

modelbased: An R package to make the most out of your statistical models through marginal means, marginal effects, and model predictions

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Statement of need

Applied statistics have historically focused on statistical tests (e.g., t tests, correlation tests, and analyses of variances, ANOVAs), seen as most apt to provide researchers with interpretable answers to the questions they seek. However, these tests typically rely on statistical models—the true underlying cornerstone of modern data science. The replication crisis (Camerer et al., 2018; Open Science Collaboration, 2015) and methodological revolutions (Makowski & Waggoner, 2023) have underlined some of the issues with the traditional focus on statistical tests (e.g., the effacement of model assumptions, a focus on null-hypothesis testing, non-compatibility with more complex variance structures) and called for shifting the focus to the models themselves.

In line with these efforts, new tools have been created to facilitate the direct usage and reporting of statistical models. For instance, the easystats collection of R packages (Lüdecke et al., 2023) has been developed to help researchers "tame, discipline, and harness" the power of statistical models. Existing packages are dedicated to model parameters (the parameters package, Lüdecke et al., 2020), predictive performance (the performance package, Lüdecke et al., 2021) or effect importance (the effectsize package, Ben-Shachar et al., 2020).

But the models themselves hide even more critical information!

The fundamental nature of these models—a statistical link between an outcome y and predictor variables X—enables the generation of predictions for any combination of predictors, observed or unobserved alike. These predictions refer to expected values of the outcome for given levels of predictors of interest, as well as contrasting them, making it possible to visualize the model's behaviour in a more meaningful and comprehensive way, and answering a broad range of research questions.

The two most popular R packages for extracting these quantities of interest from statistical models are emmeans (Lenth, 2024) and marginaleffects (Arel-Bundock et al., 2024). These packages pack an enormously rich set of features and cover (almost) all imaginable needs for post-hoc analysis of statistical models. However, their power and flexibility come at a cost: ease of use—especially for users not familiar with the underlying statistical concepts. The modelbased package, built on top of these two packages, aims to unleash this vast, untapped potential by providing a unified interface to extract marginal means, marginal effects, contrasts, comparisons, and model predictions from a wide range of

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statistical models. In line with the easystats' raison d'être, the modelbased package focuses on simplicity, flexibility, and user-friendliness to help researchers harness the full power of their models.

Key concepts

Answering research questions based on statistical models means describing the relationship between predictors (also called *focal* predictors) of interest and the outcome, as well as differences between observed groups in the sample. There are four key concepts in modelbased to achieve this:

- **Predictions:** Estimate the outcome for a specific combination of predictor values (which may or may not exist in the data).
- Marginal Means: Estimate the average outcome across the observed distribution of other predictors, representing a "typical" observation.
- Marginal Effects: Quantify the strength of a predictor's effect on the outcome (the average slope), which is especially useful when slopes vary (e.g., with interactions or in logistic regression).
- Contrasts: Compare predicted outcomes between groups or levels of a predictor.

Predictions

At a fundamental level, modelbased and similar packages leverage model predictions. These predictions can be of different types, depending on the model and the question at hand. For instance, predictions can be associated with confidence intervals (predict = "expectation") or prediction intervals (predict = "prediction"). The former corresponds to the uncertainty around the "relationship" (i.e., the conditional estimate, typically of the expectation (E[X]) according to a model's parameters), while the latter is typically larger and provides information about the range which individual observations might take. Moreover, for generalized linear models (GLMs), predictions can be made on the response scale (predict = "response") or the link scale (predict = "link"). This corresponds for instance to predictions in terms of probability (response scale) or log odds (link scale) for logistic regression models.

These different types of estimates can be obtained for observations in the original dataset—which is useful to assess the model's goodness-of-fit—or for new data (typically a "data grid")—which is useful for visualization.

For convenience, the modelbased package includes four related functions, which mostly differ in their default arguments for data and predict¹:

- estimate_prediction(): original data, prediction intervals.
- estimate expectation(): original data, confidence intervals.
- estimate_relation(): data grid, predictions on the response scale.
- estimate_link(): data grid, predictions on the link scale.

Marginal means

The concept of "marginal" in this context refers to how non-focal variables are treated. While predictions, as described above, fix non-focal variables at their reference level, marginal means compute the empirical or theoretical averages of them. These kind of predictions are a good representation of the sample, because they are not based on very

¹These functions can become redundant if the defaults are changed. For instance, estimate_relation(..., predict = "link") matches estimate_link(...).



specific characteristics. E.g., predictions are made for *female* persons with *high* income, while marginal means calculate the expected outcome for an *average* observation.

The modelbased package provides a simple and clear interface to extract marginal means via the estimate_means() function, which can be considered as "marginal" pendant to estimate_relation(). estimate_means() typically returns results in line with the emmeans package. Focal predictors are specified in the by argument.

Marginal effects

Predictions and marginal means can be used to better understand the *relationship* of predictors with the outcome. They tell you that "the average health score for a person at the age of sixty is 80 points". Marginal *effects*, in turn, evaluate the (average) *strength* of an effect (also called "slope"), telling you that "the average effect of age on the health score is an decrease 5 points".

For the simple case of linear regression without interaction terms, the regression coefficient (slope) equals the marginal effect. However, in even slightly more complex situations (e.g., when interaction terms are involved, or logistic regression models), the slope is not constant across the predictor's values. Here we can estimate an *average* slope, or marginal effect.

Again, the modelbased package has a simple function to do so, estimate_slopes(). This function calculates the *trend* or average effect, usually for numeric predictors. The trend argument specifies the focal predictors, while by allows for further grouping.

Contrasts

Contrast analysis, or pairwise comparison, of estimated marginal means allows for direct statistical comparison of the predicted outcomes across different groups or levels of a focal predictor. Rather than simply observing differences in marginal means, contrast analysis quantifies these differences and assesses their statistical significance, which also involves determining the associated uncertainty (e.g., confidence intervals).

In modelbased, this is achieved using the estimate_contrasts() function. Focal predictors are specified in the contrast argument. For further stratification or grouping, use the by argument.

Interpretation

The interpretation of predicted outcome values requires careful consideration of whether they are derived from *predictions* or *marginal means*, despite both originating from the same underlying model and data. The modelbased package facilitates the estimation of several distinct prediction quantities, broadly categorized as *data grid-based* and *empirical*.

Data grid-based predictions

The estimate_relation() and estimate_means() functions utilize a balanced data grid, representing all combinations of focal predictor levels. These functions emphasize the *predictors themselves*, enabling the analysis of associations and comparisons of specific characteristics. estimate_relation() provides predictions for a *specific* observation, while estimate_means() represents a *typical* observation from the sample.

Empirical predictions

When the focus is on the *predicted outcome*, it is more appropriate to consider the empirical distribution of focal predictor characteristics rather than a balanced data grid. This can be achieved by changing the estimate argument within estimate_means(). Setting



estimate = "average" calculates the average expected outcome from those observations
from the sample defined by the focal predictors.

For analyses emphasizing outcome differences between groups (e.g., when computing contrasts) and particularly when causal effects are being considered, it may be beneficial to model a hypothetical population not directly represented in the sample. This approach, known as G-computation (Chatton & Rohrer, 2024), is implemented by setting estimate = "population" within $estimate_means()$. This option is also available for the $estimate_contrasts()$ function.

Technical details

The algorithmic heavy lifting is done by modelbased's two back-end packages, emmeans and marginaleffects (the default), which can be set as a global option (e.g., with options(modelbased_backend = "emmeans")).

Of the two, emmeans (Lenth, 2024) is the more senior package and was originally known as lsmeans (for "Least-Squares Means"). This term has been historically used to describe what are now more commonly referred to as "Estimated Marginal Means" or EMMs: predictions made over a regular grid—a grid typically constructed from all possible combinations of the categorical predictors in the model and the mean of numerical predictors. The package was renamed in 2016 to emmeans to clarify its extension beyond least-squares estimation and its support of a wider range of models (e.g., Bayesian models).

Within emmeans, estimates are generated as a linear function of the model's coefficients, with standard errors (SEs) produced in a similar manner by taking a linear combination of the coefficients' variance-covariance matrix. For example if b is a vector of 4 coefficients, and V is a 4-by-4 matrix of the coefficients' variance-covariance, we can get an estimate and SE for a linear combination (or set of linear combinations) L like so:

$$\hat{b} = L \cdot b$$

$$SE_{\hat{b}} = \sqrt{\mathrm{diag}(L \cdot V \cdot L^T)}$$

These grid predictions are sometimes averaged over (averaging being a linear operation itself) to produce "marginal" predictions (in the sense of marginalized-over): means. These predictions can then be contrasted using various built-in or custom contrasts weights to obtain meaningful estimates of various effects. Using linear combinations with regular grids often means that results from emmeans directly correspond to a models coefficients (which is a benefit for those who are used to understanding models by examining coefficient tables).

marginaleffects (Arel-Bundock et al., 2024) was more recently introduced, and uses a different approach: various effects are estimated by generating two counter-factual predictions of unit-level observations, and then taking the difference between them (with SEs computed using the delta method, Arel-Bundock et al., 2024). By default, such effects are estimated for every observation in the original model frame. These unit-level effects are typically averaged to obtain average effects (e.g., an Average Treatment Effect, ATE).

Using the delta method affords more flexibility in the specification of the marginal effects to be estimated. For example, while emmeans by default compares predictions from GLMs on the link scale and then transforms the comparison back to something closer to the response scales (e.g., the difference between two log-odds is taken, and then exponentiation to produce odds ratios), marginaleffects by default compares predictions on the response scale directly (e.g., taking the difference between two probabilities). The delta method implemented in marginaleffects uses iterative estimation, making it more



computationally costly relative to the simple matrix multiplication used for estimating linear combinations (though marginaleffects is very efficient).

This means that while emmeans typically produces effects at the mean, marginaleffects typically produces mean effects. Depending on the quantity of interest, model, use of a link function, design balance and weights, these can be nearly identical, or very different.

Note that emmeans can also use the delta method and can use non-regular grids, and marginaleffects can also generate linear predictions at the mean. However, obtaining these requires some deeper knowledge of the relevant packages. This is easier to achieve and more accessible in modelbased, by simply modulating the estimate argument (see section *Interpretation*).

Finally, modelbased leverages the get_datagrid() function from the insight package (Lüdecke et al., 2019) to intuitively generate an appropriate grid of data points for which predictions or effects or slopes will be estimated. Since these packages support a wider range of models—including generalized linear models, mixed models, and Bayesian models—modelbased also inherits the support for such models.

Examples

The iris dataset contains measures in centimeters of three different species of iris flowers (setosa, versicolor, and virginica, Becker et al., 1988). Imagine the following linear model in which we predict those flowers' petal width (Petal.Width) from the interaction between their petal length (Petal.Length) and their Species.

```
library(easystats)
model <- lm(Petal.Width ~ Petal.Length * Species, data = iris)
parameters::parameters(model) |>
    print(select = "minimal")
```

#>	Parameter	I	Coefficient			95% CI	1	p
#>								
#>	(Intercept)	1	-0.05		[-0.47,	0.38]		0.823
#>	Petal Length	-	0.20		[-0.09,	0.49]		0.170
#>	Species [versicolor]	-	-0.04		[-0.66,	0.59]		0.909
#>	Species [virginica]	-	1.18		[0.52,	1.84]		< .001
#>	Petal Length × Species [versicolor]	-	0.13		[-0.18,	0.44]		0.405
#>	Petal Length × Species [virginica]	I	-0.04		[-0.34,	0.26]	I	0.789

#> Uncertainty intervals (equal-tailed) and p-values (two-tailed) computed
#> using a Wald t-distribution approximation.

The model's **parameters** can be challenging to interpret and do not offer us all the insights that this model actually contains.

Visualize relationship

We can start by easily visualizing the relationship between our response variable and our predictors (Figure 1).

```
estimate_relation(model, by = c("Petal.Length", "Species"), length = 100) |>
plot(show_data = TRUE)
```

But what is the average value of Petal. Width for each species?



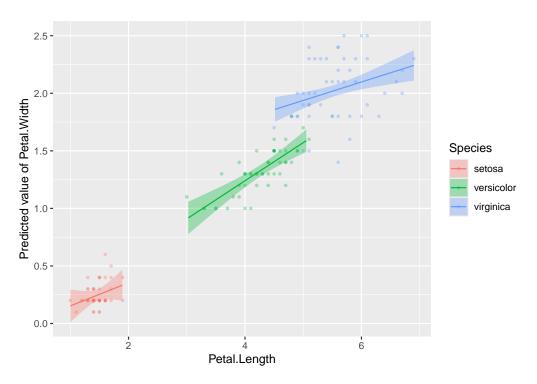


Figure 1: Scatter plot of petal length by pelal width, grouped by species

Marginal Means

The marginal means can be computed, which are the mean predictions for each level of a categorical predictor, *averaged across* all levels of other predictors (Petal.Length in this case).

```
#> Estimated Marginal Means
#>
#> Species | Mean | SE | 95% CI | t(144)
#> ------
#> setosa | 0.71 | 0.34 | [0.04, 1.37] | 2.11
#> versicolor | 1.16 | 0.04 | [1.09, 1.23] | 31.44
#> virginica | 1.74 | 0.09 | [1.57, 1.91] | 20.20
#>
#> Variable predicted: Petal.Width
#> Predictors modulated: Species
#> Predictors averaged: Petal.Length (3.8)

However, are these different species significantly different from each other?
```

Marginal Contrasts

We can estimate all the pairwise contrasts between the levels of the Species factor.



```
#> versicolor | setosa | 0.45 | 0.34 | [-0.22, 1.12] | 1.34 | 0.183
#> virginica | setosa | 1.03 | 0.35 | [ 0.35, 1.72] | 2.97 | 0.003
#> virginica | versicolor | 0.58 | 0.09 | [ 0.39, 0.76] | 6.18 | < .001
#>
#> Variable predicted: Petal.Width
#> Predictors contrasted: Species
#> Predictors averaged: Petal.Length (3.8)
```

#> p-values are uncorrected.

As we can see, the average difference between *versicolor* and *setosa* is not significant.

Marginal Slopes

Similarly, we can compute the marginal effect of Petal.Length (i.e., the "slope") for each species.

This shows that there is a significant positive relationship between Petal.Length and Petal.Width for all species but setosa.

Marginal Contrasts of Slopes

to versicolor.

Finally, we can even compute the contrasts between the slopes of Petal.Length for each species.

```
estimate_contrasts(model, contrast = "Petal.Length", by = "Species")
#> Marginal Contrasts Analysis
#>
#> Level1
                          | Difference |
                                           SE |
                                                        95% CI |
             | Level2
#> versicolor | setosa
                          0.13 | 0.16 | [-0.17, 0.43] | 0.83 | 0.404
                                 -0.04 | 0.15 | [-0.34, 0.26] | -0.27 | 0.789
#> virginica | setosa
                          -0.17 | 0.07 | [-0.31, -0.03] | -2.41 | 0.016
#> virginica | versicolor |
#>
#> Variable predicted: Petal.Width
#> Predictors contrasted: Petal.Length
#> Predictors averaged: Petal.Length (3.8)
```

#> p-values are uncorrected.
The effect of Petal.Length on Petal.Width is significantly stronger in virginica compared

^{, ().} modelbased: An R package to make the most out of your statistical models through marginal means, marginal effects, and model predictions. *Journal of Open Source Software*, (), . https://doi.org/



Conclusion

The modelbased package provides a simple and intuitive interface to extract and visualize important information contained within statistical models.

Declarations

Funding information

This research received no external funding.

Competing Interests

The authors declare no conflict of interest

Availability of data and materials (data transparency)

All data used in this paper uses data included with base R.

Code availability

The modelbased package is available at the official website (https://easystats.github.io/modelbased), on CRAN (https://cran.r-project.org/package=modelbased), and on the R-Universe (https://easystats.r-universe.dev/modelbased). The source code is available on GitHub (https://github.com/easystats/modelbased), and the package can be installed from CRAN with install.packages("modelbased") or from R-Universe with install.packages("modelbased", repos = "https://easystats.r-universe.dev").

Contributions

DM: Writing- Original draft preparation, Writing- Reviewing and Editing, Software. MSB-S, BMW, IP, RT, and DL: Writing- Reviewing and Editing, Software.

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