm algorithm

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In error detection, the **Damm algorithm** is a check digit algorithm that detects all single-digit errors and all adjacent transposition errors. It was presented by H. Michael Damm in 2004.<sup>[1]</sup>

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## Strengths and weaknesses

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### Strengths

The Damm algorithm is similar to the Verhoeff algorithm. It too will detect *all* occurrences of the two most frequently appearing types of transcription errors, namely altering one single digit, and transposing two adjacent digits (including the transposition of the trailing check digit and the preceding digit).<sup>[1][2]</sup> But the Damm algorithm has the benefit that it makes do without the dedicatedly constructed permutations and its position specific powers being inherent in the Verhoeff scheme. Furthermore, a table of inverses can be dispensed with provided all main diagonal entries of the operation table are zero.

The Damm algorithm does not suffer from exceeding the number of 10 possible values, resulting in the need for using a non-digit character (as the X in the 10-digit ISBN check digit scheme).

Prepending leading zeros does not affect the check digit.<sup>[1]</sup>

There are totally anti-symmetric quasigroups that detect all phonetic errors associated with the English language (13 ↔ 30, 14 ↔ 40, ..., 19 ↔ 90). The table used in the illustrating example is based on an instance of such kind.

## Weaknesses

Since prepending leading zeros does not affect the check digit,<sup>[1]</sup> variable length codes should not be verified together since, e.g., 0, 01, and 001, etc. produce the same check digit. However, all checksum algorithms are vulnerable to this.

## Design

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Its essential part is a quasigroup of order 10 (i.e. having a  $10 \times 10$  Latin square as the body of its operation table) with the special feature of being weakly totally anti-symmetric.<sup>[3][4][i][ii][iii]</sup> Damm revealed several methods to create totally anti-symmetric quasigroups of order 10 and gave some examples in his doctoral dissertation.<sup>[3][i]</sup> With this, Damm also disproved an old conjecture that totally anti-symmetric quasigroups of order 10 do not exist.<sup>[5]</sup>

A quasigroup  $(Q, *)$  is called totally anti-symmetric if for all  $c, x, y \in Q$ , the following implications hold:<sup>[4]</sup>

1.  $(c * x) * y = (c * y) * x \Rightarrow x = y$
2.  $x * y = y * x \Rightarrow x = y$ ,

and it is called weak totally anti-symmetric if only the first implication holds. Damm proved that the existence of a totally anti-symmetric quasigroup of order  $n$  is equivalent to the existence of a weak totally anti-symmetric quasigroup of order  $n$ . For the Damm algorithm with the check equation  $(\dots((0 * x_m) * x_{m-1}) * \dots) * x_0 = 0$  a weak totally anti-symmetric quasigroup with the property  $x * x = 0$  is needed. Such a quasigroup can be constructed from any totally anti-symmetric quasigroup by rearranging the columns in such a way that all zeros lay on the diagonal. And, on the other hand, from any weak totally anti-symmetric quasigroup a totally anti-symmetric quasigroup can be constructed by rearranging the columns in such a way that the first row is in natural order.<sup>[3]</sup>

## Algorithm

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The validity of a digit sequence containing a check digit is defined over a quasigroup. A quasigroup table ready for use can be taken from Damm's dissertation (pages 98, 106, 111).<sup>[3]</sup> It is useful if each main diagonal entry is 0,<sup>[1]</sup> because it simplifies the check digit calculation.

### Validating a number against the included check digit

1. Set up an interim digit and initialize it to 0.
2. Process the number digit by digit: Use the number's digit as column index and the interim digit as row index, take the table entry and replace the interim digit with it.
3. The number is valid if and only if the resulting interim digit has the value of 0.<sup>[1]</sup>

### Calculating the check digit

**Prerequisite:** The main diagonal entries of the table are 0.

1. Set up an interim digit and initialize it to 0.

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2. Process the number digit by digit: Use the number's digit as column index and the interim digit as row index, take the table entry and replace the interim digit with it.

3. The resulting interim digit gives the check digit and will be appended as trailing digit to the number.<sup>[1]</sup>

## Example

The following operation table will be used.<sup>[1]</sup> It may be obtained from the totally anti-symmetric quasigroup  $x * y$  in Damm's doctoral dissertation page 111<sup>[3]</sup> by rearranging the rows and changing the entries with the permutation  $\varphi = (1\ 2\ 9\ 5\ 4\ 8\ 6\ 7\ 3)$  and defining  $x \cdot y = \varphi^{-1}(\varphi(x) * y)$ .

.	0	1	2	3	4	5	6	7	8	9
0	0	3	1	7	5	9	8	6	4	2
1	7	0	9	2	1	5	4	8	6	3
2	4	2	0	6	8	7	1	3	5	9
3	1	7	5	0	9	8	3	4	2	6
4	6	1	2	3	0	4	5	9	7	8
5	3	6	7	4	2	0	9	5	8	1
6	5	8	6	9	7	2	0	1	3	4
7	8	9	4	5	3	6	2	0	1	7
8	9	4	3	8	6	1	7	2	0	5
9	2	5	8	1	4	3	6	7	9	0

Suppose we choose the number (digit sequence) **572**.

### Calculating the check digit

digit to be processed → column index	5	7	2
old interim digit → row index	0	9	7
table entry → new interim digit	9	7	4

The resulting interim digit is **4**. This is the calculated check digit. We append it to the number and obtain **5724**.

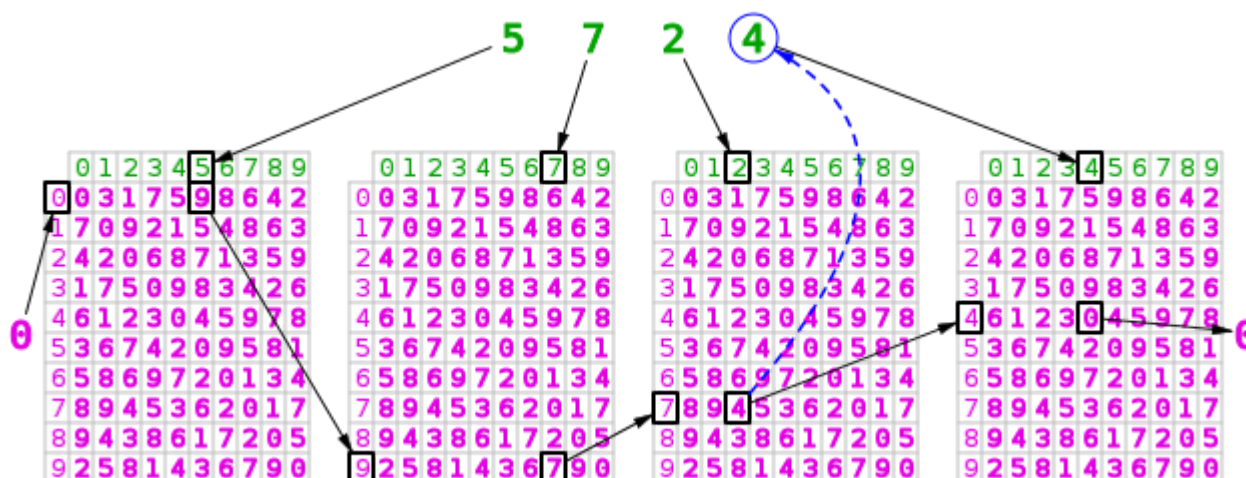
### Validating a number against the included check digit

digit to be processed → column index	5	7	2	4
old interim digit → row index	0	9	7	4
table entry → new interim digit	9	7	4	0

The resulting interim digit is **0**, hence the number is **valid**.

### Graphical illustration

This is the above example showing the detail of the algorithm generating the check digit (broken blue arrow) and verifying the number **572** with the check digit.



## References

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2. For the types of common errors and their frequencies, see Salomon, David (2005). *Coding for Data and Computer Communications* (<https://books.google.com/books?id=Zr9bjEpXKnIC&pg=PA36>). Springer Science+Business Media, Inc. p. 36. ISBN 978-0387-21245-6.
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4. Damm, H. Michael (2007). "Totally anti-symmetric quasigroups for all orders  $n \neq 2, 6$ " (<https://doi.org/10.1016%2Fj.disc.2006.05.033>). *Discrete Mathematics*. **307** (6): 715–729. doi:10.1016/j.disc.2006.05.033 (<https://doi.org/10.1016%2Fj.disc.2006.05.033>). ISSN 0012-365X (<https://www.worldcat.org/issn/0012-365X>).
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- ii. Chen Jiannan (2009). "The NP-completeness of Completing Partial anti-symmetric Latin squares" (<http://www.academpublisher.com/proc/iwisa09/papers/iwisa09p322.pdf>) (PDF). *Proceedings of 2009 International Workshop on Information Security and Application (IWISA 2009)* (<http://www.academpublisher.com/proc/iwisa09/>). Academy Publisher. pp. 322–324 (<http://www.academpublisher.com/proc/iwisa09/papers/iwisa09p322.htm>). ISBN 978-952-5726-06-0. See page 324.
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*Contributions, Sec. Math. Tech. Sci., MANU/MASA. XXX (1–2): 75–93. ISSN 0351-3246 (<https://www.worldcat.org/issn/0351-3246>). See page 78.*

## External links

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- [Damm validation & generation code in several programming languages](#)
  - [Practical application in Singapore \(http://blog.cantab-ip.com/blog/2014/01/20/new-format-for-singapore-ip-application-numbers-at-ipos/\)](http://blog.cantab-ip.com/blog/2014/01/20/new-format-for-singapore-ip-application-numbers-at-ipos/)
  - [Quasigroups for the Damm algorithm up to order 64 \(http://www.md-software.de/math/DAMM\\_Quasigruppen.txt\)](http://www.md-software.de/math/DAMM_Quasigruppen.txt)
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