






Article

Check your outliers! An accessible introduction to identifying statistical outliers in R with *easystats*

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Simple Summary: The *{performance}* package from the *easystats* ecosystem makes it easy to diagnose outliers in R and according to current best practices thanks to the `check_outliers()` function.

Abstract: Beyond the challenge of keeping up-to-date with current best practices regarding the diagnosis and treatment of outliers, an additional difficulty arises concerning the mathematical implementation of the recommended methods. In this paper, we provide an overview of current recommendations and best practices and demonstrate how they can easily and conveniently be implemented in the R statistical computing software, using the *{performance}* package of the *easystats* ecosystem. We cover univariate, multivariate, and model-based statistical outlier detection methods, their recommended threshold, standard output, and plotting method. We conclude with recommendations on the handling of outliers: the different theoretical types of outliers, whether to exclude or winsorize them, and the importance of transparency.

Keywords: univariate outliers; multivariate outliers; robust detection methods; R; *easystats*

1. Introduction

Real-life data often contain observations that can be considered *abnormal* when compared to the main population. The cause of it—be it because they belong to a different distribution (originating from a different generative process) or simply being extreme cases, statistically rare but not impossible—can be hard to assess, and the boundaries of “abnormal” are hard to define.

Nonetheless, the improper handling of these outliers can substantially affect statistical model estimations, biasing effect estimations and weakening the models’ predictive performance. It is thus essential to address this problem in a thoughtful manner. Despite the existence of established recommendations and guidelines, many researchers still do not treat outliers in a consistent manner, or do so using inappropriate strategies [1,2]. Fortunately, guidelines exist in this regard. Yet, especially in the field of psychology, many researchers still do not treat outliers in a consistent manner or do so using inappropriate strategies [1,2].

One possible reason is that researchers are not aware of the existing recommendations, or do not know how to implement them using their analysis software. In this paper, we show how to follow current best practices for automatic and reproducible statistical outlier detection (SOD) using R and the *{performance}* package [3] from the *easystats* ecosystem [4].

2. Identifying Outliers

Although many researchers attempt to identify outliers with measures based on the mean (e.g., z scores), those methods are problematic because the mean and standard deviation themselves are not robust to the influence of outliers and they assume a normal distribution. Therefore, current guidelines recommend using robust methods to identify outliers, such as those relying on the median as opposed to the mean [2,5,6].

Nonetheless, which exact outlier method to use depends on many factors. In some cases, eye-gauging odd observations can be an appropriate solution, though many researchers will favour algorithmic solutions to detect potential outliers, for example, based on a mathematical score.

One of the factor to consider when selecting an algorithmic outlier detection method is the statistical test of interest. When using a regression model, for example, relevant information can be found by identifying observations that do not fit well with the model. This approach, known as model-based outliers detection (as outliers are extracted after the statistical model has been fit), can be contrasted with distribution-based outliers detection, which is based on the distance between an observation and the “center” of its population. Various quantification strategies of this distance exist for the latter, some being univariate (involving only one variable at a time) or multivariate (involving multiple variables).

When no method is readily available to detect model-based outliers, such as for structural equation modelling (SEM), looking for multivariate outliers may be of relevance. For simple tests (t tests or correlations) that compare values of the same variable, it can be appropriate to check for univariate outliers. However, univariate methods can give false positives since t tests and correlations, ultimately, are also models/multivariable statistics. They are in this sense more limited, but we show them nonetheless for educational purposes.

Importantly, whatever approach researchers choose remains a subjective decision, which usage (and rationale) must be transparently documented and reproducible [5]. Researchers should commit (ideally in a preregistration) to an outlier treatment method before collecting the data. They should report in the paper their decisions and details of their methods, as well as any deviation from their original plan. These transparency practices can help reduce false positives due to excessive researchers’ degrees of freedom (i.e., choice flexibility throughout the analysis). In the following section, we will go through each of the mentioned methods and provide examples on how to implement them with R.

2.1. Univariate Outliers

Researchers frequently attempt to identify outliers using measures of deviation from the center of a variable’s distribution. One of the most popular such procedure is the z score transformation, which computes the distance in standard deviation (SD) from the mean. However, as mentioned earlier, this popular method is not robust. Therefore, for univariate outliers, it is recommended to use the median along with the Median Absolute Deviation (MAD), which are more robust than the interquartile range or the mean and its standard deviation [2,5].

Researchers can identify outliers based on robust (i.e., MAD-based) z scores using the `check_outliers()` function of the *{performance}* package, by specifying `method = "zscore_robust"`. Although Leys *et al.* [2] suggest a default threshold of 2.5 and Leys *et al.* [5] a threshold of 3, *{performance}* uses by default a less conservative threshold of ~ 3.29 .¹ That is, data points will be flagged as outliers if they go beyond $\pm \sim 3.29$ MAD. Users can adjust this threshold using the `threshold` argument, as demonstrated below.

¹ 3.29 is an approximation of the two-tailed critical value for $p < .001$, obtained through `qnorm(p = 1 - 0.001 / 2)`. We chose this threshold for consistency with the thresholds of all our other methods.

```
library(performance)

# Create some artificial outliers and an ID column
data <- rbind(mtcars[1:4], 42, 55)
data <- cbind(car = row.names(data), data)

outliers <- check_outliers(data, method = "zscore_robust", ID = "car")
outliers
```

```
72 #> 2 outliers detected: cases 33, 34.
73 #> - Based on the following method and threshold: zscore_robust (3.09).
74 #> - For variables: mpg, cyl, disp, hp.
75 #>
76 #> -----
77 #>
78 #> The following observations were considered outliers for two or more
79 #> variables by at least one of the selected methods:
80 #>
81 #> Row car n_Zscore_robust
82 #> 1 33 33 2
83 #> 2 34 34 2
84 #>
85 #> -----
86 #> Outliers per variable (zscore_robust):
87 #>
88 #> $mpg
89 #> Row car Distance_Zscore_robust
90 #> 33 33 33 3.709699
91 #> 34 34 34 5.848328
92 #>
93 #> $cyl
94 #> Row car Distance_Zscore_robust
95 #> 33 33 33 12.14083
96 #> 34 34 34 16.52502
```

97 The row numbers of the detected outliers can be obtained by using `which()` on the output object,
98 which can be used for exclusions for example:

```
which(outliers)
```

```
99 #> [1] 33 34
```

```
data_clean <- data[-which(outliers), ]
```

100 All `check_outliers()` output objects possess a `plot()` method, meaning it is also possible to
101 visualize the outliers:

```
library(see)

plot(outliers)
```

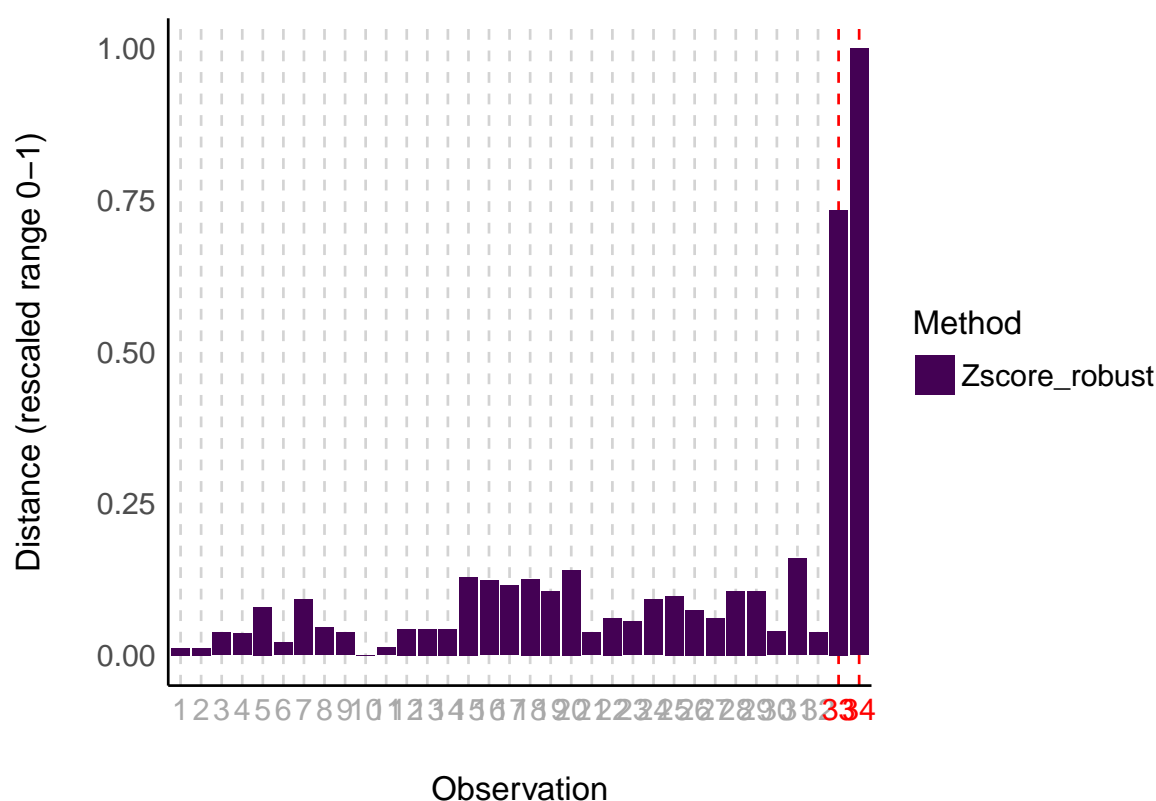


Figure 1. Visual depiction of outliers using the robust z-score method.

Other univariate methods are available, such as using the interquartile range (IQR), or based on different intervals, such as the Highest Density Interval (HDI) or the Bias Corrected and Accelerated Interval (BCI). These methods are documented and described in the function's [help page](#).

2.2. Multivariate Outliers

Univariate outliers can be useful when the focus is on a particular variable, for instance the reaction time, as extreme values might be indicative of inattention or non-task-related behavior².

However, in many scenarios, variables of a data set are not independent, and an abnormal observation will impact multiple dimensions. Let's imagine a participant giving random answers to a questionnaire. In this case, computing the z score for each of the questions might not lead to satisfactory results. Instead, one might want to look at these variables together.

One common approach for this is to compute multivariate distance metrics such as the Mahalanobis distance. Although the Mahalanobis distance is very popular, just like the regular z scores method, it is not robust and is heavily influenced by the outliers themselves. Therefore, for multivariate outliers, it is recommended to use the Minimum Covariance Determinant, a robust version of the Mahalanobis distance [MCD, 5,6].

In *performance*'s `check_outliers()`, one can use this approach with `method = "mcd"`.³

```
results <- check_outliers(data, method = "mcd")
results
```

² Note that they might not be the optimal way of treating reaction time outliers [7,8]

³ Our default threshold for the MCD method is defined by `stats::qchisq(p = 1 - 0.001, df = ncol(x))`, which again is an approximation of the critical value for $p < .001$ consistent with the thresholds of our other methods.

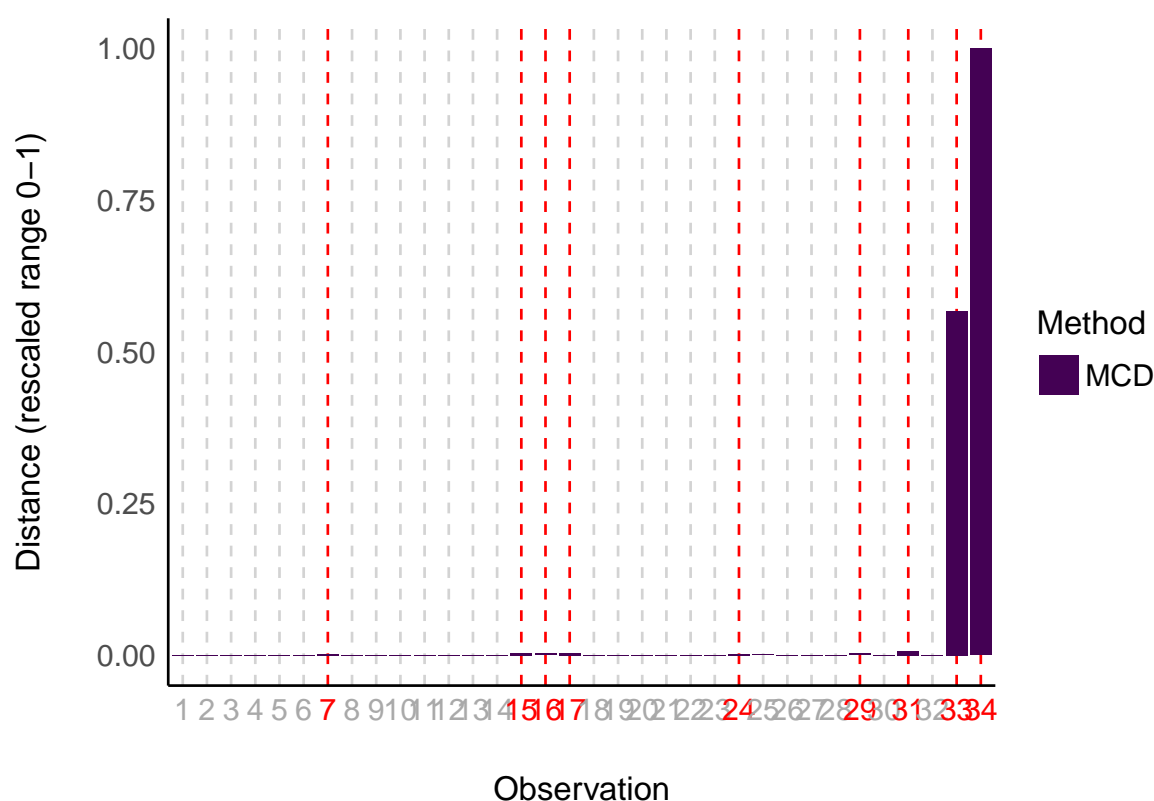


Figure 2. Visual depiction of outliers using the Minimum Covariance Determinant (MCD) method, a robust version of the Mahalanobis distance.

```

118 #> 9 outliers detected: cases 7, 15, 16, 17, 24, 29, 31, 33, 34.
119 #> - Based on the following method and threshold: mcd (20).
120 #> - For variables: mpg, cyl, disp, hp.

```

```
plot(results)
```

Other multivariate methods are available, such as another type of robust Mahalanobis distance that in this case relies on an orthogonalized Gnanadesikan-Kettenring pairwise estimator [9]. These methods are documented and described in the function's [help page](#).

2.3. Model-Based Outliers

Working with regression models creates the possibility of using model-based SOD methods. These methods rely on the concept of *leverage*, that is, how much influence a given observation can have on the whole model. If few observations have a relatively strong leverage/influence on the model, one can suspect that the model's estimates are biased by these observations, in which case flagging them as outliers could prove helpful.

`check_outliers()` can be applied directly on regression models, specifying `method = "cook"` (or `method = "pareto"` for Bayesian models).⁴

⁴ Our default threshold for the Cook method is defined by `stats::qf(0.5, ncol(x), nrow(x) - ncol(x))`, which again is an approximation of the critical value for $p < .001$ consistent with the thresholds of our other methods.

Influential Observations

Points should be inside the contour lines

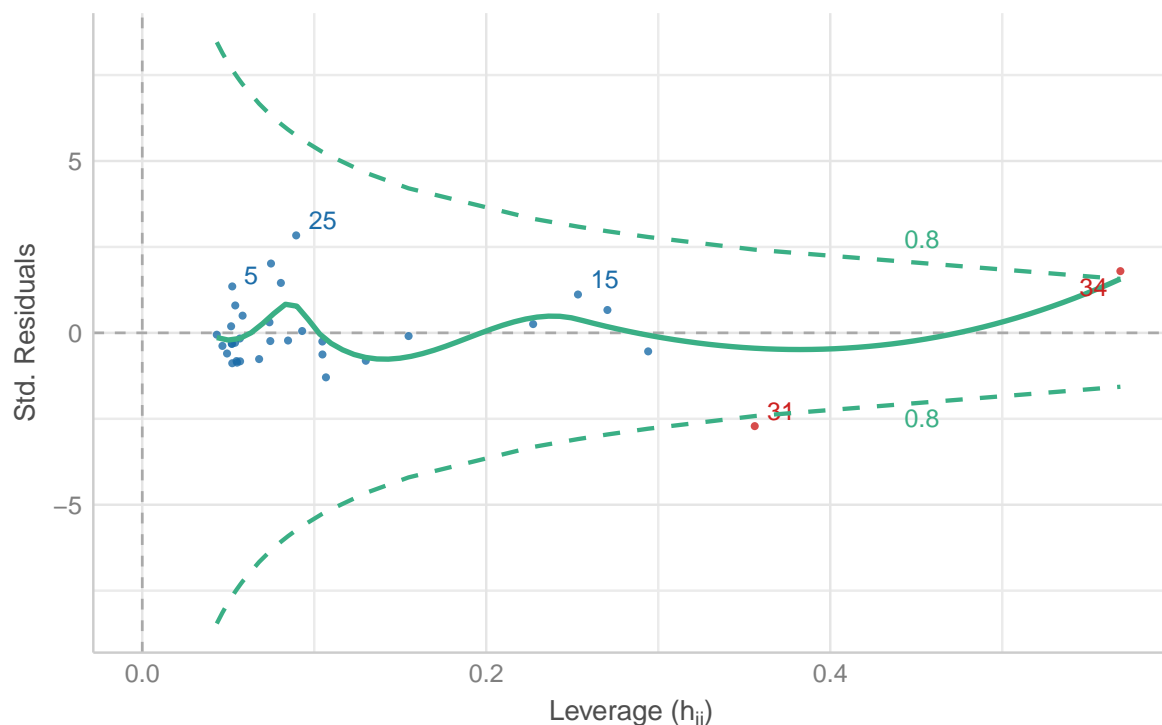


Figure 3. Visual depiction of outliers based on Cook's distance (leverage and standardized residuals).

```
model <- lm(displ ~ mpg * hp, data = data)
outliers <- check_outliers(model, method = "cook")
outliers
```

```
132 #> 2 outliers detected: cases 31, 34.
133 #> - Based on the following method and threshold: cook (0.9).
134 #> - For variable: (Whole model).
```

```
plot(outliers)
```

2.3.1. Cook's Distance vs. MCD

Leys *et al.* [6] report a preference for the MCD method over Cook's distance. This is because Cook's distance removes one observation at a time and checks its corresponding influence on the model each time [10], and flags any observation that has a large influence. In the view of these authors, when there are several outliers, the process of removing a single outlier at a time is problematic as the model remains "contaminated" or influenced by other possible outliers in the model, rendering this method suboptimal in the presence of multiple outliers.

However, distribution-based approaches are not a silver bullet either, and there are cases where the usage of methods agnostic to theoretical and statistical models of interest might be problematic. For example, a very tall person would be expected to also be much heavier than average, but that would still fit with the expected relationship between height and weight (i.e., it would be in line with a model such as $\text{weight} \sim \text{height}$). In contrast, using multivariate outlier detection methods there may flag this person as being an outlier—being unusual on two variables, height and weight—even though the pattern fits perfectly with our predictions.

Furthermore, unusual observations happen naturally: extreme observations are expected even when taken from a normal distribution. While statistical models can integrate this “expectation”, multivariate outlier methods might be too conservative, flagging too many observations despite belonging to the right generative process. For these reasons, we believe that model-based methods are still preferable to the MCD when using compatible regression models. Additionally, if the presence of multiple outliers is a significant concern, robust regression methods should be considered—like t regression or quantile regression—as they are more robust to outliers, rendering their precise identification less critical.

2.4. Multiple Methods

An alternative approach suggested by *easystats* is to combine several methods, based on the assumption that different methods provide different angles of looking at the problem. By applying a variety of methods, one can hope to “triangulate” the true outliers (those consistently flagged by multiple methods) and thus attempt to minimize false positives.

In practice, this approach computes a composite outlier score, formed of the average of the binary (0 or 1) classification results of each method. It represents the probability that each observation is classified as an outlier by at least one method. The default decision rule classifies rows with composite outlier scores superior or equal to 0.5 as outlier observations (i.e., that were classified as outliers by at least half of the methods). In *performance*'s `check_outliers()`, one can use this approach by including all desired methods in the corresponding argument.

```
# Combine multiple methods
outliers <- check_outliers(
  data[1:5],
  method = c("zscore_robust", "iqr", "mcd", "ics")
)

outliers
```

```
#> 3 outliers detected: cases 31, 33, 34.
#> - Based on the following methods and thresholds: zscore_robust (3.09),
#>   iqr (2), mcd (20), ics (0.001).
#> - For variables: mpg, cyl, disp, hp.
#>
#> Note: Outliers were classified as such by at least half of the selected methods.
#>
#> -----
#>
#> The following observations were considered outliers for two or more
#>   variables by at least one of the selected methods:
#>
#>   Row n_Zscore_robust n_IQR          n_MCD          n_ICS
#> 1   33                2      2 (Multivariate) (Multivariate)
#> 2   34                2      2 (Multivariate) (Multivariate)
#> 3   31                0      1 (Multivariate) (Multivariate)
#> 4    7                0      0 (Multivariate)              0
#> 5   15                0      0 (Multivariate)              0
#> 6   16                0      0 (Multivariate)              0
#> 7   17                0      0 (Multivariate)              0
#> 8   24                0      0 (Multivariate)              0
#> 9   29                0      0 (Multivariate)              0
```

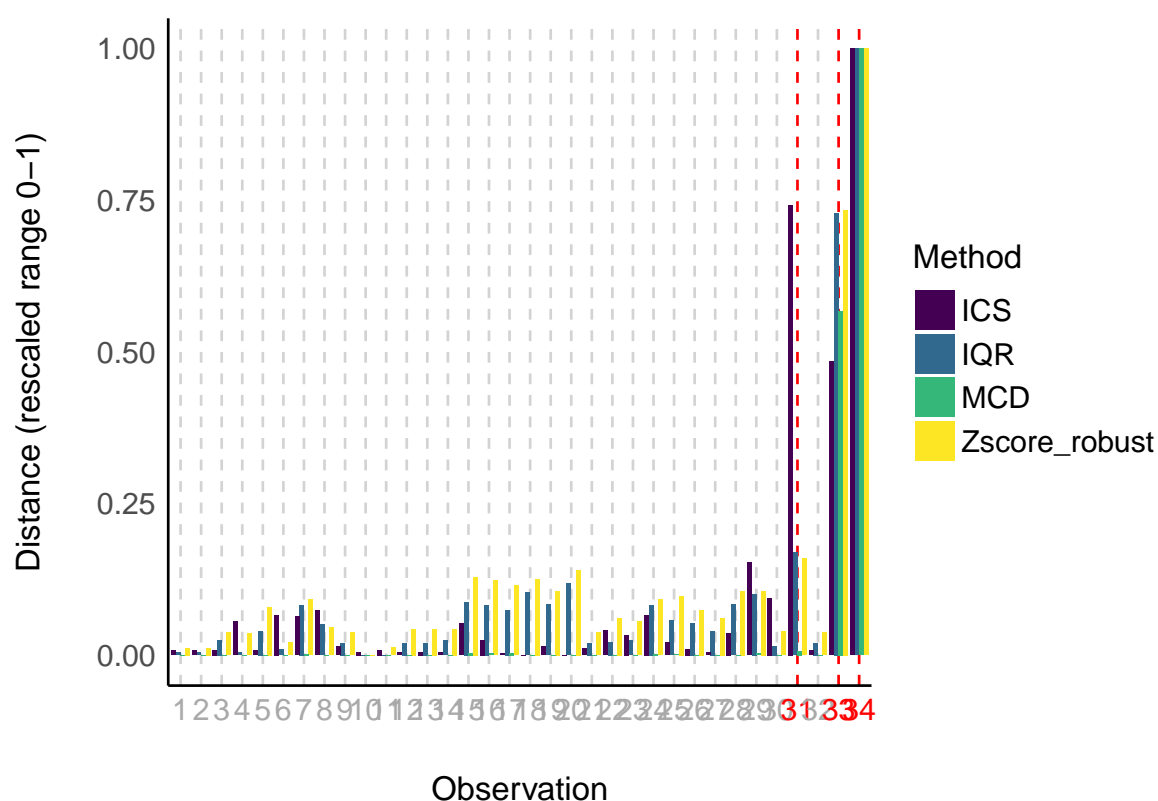


Figure 4. Visual depiction of outliers using several different statistical outlier detection methods.

```
plot(outliers)
```

190 Outliers (counts or per variables) for individual methods can then be obtained through attributes.
191 For example:

```
attributes(outliers)$outlier_var$iqr
```

```
192 #> $mpg
193 #>   Row Distance_IQR
194 #> 33 33      1.550881
195 #> 34 34      2.458544
196 #>
197 #> $cyl
198 #>   Row Distance_IQR
199 #> 33 33      5.294118
200 #> 34 34      7.205882
201 #>
202 #> $hp
203 #>   Row Distance_IQR
204 #> 31 31      1.348181
```

205 An example sentence for reporting the usage of the composite method could be:

206 Based on a composite outlier score [see the ‘check_outliers’ function in the ‘performance’ R
207 package, 3] obtained via the joint application of multiple outliers detection algorithms [(a)
208 median absolute deviation (MAD)-based robust z scores, 2; (b) interquartile range (IQR),

(c) Mahalanobis minimum covariance determinant (MCD), [5](#); and (d) invariant coordinate selection (ICS), [11](#)], we excluded three participants that were classified as outliers by at least half of the methods used.

3. Handling Outliers

The above section demonstrated how to identify outliers using the `check_outliers()` function in the `{performance}` package. But what should we do with these outliers once identified? Although it is common to automatically discard any observation that has been marked as “an outlier” as if it might infect the rest of the data with its statistical ailment, we believe that the use of SOD methods is but one step in the get-to-know-your-data pipeline; a researcher or analyst’s *domain knowledge* must be involved in the decision of how to deal with observations marked as outliers by means of SOD. Indeed, automatic tools can help detect outliers, but they are nowhere near perfect. Although they can be useful to flag suspect data, they can have misses and false alarms, and they cannot replace human eyes and proper vigilance from the researcher.

3.1. Error, Interesting, and Random Outliers

Leys *et al.* [\[5\]](#) distinguish between error outliers, interesting outliers, and random outliers. *Error outliers* are likely due to human error and should be corrected before data analysis or outright removed since they are invalid observations. *Interesting outliers* are not due to technical error and may be of theoretical interest; it might thus be relevant to investigate them further even though they should be removed from the current analysis of interest. *Random outliers* are assumed to be due to chance alone and to belong to the correct distribution and, therefore, should be retained.

It is recommended to *keep* observations which are expected to be part of the distribution of interest, even if they are outliers [\[5\]](#). However, if it is suspected that the outliers belong to an alternative distribution, then those observations could have a large impact on the results and call into question their robustness, especially if significance is conditional on their inclusion.

On the other hand, there are also outliers that cannot be detected by statistical tools, but should be found and removed. For example, if we are studying the effects of X on Y among teenagers and we have one observation from a 20-year-old, this observation might not be a *statistical outlier*, but it is an outlier in the *context* of our research, and should be discarded to allow for valid inferences.

3.2. Winsorization

Removing outliers can in this case be a valid strategy, and ideally one would report results with and without outliers to see the extent of their impact on results. This approach however can reduce statistical power. Therefore, some propose a *recoding* approach, namely, winsorization: bringing outliers back within acceptable limits [e.g., 3 MADs [12](#)]. However, if possible, it is recommended to collect enough data so that even after removing outliers, there is still sufficient statistical power without having to resort to winsorization [\[5\]](#).

The *easystats* ecosystem makes it easy to incorporate this step into your workflow through the `winsorize()` function of the `{datawizard}` package [\[13\]](#). This procedure will bring back univariate outliers within the limits of ‘acceptable’ values, based either on the percentile, the z score, or its robust alternative based on the MAD.

```
data[33:34, ] # See outliers rows
```

```
#>   car mpg cyl disp hp
#> 33  33  33  42  42   42 42
#> 34  34  34  55  55   55 55
```

```
# Winsorizing using the MAD
library(datawizard)
winsorized_data <- winsorize(data, method = "zscore", robust = TRUE, threshold = 3)

# Values > +/- MAD have been winsorized
winsorized_data[33:34, ]
```

```
251 #>      car      mpg      cyl disp hp
252 #> 33   33 37.68598 14.8956   42 42
253 #> 34   34 37.68598 14.8956   55 55
```

254 3.3. The Importance of Transparency

255 Once again, it is a critical part of a sound outlier treatment that regardless of which SOD method
 256 used, it should be reported in a reproducible manner. Ideally, the handling of outliers should be
 257 specified *a priori* with as much detail as possible, and preregistered, to limit researchers' degrees
 258 of freedom and therefore risks of false positives [5]. This is especially true given that interesting
 259 outliers and random outliers are often times hard to distinguish in practice. Thus, researchers should
 260 always prioritize transparency and report all of the following information: (a) how many outliers
 261 were identified; (b) according to which method and criteria, (c) using which function of which R
 262 package (if applicable), and (d) how they were handled (excluded or winsorized, if the latter, using
 263 what threshold). If at all possible, (e) the corresponding code script along with the data should be
 264 shared on a public repository like the Open Science Framework (OSF), so that the exclusion criteria
 265 can be reproduced precisely.

266 4. Conclusion

267 In this paper, we have showed how to investigate outliers using the `check_outliers()` function
 268 of the *{performance}* package while following current good practices. However, best practice for outlier
 269 treatment does not stop at using appropriate statistical algorithms, but entails respecting existing
 270 recommendations, such as preregistration, reproducibility, consistency, transparency, and justification.
 271 Ideally, one would additionally also report the package, function, and threshold used (linking to the
 272 full code when possible). We hope that this paper and the accompanying `check_outlier()` function
 273 of *easystats* will help researchers engage in good research practices while providing a smooth outlier
 274 detection experience.

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 276 [of easystats](#), contributors, and users alike.

277 **Author Contributions:** R.T. drafted the paper; all authors contributed to both the writing of the paper and the
 278 conception of the software.

279 **Conflicts of Interest:** The authors declare no conflict of interest.

280 Abbreviations

281 The following abbreviations are used in this manuscript:
 282

SOD	Statistical outlier detection
SEM	Structural equation modelling
SD	Standard deviation
MAD	Median absolute deviation
IQR	Interquartile range
HDI	Highest density interval
BCI	Bias corrected and accelerated interval
MCD	Minimum covariance determinant
ICS	invariant coordinate selection
OSF	Open Science Framework

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