

# Thesis

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November 21, 2016

## Abstract

This paper reviews

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## 35 1 Introduction

36 Elementary particle physics describes our world in terms of its smallest constituents, fundamen-  
37 tal particles, and their interactions. Going from larger to smaller scales, substances around us  
38 consist of molecules, molecules consist of atoms, in an atom, there is a nucleus made of neutrons  
39 and protons and some number of electrons occupying their orbits around the nucleus. Protons  
40 and neutrons have a structure while an electron is not known to have any structure, therefore,  
41 an electron is an example of a particle which is considered to be fundamental.

42 Interactions of elementary particles are described by quantum field theories which incorporate  
43 principles of the quantum mechanics and the special theory of relativity. The set of such theories,  
44 including quantum elecrtrodynamics (QED), quantum chromodynamics (QCD) and the theory  
45 of weak interactions is called the Standard Model (SM). It has been proven to be an accurate  
46 description of interactions of elementary particles observed by now.

47 However, there are several experimental observations which are not described by the SM such  
48 as gravity, dark matter, dark energy, matter/antimatter asymmetry and others. Therefore, the  
49 SM is not the complete theory of particle interactions. There are several SM extensions offered by  
50 theorists as well as radically new theories waiting for the experimental confirmation or disproof.

51 Some SM extensions and new theories predict the existence of heavy particles mass of which  
52 possibly lies beyond experimentally reachable energies. The search of these particles is one of  
53 the prioritized directions in particle physics. For such searches we need to reach higher ener-  
54 gies than those which were probed before. One source of highly energetic elementary particles  
55 is cosmic rays. The most energetic particles ever observed came from this source. However,  
56 cosmic rays are totally uncontrollable and such highly energetic particles are rare. If we want  
57 to produce a large number of particles at certain energies, we need to use a particle accelera-  
58 tor. A large number of events at certain energy allows experimentalists to perform a statistical  
59 analysis and increase the probability of finding a new particle if it exists in the given energy range.

60 Symmetric colliding beams is the most effective way to produce as heavy particles as possible  
61 given the energies of the colliding particles. The Large Hadron Collider (LHC) is such a collider  
62 with the highest energy in the world ever built. It can produce the most massive particles to  
63 probe physics beyond the SM. It collides two proton beams with the several TeV of energy each.  
64 The design center-of-mass energy of LHC is 14 TeV but it also probes several lower energy points  
65 and may go higher.

66 Compact Muon Solenoid (CMS) is one of two general-purpose detectors at the LHC. It is  
67 placed at one of six collision points. CMS has a wide physics program including searches for the  
68 beyond SM (BSM) physics as well as the precision measurements of the SM parameters them-  
69 selves.

70 In this dissertation the analysis of  $pp \rightarrow W\gamma + X$  processes using leptonic decays of  $W \rightarrow \ell\nu$   
71 where  $\ell = e, \mu$  is reported. The  $W\gamma$  productions with leptonic  $W$  decays can go through one of  
72 the following three processes: initial state radiation where a photon is produced from one of the  
73 incoming partons, final state radiation where a photon is radiated off the charged lepton from  
74 the  $W$  boson decay, and finally when a photon is produced via the triple gauge coupling (TGC)  
75 where a photon is emitted from the  $W$  boson.

76 To search for the deviations from the SM, one would search for an anomalous TGC which  
77 would be indicated by the enhance of the TGC production over the SM prediction.

78 The total and the differential cross section with respect to the photon transverse momentum  
79 ( $P_T^\gamma$ ) has been measured. The  $P_T^\gamma$  is sensitive to the potential anomalous TGC (aTGC) in the  
80 high  $P_T^\gamma$  region. The disagreement between the measured and theoretically predicted differential  
81 cross section at the higher  $P_T^\gamma$  end would be an indication of the possible presence of the aTGC.

90  
91     The rest of this chapter gives general introductory information about the SM while chapter  
92     2 concentrates on the theory of the SM and BSM  $W\gamma$  production and also discusses previous  
93     measurements of this process. Chapter 3 describes LHC and CMS in more details. Chapter  
94     4 explaines on specific aspect of the CMS operation which is the tracker alignment. Finally,  
95     chapter 5 describes the details of the measurement of this dissertation and reports the results.  
96

## 97 1.1 Fundamental Particles and Interactions

98 The SM describes interactions of elementary particles. There are four fundamental interactions:  
99 electromagnetic, strong, weak and gravitational. The gravity is not included into the SM but its  
100 effect on particles is negligible compared to the other forces which makes it possible to develop a  
101 theory of the particle physics and conduct experiments even without having the gravity included  
102 into the model.

103 All fundamental elementary particles in the SM can be split into three categories by their  
104 spins. There are fermions which possess spin  $s=1/2$ , there are gauge bosons which are also called  
105 force mediators are vector particles ( $s=1$ ) and there is the Higgs boson which is a scalar particle  
106 ( $s=0$ ).  
107

108 The fermions are arranged into three generations, each generation consists of a quark with  
109 charge  $Q=+2/3$  (up, charm, and top quarks), a quark with  $Q=-1/3$  (down, strange, and bottom  
110 quarks), a charged lepton with  $Q=-1$  (electron, muon, and tau-lepton) and a neutrino (electron,  
111 muon, and tau neutrinos) which is electrically neutral. Each quark can carry any of three colors:  
112 red, blue, or green. Additionally, each fermion has its antiparticle. Therefore, the total number  
113 of fundamental fermions is  $(6(\text{leptons}) + 6(\text{quarks}) \cdot 3(\text{colors})) \cdot 2(\text{to include antiparticles}) = 48$ .  
114

115 Corresponding particles in different generations have the same charges, spins and interaction  
116 properties but masses of particles increase with a generation. These mass differences  
117 lead to different decay properties because a particle A can decay to particles B and C only  
118 if the mass of A  $m_A > m_B + m_C$ . Thus, an electron is a stable particle, a muon decays as  
119  $\mu^- \rightarrow e^- + \bar{\nu}_e + \nu_\mu$ , a tau-lepton, as the heaviest charged lepton, has the largest number of decay  
120 channels:  $\tau^- \rightarrow \mu^- + \bar{\nu}_\mu + \nu_\tau$ ,  $\tau^- \rightarrow e^- + \bar{\nu}_e + \nu_\tau$ ,  $\tau^- \rightarrow \nu_\tau + \text{quarks}$ .  
121

122 In addition to fermions, the SM includes gauge bosons which are mediators for the SM interactions.  
123 A photon is a mediator for the electromagnetic interactions, a gluon is a mediator  
124 for the strong interactions, and  $W^\pm$  and  $Z^0$  bosons are mediators for the weak interactions.  $W^\pm$   
125 and  $Z^0$  bosons are massive while a photon and a gluon are massless particles.  
126

127 The last SM particle is the Higgs boson. The Higgs boson is a scalar neutral particle which  
128 is playing a critical role in the electroweak symmetry breaking. The Higgs mechanism describes  
129 how  $W$  and  $Z$  bosons become massive particles.  
130

131 All the particles are summarized in Fig. 1. These and only these fundamental particles and  
132 their antiparticles have been discovered by now. However, there are many composite particles  
133 which are called hadrons. Hadrons can consist of three quarks (baryons), quark and antiquark  
134 (meson), or three antiquarks (antibaryons). Hadrons always possess an integer charge.  
135

136 Most of the particles are short-lived and decay within microseconds. The only stable particles  
137 are protons and antiprotons, electrons and positrons, neutrinos and antineutrinos, photons,  
138 and, in some sense, gluons. However, if a particle cannot decay, it does not mean that it would  
139 live forever. There are many different kinds of reactions in which particles can disappear. An-  
140 tiprotons and positrons would immediately annihilate with protons and electrons, photons can  
141 be absorbed by charged particles, electrons and protons can scatter to produce neutrons and  
142 neutrinos and many other reactions are possible.  
143

144 In this dissertation a process is studied where quark and antiquark interact to produce a  $W$   
145 boson which then decay as  $W^\pm \rightarrow e^\pm \nu_e (\bar{\nu}_e)$  or  $W^\pm \rightarrow \mu^\pm \nu_\mu (\bar{\nu}_\mu)$ . A photon is radiated off a  
146 quark or antiquark, a charged lepton or a  $W$  boson. The most interesting mechanism out of three  
147 is a radiation from a  $W$  boson because this is the triple gauge coupling where we potentially  
148 can have a new physics. Therefore, the focus of this study is an interaction between a photon  
149 and a  $W$  boson however many other SM particles are relevant too. Thus, a charged lepton and  
150 a neutrino appear as the final state particles, a quark and an antiquark appear as initial state  
151

152 particles and all fundamental particles except the Higgs boson participate in various background  
 153 processes. Subsections 1.2-1.4, chapter 2 and [1] describe particle interactions in more details.

154

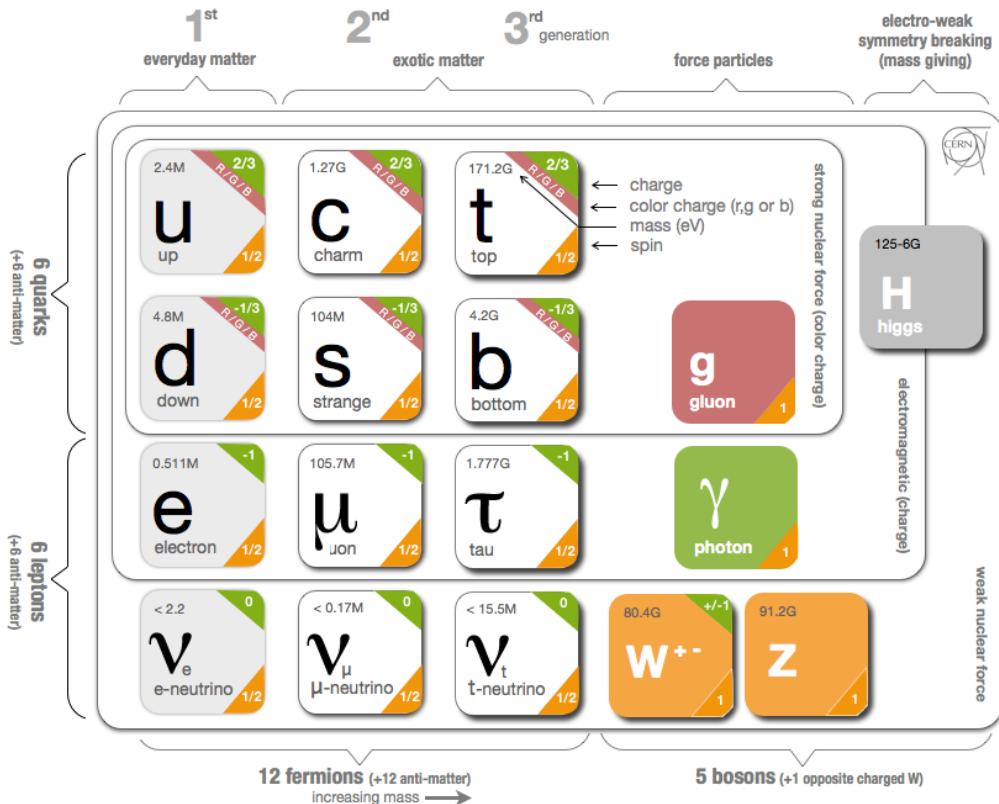


Figure 1: Standard Model Particles and Interactions. Source of the figure: [2].

155 **1.2 Electroweak Interactions**

156 All electrically charged particles participate in electromagnetic interactions. All electromagnetic  
 157 interactions are mediated by a photon, a spin-one electrically neutral massless particle, and can  
 158 be reduced to one elementary process (Fig. 2, left). This process represents an electron radiating  
 159 or absorbing a photon. Although an electron is drawn in this figure, it can be any other charged  
 160 particle as well. Such elementary process itself is forbidden by the energy conservation law but  
 161 this element is a base of actual process (for example, Fig. 2, middle and right). Such graphical  
 162 representations of the particle physics processes are called Feynman diagrams.

163

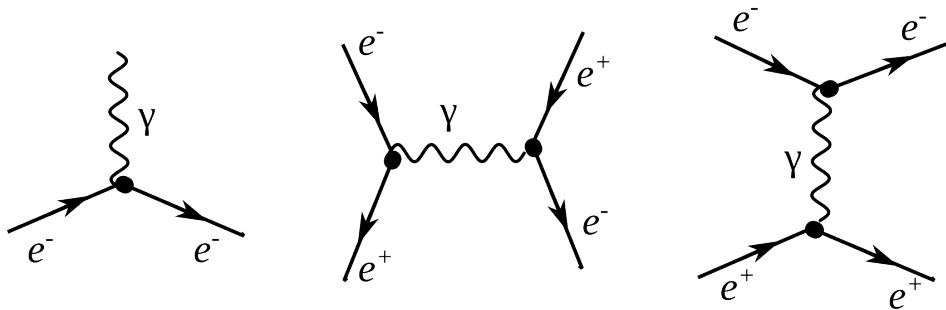


Figure 2: Electromagnetic interactions

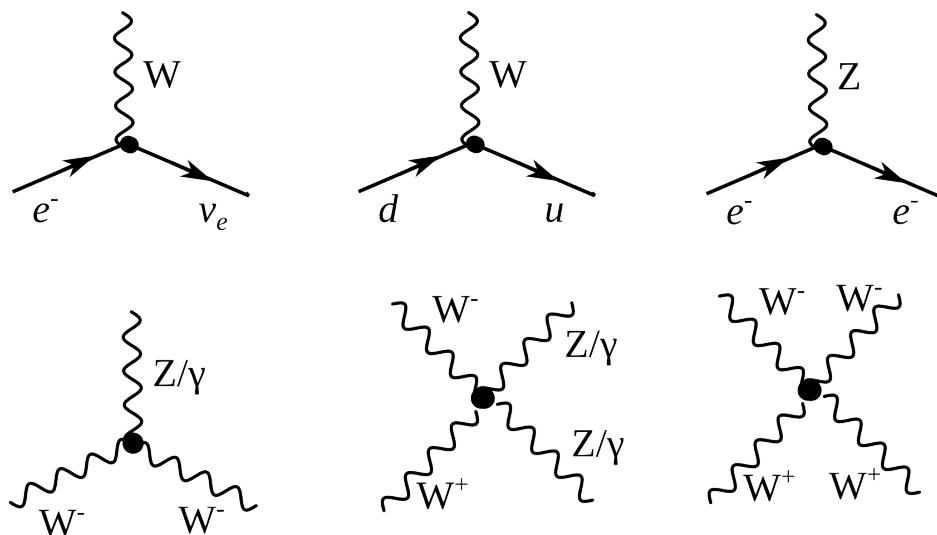


Figure 3: Weak elementary processes and gauge couplings

164 As for the weak interactions, there are two kinds of them: neutral (mediated by a  $Z$  boson)  
 165 and charged (mediated by a  $W^\pm$  boson). Elementary processes with  $W$  and  $Z$  bosons are shown

in Fig. 3. Because the electric charge must be conserved at any vertex, a particle radiating or absorbing a  $W$  boson converts to a different particle. Thus, a charged lepton converts to a neutrino (or vice versa) as shown in Fig. 3, top left. Each lepton carries a lepton flavor number (Tab. 1). A lepton flavor number is conserved in any interaction, thus an electron radiating a  $W$  boson always converts to an electron neutrino, a muon converts to a muon neutrino etc.

171

Table 1: Lepton Flavor Number

particles	$L_e$	$L_\mu$	$L_\tau$
$e^-, \nu_e$	+1	0	0
$e^+, \bar{\nu}_e$	-1	0	0
$\mu^-, \nu_\mu$	0	+1	0
$\mu^+, \bar{\nu}_\mu$	0	-1	0
$\tau^-, \nu_\tau$	0	0	+1
$\tau^+, \bar{\nu}_\tau$	0	0	-1

From top middle diagram in Fig. 3 we see that if a quark with  $Q=-1/3$  enters, then a quark with  $Q=+2/3$  escapes and, therefore, the flavor of the quark is changed. The charged weak interaction is the only interaction which changes a quark flavor. The probability of each of three quarks with  $Q=+2/3$  to be born is determined by the Cabibbo Kobayashi Maskawa matrix and is the highest for the quark of the same generation as an initial state quark. In this particular case,  $d$  is the initial state quark and  $u$  has the highest probability to be produced after an interaction with a  $W$  boson but  $c$  and  $t$  can also be produced if there is enough energy.

179

An elementary process of a neutral weak interaction is an emission of a  $Z$  boson off a fermion line (right top diagram in Fig. 3). An electron is shown here as an example however it could also be any lepton, antilepton, quark or antiquark. Diagrams with a  $Z$  boson are very similar to ones with a photon except a photon can only be radiated off a charged particle but a  $Z$  boson can also be radiated off a neutrino or antineutrino.

185

The bottom diagrams in Fig. 3 are gauge bosons coupling diagrams including self-coupling of a  $W$  boson, its interaction with a  $Z$  boson and its electromagnetic radiation of a photon.  $WWZ$ ,  $WW\gamma$ ,  $WWZZ$ ,  $WWZ\gamma$ ,  $WW\gamma\gamma$  and  $WWWW$  vertices are all possible in the SM.

189

Electromagnetic and weak interactions are unified by the electroweak Glashow-Weinberg-Salam (GWS) theory which is based on  $SU(2) \times U(1)$  symmetry.  $SU(2)$  is the symmetry of weak isospin which generates three bosons:  $W^1$ ,  $W^2$  and  $W^3$ .  $U(1)$  is the symmetry of the weak hypercharge and generate one neutral boson  $B$ .  $W^1$  and  $W^2$  are mixed to create  $W^+$  and  $W^-$  mediators while  $W^3$  and  $B$  are mixed to create a  $Z$  boson and a photon. Therefore, the GWS theory considers electromagnetic and weak forces as different manifestations of the electroweak force.

196

However, weak interactions are mediated by heavy bosons ( $M_W = 80$  GeV,  $M_Z = 91$  GeV) while electromagnetic interactions are mediated by a massless photon, thus, the electroweak symmetry is broken. To explain this phenomenon, the Higgs mechanism was introduced. The mechanism predicted an existence of an additional boson: the Higgs boson. The Higgs boson was a missing piece of the SM for many years and was finally discovered in 2012 at LHC by ATLAS and CMS collaborations through the processes shown in Fig.4 [3], [4].

203

The measurement in this dissertation is an electroweak measurement because the process in-

204

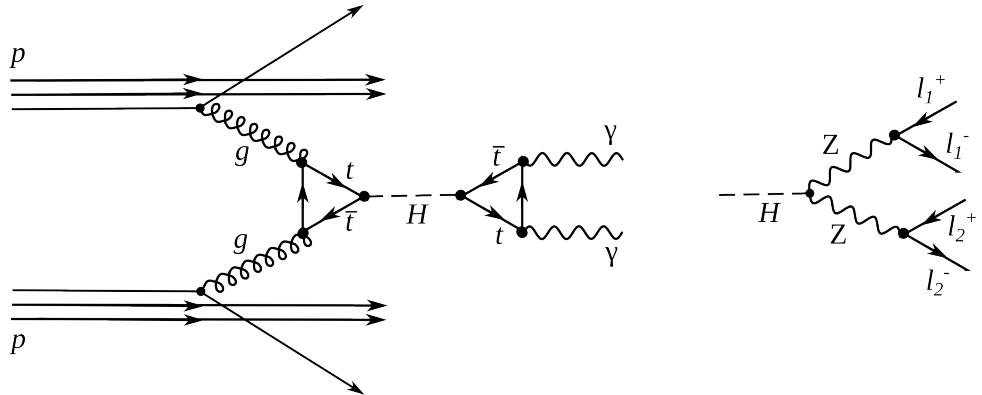
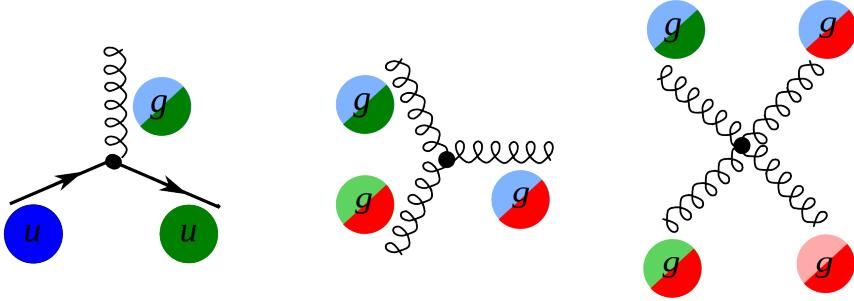


Figure 4: The Higgs boson production and decay

<sup>205</sup> involves a  $W$  boson. It includes an interaction of a  $W$  boson with leptons and quarks as well as the  
<sup>206</sup> triple gauge coupling  $WW\gamma$ . Thus, the measurement is a good test of the SM electroweak theory.

<sup>207</sup>

208 **1.3 Strong Interactions**



213 Figure 5: Elementary processes of strong interactions

214 The third fundamental force after the electromagnetic and weak ones is the strong force. The  
215 strong force is responsible for glueing protons and neutrons together in the nuclei as well as for  
216 forming protons and neutrons themselves. The strong interactions occur by exchanging gluons  
217 which are spin-one massless electrically neutral particles.

218 The elementary strong processes are shown in Fig. 5. There are three elementary processes:  
219  $qqg$ ,  $ggg$  and  $gggg$ , all are involving particles with color charges. Thus, gluons couple to quarks  
220 and self-couple. Color charges must be conserved at each elementary process of the strong in-  
221 teraction. Because quarks can possess three colors, there are eight types of gluons to cover all  
222 possible color exchanges.

223 The coupling constant of the strong interaction depends on a distance between interacting  
224 particles: it becomes larger as the distance becomes larger. This property leads to two conse-  
225 quences specific to the strong force: the confinement and the asymptotic freedom.

226 The asymptotic freedom means that when quarks are very close to each other they almost  
227 do not interact with each other and therefore they are free. The confinement is the property  
228 of quarks to always stay in the color neutral combinations (hadrons), it forbids the existence of  
229 free quarks. A combination becomes color neutral when there is the same amount of color and  
230 anticolor or if there is the same amount of each of the three colors. Thus, mesons are comprised  
231 of a quark and an antiquark with the opposite color charges, and baryons are comprised of three  
232 quarks: red, green and blue one. Examples of baryons include such well-known particles as a  
233 proton and a neutron are baryons.

234 The strong interactions can be described by the QCD which is a quantum field theory in-  
235 variant under  $SU(3)$  color transformations. When the distance between quarks is small which  
236 corresponds to high energy, and thus the coupling constant  $\alpha_s \ll 1$  is small, the perturbative  
237 approach can be used to compute observables.

238 The  $W\gamma$  process being measured in this dissertation is not intended to test QCD, but a good  
239 understanding of QCD is essential for performing this measurement because the QCD correc-  
240 tions to the Feynman diagrams of the process are large and has to be taken into account in  
241 producing simulation. Possible QCD corrections include quark-gluon loops at any of three quark  
242 lines as well as exchanges of gluons between different quark lines. In addition, QCD describes  
243 the dynamics of quarks and gluons within colliding protons and predicts probabilities of one or  
244 another quark-antiquark pair to interact. Physics of proton-proton collisions is discussed in the  
245 subsection 1.4.

## 247 1.4 Physics of Proton-Proton Collisions

248 At LHC two protons are collided. The LHC energy is so high that a proton behaves as a complex  
 249 structure. A proton is a baryon, it consists of three quarks:  $uud$ . These three quarks are called  
 250 valence quarks. They interact with each other by exchanging gluons which produce virtual  $q\bar{q}$   
 251 pairs (Fig. 6). Such quarks are called sea quarks.  
 252

253 Any parton from one proton can interact with any parton from another proton. Probabilities  
 254  $f_i(x, Q^2)$  of any particular constituent  $i$  to interact are described partially by QCD and par-  
 255 tially by experimental measurements and depend on the momentum transfer  $Q$  and the momen-  
 256 tum fraction of a specific parton  $x$ . These probabilities are called parton distribution functions  
 257 (PDFs).  
 258

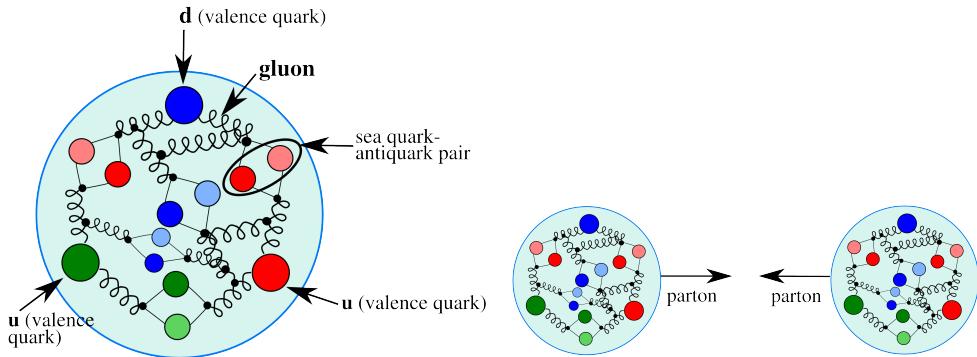


Figure 6: The proton structure (left) and the proton-proton collision (right).

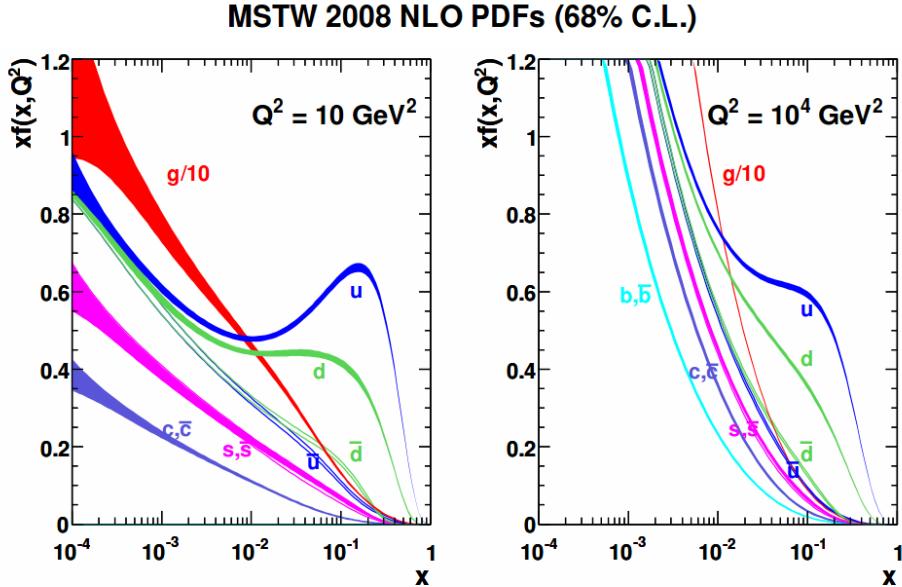


Figure 7: Martin-Stirling-Thorne-Watt parton distribution functions [5].

259 For large  $Q^2$  and  $x$  gluon-gluon interactions have the largest probabilities to occur (Fig. 7).

260 However, gluons do not couple directly to a  $W$  boson, thus, in the  $W\gamma$  measurement we are  
261 mostly interested in quark-antiquark pairs which would have a total charge corresponding to the  
262 charge of a  $W$  boson ( $\pm 1$ ). Since we have  $u$  and  $d$  as valence quarks and we know that the  
263 probability to couple to the same generation quark in charged weak interactions is the highest,  
264 most of the  $W$  bosons are created by  $u\bar{d}$  and  $d\bar{u}$  pairs however other  $q\bar{q}'$  combinations with the  
265 total charges of  $\pm 1$  are also possible. The antiquarks come from virtual  $q\bar{q}$  pairs inside of each  
266 proton.

267  
268 As we look for events containing  $W\gamma$  we also have other events mimicking our process. Such  
269 background events can be produced by any pair of partons.  
270

## 271 1.5 Open Questions of the Standard Model

272 While the SM is an accurate description of all particle physics experimental results, there are  
273 certain phenomena which are not included into the SM. In this subsection we discuss some of  
274 them.

275 The gravitational interactions do not fit into the SM. It is the open question whether the  
276 quantum theory of gravity is possible and whether there is a mediator of the gravitational in-  
277 teractions. Also, it is not known why the gravitational force is so much weaker than any other  
278 force. One possible explanation comes from a theory which predicts extra spatial dimensions  
279 beyond the three we are dealing with (e.g. the string theory). In this case, it is possible that the  
280 gravitational force is shared with other dimensions and that is why the fraction available in our  
281 three dimensions is that small.

283 Another mystery of the Universe is its composition: it is known from the studies of the grav-  
284 itational effects that our Universe consists of dark energy by 70%, of dark matter by 26% and of  
285 baryon matter only by 4%. The dark energy resists the gravitational attraction and accelerates  
286 the expansion of the Universe, and is not detectable by any effects except gravitational. The  
287 understanding of the dark energy is a question of the general relativity rather than the particle  
288 physics. The dark matter however likely consists of particles and therefore is a subject of the  
289 particle physics. It does not radiate and that is why it cannot be detected by telescopes. The  
290 nature of the dark matter is not known but its constituents must be very stable to remain since  
291 the Big Bang. The theory of the supersymmetry which is unifying fundamental particles and  
292 mediators predicts many of new heavy particles and the lightest supersymmetric particle, the  
293 neutralino, is a good candidate for the dark matter.

295 One more open question is the reason for the matter/antimatter asymmetry. The matter  
296 and antimatter should have been created in the same amount at the moment of the Big Bang.  
297 Then most of it has annihilated but because of asymmetry, there was more matter than anti-  
298 matter which led to the state of the Universe we observe now. There is a phenomenon of  
299 the CP-violation in weak interactions observed and described that predicts the asymmetry at  
300 a certain level. However, the effect of the CP-violation is not large enough to account for the  
301 observed amount of the matter and, therefore, the total matter/antimatter asymmetry remains  
302 unexplained.

304 The measurement of the photon transverse momentum spectrum ( $P_T^\gamma$ ) of the  $W\gamma$  process has  
305 a goal to both test the SM and search for the BSM physics. The low  $P_T^\gamma$  region is not expected to  
306 be affected by any new physics and must agree well with the SM predictions while the high  $P_T^\gamma$   
307 region may indicate an existence of a new physics if there is an enhancement over the SM predictions.  
308 The enhancement would be an indirect evidence of the BSM particles like supersymmetric particles,  
309 additional gauge bosons or higher generation fermions. More theoretical details about the SM  
310 description of  $W\gamma$  process as well as the possible BSM physics are given in the chapter 2.

<sup>313</sup> **2 W $\gamma$  Production Theory and Former Experimental Re-**

<sup>314</sup> **sults**

## 315 2.1 Electroweak Theory of the Standard Model

316 To develop a quantum field theory, we start with the Lagrangian of free fermions. In order  
317 to describe a system with a conservation of a physical quantity, the Lagrangian is required to  
318 satisfy a local invariance with respect to a certain transformation. For instance, a conservation  
319 of an electric charge requires a local invariance under  $U(1)$  transformation for the QED La-  
320 grangian [6]. The requirement of the local invariance introduces an interaction of a new vector  
321 field (or several fields) with our free fermions. The new vector field is a mediator of an inter-  
322 action conserving the physical quantity. To provide a full description for a new boson field, in  
323 addition to the interaction term we introduce an invariant term for the kinetic energy of the bo-  
324 son. Such approach allows us to derive the Lagrangian which is locally invariant with respect to  
325 a certain gauge transformation and contains interacting fermions as well as interaction mediators.  
326

327 The SM is a quantum field theory invariant under the local  $SU(3)_C \times SU(2)_L \times U(1)_Y$  trans-  
328 formation [6]. The SM Lagrangian includes all observed quantum fields and their interactions.  
329

330 The  $SU(3)_C$ -invariant Lagrangian describes QCD: interactions of quarks and antiquarks.  
331 QCD has three types of charges which are called colors: red, blue, and green. The requirement  
332 to satisfy the gauge invariance with respect to  $SU(3)_C$  transformations generates eight massless  
333 gluons, and the non-abelian nature of the  $SU(3)$  group generates self-interactions of gluons in-  
334 cluding three-gluon and four-gluon vertices.  
335

336 The Lagrangian based on the  $SU(2)_L \times U(1)_Y$  symmetry is a foundation of the unified theory  
337 of electroweak interactions.  $SU(2)_L$  reflects transformations in the weak isospin space of left-  
338 handed fermions ([1], Ch. 9) while  $U(1)_Y$  reflects transformations in a weak hypercharge space  
339 of all fermions. The requirement of the local gauge invariant generates four massless vector  
340 bosons which are mediators of electromagnetic and weak interactions. The non-abelian struc-  
341 ture of  $SU(2)$  group introduces gauge boson couplings just like self-interactions of gluons appear  
342 in QCD.  
343

344 Mass terms for the vector bosons would violate the gauge invariance of the electroweak La-  
345 grangian, however it is experimentally known that mediators of weak interactions are heavy  
346 particles with masses  $M_W = 80$  GeV and  $M_Z = 91$  GeV. A possible solution of the discrepancy  
347 is a mechanism of the spontaneous symmetry breaking. QED symmetry group  $U(1)$  remains  
348 unbroken because a photon is massless.  
349

350 The mechanism of the Spontaneous Symmetry Breaking and the appearance of the mass  
351 terms for  $W$  and  $Z$  boson is described by introducing an additional doublet of scalar fields which  
352 correspond to a new particle: a Higgs boson ( $H$ ). The Higgs boson couples to  $W$  and  $Z$  bosons  
353 generating their masses while a photon does not couple to the Higgs boson remaining a massless  
354 particle and keeping  $U(1)_{QED}$  symmetry unbroken.  
355

356 The measurement in this dissertation provides a test for the electroweak sector of the SM.  
357 Thus, we will retrace the steps of the derivation of the EWK part of the SM Lagrangian starting  
358 from Lagrangians of free particles. The resulting Lagrangian accommodates electroweak gauge  
359 bosons including their self-couplings which are the primary focus of our measurement.  
360

361 It is experimentally known that dynamics of weak interactions depends on particle's chirality  
362 ([1], Ch. 4.4.1). In particular, a  $W$  boson couples to left-handed fermions and right-handed an-  
363 tifermions only. A  $Z$  boson couples to both left-handed and right-handed charged fermions and  
364 antifermions but only to left-handed neutrinos and right-handed antineutrinos.  
365

366 Given different properties of left-handed and right-handed fermions, they are treated dif-  
367 ferently by the electroweak theory.  $SU(2)$  doublets are introduced for the wave functions of  
368 left-handed fermions while  $SU(2)$  singlets are introduced for the wave functions of right-handed  
369 fermions. Eq. 1 and Eq. 2 show wave functions for the first generation fermions. Wave functions

<sup>370</sup> for the other two generations are constructed the same way.

<sup>371</sup>

$$\psi_1(x) = \begin{pmatrix} u \\ d' \end{pmatrix}_L, \psi_2(x) = u_R, \psi_3(x) = d'_R. \quad (1)$$

$$\psi_1(x) = \begin{pmatrix} \nu_e \\ e^- \end{pmatrix}_L, \psi_2(x) = \nu_{eR}, \psi_3(x) = e^-_R. \quad (2)$$

<sup>372</sup> The state  $d'$  is a mixture of  $d$ ,  $c$  and  $b$  quark's wave functions and is determined by the quark  
<sup>373</sup> mixing matrix which is also called Cabibbo-Kobayashi-Maskawa matrix [6]:

<sup>374</sup>

$$\begin{pmatrix} d' \\ c' \\ b' \end{pmatrix} = V \begin{pmatrix} d \\ c \\ b \end{pmatrix} \quad (3)$$

<sup>375</sup> To derive the unified electroweak Lagrangian, we start with the free fermion terms:

<sup>376</sup>

$$L_0 = \sum_{j=1}^3 i\bar{\psi}_j(x)\gamma^\mu\partial_\mu\psi_j(x), \quad (4)$$

<sup>377</sup> where  $\gamma^\mu$  are Dirac matrices ([1], Ch. 7.1) and  $\psi_j(x)$  are wave functions determined by Eq. 1  
<sup>378</sup> and Eq. 2.

<sup>379</sup>

<sup>380</sup> The wave function  $\psi_1$  changes under the  $SU(2)_L \times U(1)_Y$  transformations in the following  
<sup>381</sup> way:

<sup>382</sup>

$$\psi_1(x) \rightarrow e^{iy_1\beta}U_L\psi_1(x) \quad (5)$$

<sup>383</sup> The wave functions  $\psi_{(2,3)}(x)$  are singlets of  $SU(2)_L$  and are affected only by  $U(1)$  transfor-  
<sup>384</sup> mations:

<sup>385</sup>

$$\psi_{(2,3)}(x) \rightarrow e^{iy_{(2,3)}\beta}\psi_{(2,3)}(x) \quad (6)$$

<sup>386</sup> The transformation  $U_L \equiv e^{i\sigma_i\alpha_i/2}$  where  $\sigma_i$  are Pauli matrices ([1], Ch. 4.2.2). Phases  $\alpha_i(x)$   
<sup>387</sup> and  $\beta(x)$  are arbitrary functions,  $y_{(1,2,3)}$  are hypercharges which are named analogous to electric  
<sup>388</sup> charges in QED.

<sup>389</sup>

<sup>390</sup> In order to satisfy the local  $SU(2)_L \times U(1)_Y$  invariance, partial derivatives in Eq. 4 have to  
<sup>391</sup> be substituted with covariant derivatives:

<sup>392</sup>

$$D_\mu\psi_1(x) = [\partial_\mu - ig\tilde{W}_\mu(x) - ig'y_1B_\mu(x)]\psi_1(x) \quad (7)$$

$$D_\mu\psi_{(2,3)}(x) = [\partial_\mu - ig'y_{(2,3)}B_\mu(x)]\psi_{(2,3)}(x) \quad (8)$$

<sup>393</sup> where  $g$ ,  $g'$  are arbitrary constants,

<sup>394</sup>

$$\tilde{W}_\mu(x) \equiv \frac{\sigma_i}{2}W_\mu^i(x) = \frac{1}{\sqrt{2}} \begin{pmatrix} \sqrt{2}W_\mu^3 & (W_\mu^1 - iW_\mu^2)/\sqrt{2} \\ ((W_\mu^1 + iW_\mu^2)/\sqrt{2} & -W_\mu^3 \end{pmatrix}, \quad (9)$$

<sup>395</sup>  $B_\mu$ ,  $W_\mu^1$ ,  $W_\mu^2$ ,  $W_\mu^3$  are four vector bosons that arise from the requirement of the Lagrangian  
<sup>396</sup> to be invariant under local  $SU(2)_L \times U(1)$  transformations.

<sup>397</sup>

The Lagrangian becomes:

$$L_0 \rightarrow L = \sum_{j=1}^3 i\bar{\psi}_j(x)\gamma^\mu D_\mu \psi_j(x) \quad (10)$$

To make new vector bosons physical fields it is necessary to add terms for their kinetic energies:

$$L_{KIN} = -\frac{1}{4}B_{\mu\nu}B^{\mu\nu} - \frac{1}{4}W_{\mu\nu}^i W_i^{\mu\nu} \quad (11)$$

where  $B_{\mu\nu} \equiv \partial_\mu B_\nu - \partial_\nu B_\mu$ ,  $W_{\mu\nu}^i \equiv \partial_\mu W_\nu^i - \partial_\nu W_\mu^i + g\epsilon^{ijk}W_\mu^j W_\nu^k$

Off-diagonal terms of  $\tilde{W}_\mu$  are wave functions of charged vector bosons  $W^\pm = (W_\mu^1 \mp iW_\mu^2)/\sqrt{2}$  while  $W_\mu^3$  and  $B_\mu$  are neutral fields which are mixtures of a  $Z$  boson and a photon determined by:

$$\begin{pmatrix} W_\mu^3 \\ B_\mu \end{pmatrix} \equiv \begin{pmatrix} \cos\theta_W & \sin\theta_W \\ -\sin\theta_W & \cos\theta_W \end{pmatrix} \begin{pmatrix} Z_\mu \\ A_\mu \end{pmatrix} \quad (12)$$

where  $\theta_W$  is an electroweak mixing angle,  $A_\mu$  is a photon field.

In order to be consistent with QED, terms involving  $A_\mu$  in the electroweak Lagrangian must be equal to the corresponding terms in QED Lagrangian [6]:

$$L_{QED} = i\bar{\psi}(x)\gamma^\mu \partial_\mu \psi(x) - m\bar{\psi}(x)\psi(x) + qA_\mu(x)\bar{\psi}(x)\gamma^\mu \psi(x) - \frac{1}{4}F_{\mu\nu}(x)F^{\mu\nu}(x), \quad (13)$$

where  $q$  is electric charge of  $\psi(x)$  field,  $F_{\mu\nu} \equiv \partial_\mu A_\nu - \partial_\nu A_\mu$ .

This requirement relates  $g$ ,  $g'$ ,  $\theta_W$  and  $e$  as  $g \sin\theta_W = g' \cos\theta_W = e$  and provides expression for weak hypercharges:  $y = q - t_3$ , where  $q$  is the electric charge and  $t_3$  is a  $z$ -component of the weak isospin. This gives  $y_1 = 1/6$ ,  $y_2 = 2/3$ , and  $y_3 = -1/3$  for quarks and  $y_1 = -1/2$ ,  $y_2 = 0$ , and  $y_3 = -1$  for leptons. A right-handed neutrino has a hypercharge of  $y_2 = 0$ . It also does not have an electric charge and, as a right-handed particle, cannot couple to a  $W$  boson. Thus, a right-handed neutrino does not participate in any SM interaction.

Writing  $\tilde{W}_\mu$  in Eq. 11 explicitly, we will get TGC and QGC coupling terms:

$$L_{TGC} = -\frac{g}{4}(\partial_\mu W_\nu^i - \partial_\nu W_\mu^i)\epsilon^{ijk}W^{\mu j}W^{\nu k} - \frac{g}{4}\epsilon^{ijk}W_\mu^j W_\nu^k(\partial^\mu W^{\nu i} - \partial^\nu W^{\mu i}) \quad (14)$$

$$L_{QGC} = -\frac{g^2}{4}\epsilon^{ijk}\epsilon^{ilm}W_\mu^j W_\nu^k W^{\mu l}W^{\nu m} \quad (15)$$

Substitute  $W_\mu^i$  and  $B_\mu$  in Eq. 14 and Eq. 15 with the wave functions of  $W^\pm$ ,  $Z$  and a photon:

$$B_\mu = -\sin\theta_W Z_\mu + \cos\theta_W A_\mu, \quad W_\mu^3 = \cos\theta_W Z_\mu + \sin\theta_W A_\mu \quad (16)$$

$$W_\mu^1 = \sqrt{2}(W^+ + W^-), \quad W_\mu^2 = \sqrt{2}(W^- + W^+) \quad (17)$$

we will receive charged TGC Lagrangians in the form of Eq. 18:

$$L_{TGC} = L_{TGC}^{(1)} + L_{TGC}^{(2)}, \quad (18)$$

which involves  $WWZ$  (Eq. 19) and  $WW\gamma$  (Eq. 20) interactions:

$$L_{TGC}^{(1)} = -ie \cot \theta_W (W^{-\mu\nu} W_\mu^+ Z_\nu - W^{+\mu\nu} W_\mu^- Z_\nu + W_\mu^- W_\nu^+ Z^{\mu\nu}), \quad (19)$$

$$L_{TGC}^{(2)} = -ie (W^{-\mu\nu} W_\mu^+ A_\nu - W^{+\mu\nu} W_\mu^- A_\nu + W_\mu^- W_\nu^+ A^{\mu\nu}), \quad (20)$$

and charged QGC Lagrangians in the form of Eq. 21:

$$L_{QGC} = L_{QGC}^{(1)} + L_{QGC}^{(2)} + L_{QGC}^{(3)} + L_{QGC}^{(4)} \quad (21)$$

which involves  $WWWW$  (Eq. 22),  $WWZZ$  (Eq. 23),  $WWZ\gamma$  (Eq. 24), and  $WW\gamma\gamma$  (Eq. 25) interactions:

$$L_{QGC}^{(1)} = -\frac{e^2}{2 \sin^2 \theta_W} (W_\mu^+ W^{-\mu} W_\nu^+ W^{-\nu} - W_\mu^+ W^{\mu+} W_\nu^- W^{-\nu}) \quad (22)$$

$$L_{QGC}^{(2)} = -e^2 \cot^2 \theta_W (W_\mu^+ W^{-\mu} Z_\nu Z^\nu - W_\mu^+ Z^\mu W_\nu^- Z^\nu) \quad (23)$$

$$L_{QGC}^{(3)} = -e^2 \cot \theta_W (2W_\mu^+ W^{-\mu} Z_\nu A^\nu - W_\mu^+ Z^\mu W_\nu^- A^\nu - W_\mu^+ A^\mu W_\nu^- Z^\nu) \quad (24)$$

$$L_{QGC}^{(4)} = -e^2 (W_\mu^+ W^{-\mu} A_\nu A^\nu - W_\mu^+ A^\mu W_\nu^- A^\nu) \quad (25)$$

In the measurement of this dissertation we probe  $WW\gamma$  coupling.

The unified electroweak Lagrangian discussed above involves kinetic energy terms for fermions and gauge bosons as well as interactions of fermions with gauge bosons, TGC, and QGC. However, this Lagrangian does not contain any mass terms.

Because left-handed and right-handed wave functions transform differently under the electroweak symmetry, adding fermion mass terms of  $\frac{1}{2}m_f^2 \bar{\psi}\psi$  would violate the Lagrangian invariance and, therefore, fermion mass terms are forbidden by the  $SU(2) \times U(1)$  symmetry requirement. Mass terms for gauge bosons also would violate the Lagrangian invariance just as a photon mass term  $\frac{1}{2}m^2 A^\mu A_\mu$  would violate  $U(1)$  invariance of  $L_{QED}$  [1]. Therefore, Largangian  $L$  in Eq. 10 contains massless particles only.

However, it is known from experiments that a  $Z$  boson, a  $W$  boson and fermions are massive particles and, therefore, our theory should accommodate their masses. To introduce masses into the electroweak Lagrangian, an  $SU(2)_L$  doublet of complex scalar fields  $\phi(x)$  is added to the Lagrangian:

$$\phi(x) \equiv \begin{pmatrix} \phi^{(+)}(x) \\ \phi^{(0)}(x) \end{pmatrix} \quad (26)$$

By selecting a special gauge of  $\phi(x)$  it is possible to spontaneously break electroweak symmetry, generate a new scalar particle, a Higgs boson [6], and introduce mass terms for  $W$  and  $Z$  bosons and charged fermions through their couplings to the Higgs boson. The strength of the coupling constant is proportional to the square of the particle's mass, therefore, heavier particles are more likely to interact with  $H$ , and massless particles do not couple to  $H$ .

The mechanism of generating a fermion's mass involve both left-handed and right-handed components of the fermion. If our hypothesis that right-handed neutrinos do not exist is right, then the Higgs mechanism does not generate neutrino masses. However, from the experiments of neutrino oscillations, neutrinos are known to have masses even though they are orders of magnitude smaller than those of other fermions. Several hypotheses were offered to resolve this

463 contradiction however at the moment the mechanism of neutrinos to acquire masses remain un-  
464 known [7].

465  
466 In this dissertation, we study an electroweak process  $W\gamma \rightarrow l\nu_l\gamma$ , more specifically, probe  
467 TGC vertex  $WW\gamma$  (Eq. 20). To do that, we are measuring a differential cross section with  
468 respect to the photon transverse momentum. The concept of the cross section in particle physics  
469 is discussed in Chapter 2.2.

470

## 2.2 Cross Section and Luminosity

In this dissertation we are measuring the total and the differential cross section. The cross section in particle physics is the interaction probability per unit flux of incident particles [12]. It can be interpreted as area which must be crossed by an incident particle in order to interact with a scattering center, or, in case of a differential cross section, area  $d\sigma$  within which an incident particle must appear to be scattered off by an angle  $d\theta$  (Fig. 8). The relationship between  $d\sigma$  and  $d\theta$  gives us the expression for a differential cross section  $d\sigma/d\theta$ . Integrating over  $d\theta$ , one would get the total cross section  $\sigma$ .

In Fig. 8 an incident particle is the same as a final state particle, however in particle physics final state particles can differ from initial state particles, and we measure a differential cross section with respect to a parameter  $X$  of the final state particle. Differentiating  $\sigma$  by  $X$  we get the expression for the differential cross section  $d\sigma/dX$ .

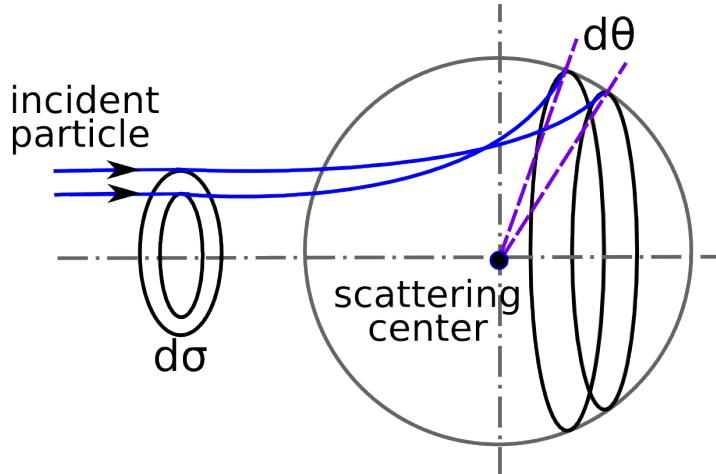


Figure 8: Illustration of the differential cross section concept in the classical case.

Referring to the Fig. 8, a number of particles passing through the area  $\sigma$  per unit time is  $N = L \cdot \sigma$ , where  $L$  is the flux of incident particles and is called luminosity. Therefore, the cross section  $\sigma$  of a specific process can be determined from an experiment as  $\sigma = N/L$ .

A cross section also can be computed theoretically. The formula to compute a cross section is:

$$\sigma = \frac{W_{fi}}{L} N_{fs}, \quad (27)$$

where  $W_{fi}$  is a transition probability between final and initial states of the system per unit volume,  $L$  is the flux of initial particles, and  $N_{fs}$  is the density of final states [8], Ch. 4.3.

The formula of the cross section is called the Fermi's Golden Rule [1]. In case of the scattering of two particles to three final state particles  $1 + 2 \rightarrow 3 + 4 + 5$ , it takes the following form:

$$\sigma = \frac{1}{4\sqrt{(p_1 p_2)^2 - (m_1 m_2)^2}} \int |M|^2 (2\pi)^4 \delta^4(p_1 + p_2 - p_3 - p_4 - p_5) \prod_{j=3}^5 \frac{1}{2\sqrt{\bar{p}_j^2 + m_j^2}} \frac{d^3 \bar{p}_j}{(2\pi)^3}, \quad (28)$$

497 where  $p_i$  are 4-momenta and  $\bar{p}_i$  are three momenta of the initial state and the final state  
498 particles,  $m_i$  are masses of particles,  $M$  is the process amplitude determined by the dynamics  
499 of the particles interaction. All available momenta of the final state particles is called the phase  
500 space.

501

502 The cross section of the hard scattering in proton-proton collisions  $pp \rightarrow X + Y$  has two  
503 ingridients: PDFs and a partonic cross section  $\sigma_{ab \rightarrow X}$ . The partonic cross section is described  
504 by perturbative QCD while PDFs require non-perturbative computations and are determined,  
505 in part, from experiments (Fig. 7). According to the QCD factorization theorem [9]:  
506

$$\sigma(pp \rightarrow X + Y) = \sum_{a,b} \int dx_a dx_b f_a(x_a, Q^2) f_b(x_b, Q^2) \sigma(ab \rightarrow X). \quad (29)$$

507 In case of  $W\gamma$  process,  $X$  is  $l\nu\gamma$ ,  $ab$  are  $q_i\bar{q}_j$  or  $q_j\bar{q}_i$ .  $Q^2$  is the large momentum scale that char-  
508 acterizes hard scattering,  $f_a$  and  $f_b$  are PDFs,  $x_a$  and  $x_b$  are fractions of momenta of the partons.  
509

### 2.3 Standard Model $W\gamma$ Production

A  $W$  boson in proton-proton collisions can be produced in the processes  $q\bar{q}' \rightarrow W$  where  $q$  and  $\bar{q}'$  are a quark and an antiquark which have a total charge of +1 if producing a  $W^+$  boson or of -1 if producing a  $W^-$  boson. The processes  $u\bar{d} \rightarrow W^+$  and  $d\bar{u} \rightarrow W^-$  are the most likely to occur because  $u$  and  $d$  are valence quarks in a proton. Antiquarks  $\bar{d}$  and  $\bar{u}$  come from sea  $q\bar{q}$  pairs of the other proton.

A  $W$  boson decays immediately after being created, and we do not detect the  $W$  boson itself but its decay products. Decay modes of a  $W$  boson include  $W^\pm \rightarrow l^\pm \nu_l (\bar{\nu}_l)$  where  $l^\pm = e^\pm, \mu^\pm$  or  $\tau^\pm$  with branching fractions of 11% per a leptonic channel [7]. The rest 67% stands for various  $W \rightarrow q\bar{q}'$  decays. In this dissertation we only consider  $W^\pm \rightarrow \mu^\pm \nu_\mu (\bar{\nu}_\mu)$  and  $W^\pm \rightarrow e^\pm \nu_e (\bar{\nu}_e)$  as the cleanest channels.

A photon can be emitted from any charged particle of the process: a quark, an antiquark, a charged lepton or a  $W$  boson (Fig. 9, top). A quark and an antiquark are initial state particles and, therefore, if one of them radiates a photon, we call such process the Initial State Radiation (ISR). A muon or an electron is a final state particle and if it radiates a photon, we call such process the Final State Radiation (FSR). Finally, a  $W$  boson is a gauge boson and if it radiates a photon, the process has a vertex with three gauge bosons:  $WW\gamma$ , and we call such process the Triple Gauge Coupling (TGC).

530

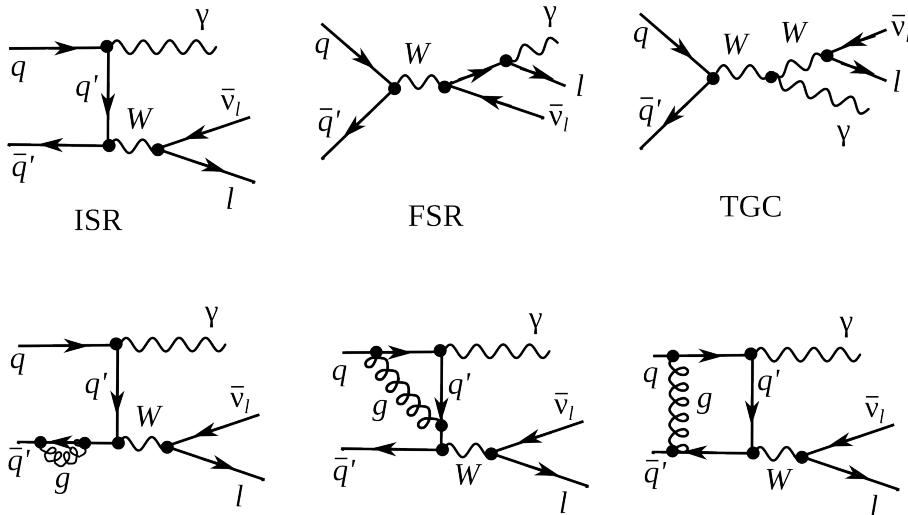


Figure 9: Feynman diagrams of  $W\gamma$  production

The electroweak Lagrangian is described in Chapter 2.1. It is possible to derive equations of motion from the Lagrangian for any fields involved [1]. However, in a quantum field theory equations of motion cannot be solved exactly and, therefore, the perturbative approach is used if coupling constants are  $g \ll 1$ .

535

To represent the process graphically Feynman diagrams were invented. Also the diagrams can be used to calculate the process amplitude  $M$  from Eq. 28 because they are determined by Lagrangian terms relevant to the process. There is infinite number of Feynman diagrams corresponding to any specific process and the total amplitude of the process is a sum of individual amplitudes of each diagram and it is not technically possible to take into account all of them.

541 The perturbative approach arranges all the diagrams by orders of contribution because each  
542 vertex is assigned a coupling constant and, therefore, the Feynman diagrams with fewer vertices  
543 would give a significantly larger contribution to the amplitude. In Fig. 9 we have examples of the  
544 Leading Order (LO) and the Next-to-Leading Order (NLO) Feynman diagrams (top and bottom  
545 diagrams respectively).

546  
547 The  $W\gamma$  process is represented by four LO Feynman diagrams with three vertices each. The  
548  $W\gamma$  process amplitude and cross section are long, complicated expressions, therefore, they are not  
549 quoted in this dissertation. The first calculation of the  $W\gamma$  process with necessary formulas can  
550 be found in [14].

551  
552 The NLO corrections shown in Fig. 9 are QCD corrections only which include gluon loops  
553 at the same quark line and exchange of a gluon between two different quark lines however QED  
554 and weak NLO diagrams are also possible. QED corrections mean radiations of extra photons  
555 by charged particles, exchange of photons between different charged particles or a photon can be  
556 radiated and absorbed by the same charged particle forming a loop. Similarly, weak corrections  
557 mean extra virtual  $W$  or  $Z$  bosons. But the QCD corrections are the largest.

558  
559 The theoretical cross section in particle physics is important not only for analyzing the measurement  
560 result but also for producing the simulation which is then actively used while performing the measurement.  
561 The simulation consists of two parts: the generation of the process and the simulation of the particles paths through the detector. While the second one depends on the well-known properties of the particles and the detector configurations, the first part relies on the  
562 theory.

563  
564 The most precise theoretical  $W\gamma$  cross section available is the Next-to-Next-to-Leading Order  
565 (NNLO) cross section in QCD [15]. The effect of the NNLO correction ranges from 19% to 26%  
566 compared to the NLO cross section depending on the selection conditions. The contributions  
567 from the higher order corrections is estimated to be  $\pm 4\%$ . However, the NNLO theoretical result  
568 was published in 2015 only and there is still no simulation available based on that result. The  
569 simulation used in this analysis is LO + up to two hadronic jets simulation which found to give  
570 the same predictions as the NLO result.

571  
572 In addition to the SM predictions, there are certain BSM theories which predict an enhancement  
573 of the contribution from the TGC diagram. The discussion of these BSM effects and how  
574 they affect the  $W\gamma$  process takes place in Chapter 2.4.

575  
576  
577

## 2.4 Anomalous $W\gamma$ Production

Most BSM physics theories predict the existence of particles which are heavier than the discovered energy range. If their masses are not accessible even by the most energetic machines, the direct detection of such particles is not possible. However, they can contribute to the productions of lower energetic particles producing loops where such heavy particles would be off-shell. The loops would give additional contributions to the process amplitude and, therefore, there would be more events produced in the process than one can expect based on the SM predictions.

These effects can be probed by precision measurements of the SM processes. In the electroweak sector processes of such interest include diboson and triboson productions which can occur through triple gauge couplings and quartic gauge couplings.

Triple and quartic gauge couplings (QGC) are represented by vertices with three and four bosons (Fig. 10). As discussed in Chapter 2.1, charged TGC and QGC are possible at tree level in the SM while neutral TGC and QGC are not.

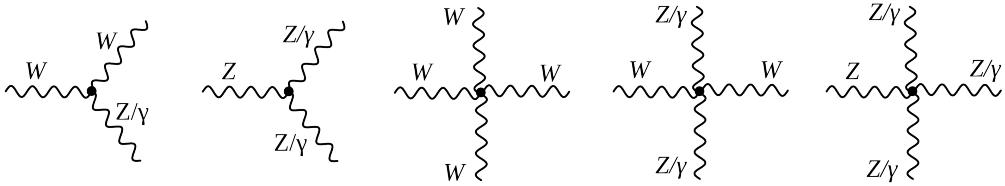


Figure 10: TGC and QGC vertices

To account for the effects from the potential loops of heavy particles, we introduce an effective Lagrangian with arbitrary values of coupling constants which can be shrunk to the SM Lagrangian if these constants would have their SM values. Such approach makes our searches model-independent because we do not specify which exactly particles form the loops but instead just check whether there is a deviation from the SM.

In  $W\gamma$  measurement we can probe  $WW\gamma$  vertex only. The most general Lorentz invariant Lagrangian of this vertex takes the following form [17]:

$$iL_{eff}^{WW\gamma} = iL_{eff(1)}^{WW\gamma} + iL_{eff(2)}^{WW\gamma} + iL_{eff(3)}^{WW\gamma} \quad (30)$$

$$iL_{eff(1)}^{WW\gamma} = e[g_1^\gamma A^\mu (W_{\mu\nu}^- W^{+\nu} - W_{\mu\nu}^+ W^{-\nu}) + \kappa_\gamma W_\mu^+ W_\nu^- A^{\mu\nu} + \frac{\lambda_\gamma}{m_W^2} A^{\mu\nu} W_\nu^{+\rho} W_{\rho\mu}^-] \quad (31)$$

$$iL_{eff(2)}^{WW\gamma} = e[i g_5^\gamma \epsilon_{\mu\nu\rho\sigma} ((\partial^\rho W^{-\mu}) W^{+\nu} - W^{-\mu} (\partial^\rho W^{+\nu})) V^\sigma + i g_4^\gamma W_\mu^- W_\nu^+ (\partial^\mu A^\nu + \partial^\nu A^\mu)] \quad (32)$$

$$iL_{eff(3)}^{WW\gamma} = e[\frac{\tilde{\kappa}_\gamma}{2} W_\mu^- W_\nu^+ \epsilon^{\mu\nu\rho\sigma} A_{\rho\sigma} - \frac{\tilde{\lambda}_\gamma}{2m_W^2} W_{\rho\mu}^- W_\nu^{+\mu} \epsilon^{\nu\rho\alpha\beta} A_{\alpha\beta}] \quad (33)$$

where  $e$  is the absolute value of the electron charge,  $A^\mu$  is the photon field,  $W^{\pm\mu}$  are fields of  $W^\pm$  bosons,  $W_{\mu\nu} = \partial_\mu W_\nu - \partial_\nu W_\mu$ ,  $A_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu$ ,  $m_W$  is the mass of a  $W$  boson,  $g_1^\gamma$ ,  $\kappa_\gamma$ ,  $\lambda_\gamma$ ,  $g_5^\gamma$ ,  $g_4^\gamma$ ,  $\tilde{\kappa}_\gamma$ , and  $\tilde{\lambda}_\gamma$  are constants.

607     Despite there are 7 constants in the extended Lagrangian, only  $\lambda_\gamma$  and  $\kappa_\gamma$  are considered  
 608     in the aTGC searches. The rest of the constants are fixed to their SM values based on various  
 609     considerations. Thus,  $g_1^\gamma = 1$  and  $g_5^\gamma = 0$  are fixed to obey the electromagnetic gauge invariance  
 610     for the on-shell photons. The non-zero value of  $g_5^\gamma$  also violates C and P conservations, and  
 611     non-zero values of  $g_4^\gamma$ ,  $\kappa_\gamma$ ,  $\tilde{\lambda}_\gamma$  violate the CP conservation law. Such violation parametrizations  
 612     are not considered in charged TGC measurements now but might get considered in the future.  
 613

614     The presence of aTGC would have larger effects at high energy scales. Fig. 11 shows these  
 615     effect in  $P_T^\gamma$  spectrum of 7 TeV  $W\gamma \rightarrow \mu\nu\gamma$  measurement. Fig. 12 shows the examples of these  
 616     effects in  $m_{ll}$  spectrum in 8 TeV  $WW \rightarrow l\bar{l}l\nu$  measurement (left) and  $P_T^\gamma$  spectrum in 7 TeV  
 617      $Z\gamma \rightarrow \nu\nu\gamma$  measurement (right). It is seen on the plots that aTGC spectrum at low  $m_{ll}$  or low  
 618      $P_T^\gamma$  coincides with the SM prediction but for higher  $m_{ll}$  or  $P_T^\gamma$  the disagreement becomes more  
 619     significant.  
 620

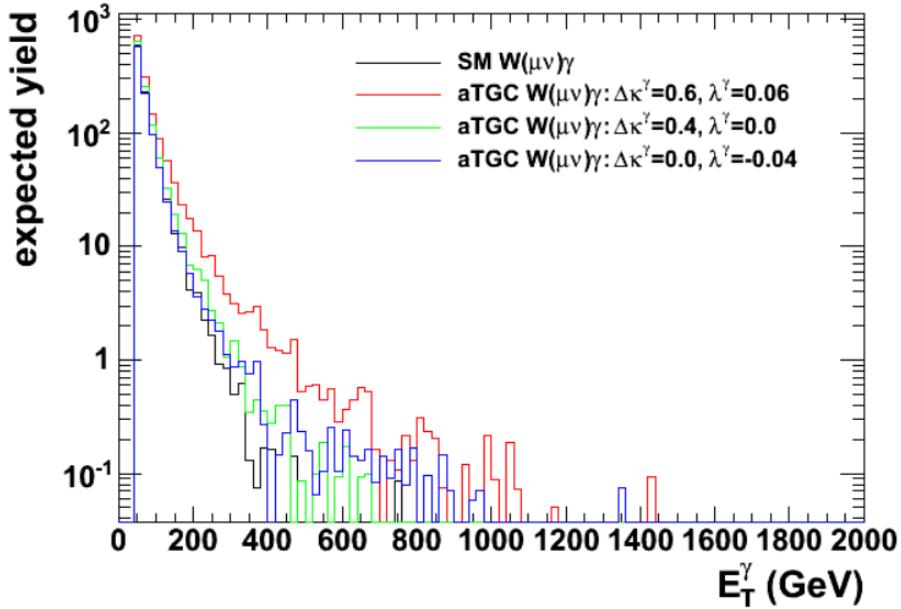


Figure 11: Distributions of  $P_T^\gamma$  of simulated  $W\gamma \rightarrow \mu\nu\gamma$  events with different values of aTGC constants at LHC energy of  $\sqrt{s} = 7$  TeV. Source of figure: [18].

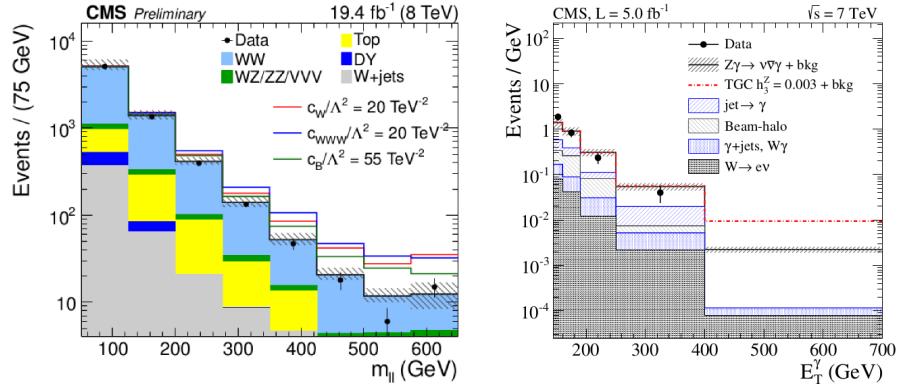


Figure 12: Examples of the potential effects of non-zero TGC constants in  $m_{ll}$  spectrum in 8 TeV  $WW \rightarrow l\nu l\nu$  measurement (left) [29] and  $P_T^\gamma$  spectrum in 7 TeV  $Z\gamma \rightarrow \nu\nu\gamma$  measurement (right) [30].

## 2.5 Measurements in the Past

ATGC parameters of  $WW\gamma$  vertex can be probed in  $W\gamma$ ,  $WW$ , and  $WZ$  measurements. Limits on  $\Delta\kappa_\gamma$  and  $\lambda_\gamma$  constants from different D0 [19], LEP [20], ATLAS [21], [22], [23] and CMS [25], [26], [27], [28] measurements are summarized in Fig. 13.

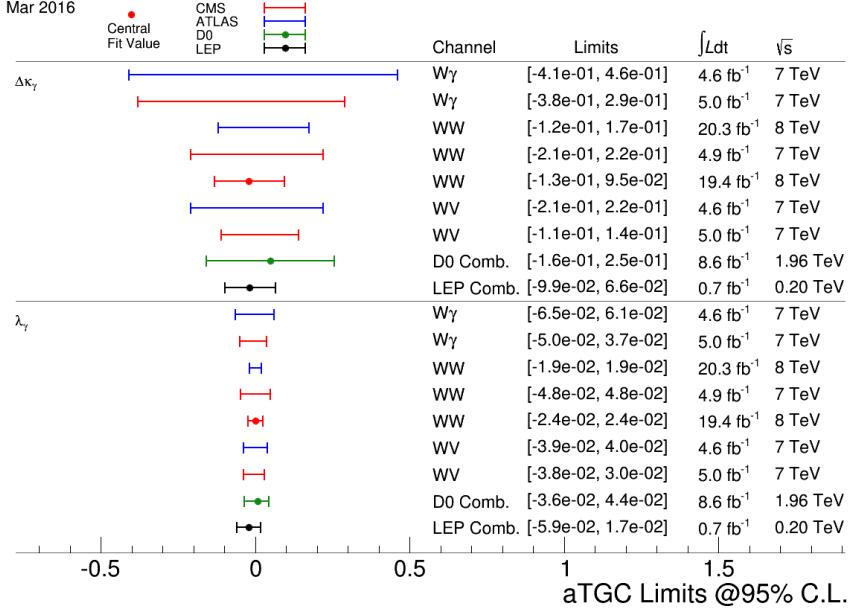


Figure 13: Summary of limits on the  $WW\gamma$  aTGC coupling constants. Figure from [24]

The most recent measurements of  $W\gamma$  production were performed by CMS [25] and ATLAS [21] collaborations with  $pp$  collisions at  $\sqrt{s} = 7$  GeV collected in 2011. The measurements are based on  $5 \text{ fb}^{-1}$  and  $4.6 \text{ fb}^{-1}$  of integrated luminosity with CMS and ATLAS respectively. Both collaborations considered two channels:  $W\gamma \rightarrow \mu\nu\gamma$  and  $W\gamma \rightarrow e\nu\gamma$ .

Dibosons processes are rare in  $pp$ -collisions and we have to filter out events of our interest from many processes which are more likely to happen. To do that, we apply variety of selection criteria which reject most of background events increasing our signal rate as much as possible. However, even after we applied all possible selection critaria, majority of our selected events are still background events and it is not possible to reduce the background any further without also significantly reducing signal.

The major source of such irreducible background is the fake photon background where hadronic jets are misidentified as photons. Such events originate from  $W+\text{jets}$  process mostly but  $Z+\text{jets}$  and  $t\bar{t}+\text{jets}$  events contribute to this source of the background as well. The second major background for the electron channel is the fake photon background where electron can be misidentified as a photon. Such events are coming from  $Z+\text{jets}$  events. Other sources of backgrounds include real- $\gamma$  backgrounds, fake lepton + real photon and fake lepton + fake photon sources.

Both channels provide measurements of  $p_T^\gamma$  spectra because this variable is the most sensitive to the potential ATGC. The  $p_T^\gamma$  spectra of the selected events in data superimposed with selected events in the simulation of the signal and estimated background contribution for the muon and electron channels are shown in Fig. 14 for CMS and in Fig. 15 for ATLAS. Both measurements show a good agreement.

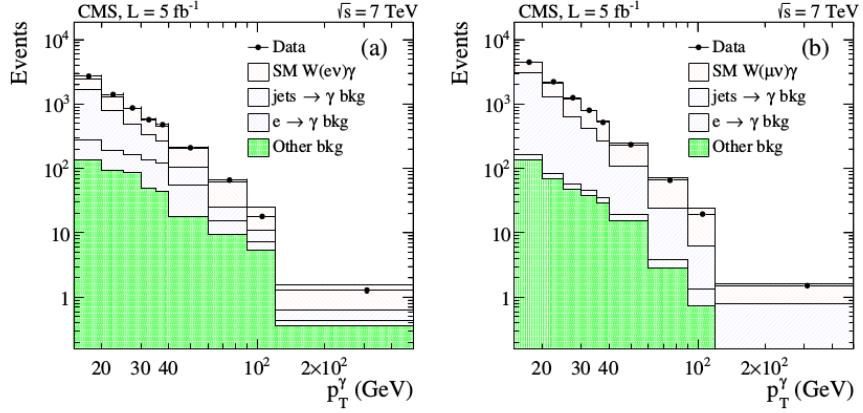


Figure 14: The distribution fo the  $p_T^\gamma$  of  $W\gamma$  candidates in the analysis of 7 TeV CMS data. Data vs signal MC + background estimates. Left:  $W\gamma \rightarrow e\nu\gamma$ , right:  $W\gamma \rightarrow \mu\nu\gamma$  [25].

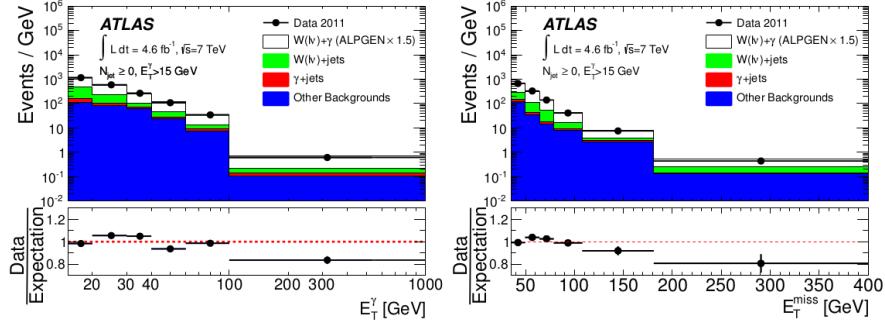


Figure 15: The distribution fo the  $p_T^\gamma$  (left) and  $E_T^\gamma$  (right) of  $W\gamma$  candidates in the analysis of 7 TeV ATLAS data. Data vs signal MC + background estimates [21].

CMS provides measurements of the  $P_T^\gamma$  spectrum, the total cross section within the phase spaces of  $\Delta R > 0.7$ ,  $P_T^\gamma > 15$  GeV,  $P_T^\gamma > 60$  GeV and  $P_T^\gamma > 90$  GeV, and limits on aTGC coupling constants. The phase space restrictions come from the considerations of the detector acceptance, reducing heavily background-dominated regions and theory.

ATLAS, in addition to the  $P_T^\gamma$  spectrum, total cross section and limits, provides the differential cross section and cross section with different number of associated jets. No evidence of a new physics is observed.

In this dissertation we are measuring total and differential  $d\sigma/dP_T^\gamma$  cross section however we do not derive limits on aTGC coupling constants. The measurement details and results are available in Chapter 5.

664

665 **3 Experimental Setup**

### 666 3.1 Large Hadron Collider

667 Large Hadron Collider (LHC) [31], [32], [33] is the last element of the chain of the CERN's  
668 accelerator complex (Fig. 16). Before entering LHC, particle beams are going through several  
669 stages of the acceleration. Thus, protons are extracted from hydrogen atoms, are accelerated by  
670 Linac2 to energies of 5 MeV, then injected into the Proton Synchrotron Booster (PSB) where  
671 they reach energies of 1.4 GeV. After that protons are to PS and Super PS (SPS) where they are  
672 accelerated to 25 GeV and 450 GeV respectively. Finally, protons enter LHC and are accelerated  
673 for 20 minutes to reach their design energies of 7 TeV per beam.

674  
675 Besides protons, the complex also works with lead ions however in this dissertation we ana-  
676 lyze data from proton-proton collisions only and, therefore, are not discussion lead ion collisions  
677 in more details.

678  
679 LHC is the largest particle accelerator ever built: it is about 27 km in circumference. Also  
680 LHC re-uses the tunnel built for Large Electron-Positron (LEP) Collider which determines the  
681 size of the machine. The large size is necessary to reach design high energies.

682  
683 Main goals of LHC were to detect the Higgs boson if it existed and to search for evidences of  
684 BSM physics which may give a clue on understanding the phenomena which are not described by  
685 the SM including dark matter, matter-antimatter asymmetry, gravitational force and others. Six  
686 detectors are installed at the LHC to detect particles and perform the relevant measurements.  
687 There are general purpose detectors ATLAS and CMS, there is LHCb which specializes of the  
688 physics of B-mesons, ALICE which is designed to detect products of heavy ion collisions. In  
689 addition, there are two small detectros with very specific tasks: LHCf and TOTEM which are  
690 installed close to the ATLAS and CMS interaction points respectively.

691  
692 No deviations from the SM were found by any of the experiments. The main achievement of the  
693 LHC to date is the discovery of the Higgs boson in 2012 by CMS [3] and ATLAS [4] collaborations.

694  
695 LHC is constructed of eight arcs, each arc corresponds to a sector as shown in Fig. 17. In be-  
696 tween there are eight insertions where beams are either collided or injected or dumped or cleaned.

697  
698 From the other hand, LHC is split on eight octants, each starting from the middle of one  
699 sector and ending at the middle of the next one. Thus, each octant includes one full insertion.

700  
701 Main parameters are summarized in Tab. 2.

702 Besides a beam energy, the most important quality of the accelerator is ability to produce  
703 a large number of interesting collisions which is determined by luminosity. The instantaneous  
704 luminosity is determined by the following expression [7]:

705  
706 
$$L = f \frac{n_1 n_2}{4\pi\sigma_x \sigma_y}$$

707 where  $n_1$  and  $n_2$  are numbers of particles in colliding bunches,  $f$  is a frequency of collisions,  
708  $\sigma_x$  and  $\sigma_y$  are beam sizes in horizontal and vertical directions.

709  
710 To determine the integrated luminosity, one has to integrate the instantaneous luminosity  
711 over time:

712  
713 
$$L_{int} = \int L dt$$

714  
715 Run periods of LHC in 2010-2012 refer to Run I of the LHC operation. While working on  
716 energy of  $\sqrt{s} = 7$  TeV (3.5 TeV pae beam), LHC delivered  $44.96 \text{ pb}^{-1}$  and  $6.1 \text{ fb}^{-1}$  of data  
717 in 2010 and 2011 year respectively. In 2012 the working energy of LHC was  $\sqrt{s} = 8$  TeV, and  
718 the integrated luminosity was  $L_{int} = 23.3 \text{ fb}^{-1}$ . After a long shutdown, LHC was upgraded for  
719 Run II, to operate on  $\sqrt{s} = 13$  TeV in 2015 and delivered  $4.22 \text{ fb}^{-1}$  of data by the end of 2015.  
720 In 2016 LHC continues operation on  $\sqrt{s} = 13$  TeV and by the end of September the integrated

<sup>721</sup> luminosity already exceeded a value of  $30 \text{ fb}^{-1}$  [37].

<sup>722</sup>

## CERN's Accelerator Complex

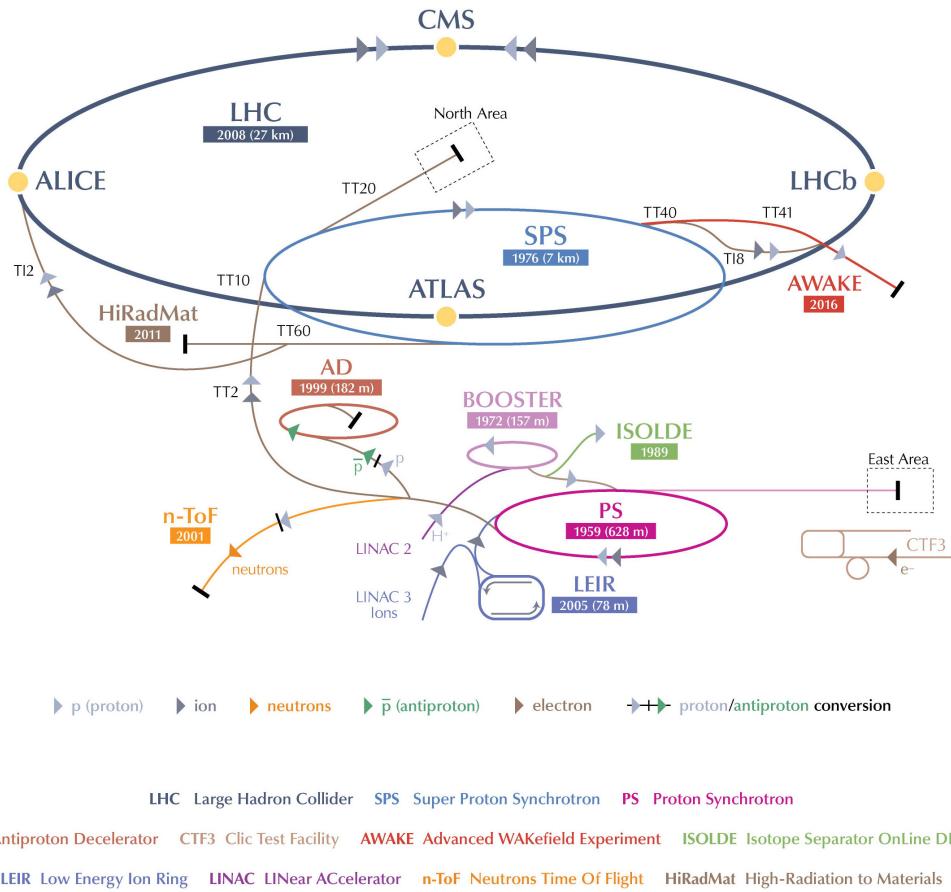


Figure 16: CERN's accelerator complex. Source of the figure: [34].

Table 2: Main parameters of LHC [31]

Circumference	27 km
Dipole operating temperature	1.9 K
Number of magnets	9593
Number of main dipoles	1232
Number of main quadrupoles	392
Number of RF cavities	8 per beam
Nominal energy, protons	7 TeV
Nominal energy, lead ions	2.76 TeV per nucleon
Peak magnetic dipole field	8.33 T
Min. distance between bunches	7 m
Design luminosity	$10^{34} \text{ cm}^{-2} \text{ s}^{-1}$
No. of bunches per proton beam	2808
No. of protons per bunch (at start)	$1.1 \times 10^{11}$
No. of collisions per second	600 millions

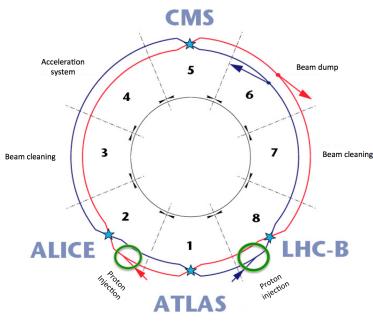
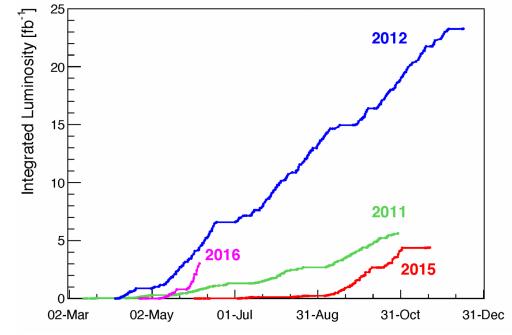


Figure 17: Schematic view of LHC sectors. Figure 18: LHC integrated luminosity by year.

Source of the figure: [36].



Source of the figure: [35].

### 3.2 Compact Muon Solenoid

#### 3.2.1 Introduction

CMS is a general-purpose detector designed for detecting various particles which are being produced in pp collisions at LHC. Its main feature is a huge magnet to create a magnetic field of 4T to curve charged particles in the tracking system and 2T outside to curve muons in the muon system.

CMS detector is a cylindrically symmetric with a colliding beam as a central axis. The detector consists, from inner to outer layer, of a tracking system, an electromagnetic calorimeter (ECal), a hadronic calorimeter (HCal), a magnet and a muon system. Having the tracking system, ECal and HCal inside of a large solenoid makes the detector "compact". A segment of a CMS slice in  $r - \phi$  plane is shown in Fig. 19.

When a heavy particle is produced in a collision, it decays immediately, and we detect its long-living decay products including an electron, a photon, a muon, a neutral hadron or a charged hadron. Depending on the trace left by a particle in different subdetectors we can identify a particle. Electrons and positrons leave curved tracks in the tracking system and then induce showers in the electromagnetic calorimeter (ECal) where they are typically stopped. Photons induce the same electromagnetic showers in ECal however, as neutral particles, they do not leave tracks in the tracking system. Hadrons normally travel through the ECal undisturbed and induce a hadronic shower in the hadronic calorimeter (HCal). Charged and neutral hadrons can be distinguished from each other by checking whether they leave a track in the tracking system or not. Muons are the only particles which are not stopped by the layer of ferrum and leave tracks in the CMS muon system. Neutrinos are not detected by CMS.

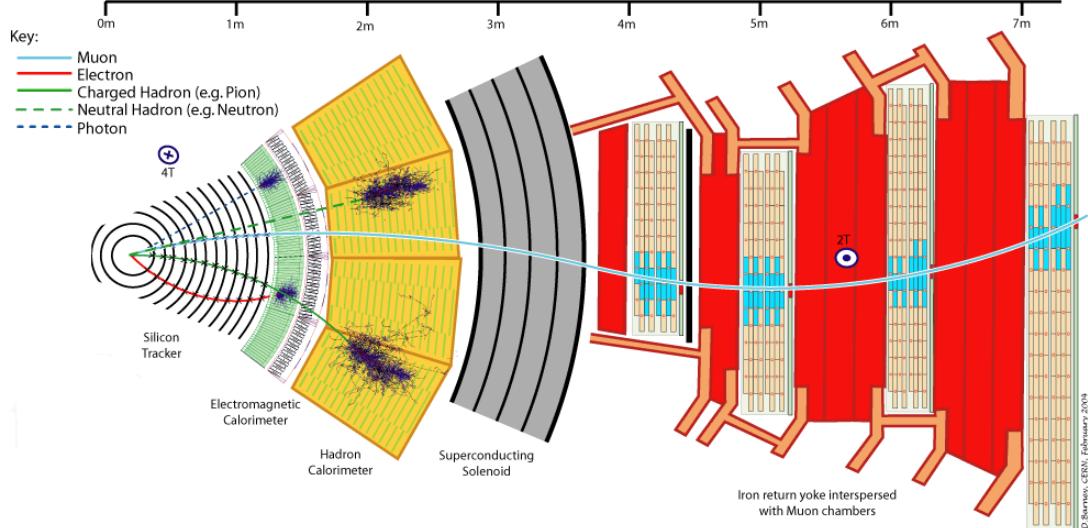


Figure 19: CMS slice.

In  $W\gamma$  measurement we have muons and electrons as final state particles. They are both affected by CMS magnetic field allowing the tracking system and the muon system to measure their trajectory parameters and momenta.

In this dissertation we use the information of the primary vertex determined by the tracking system to select our events. Also the tracker provide us the information about electrons trajectories and momenta in the electron channel and distinguishes between electrons and photons.

754

755 **3.2.2 Magnet**

756 A magnetic field in a particle detector is necessary to measure momenta of charged particles  
757 by track curvatures. The higher the momentum is, the less a particles's path is affected by the  
758 magnetic field. In CMS it is done in the tracking system for all charged particles and in the  
759 muon system for muons.

760

761 The CMS magnet is placed between layers of HCal and a muon system. It creates a magnetic  
762 field of 4T inside the magnet, for the tracking system, and 2T outside the magnet, for the muon  
763 system. It is necessary to have stronger field in the tracking system because a density of tracks  
764 is much higher there than in the muon system and also the tracking system is much smaller and,  
765 therefore, more significant curvature is necessary to measure the momentum with high precision.

766

767 The magnet is made of superconducting wires. An electric current flowing in the wires creates  
768 a uniform field inside the solenoid and also provides a magnetic field of a certain configuration  
769 outside the solenoid.

770

771 **3.2.3 Tracking System**

772 The tracking system measures track geometry including particles trajectories and locations of  
773 primary and secondary vertices and momenta of charged particles. It needs to disturb particles  
774 as little as possible so that they can pass through. Therefore, just a few measurements must be  
775 enough to reconstruct the track. The accuracy of a measurement of each hit is  $10 \mu\text{m}$ .

776

777 The tracking system consists of silicon pixels and silicon strips (Fig. 20). Collision tracks  
778 start at the center and then cross the layers of the tracking system. Tracks are straight in  $r - z$   
779 plane and curved by the magnetic field in the  $r - \phi$  plane. The acceptance of the tracker sys-  
780 tem in  $r - z$  plane is geometrically limited by  $\eta = 2.5$  ( $\eta = -\ln[\tan \theta/2]$ , where  $\theta$  is a polar angle).

781

782 The pixel tracker is the closest subsystem of CMS to the collision point thus it receives the  
783 largest particle flux: at 8 cm from the collision point the flux is about 10 million  $1/(cm^2 s)$ , and  
784 the pixel detector with its 65 millions sensors is capable to reconstruct all these tracks. It consists  
785 of three layers of cylinders in the barrel with radii of 4 cm, 7 cm and 11 cm and four disks in  
786 the endcap, two disks at each side. The tracker is designed in such a way that a single track hits  
787 multiple sensors. Then the trajectory is reconstructed based on how much charge is collected on  
788 each sensor. This allows us to reach a spacial resolution of  $15\text{-}20 \mu\text{m}$  which is much smaller than  
789 a distance between sensors.

790

791 The strip tracker is placed right after the pixel tracker and occupies the detector volume up  
792 to 130 cm around the beam axis. The strip tracker consists of four parts: the tracker inner barrel  
793 (TIB), the tracker inner disks (TID), the tracker outer barrel (TOB) and the tracker endcap  
794 (TEC) as shown in Fig. 20. In the strip tracker there are over 15,000 sensitive modules with a  
795 total number of 10 million strips. Each sensitive module consists of a set of sensors, its support  
796 structure and readout elements.

797

798 **3.2.4 Electromagnetic Calorimeter**

799 The ECal measures energy of electrons and photons and also measures geometries of their tra-  
800 jectories. Electrons and photons interact with the ECal substance by inducing electromagnetic  
801 showers. Traces left by photons and electrons in the ECal are the same. To distinguish between  
802 these two particles, it is necessary to perform matching to the track in the tracking system. If

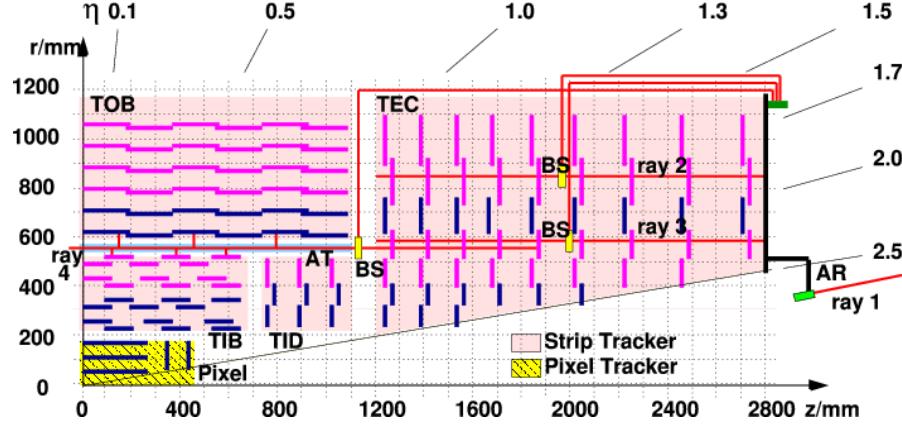


Figure 20: Slice of the CMS tracking system in  $r - z$  plane.

there is a track, then there is an electron (or positron). If there is no track, then the particle is a photon.

The Ecal is a layer between the tracking system and the HCal. It is made of high-density lead tungstate crystals arranged in a barrel section and two endcap sections. The crystals work as scintillators. When electrons and photons pass through it, it produces light proportional to the particle's energy. The scintillated light then is amplified by photomultipliers producing signals on sensitive elements.

It is important for the Ecal to be able to distinguish between high energetic photons and pairs of lower energetic photons e.g. from a  $\pi^0$  decay. It is especially difficult in the endcap sections where angle between two photon trajectories is small. Ecal preshower located in front of the endcaps which have much smaller granularity provide extra spacial precision. Their strips are 2 mm wide compared to 3 cm wide crystals in the main volume of the ECal.

### 3.2.5 Hadron Calorimeter

The HCal is placed right after the ECal and is the last subdetector within the magnet. The HCal measures energies of charged and neutral hadrons. In addition, the HCal determines the track parameters. Match to the tracking system has to be done: if a matching track found, then it is a charged hadron otherwise it is a neutral hadron.

The HCal consists of alternate layers of absorbers and scintillators. Hadrons hit brass or steel plate of absorber producing secondary particles. When emerge into the scintillator, the particles induce hadronic and electromagnetic showers and emit blue-violet light which is further shifted to the green region and read out by special boxes within the HCal. The secondary hadrons produced during the interaction with the absorber interact with the next absorber producing more showers in the next layers of scintillators and also affect the total energy deposit. All hadrons must be stopped inside the layers of the HCal.

### 3.2.6 Muon System

Muons pass through the ECal, the HCal and the magnet without interacting. They are the only particles which are registered in the muon system which is placed outside the magnet and which is the largest part of CMS detector.

836  
 837 There are four concentric layers of muon detectors (stations) and iron return yoke between  
 838 them. Muons induce several hits in the muon stations which are later fitted and matched to the  
 839 tracking system measurements to provide the best possible resolution in the measurements of all  
 840 parameters of the muon's trajectory and momentum.

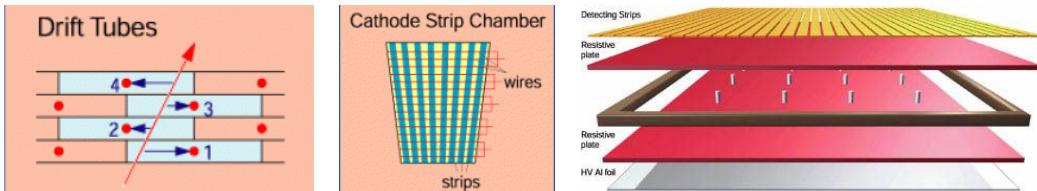
841  
 842 There are three types of muon chambers used in the CMS muon system: drift tubes (DTs),  
 843 cathode strip chambers (CSCs) and resistive plate chambers (RPCs). Overall, there are 1400  
 844 muon chambers including 250 DTs, 540 CSCs and 610 RPCs.

845  
 846 The system of DTs measures positions of muons in the barrel. Each DT chamber is about 2 m  
 847 by 2.5 m in size. It consists of 12 layers of aluminium which are grouped by four. There are up  
 848 to 60 drift tubes in a layer. The middle group of layers measures  $z$ -coordinate and two other  
 849 groups determine the perpendicular coordinate.

850  
 851 Each drift tube is 4 cm in width, is filled with a gas and has a wire inside. When a charged  
 852 particle passes through the volume, it ionizes atoms and the wire receives an electric charge.

853  
 854 CSCs are placed in endcap regions. CSCs are arrays of anode wires which are crossed by  
 855 copper cathode strips placed in a gas volume. When a charged particle penetrates to the gas  
 856 volume, it ionizes the gas. Electrons drift to the wires while ions move to the strips. Strips are  
 857 perpendicular to wires, thus, we measure two coordinates for each particle.

858  
 859 RPCs are parallel capacitors made of high-resistivity plastic plates with a space between  
 860 them filled with a gas. RPCs provide quick measurements of muon momenta and are used for  
 861 triggering.



862  
 863 Figure 21: Components of the CMS muon system. Left to right: drift tubes, cathode strip  
 864 chambers (CSCs), resistive plate chambers (RPCs).

### 863 3.2.7 Triggering and Data Aquisition

864 At peak luminosity, CMS experiences one billion proton-proton collisions per second which come  
 865 in bunches separated just by 25 ns from one other. New events come before the events from  
 866 the previous bunch crossing left the detector. To process the information from many different  
 867 collisions at the same time, data is stored in pipelines.

868  
 869 It is not technically possible to readout all these events. Moreover, we do not need most  
 870 of these events for a physics analysis because most of these events do not have a potential to  
 871 discover a new physics. We have resources to store about one hundred events out of one billion  
 872 that is why we need a trigger system which quickly decides what the best one hundred events are.

873  
 874 If the triggers were too loose, and we would select one hundred events too quickly, e.g., out  
 875 of a hundred million events, then CMS would not be able to process the rest 90% of events in a

givem set of one billion and we would lose 90% of potentially interesting events.

877

878 If the triggers were too strict, we would select, e.g, ten events out of one billion, not one  
879 hundred and lose CMS potential to store and process data by 90% which would significantly  
880 reduce our chances for a discovery.

881

882 Thus, the challenge of the trigger system is to select the best one hundred events out of one  
883 billion and do that fast to be able to process every single event. To achieve this goal, a two-level  
884 trigger system was developed consisting from the Level 1 (L1) trigger and the high level trigger  
885 (HLT) as shown in Fig. 22.

886

887 L1 is a hardware based trigger (Fig. 23). It uses information from the ECal, HCal and muon  
888 system. L1 reduces frequency of coming events from 40 MHz to 100 kHz. Events which did not  
889 pass the L1 trigger are lost forever while events which pass the L1 trigger are temporarily stored  
890 to get checked by the HLT.

891

892 HLT is a software-based trigger. It uses information from all subdetectors and runs quick  
893 reconstruction and identification algorithms to determine types of particles and their kinematics.  
894 It reduces the number of events to 100 Hz. Events which did not pass HLT are lost forever.  
895 Events which pass HLT are arranged into appropriate datasets depending on HLT selection cri-  
896 teria they passed and stored for physics analyses.

897

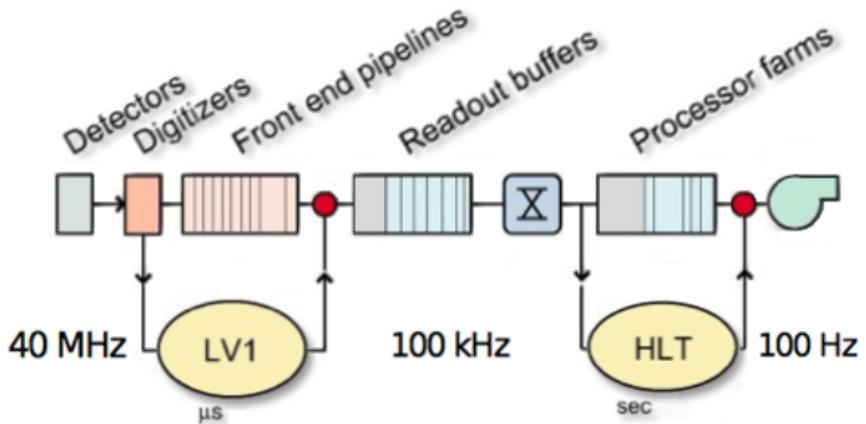


Figure 22: Two-level CMS trigger system.

### 898 3.2.8 Event Reconstruction

899 Where to place particle reconstruction, particle flow algorithm and MET? Check other theses

900 Acceptance: particles which are too collinear and go to pipe; particles which get curved too  
901 strongly

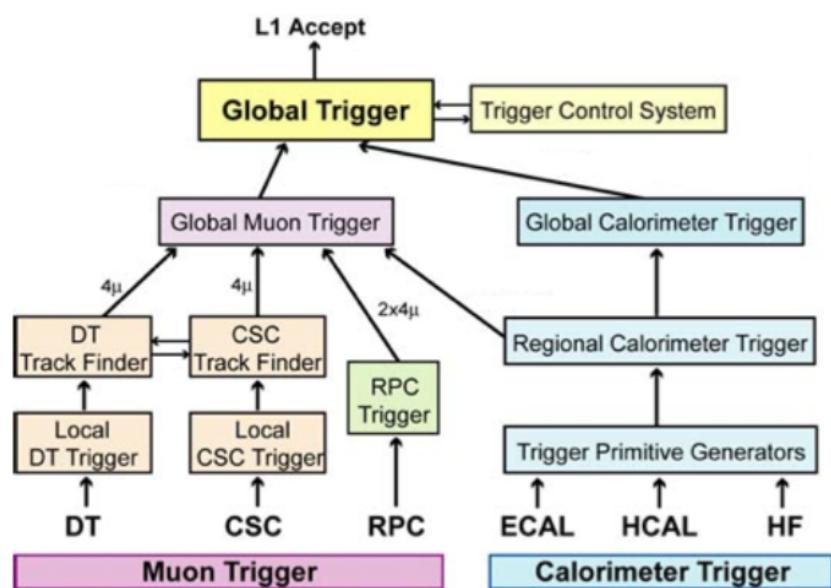


Figure 23: Level 1 CMS trigger system.

902 **4 CMS Tracker Alignment**

---

## 903 4.1 Algorithm

904 Why align?

905 How to align?

906 When align?

907 How to check that your alignment is good?

908

909 A tracking system detects hits produced by a charged particle traveling through the detector.  
 910 In a presence of a constant magnetic field the particle has a helical trajectory. A reconstruction  
 911 algorithm determines the track parameters by fitting the positions of hits assuming the helix  
 912 trajectory.

913

914 Better hit resolution and the location uncertainty lead to better precision of a measurement  
 915 of the track parameters. The location uncertainty depends on our knowledge of the positions and  
 916 orientations in space of the tracking system modules. The hit resolution in the CMS pixel detector  
 917 is  $\sim 15 \mu\text{m}$ . When the modules are mounted, their positions are known with precision of  $\sim 200 \mu\text{m}$ .  
 918 Thus, we need to know positions of modules 20 times better than they are known when mounted.

919

920 The procedure of the determination of the modules locations and orientations is called the  
 921 tracker alignment. The concept of the track-based alignment can be illustrated in the example of  
 922 the alignment of a toy tracker. When a charged particle passing through a detector (Fig. 24, top  
 923 left) it crosses a toy tracker which consists of six flat equidistant modules (Fig. 24, top right). If  
 924 the modules were placed exactly at their designed positions, we would observe the hits exactly at  
 925 the points where the track crosses modules at the points of ideal geometry (Fig. 24, middle left).  
 926 However, in a reality the positions and tilts of the modules are different from ones suggested by  
 927 the ideal geometry (Fig. 24, middle right). Hits, indeed, are recorded at the places where mod-  
 928 ules are actually mounted, not at the design ideal places (Fig. 24, bottom left). If we assumed a  
 929 tracker to be ideal and a track to be smooth, we would see that our hits are off-track (Fig. 24,  
 930 bottom right). So, we recalculate positions of the modules so that all the hits are laying on the  
 931 same smooth track (Fig. 25, top left). But these recalculated positions still do not coincide with  
 932 the actual positions (Fig. 25, top right). Then we record more and more tracks (Fig. 25, middle  
 933 left and right). We take into account them all and determine the alignment parameters with  
 934 necessary precision (Fig. 25, bottom left and right).

935

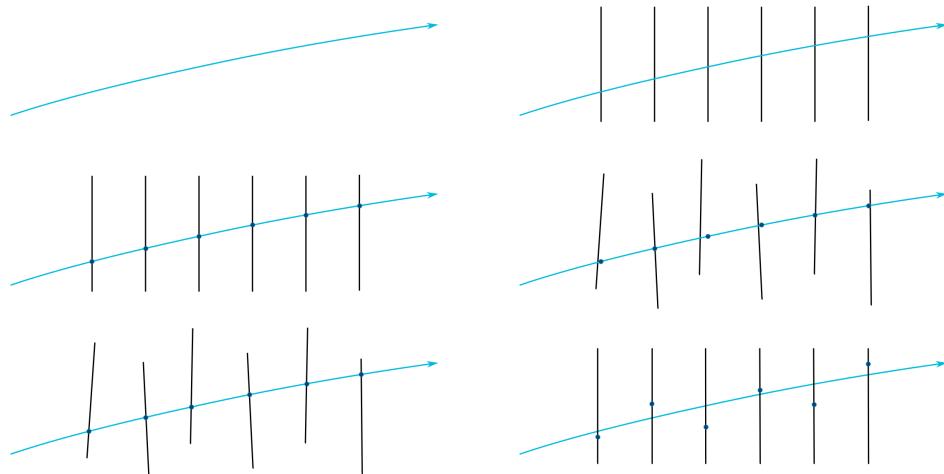


Figure 24: The alignment of a toy tracker, part 1.

936

When we record a track with a not-aligned tracker, we see that the track is not smooth. But

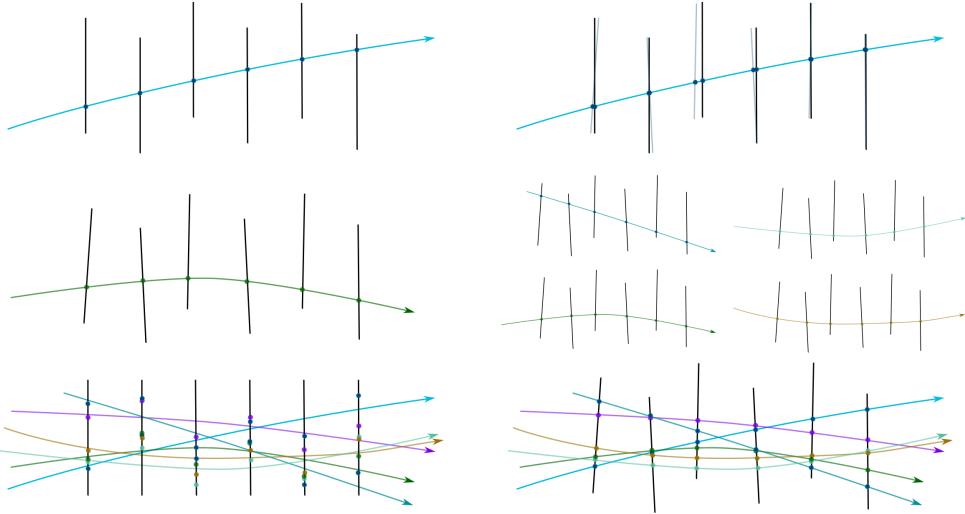


Figure 25: The alignment of a toy tracker, part 2.

937 that is because our knowledge of module positions is not exact. Thus, we can correct the posi-  
 938 tions assuming the track is smooth. But when we process the next track, we may find out that  
 939 the positions have to be corrected again. Thus, we record many tracks and minimize residuals  
 940 between measured and predicted hits.

941  
 942 The CMS tracker contains 1440 silicon pixel modules in PXB and PXF and 15148 silicon  
 943 strip modules in TIB, TOB, TID, TEC.

944  
 945 The tracker alignment problem is the least squared problem. The expression to minimize is  
 946 the following:

$$\chi^2(\mathbf{p}, \mathbf{q}) = \sum_j^{\text{tracks}} \sum_i^{\text{tracks}} \left( \frac{m_{ij} - f_{ij}(\mathbf{p}, \mathbf{q}_j)}{\sigma_{ij}} \right)^2 \quad (34)$$

948 where  $\mathbf{p}$  are parameters describing the tracker geometry,  $\mathbf{q}_j$  are parameters of the  $j^{th}$  track,  
 949  $m_{ij} - f_{ij}$  are residuals, distances between the measured hit and a position predicted by the track  
 950 fit,  $\sigma_{ij}$  is the Gaussian error of the measurement.

951  
 952 We can align the large substructures and individual modules with respect to their substruc-  
 953 tures. The parameters to align large substructures include their positions and orientations of the  
 954 subdetectors (rotations). Thus, each subsystem is described by six parameters: three coordinates  
 955 X, Y, Z and three angles  $\alpha, \beta, \gamma$ . At the module level, we align positions and rotations with  
 956 respect to the position s and angles of the corresponding large structure (Fig. 26). In addition,  
 957 at the module level we align for surface deformations which are described by three parameters  
 958 per sensor (Fig. 27).

959 A track can be described with five parameters.

960 We have two alignment algorithms: Millepede and HIP. Millepede performs a simultaneous fit  
 961 of all alignment parameters and all track parameters while HIP performs iterative fits of alignment  
 962 parameters  $\mathbf{p}$  and track parameters  $\mathbf{q}_j$ .

963  
 964 It is important to use different sorts of tracks for the alignment. Cosmic tracks pass through  
 965 the detector vertically and do not allow us to connect different subdetectors to one another.

967 Collision tracks originate from the collision point and go in all directions. However, those tracks  
 968 which cross TEC are all almost collinear and, therefore, it is difficult to measure  $z$ -coordinate of  
 969 TEC modules with collision tracks only.

970

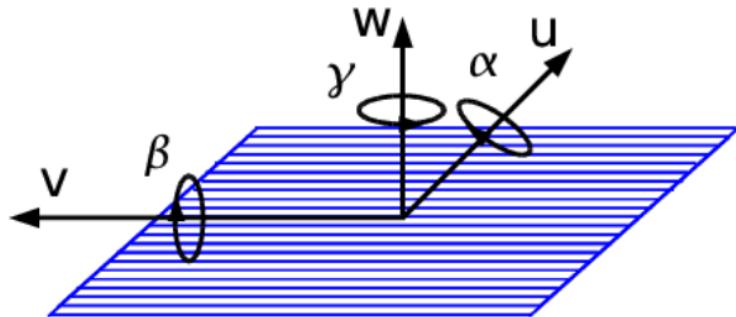


Figure 26: Alignment parameters.

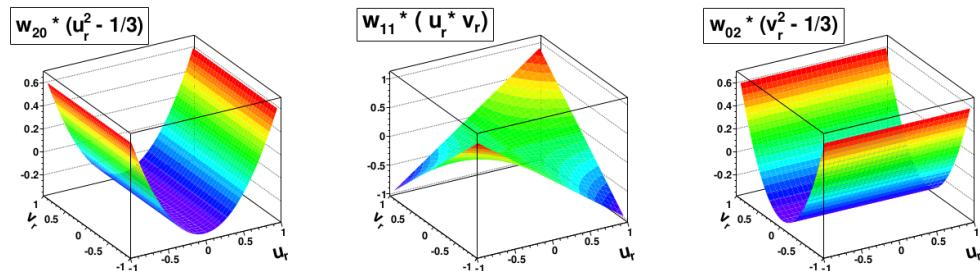


Figure 27: Surface deformations.

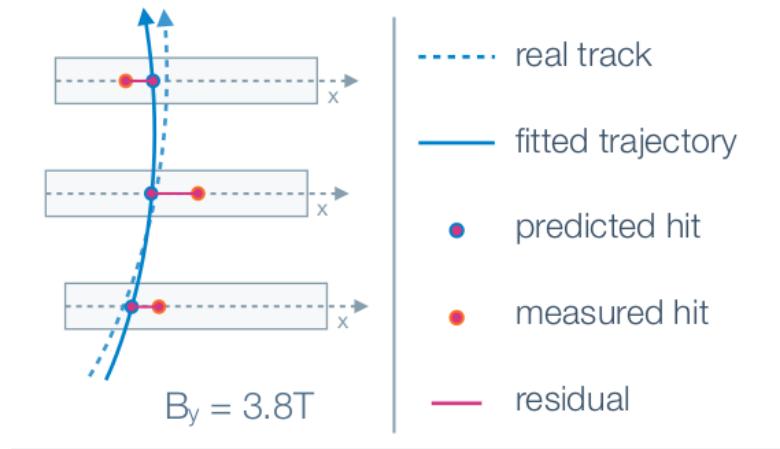


Figure 28: Track residuals.

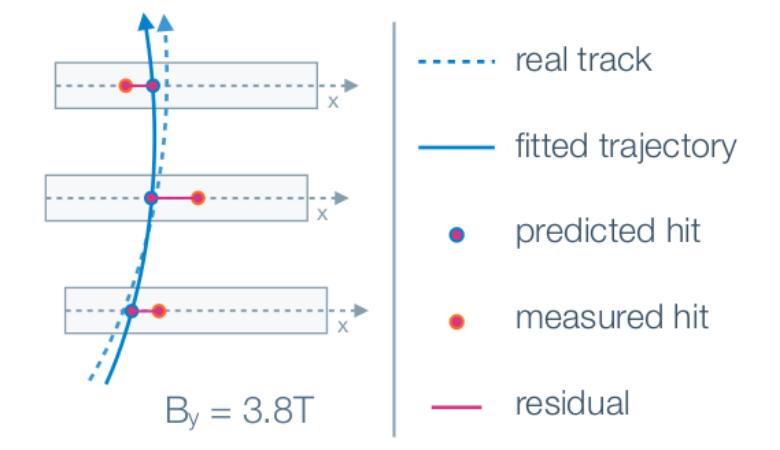


Figure 29: Track residuals.

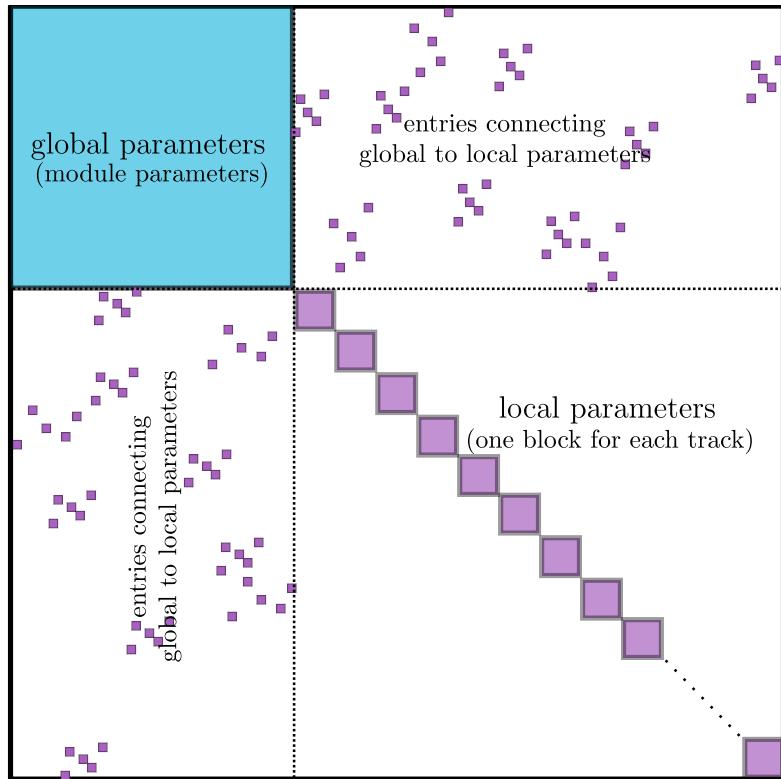


Figure 30: Track residuals.

971 **4.2 Selected Results**

972 CRUZET, CRAFT and first collisions of 2015

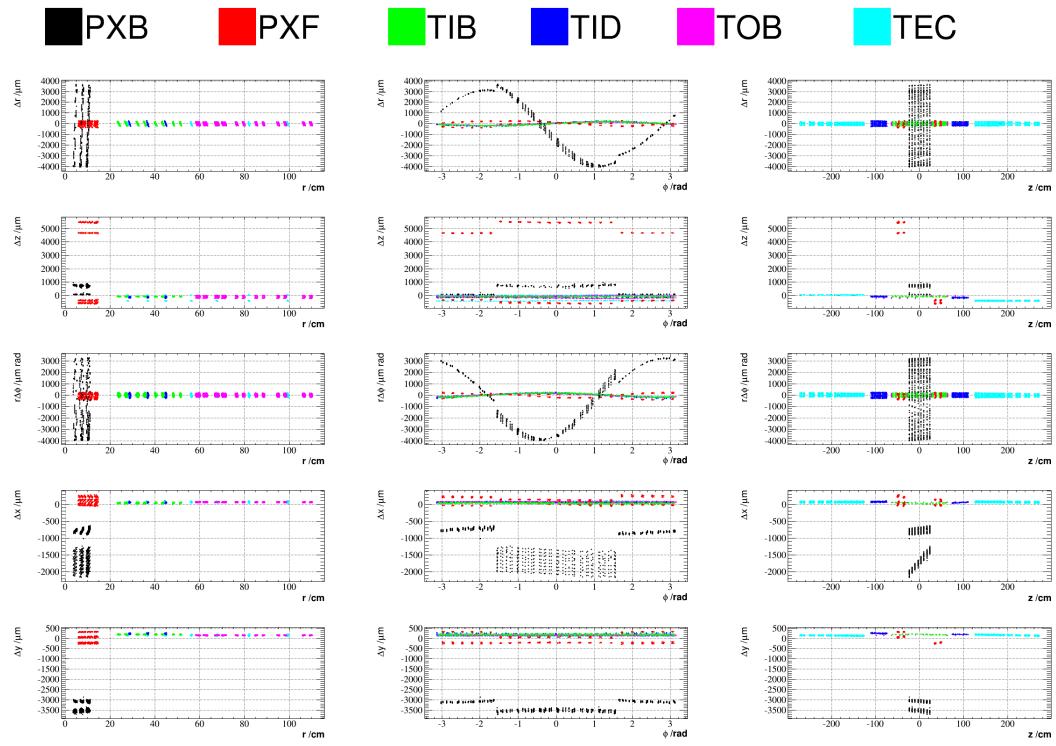


Figure 31: Geometry comparison plot of CRUZET 2015 object vs Run I.

**973 5  $W\gamma$  Cross Section Measurement**

974 Place analysis outline here

## 975 References

- [1] Griffiths textbook  
[2] website: <http://www.isgtw.org/spotlight/go-particle-quest-first-cern-hackfest>  
[3] CMS Paper about Higgs boson discovery  
[4] ATLAS Paper about Higgs boson discovery  
[5] website: <https://mstwpdf.hepforge.org/>  
[6] Pich lectures: The Standard Model of Electroweak interactions  
[7] PDG  
[8] Halzen, Martin "Quarks and leptons"  
[9] <http://iopscience.iop.org/article/10.1088/0034-4885/70/1/R02>  
[10] Peskin, Schroeder  
[11] Lindsey's thesis (CMS Zg- $\zeta$ llg, 7 TeV)  
[12] website: [https://www-d0.fnal.gov/results/publications\\_talks/thesis/snyder/html/node17.html](https://www-d0.fnal.gov/results/publications_talks/thesis/snyder/html/node17.html)  
[13] website: [https://en.wikipedia.org/wiki/Cross\\_section\\_%28physics%29](https://en.wikipedia.org/wiki/Cross_section_%28physics%29)  
[14] LO (1969) theory paper  
[15] NNLO theory paper  
[16] NLO theory paper  
[17] aTGC paper  
[18] Senka's thesis (CMS Wg- $\zeta$ munug, 7 TeV)  
[19] D0 Combination of  $W\gamma$ , WW, WZ and VW using 8.6 fb-1 of 2 TeV  $p\bar{p}$  collisions Phys.Lett. B718 (2012) 451-459  
[20] LEP Combination of WW and single W using 0.7 fb-1 per experiment of  $e^+e^-$  collisions at WW pair production energies arXiv:1302.3415  
[21] 7TeV Wg ATLAS paper  
[22] ATLAS WW using 20.3 fb-1 of 8 TeV pp collisions Submitted to JHEP  
[23] ATLAS VW ( $V=W,Z \rightarrow jj$ ) using 4.6 fb-1 of 7 TeV pp collisions JHEP 01 (2015) 049  
[24] website: [https://twiki.cern.ch/twiki/bin/view/CMSPublic/PhysicsResultsSMPaTGC#Figure\\_1\\_Limits\\_on\\_WW](https://twiki.cern.ch/twiki/bin/view/CMSPublic/PhysicsResultsSMPaTGC#Figure_1_Limits_on_WW)  
[25] 7TeV Wg CMS paper  
[26] CMS WW using 4.9 fb-1 of 7 TeV pp collisions Eur. Phys. J. C 73 (2013) 2610  
[27] CMS WW using 19.4 fb-1 of 8 TeV pp collisions Submitted to EPJC  
[28] CMS VW ( $V=W,Z \rightarrow jj$ ) using 5.0 fb-1 of 7 TeV pp collisions Eur.Phys.J. C73 (2013) 2283  
[29] CMS 8 TeV WW lnlnmu  
[30] CMS 7 TeV Zg nunug  
[31] CERN brochure, <http://cds.cern.ch/record/1165534/files/CERN-Brochure-2009-003-Eng.pdf>

- 1010 [32] LHC TDR
- 1011 [33] website: <http://home.cern/topics/large-hadron-collider>
- 1012 [34] website: <http://cds.cern.ch/record/1621583/files/>
- 1013 [35] [http://home.cern/sites/home.web.cern.ch/files/image/update-for\\_cern\\_people/2016/06/intlumirunall\\_image.png](http://home.cern/sites/home.web.cern.ch/files/image/update-for_cern_people/2016/06/intlumirunall_image.png)
- 1014
- 1015 [36] website: <http://cds.cern.ch/journal/CERNBulletin/2014/24/News%20Articles/1706606>
- 1016 [37] website: <https://twiki.cern.ch/twiki/bin/view/CMSPublic/LumiPublicResults>