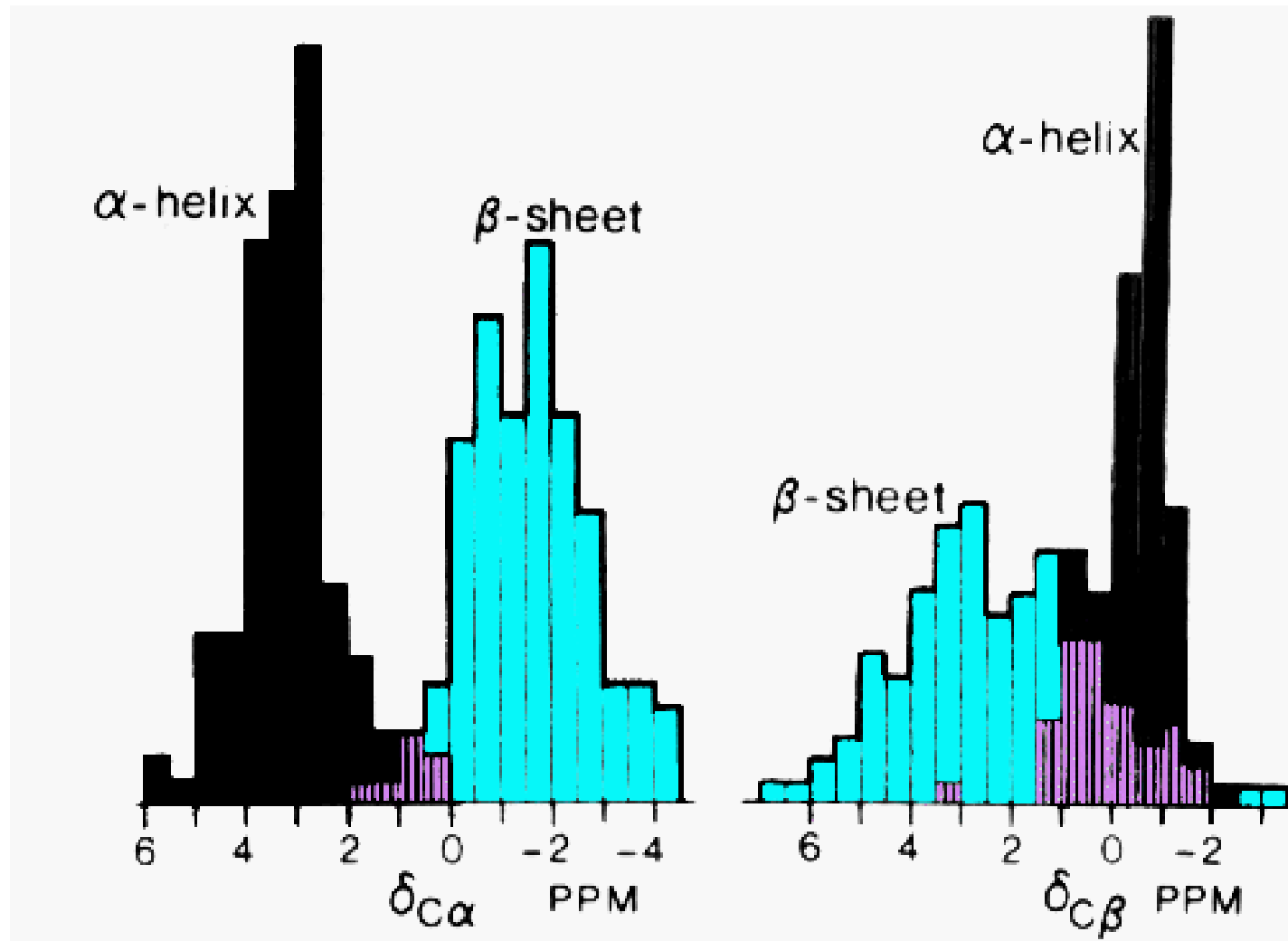


# Summary Lecture 10

*Secondary structure, distance restraints and preparation of calculation*

# Secondary chemical shifts encode secondary structure information



$$\delta C_{\alpha}(\text{exp}) - \delta C_{\alpha}(\text{RC})$$

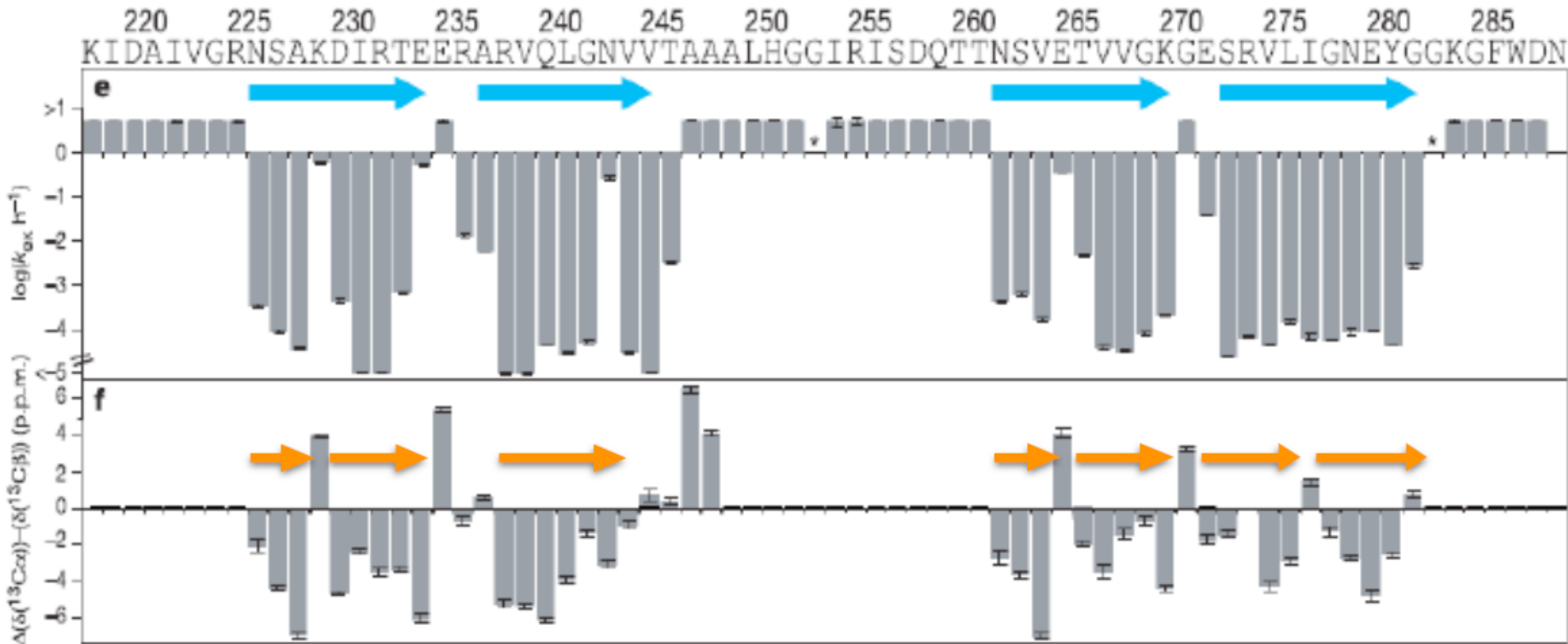
$$\delta C_{\beta}(\text{exp}) - \delta C_{\beta}(\text{RC})$$

# Chemical shifts encode secondary structure information

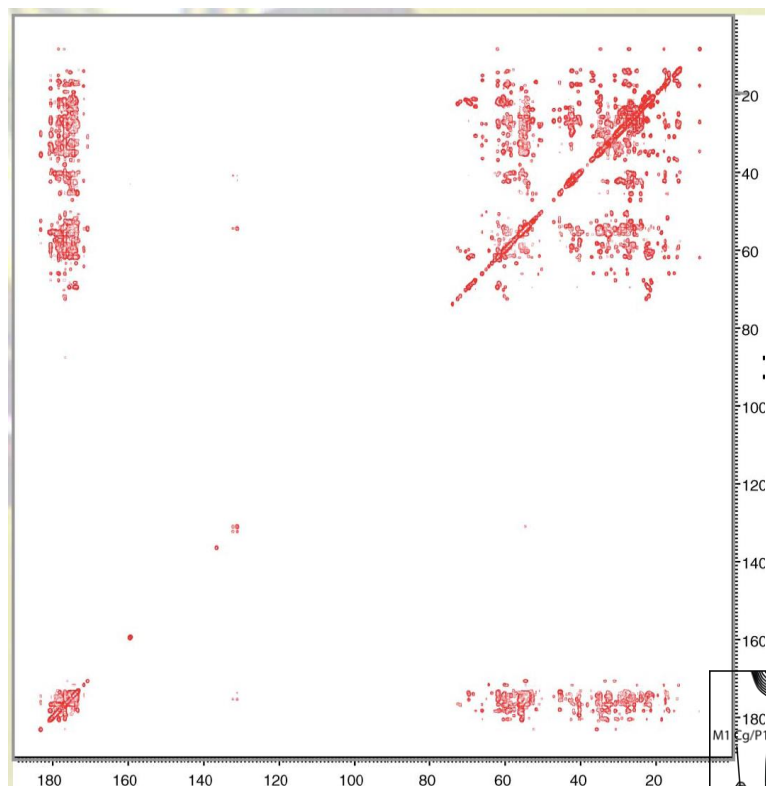
## Definitions

- a)  **$\alpha$ -helix**: At least 4 residues in a row with a positive secondary chemical shift
- b)  **$\beta$ -sheet**: At least 3 residues in a row with a negative secondary chemical shift

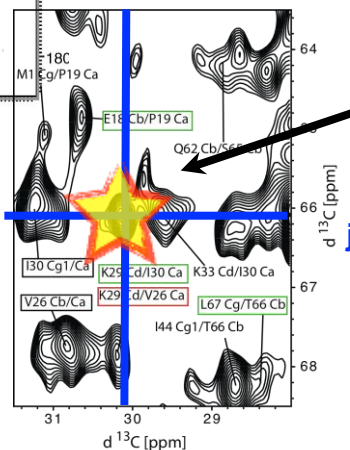
Example: HET-s       $(\delta C_{\alpha}(\text{exp}) - \delta C_{\alpha}(\text{RC})) - (\delta C_{\beta}(\text{exp}) - \delta C_{\beta}(\text{RC}))$



# Cross-Peak Intensities somehow represent the Dipolar Interaction



19 kHz MAS, 200 ms mix  
DARR, 258 K, 850 MHz,  
U-<sup>13</sup>C-<sup>15</sup>N Ubiquitin



Kinetic Master Equation for Populations  
(through perturbation theory)

$$\frac{d}{dt} \begin{bmatrix} p_1 \\ p_2 \\ \vdots \\ p_N \end{bmatrix} = \begin{bmatrix} W_{11} & W_{12} & \dots & W_{1N} \\ W_{21} & & & \\ \vdots & \vdots & \vdots & \vdots \\ W_{N1} & & & W_{NN} \end{bmatrix} \begin{bmatrix} p_1 \\ p_2 \\ \vdots \\ p_N \end{bmatrix}$$

$W_{ij}$ : Rate constants for Polarization Transfer

**Cross-Peak Intensity  
encodes dipole  
interaction  $d_{ij}$**

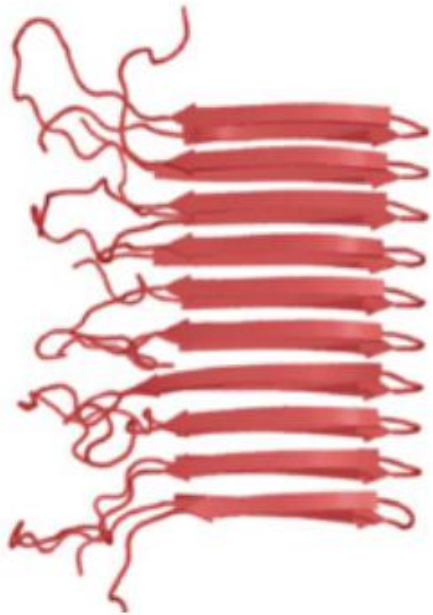
$$W_{ij} = \frac{\pi}{2} (d^{(i,j)})^2 f_{ij}(0)$$

# Distance Restraints

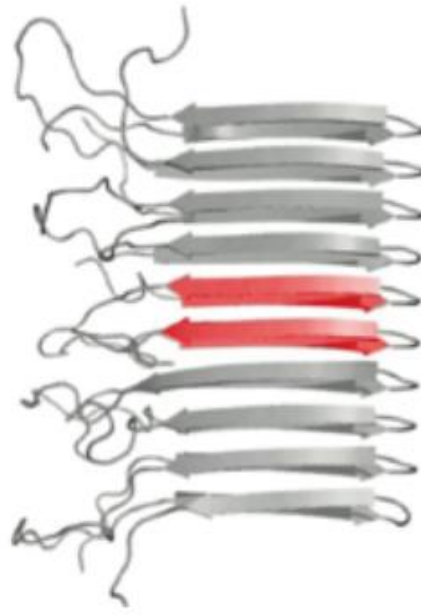
C-C	PDSD/DARR/MIRROR/ PAR
N-C	PAIN
H-H	CHHC, NHHC

# On which samples do we record these experiments?

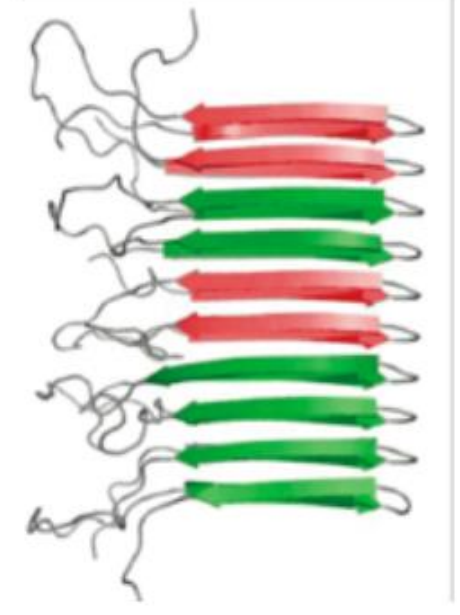
**Isotope labelling allows to disentangle the intra/inter problem**



All monomers labelled ( $^{15}\text{N}$ ,  $^{13}\text{C}$ )  
**intra** and **inter** constraints  
in PDSD / CHHC / NHHHC  
spectra  
+ PAR



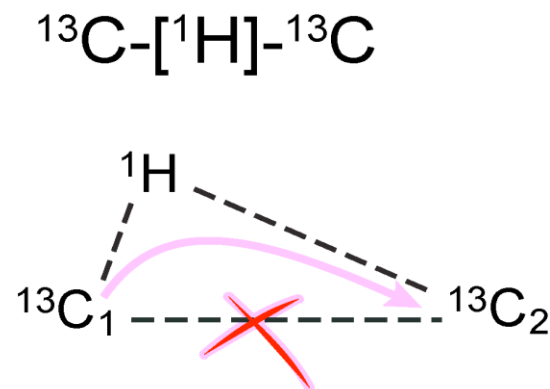
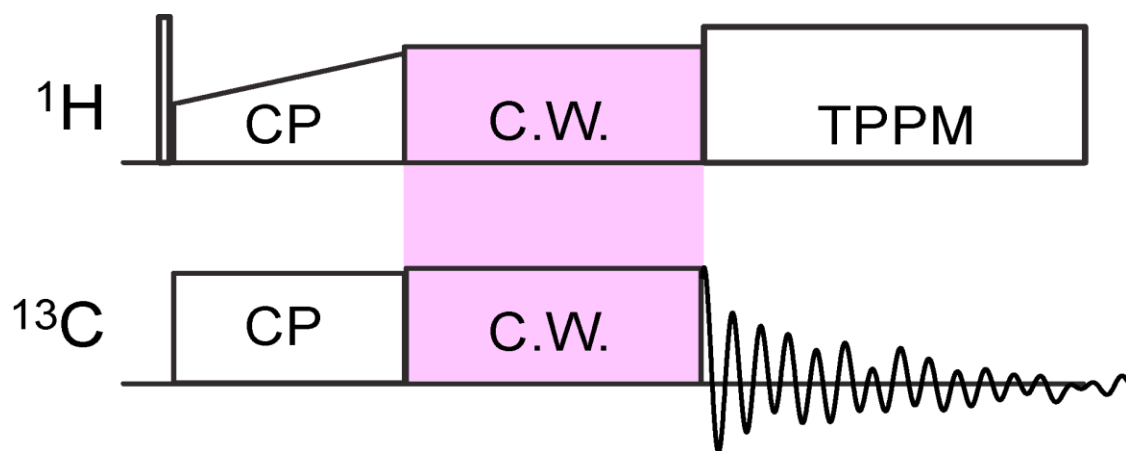
Labelled ( $^{15}\text{N}$ ,  $^{13}\text{C}$ )  
monomers diluted in  
natural abundance.  
**Only intra** constraints  
in PDSD / CHHC / NHHHC  
spectra + PAR



$^{13}\text{C}$  labelled monomers  
and  $^{15}\text{N}$  labelled monomers  
mixed.  
**Only inter** constraints  
(in NHHHC spectra)  
+ PAIN

# Proton assisted recoupling (PAR)

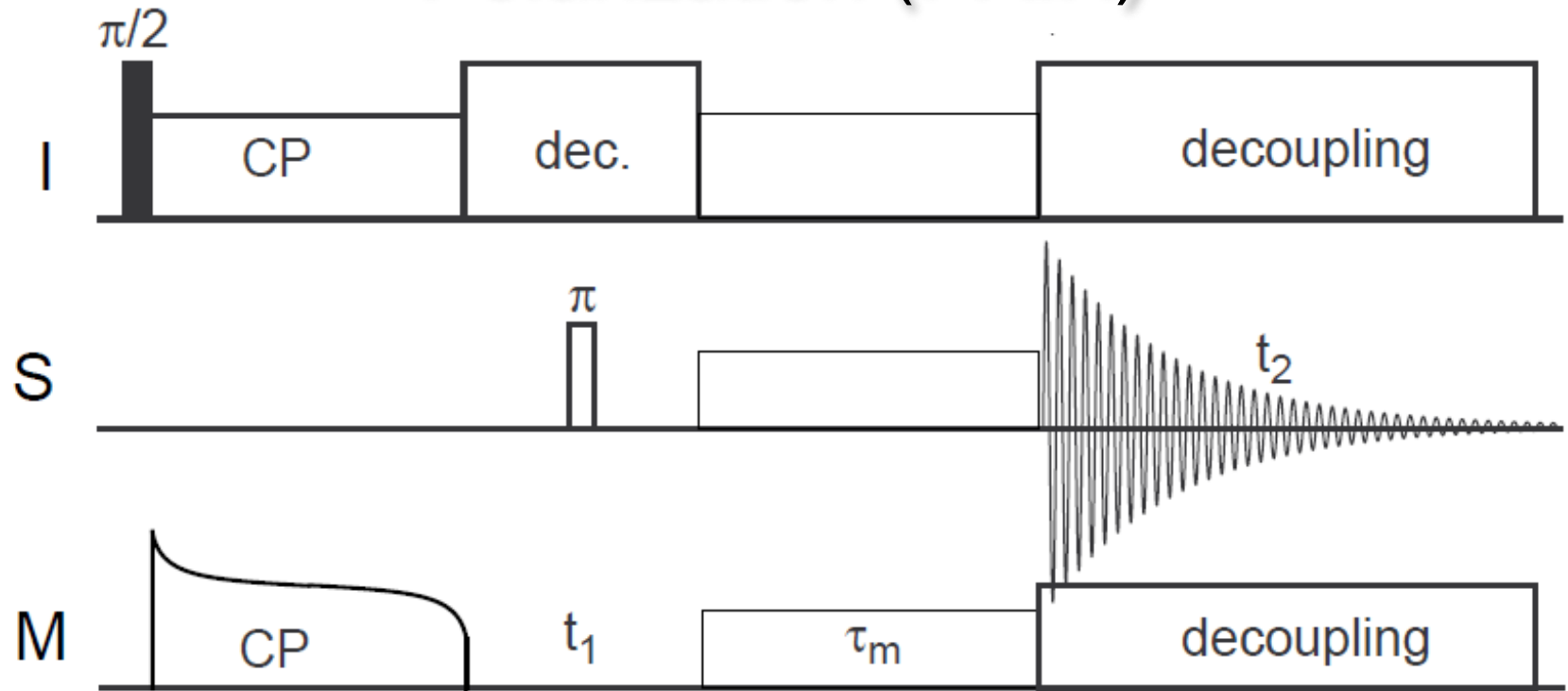
Non-resonant homonuclear correlation experiment.



Experimental aspects:

- Avoid Hartmann-Hahn matching conditions
- Avoid rotary resonance conditions

# Proton Assisted Insensitive Nuclei Cross Polarization (PAIN)



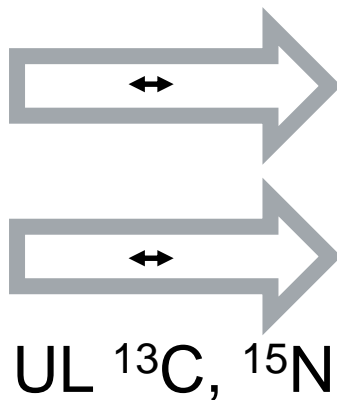
- Heteronuclear version of PAR
- Resonant polarization transfer

- Resonance condition  $\omega_{1S} - \omega_{1M} = n_r \omega_r$

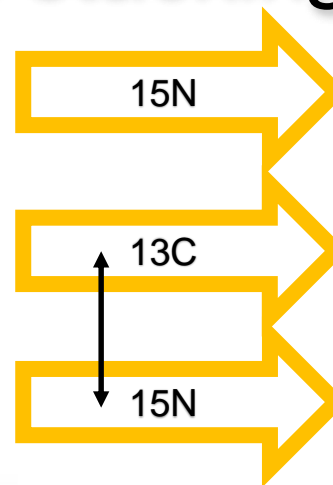


# PAIN to study fibril stacking

NCA

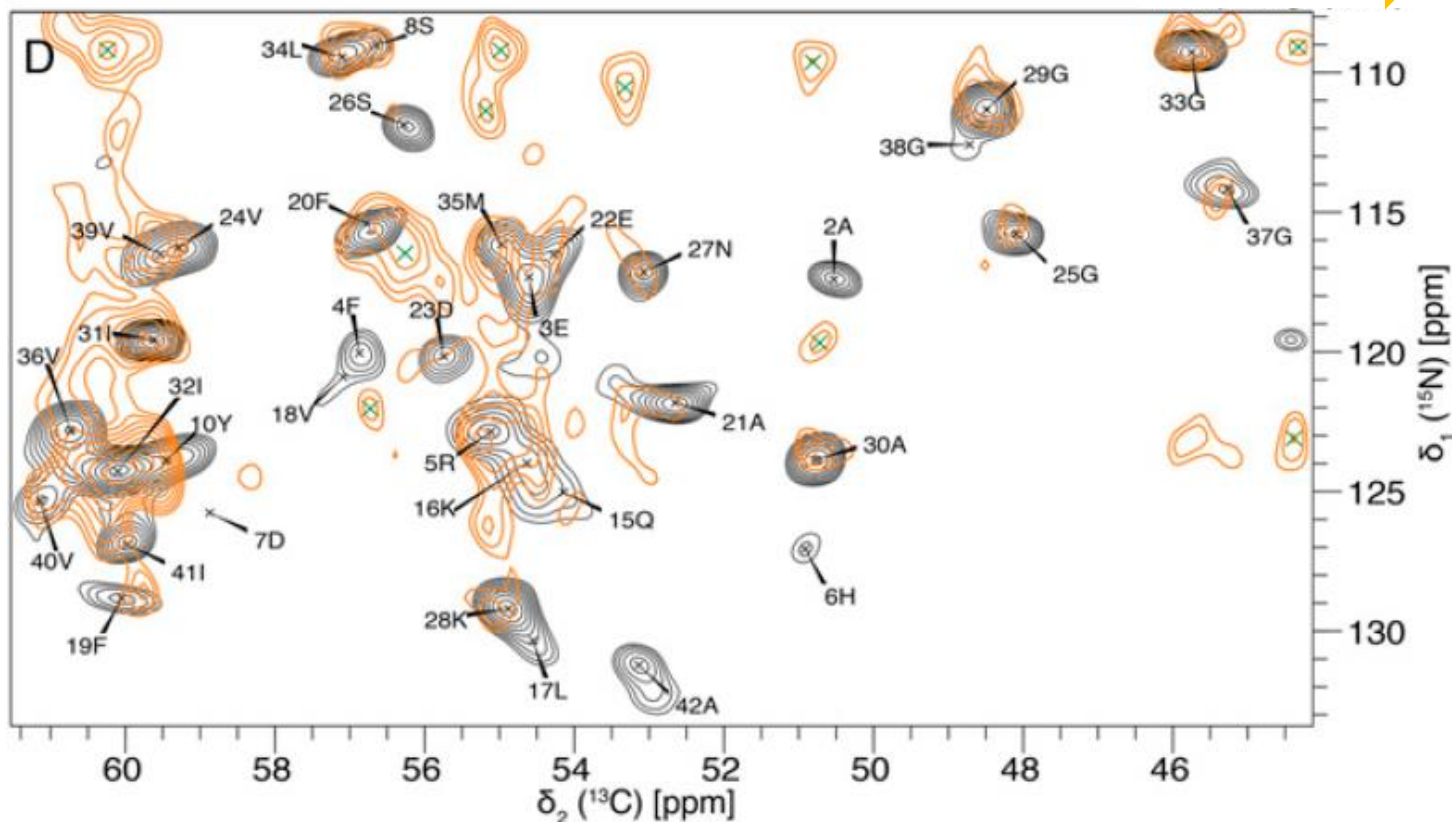


UL  $^{13}\text{C}$ ,  $^{15}\text{N}$



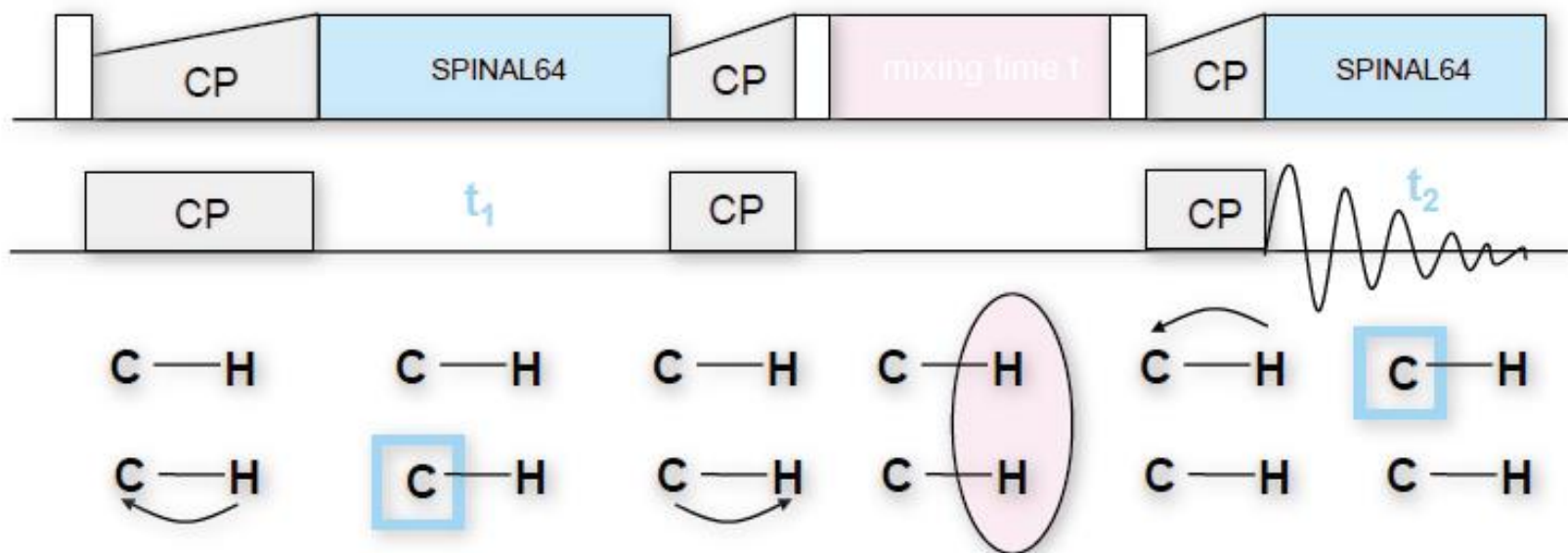
PAIN

Mixed labelled



***In-register  
parallel***

# The CHHC/NHHC experiments



$^{13}\text{C}$ - $^{13}\text{C}$  or  $^{15}\text{N}$ - $^{13}\text{C}$  correlation experiment

# Lecture 11

## *Structure calculation*

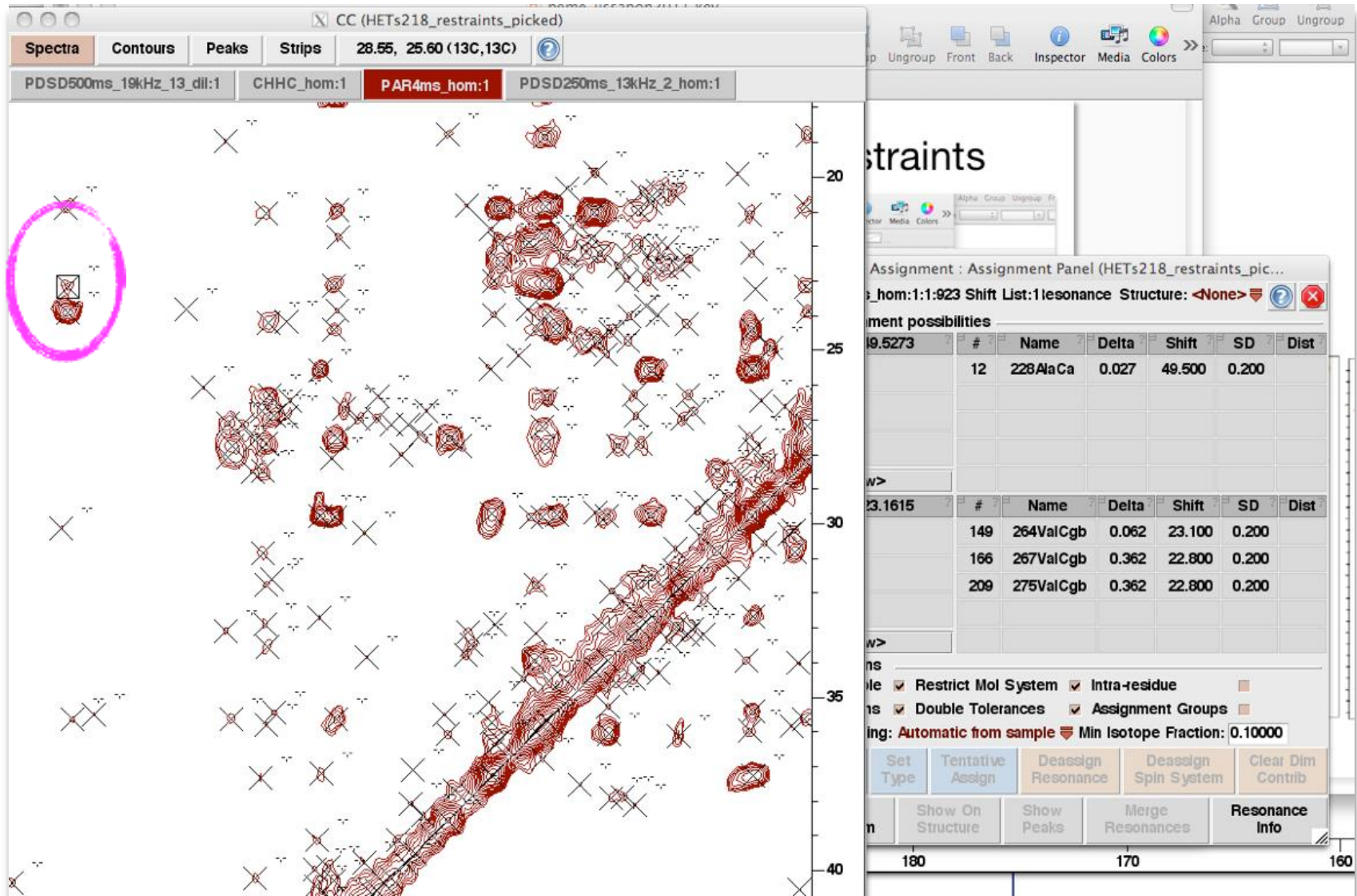
# CYANA

[www.cyana.org](http://www.cyana.org)  
[cyana wiki](#)

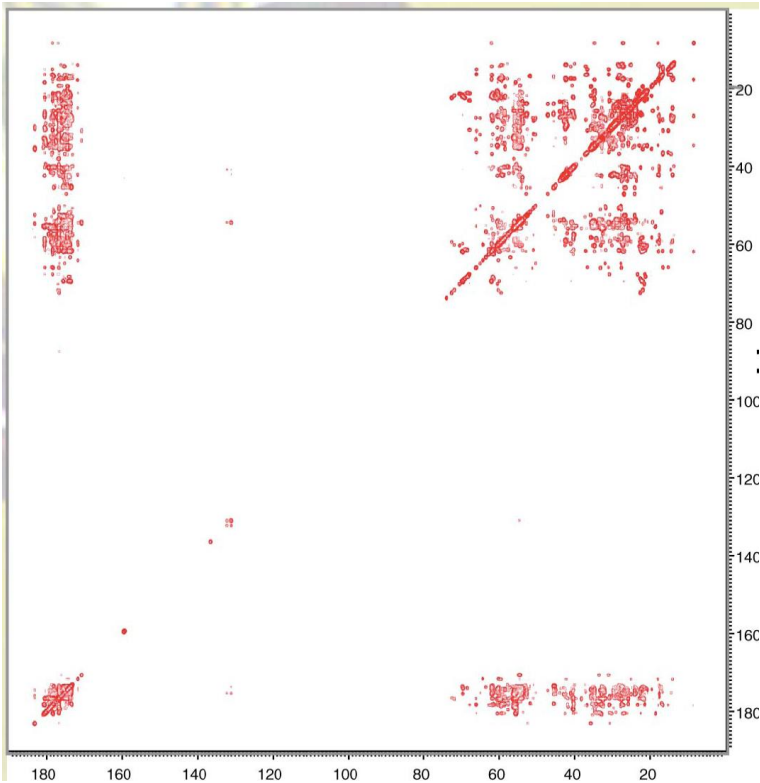
Peter Güntert

Institute for Biophysical Chemistry,  
Biomolecular Magnetic Resonance Center,  
and Frankfurt Institute for Advanced Studies  
Goethe University Frankfurt am Main

# Long-range restraints: assignment ambiguities



# Structure determination is an inverse problem

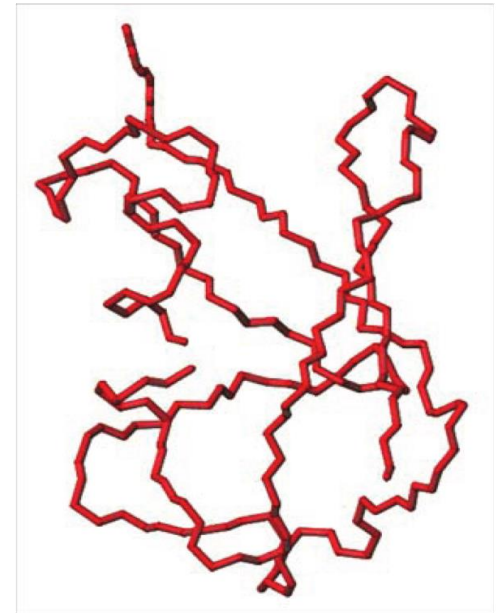


**calculate**

←

→

**???**



...but even the forward problem is not trivial

# Forward calculation in a simple approach

## ○ Rate approach for NOESY

$$p_i = \langle S_{iz} \rangle$$

*Initial rate approx.*

$$W_{ij} \sim r_{ij}^{-6}$$

$$I_{ij} \sim r_{ij}^{-6}$$

$$\frac{d}{dt} \begin{bmatrix} p_1 \\ p_2 \\ \vdots \\ p_N \end{bmatrix} = \begin{bmatrix} W_{11} & W_{12} & \cdots & W_{1N} \\ W_{21} & & \ddots & \\ \vdots & \vdots & \ddots & \vdots \\ W_{N1} & & & W_{NN} \end{bmatrix} \begin{bmatrix} p_1 \\ p_2 \\ \vdots \\ p_N \end{bmatrix}$$

## ○ Solids static (spin-diffusion concept by Bloembergen)

$$W_{ij} = \frac{(\mu_0 \hbar \gamma_i \gamma_j)^2}{32\pi} \frac{1}{r_{ij}^6} \cdot P_2(\cos \theta_{ij})^2 f_{ij}(0)$$

$$W_{ij} \cong \frac{k}{r_{ij}^6} \quad \text{Crude approximation}$$

## ○ MAS more complex!!! (but time dependent Liouville-von-Neumann equation works, of course)

# Forward calculation in a simple approach

- Complex relation between cross-peak intensity and local geometry
- BUT: no mechanism can lead to cross-peaks between nuclei if they are separated by more than an *upper distance*  $u_{ij}$
- $u_{ij}$  depends on the experiment performed
- many „unprecise“ *distance restraints* are defined

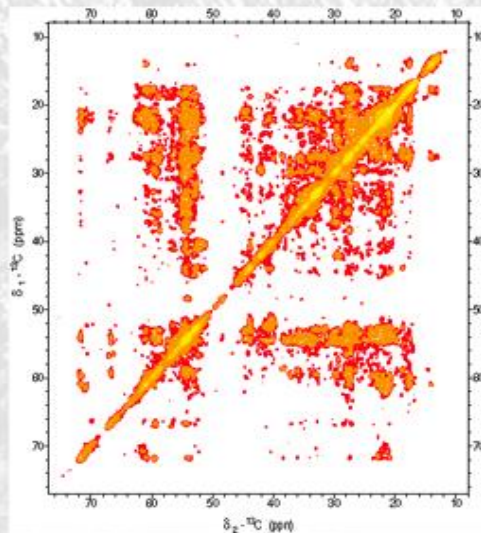


# Structure determination schemes

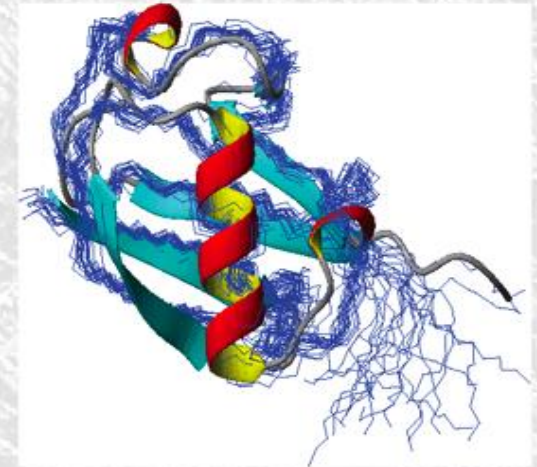
We acknowledge that  $I_{ab} = c\tau/r_{ab}^6$  is certainly wrong but believe that it is not too wrong -> we reduce the data evaluation to the NOESY problem.

**automatic/manual**

**data**



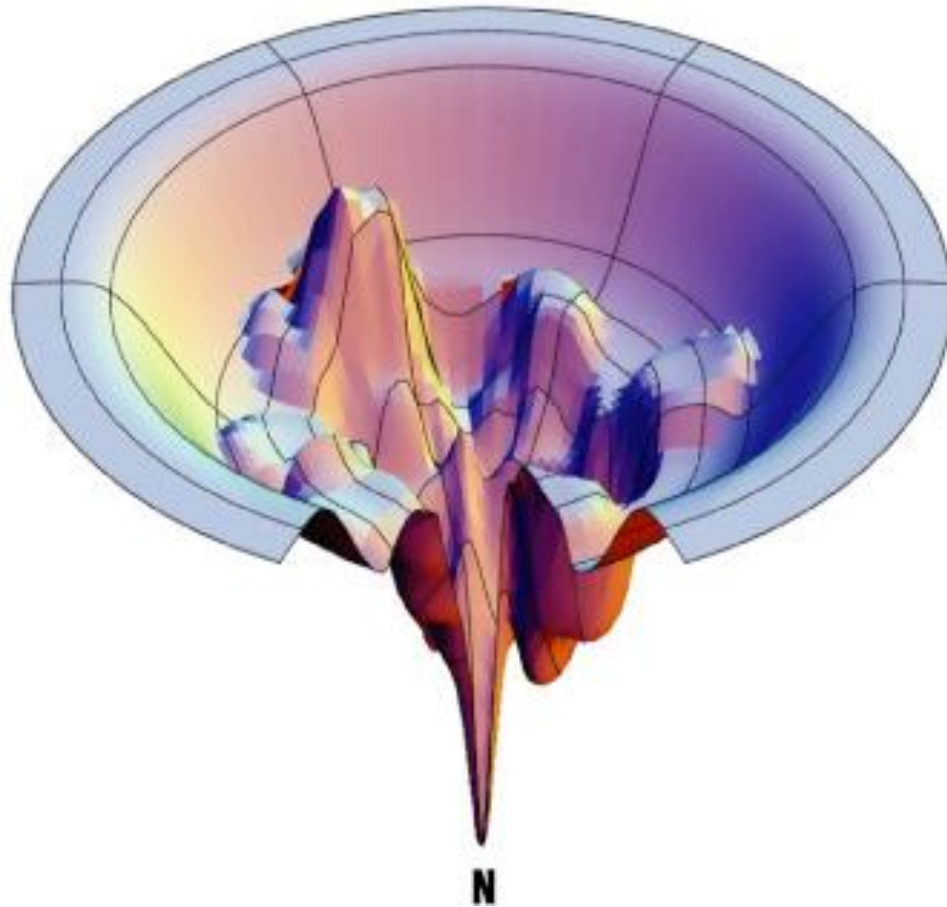
**structure**



# Structure calculations

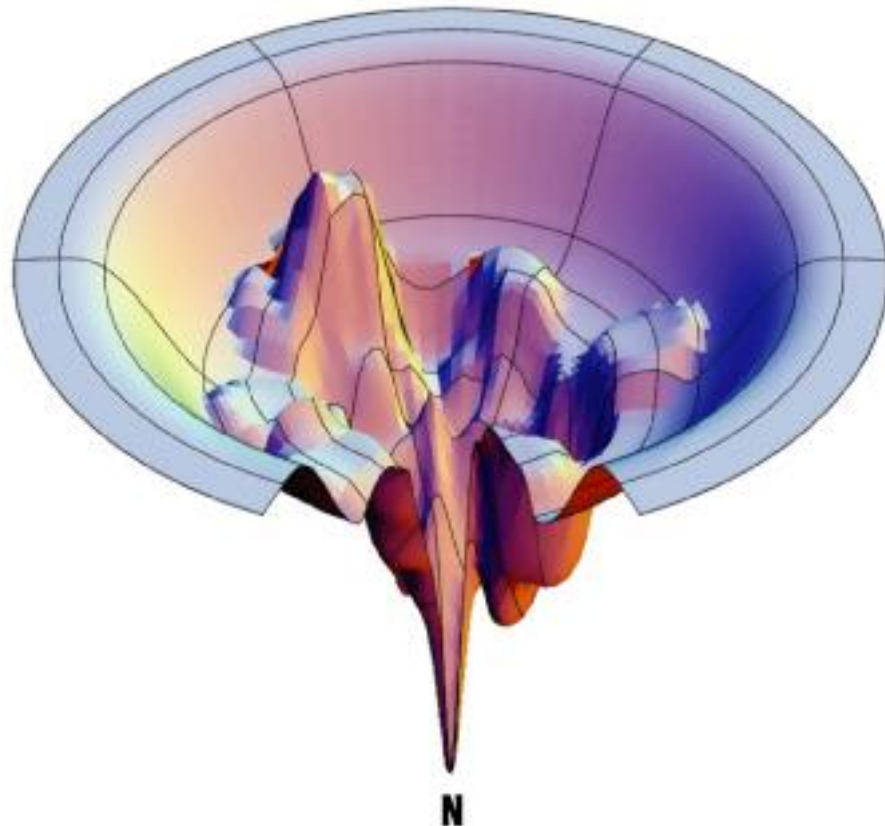
- Structure calculation programs try to “**fold**” a **protein** into a three dimensional structure that agrees with the measured data.
- Differences between measured data and the structure are manifested as **violations**.
- Violations cause forces that act on the molecule, driving it towards **minimal (pseudo)energy** and optimal agreement with the measured data.
- The **target function** (pseudoenergy) is the sum of squares (or similar) of the violations.
- The **energy landscape** of this target function is complex and has many local minima.

This is like folding of a protein



Finding the global minimum is difficult, but MD has developed concepts, e.g. simulated annealing.

...but the surface is not a real energy  
but a pseudoenergy (**Target Function**)

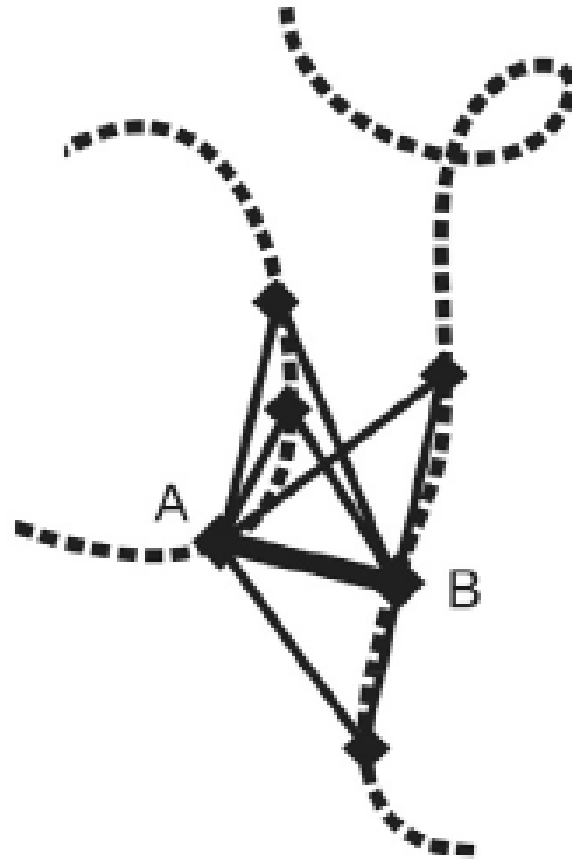


# Structure calculation using CYANA

*Please take notes, not all slides will be distributed because some are taken (with permission) from a talk from Prof. Peter Güntert and will NOT be distributed.*

# Automated Cross-peak assignment

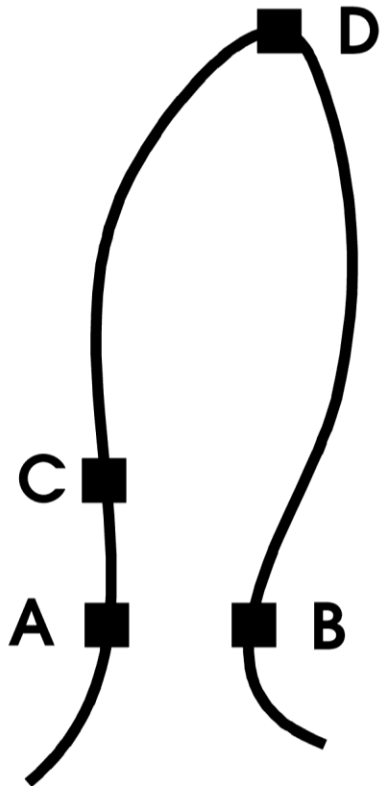
# Network-anchoring



# Restraint combination (first two cycles)

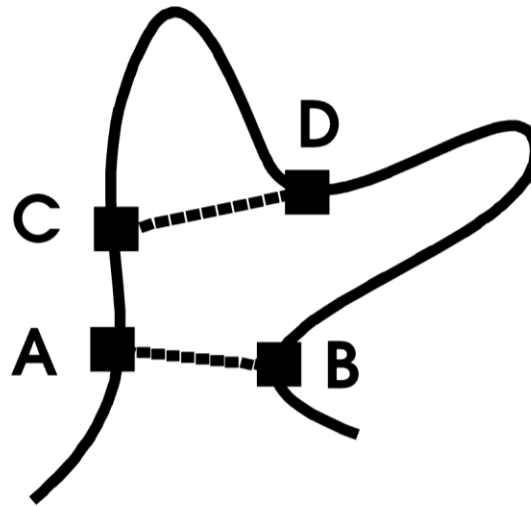
**Correct  
structure**

**(unknown)**

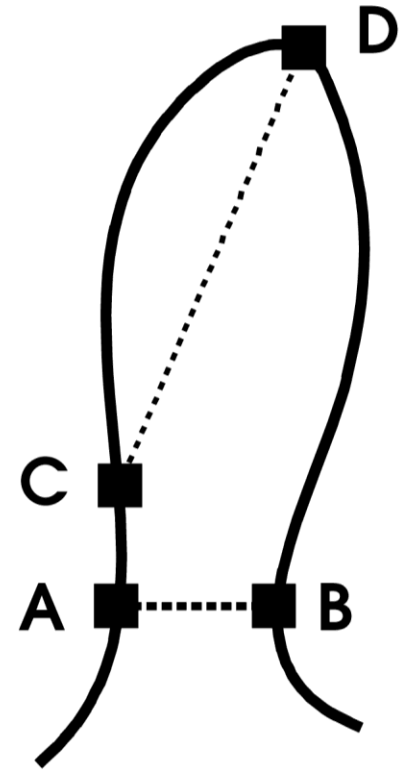


**Individual  
constraints**

**A-B (correct)  
C-D (wrong)**



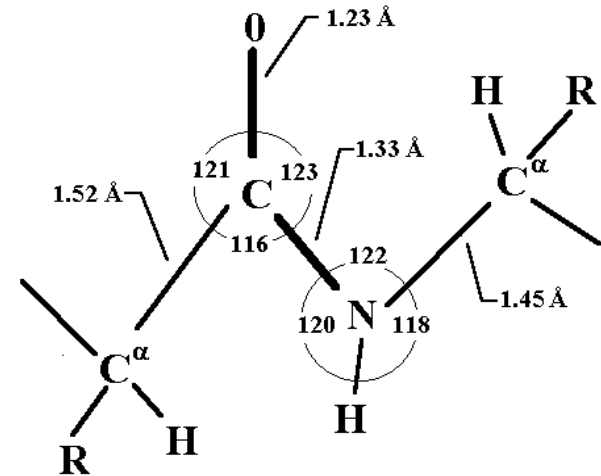
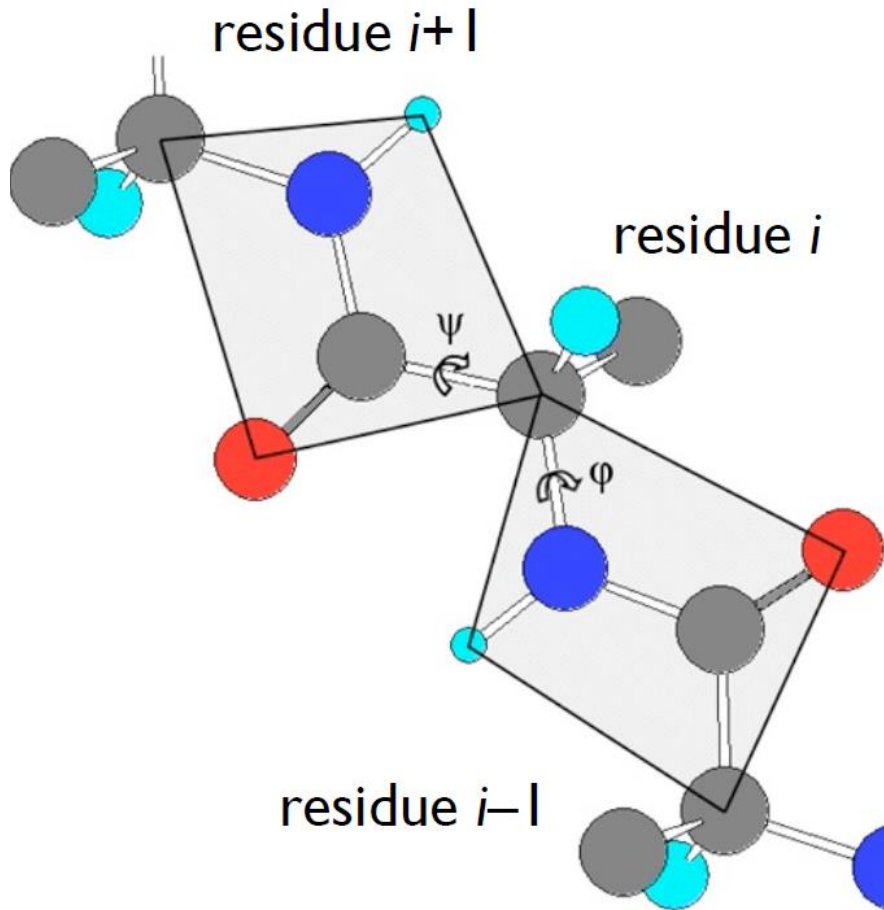
**Combined  
constraint**



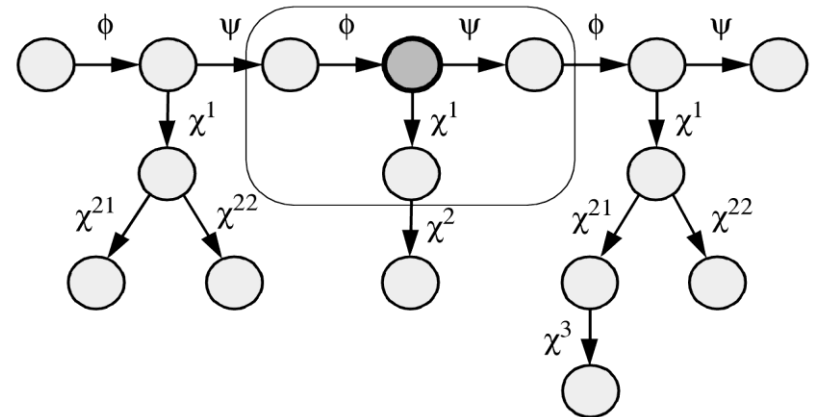


# Structure calculation using CYANA

# Torsion angles

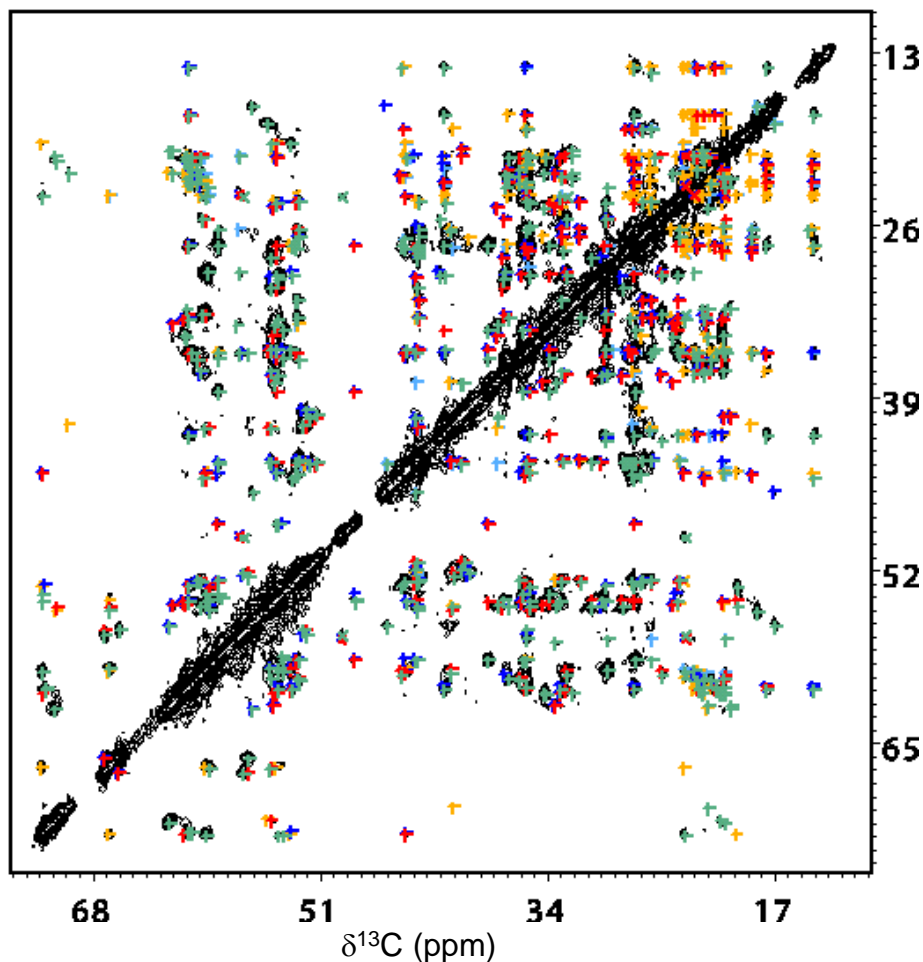


Other distances are fixed



# Structure explains NMR spectra (back-calculation matches experiment)

CHHC spectrum, U- $^{15}\text{N}$ ,  $^{13}\text{C}$  labelled HET-s(218-289),  
150  $\mu\text{s}$  mix, 9.5 kHz MAS, 850 MHz



Restraints classification:

- Short-range
- Intramolecular  $\beta$ -sheet
- Intramolecular middle and long-range
- Intermolecular  $\beta$ -sheet
- Intermolecular middle and long-range




All peaks explained

# Preparation of the structure calculation

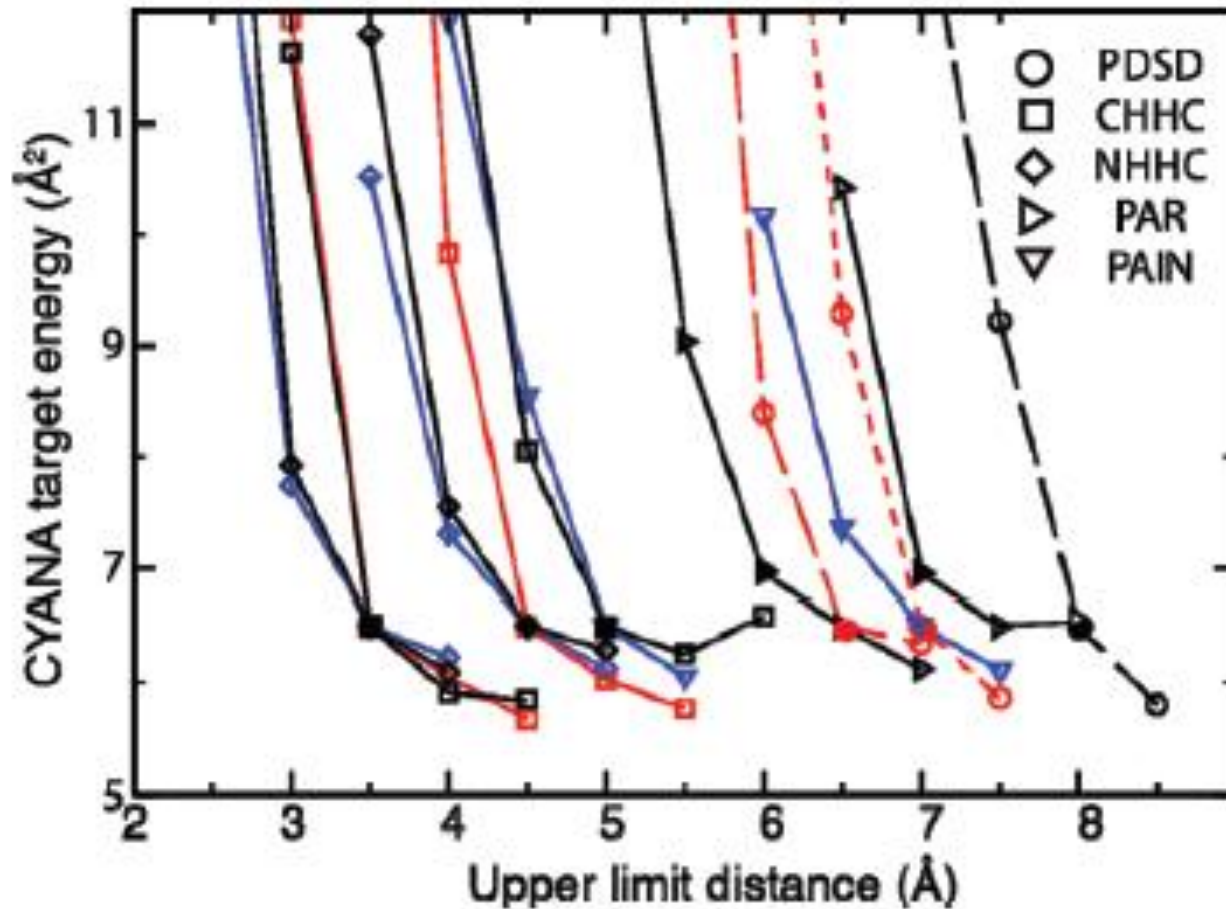
# Three ways to prepare distance restraints for structure calculation

- Pick a region automatically and export list (filename.peaks)
- Pick peaks by hand and export list for CYANA (filename.peaks)
- Pick peaks and assign them manually (and create a restraint list for CYANA manually) (filename.upl)

# Manual unambiguous restraints

atom 1		atom 2		
				
A23 ILE	CA	A2 GLY	CA	7.00
A23 ILE	CB	A2 GLY	CA	7.00
A23 ILE	CG1	A2 GLY	CA	7.00
A23 ILE	CG2	A2 GLY	CA	7.00

# Adapted upper distance limits...



Lines: uniformly labeled samples are continuous; those for Glycerol labeled samples are dashed (2-<sup>13</sup>C-Glycerol, long, 1,3-<sup>13</sup>C-Glycerol, short).

# Required files for structure calculation

- HETs\_trimer.seq (sequence)
- HETs\_trimer.prot (assignment)
- HET-s\_talos\_trimer.aco (TALOS+ data)
- \*.peaks for all experiments
- HET-s\_hbonds.lol / upl for H-bonds
- init.cya (cyana symmetries etc.)
- Auto.cya (structure calculation details)



# Sequence file (.seq)

MET A217  
LYS A218  
ILE A219  
ASP A220  
ALA A221  
ILE A222  
VAL A223  
...  
HIS A295

HET-s(218-289)  
from CCPN

PL L01  
LL2 L02  
LL2 L03  
...  
LL2 L48  
LP L49

Flexible linker

MET B217  
LYS B218  
ILE B219  
ASP B220  
ALA B221  
ILE B222  
...

HET-s(218-289)  
from CCPN

# Chemical shift files (.prot)

```
1  175.070  0.000      C  A222
2   62.000  0.000     CA  A222
3   38.262  0.000     CB  A222
4   13.014  0.000    CD1  A222
5   27.492  0.000    CG1  A222
6   18.689  0.000    CG2  A222
7  128.938  0.000      N  A222
```

...

```
328  175.070  0.000      C  B222
329   62.000  0.000     CA  B222
330   38.262  0.000     CB  B222
331   13.014  0.000    CD1  B222
332   27.492  0.000    CG1  B222
333   18.689  0.000    CG2  B222
334  128.938  0.000      N  B222
```

....

```
1180   62.000  0.000     HA  A222
1181   38.262  0.000     HB  A222
1182   13.014  0.000    QD1  A222
1183   27.492  0.000    QG1  A222
1184   18.689  0.000    QG2  A222
 982  128.938  0.000      H  A222
```

...

chemical shifts as  
exported from CCPN  
(xeasy format)

identical shifts for  
chains B and C

translation to attached  
protons for  
CHHC and NHHC

# Dihedral angle restraints from TALOS (\*.aco)

A222	ILE	PHI	-116.0	-84.0
A222	ILE	PSI	116.0	138.0
A223	VAL	PHI	-139.0	-101.0
A223	VAL	PSI	120.0	164.0
A225	ARG	PHI	-142.0	-90.0
A225	ARG	PSI	122.0	154.0
A226	ASN	PHI	-116.0	-82.0
A226	ASN	PSI	115.0	149.0
A227	SER	PHI	-140.0	-122.0
A227	SER	PSI	138.0	170.0
...				
B222	ILE	PHI	-116.0	-84.0
B222	ILE	PSI	116.0	138.0
B223	VAL	PHI	-139.0	-101.0
B223	VAL	PSI	120.0	164.0
...				

***See Exercise hour.***

# Peak files for all spectra (.peaks)

## PAIN\_mixed.peaks

# Number of dimensions 2

# INAME 1 N

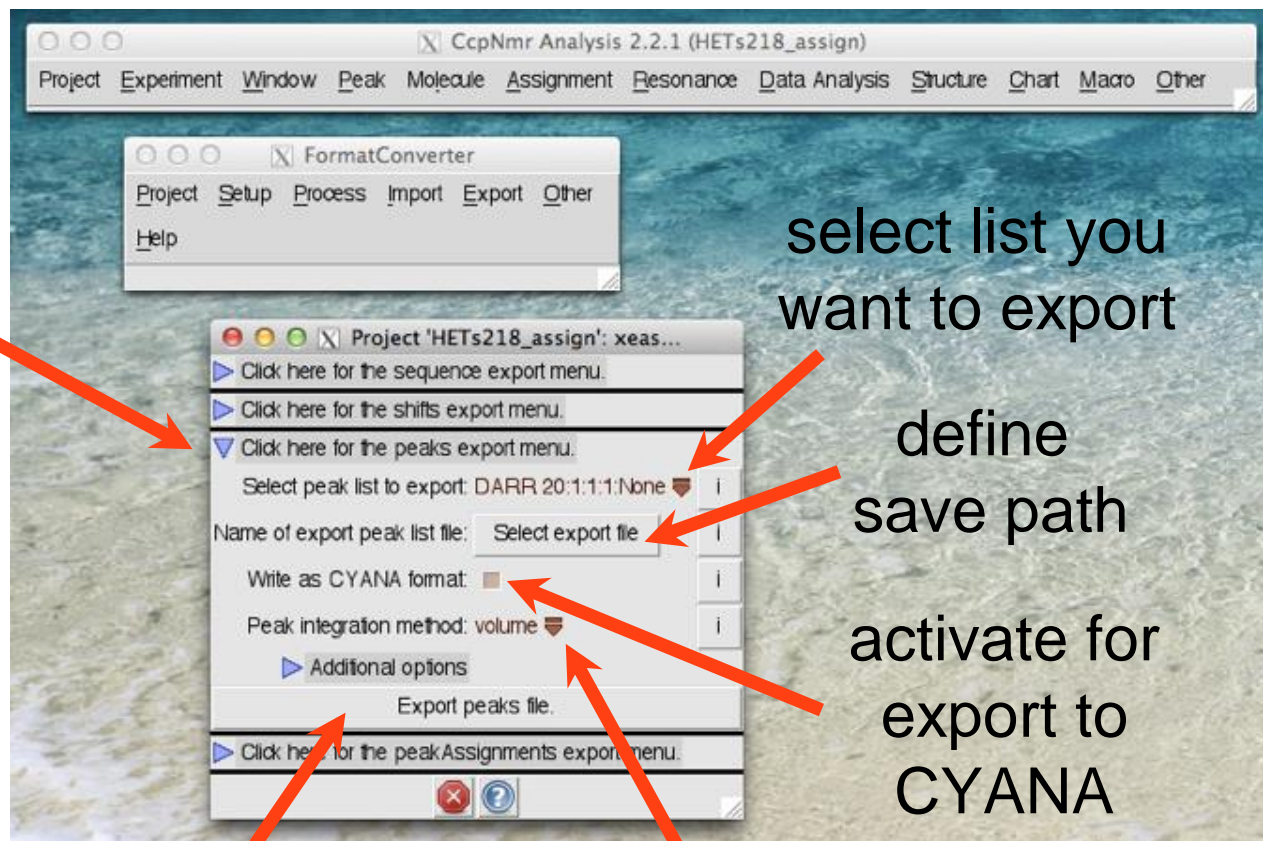
# INAME 2 C

#CYANAFORMAT NC

#TOLERANCE 0.55 0.25

1	135.022	67.146	1	T	3.727e+08	0.00e+00	a	0	0	0	0	(9: intermolecular)
2	131.784	61.415	1	T	4.263e+08	0.00e+00	a	0	0	0	0	(8: intra, 1 ambiguous)
3	130.491	52.789	1	T	6.357e+08	0.00e+00	a	0	0	0	0	
4	130.411	35.365	1	T	4.183e+08	0.00e+00	a	0	0	0	0	
5	129.779	20.938	1	T	4.401e+08	0.00e+00	a	0	0	0	0	
6	128.896	41.830	1	T	3.873e+08	0.00e+00	a	0	0	0	0	
7	128.814	27.950	1	T	5.204e+08	0.00e+00	a	0	0	0	0	
8	128.215	60.864	1	T	4.883e+08	0.00e+00	a	0	0	0	0	
9	128.504	54.278	1	T	6.229e+08	0.00e+00	a	0	0	0	0	
10	128.381	20.887	1	T	4.145e+08	0.00e+00	a	0	0	0	0	
11	127.509	52.213	1	T	3.776e+08	0.00e+00	a	0	0	0	0	
12	126.424	67.270	1	T	3.706e+08	0.00e+00	a	0	0	0	0	
13	126.643	59.764	1	T	6.177e+08	0.00e+00	a	0	0	0	0	
14	126.686	43.821	1	T	4.019e+08	0.00e+00	a	0	0	0	0	
15	125.981	53.566	1	T	3.968e+08	0.00e+00	a	0	0	0	0	
16	124.036	22.097	1	T	5.249e+08	0.00e+00	a	0	0	0	0	
17	122.955	60.715	1	T	8.797e+08	0.00e+00	a	0	0	0	0	

# Exporting Peak Lists in CCPN



# Proton-restraints for heteroatom spectra and mixed vs. complete labelling

NHHC\_mixed.peaks

.peaks

# Number of dimensions 2

# INAME 1 ~~N~~-H

# INAME 2  $\in$  H

#CYANAFORMAT ~~NC~~ HH

#TOLERANCE 0.8 0.4

1	135.022	67.146	<del>1</del> 9	T	3.727e+08	0.00e+00	a	0	0	0	0	(9: intermolecular)
2	131.784	61.415	1	T	4.263e+08	0.00e+00	a	0	0	0	0	(8: intra, 1 ambiguous)
3	130.491	52.789	1	T	6.357e+08	0.00e+00	a	0	0	0	0	
4	130.411	35.365	1	T	4.183e+08	0.00e+00	a	0	0	0	0	
5	129.779	20.938	1	T	4.401e+08	0.00e+00	a	0	0	0	0	
6	128.896	41.830	1	T	3.873e+08	0.00e+00	a	0	0	0	0	
7	128.814	27.950	1	T	5.204e+08	0.00e+00	a	0	0	0	0	
8	128.215	60.864	1	T	4.883e+08	0.00e+00	a	0	0	0	0	
9	128.504	54.278	1	T	6.229e+08	0.00e+00	a	0	0	0	0	
10	128.381	20.887	1	T	4.145e+08	0.00e+00	a	0	0	0	0	
11	127.509	52.213	1	T	3.776e+08	0.00e+00	a	0	0	0	0	
12	126.424	67.270	1	T	3.706e+08	0.00e+00	a	0	0	0	0	
13	126.643	59.764	1	T	6.177e+08	0.00e+00	a	0	0	0	0	
14	126.686	43.821	1	T	4.019e+08	0.00e+00	a	0	0	0	0	
15	125.981	53.566	1	T	3.968e+08	0.00e+00	a	0	0	0	0	
16	124.036	22.097	1	T	5.249e+08	0.00e+00	a	0	0	0	0	
17	122.955	60.715	1	T	8.797e+08	0.00e+00	a	0	0	0	0	

# H-bonds (hbonds)

B226	ASN	H	B261	THR	O	2.00	10
B262	ASN	H	B225	ARG	O	0.00	
B226	ASN	N	B261	THR	O	3.00	10
B262	ASN	N	B225	ARG	O	0.00	

intramolecular

A226	ASN	H	B261	THR	O	2.00	10
B262	ASN	H	A225	ARG	O	0.00	
A226	ASN	N	B261	THR	O	3.00	10
B262	ASN	N	A225	ARG	O	0.00	

intermolecular

.upl

B226	ASN	H	C261	THR	O	2.00	10
C262	ASN	H	B225	ARG	O	0.00	
B226	ASN	N	C261	THR	O	3.00	10
C262	ASN	N	B225	ARG	O	0.00	

....

B226	ASN	H	B261	THR	O	1.80	10
B262	ASN	H	B225	ARG	O	0.00	
B226	ASN	N	B261	THR	O	2.70	10
B262	ASN	N	B225	ARG	O	0.00	

A226	ASN	H	B261	THR	O	1.80	10
B262	ASN	H	A225	ARG	O	0.00	
A226	ASN	N	B261	THR	O	2.70	10
B262	ASN	N	A225	ARG	O	0.00	

.lol

B226	ASN	H	C261	THR	O	1.80	10
C262	ASN	H	B225	ARG	O	0.00	
B226	ASN	N	C261	THR	O	2.70	10
C262	ASN	N	B225	ARG	O	0.00	

....

# init.cya

```
name:=HETs218-289
rmsdrange:=B226-B245,B262-B281

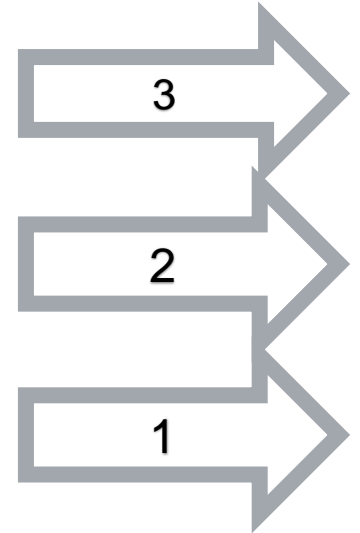
welldefined:="A226-A245,A262-A281,B226-B245,B262-B281,C226-C245,C262-C281"

cyanalib
read seq HETs_trimer.seq

molecules define A218-A289 B218-B289 C218-C289

# Symmetry-related distances
molecules contacts 1,1=2,2=3,3 \
                  1,2=2,3 \
                  2,1=3,2
molecules identity "*" $welldefined" #info=full
weight_ide=0.15
molecules symdist "CA $welldefined" "CA $welldefined" number=3000 #info=full
weight_sym=0.05

# Allowed contacts for distance restraint assignment
molecules contacts 1,1=2,2=3,3 \
                  1,2=2,3 \
                  2,1=3,2 \
                  1,3=3,1=0
```



dihedral angles in “welldefined” regions  
have to be equal in all monomers

identical interfaces between monomers,  
restraints are applied between all of them

=0 : no restraints allowed



# Auto.cya

```
peaks      := PAR4_U_hom.peaks,PAIN5_U_mix.peaks,CHHC_U_hom.peaks,NHHC_U_hom.peaks,NHHC_U_mix.peaks
# names of peak lists

prot       := HETs_trimer.prot
# names of chemical shift lists

restraints :=
SIhbonds_trimer.lol,SIhbonds_trimer.upl,HETs_talos_trimer_2std.aco,CHHC_U13C_diluted_trimer.upl,CHHC_U1
3C_trimer.upl,NHHC_U13C15N_trimer.upl,PDSD_1_3C_diluted_trimer.upl,PDSD_2C_diluted_trimer.upl
# additional constraints

#tolerance   := 0.3,0.3,0.3
#chemical shift tolerances
# order: 1H(a), 1H(b), 13C/15N(a), 13C/15N(b)

#calibration_constant := 2E+10
# NOE calibration parameters

calibration_upl := 7.5,7.5,5.5,5.0,4.0
# larger numbers lead to longer constraints

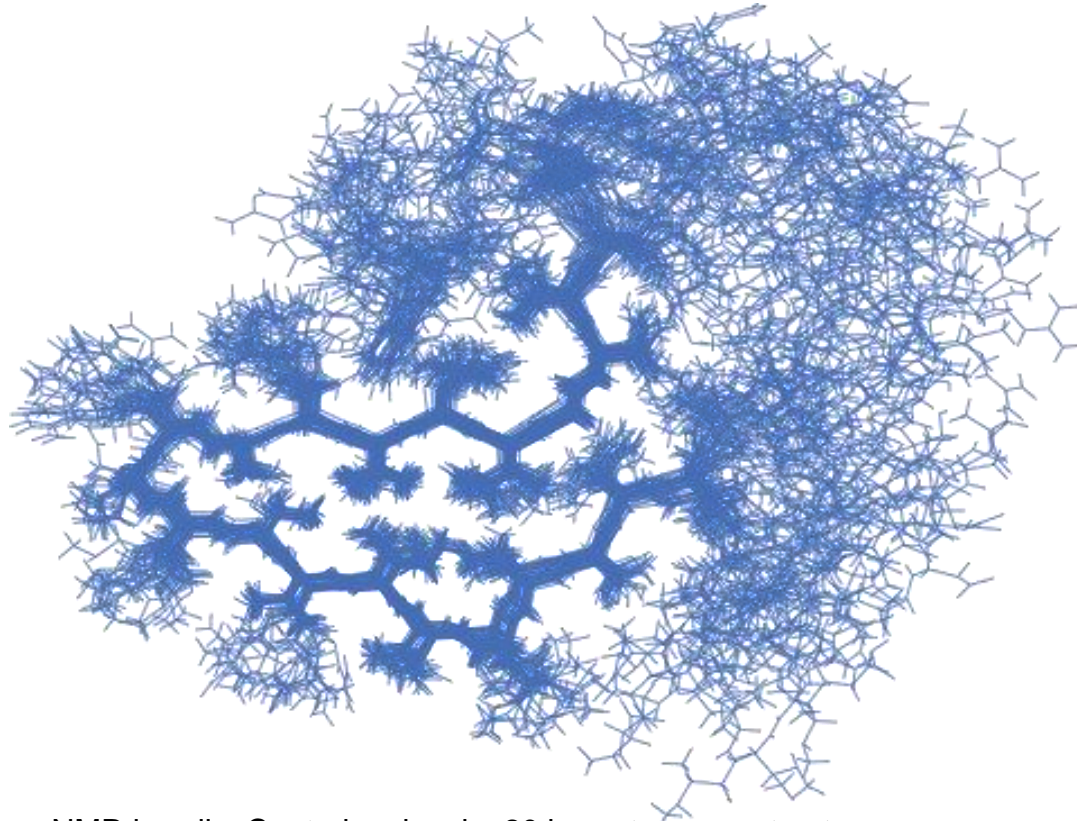
upl_values := 1.0,12.0
structures := 100,10
steps      := 20000
rmsdrange  := 226..245,262..281
randomseed := 434726

./noeassign peaks=$peaks prot=$prot autoaco
read final.pdb
atoms select "*" :A* :B* :C*"
write HETs.pdb all selected
```

Here are the  $u_{ij}$  defined!

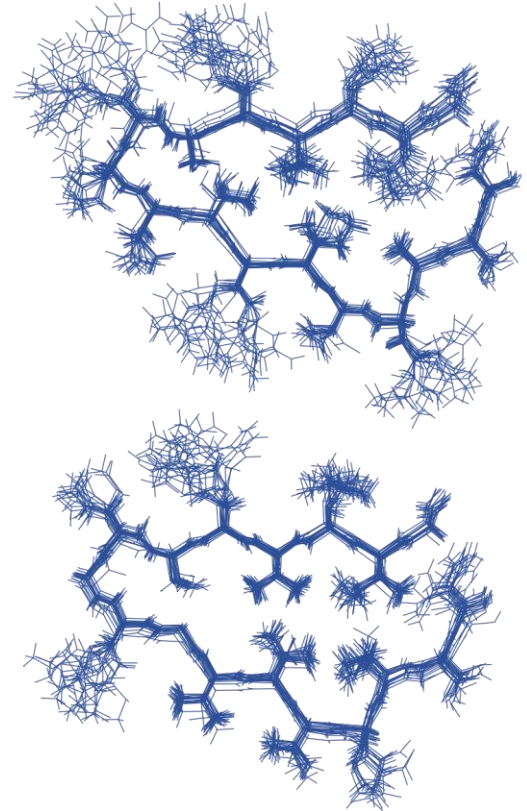
Result of structure calculation  
for HET-s(218-289)

# Overall shape and hydrophobic core



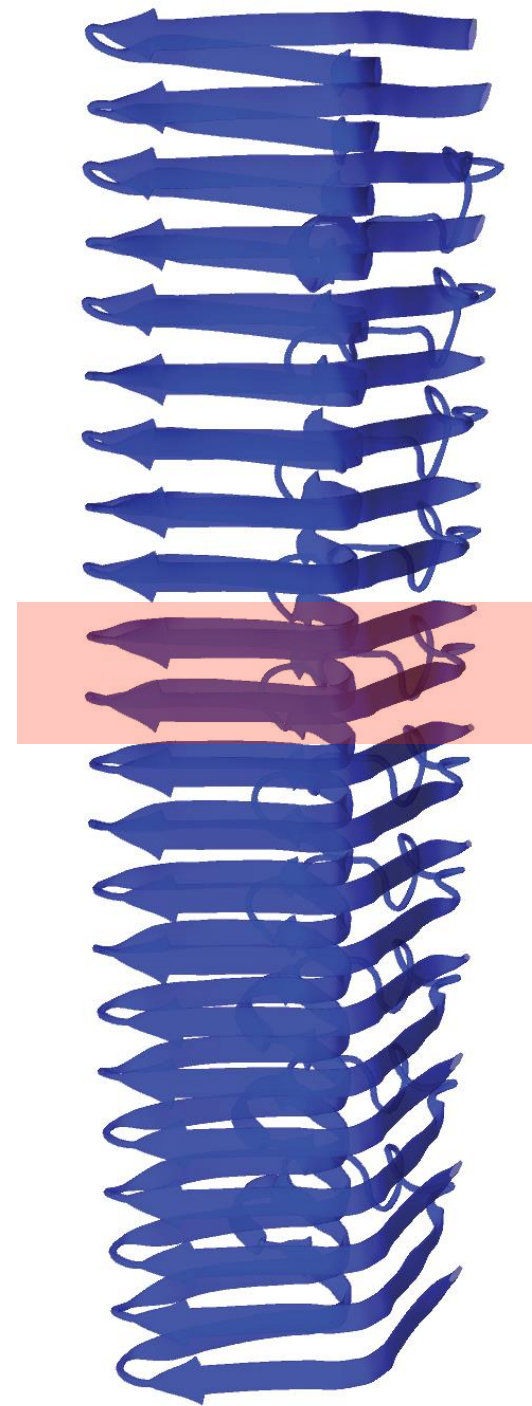
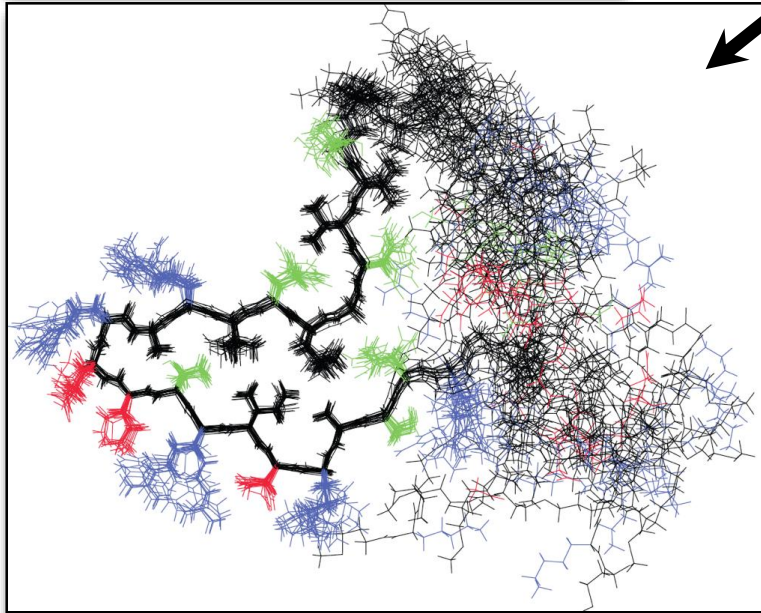
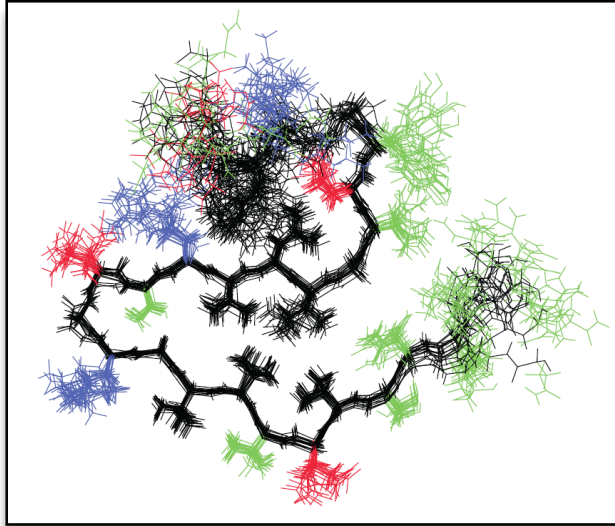
NMR bundle: Central molecule, 20 lowest energy structures

rmsd (for assigned residues:  
S226-A248, T260-G282, F286-W287) :  
Backbone 0.63 Å, All heavy atoms 1.16 Å

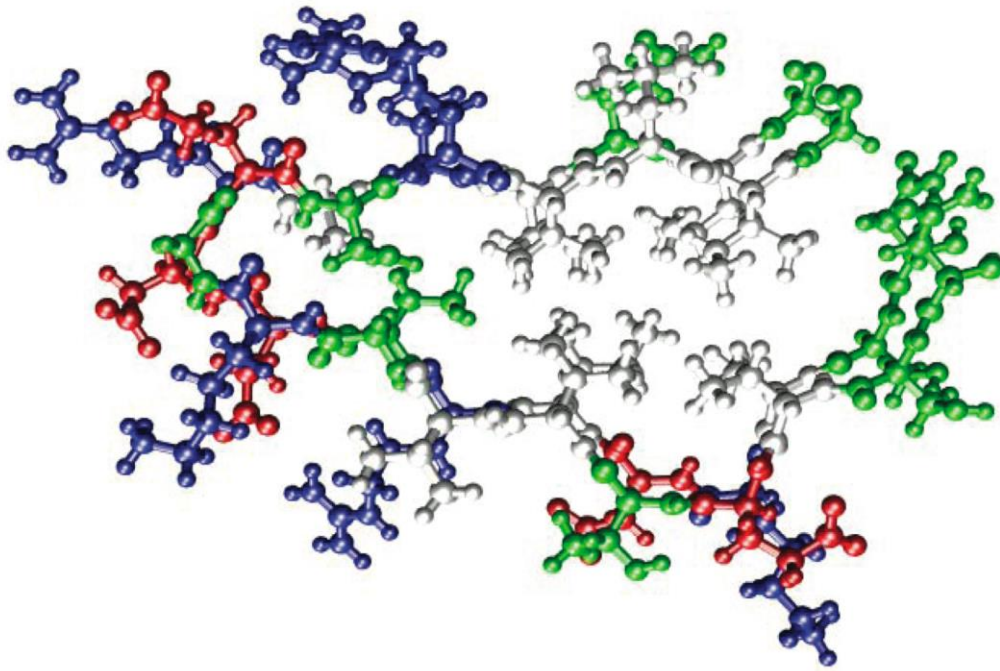


Separate bundles for the two layers

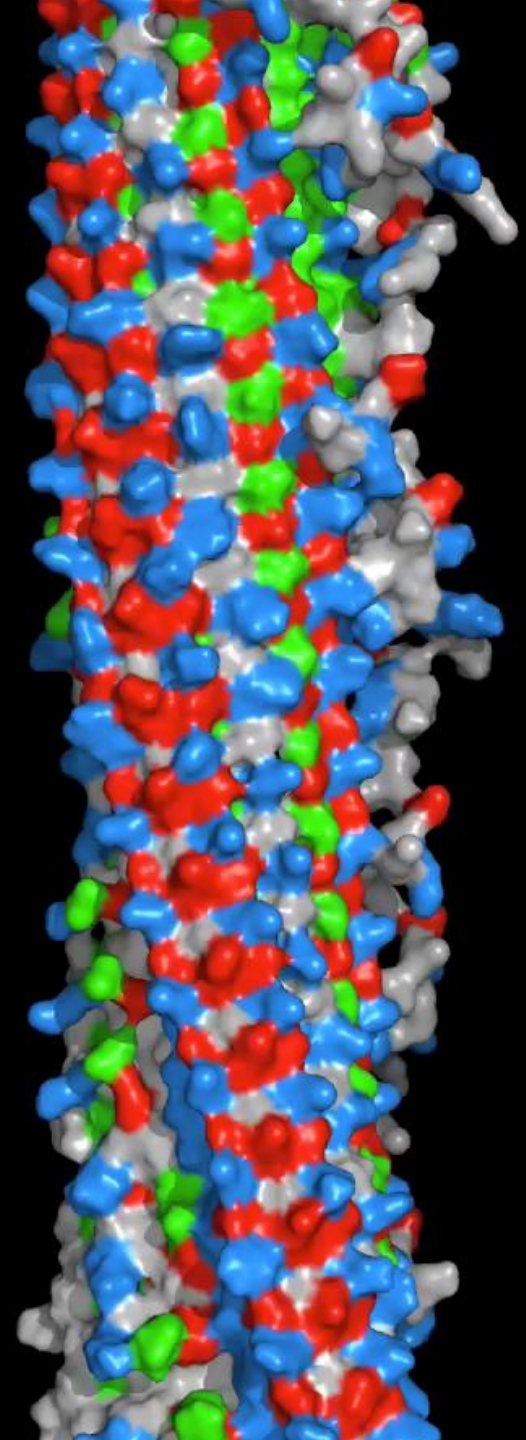
# Structure of the entire Object, e.g. a Fibril







- At least 23 H-bonds per monomer
- A hydrophobic core
- Polar and charged residues point “outside”.
- Charge compensation between the two layers of a monomer (which are pseudorepeats).
- Asparagine ladders



# Take Home Messages

- CYANA handles assignment ambiguities by network anchoring, chemical shift matching and restraint combination
- CYANA calculations are performed in Torsion Angle Space
- CYANA calculations use simulated annealing like in MD
- CYANA is based on the minimization of a target function (pseudoenergy)
- Validation of the obtained structure is very important!!!
- Exercise: How is the structure calculation performed in detail?

# Recommended literature on CYANA

Güntert, P. & Buchner, L. Combined automated NOE assignment and structure calculation with CYANA. *Journal of Biomolecular NMR* **62**, 453-471 (2015)

Güntert, P. Automated NMR Structure Calculation With CYANA. in *Protein NMR Techniques* (ed. Downing, A.K.) 353-378 (Humana Press, Totowa, NJ, 2004).