

Ask professor about his recommendation for data being repetitive in the model

# Database Systems I

CMPT 354 Summer 2024

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# Announcements (Wed., May 29)

- Homework 1 due tonight (11:59pm)
  - 2 maximum late days
- Homework 2 already assigned
  - Setup PostgreSQL now!
    - Will be used in future assignments

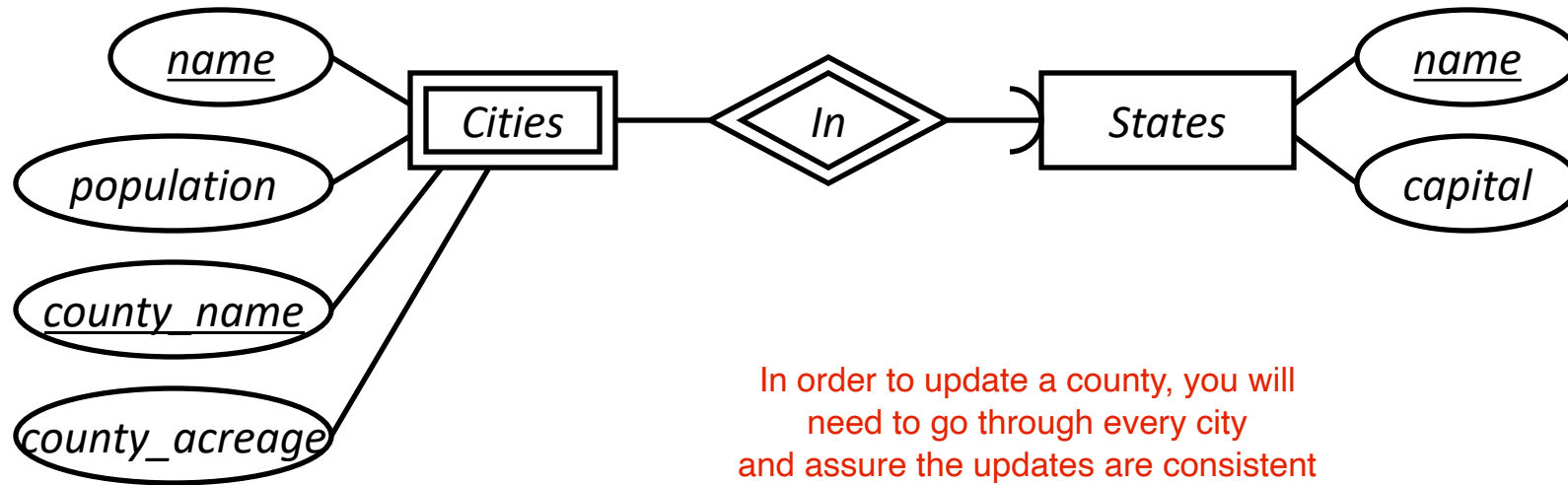
# Database design steps

- Understand the real-world domain being modeled
- Specify it using a database design model (e.g., E/R)
  - Conceptual design
- Translate specification to the data model of DBMS (e.g., relational)
  - Logical design
- Schema refinement
- Create DBMS schema

# Outline

- Database Design Theory
  - Functional Dependency
  - Schema Decomposition
  - Boyce-Codd Normal Form (BCNF) & BCNF Decomposition
  - Multivalued Dependency & 4<sup>th</sup> Normal Form

# Recap: Case study 1 in E/R design



- County acreage information is repeated for every city in the county
  - ☞ Redundancy is bad (why?)
- State capital should really be a city
  - ☞ Should “reference” entities through explicit relationships

There are no other tables to store the user name, user id, and group id

# Motivation

If we remove Milhouse, then we will have no record of him existing

If we want to update one the records here, you will need to make sure the update is propagated to any other records with the old information

Certain constraints may need redundancy



<i>uid</i>	<i>uname</i>	<i>gid</i>
142	Bart	dps
123	Milhouse	gov
857	Lisa	abc
857	Lisa	gov
456	Ralph	abc
456	Ralph	gov
...	...	...

- Why is *UserGroup* (*uid*, *uname*, *gid*) a bad design?
  - It has **redundancy** — user name is recorded multiple times, once for each group that a user belongs to
    - Leads to **update, insertion, deletion anomalies**
- Wouldn't it be nice to have a systematic approach to detecting and removing redundancy in designs?
  - **Dependencies, decompositions, and normal forms**

# Functional dependencies

- A **functional dependency (FD)** has the form  $X \rightarrow Y$ , where  $X$  and  $Y$  are sets of attributes in a relation  $R$ 
  - $X$  *functionally determines*  $Y$  if, for any tuples  $t_1$  and  $t_2$ :
    - $t_1[A] = t_2[A]$  implies  $t_1[B] = t_2[B]$
- $X \rightarrow Y$  means that whenever two tuples in  $R$  agree on all the attributes in  $X$ , they must also agree on all attributes in  $Y$

$X$	$Y$	$Z$
$a$	$b$	$c$
$a$	$b$	?
...	...	...

Must be  $b$    Could be anything

# FD examples

*Address (street\_address, city, state, zip)*

- *street\_address, city, state* → *zip*
- *zip* → *city, state*
- *zip, state* → *zip*?
  - This is a trivial FD
  - **Trivial FD**:  $\text{LHS} \supseteq \text{RHS}$
- *zip* → *state, zip*?
  - This is non-trivial, but not completely non-trivial
  - **Completely non-trivial FD**:  $\text{LHS} \cap \text{RHS} = \emptyset$



# Redefining “keys” using FD’s

A set of attributes  $K$  is a **key** for a relation  $R$  if

- $K \rightarrow$  all (other) attributes of  $R$ 
  - That is,  $K$  is a “**super key**” A key is minimal, but a superkey need not be minimal
- No proper subset of  $K$  satisfies the above condition
  - That is,  $K$  is **minimal**

# Example

An FD holds, or does not hold on a table:

<i>uid</i>	<i>name</i>	<i>age</i>	<i>pop</i>
142	Bart	10	0.9
123	Milhouse	10	0.2
857	Lisa	8	0.7
459	Lisa	8	0.3

Ask professor if an FD holds for all possible relationship instances

✓  $uid \rightarrow name$

x  $name \rightarrow pop$

✓  $name, uid \rightarrow age$

# Reasoning with FD's

Given a relation  $R$  and a set of FD's  $\mathcal{F}$

- Does another FD follow from  $\mathcal{F}$ ?
  - Are some of the FD's in  $\mathcal{F}$  redundant (i.e., they follow from the others)?
- Is  $K$  a key of  $R$ ?
  - What are all the keys of  $R$ ?

# Attribute closure

- Given  $R$ , a set of FD's  $\mathcal{F}$  that hold in  $R$ , and a set of attributes  $Z$  in  $R$ :
  - The **closure of  $Z$**  (denoted  $Z^+$ ) with respect to  $\mathcal{F}$  is the set of **all attributes  $\{A_1, A_2, \dots\}$  functionally determined by  $Z$**  (that is,  $Z \rightarrow A_1 A_2 \dots$ )
- Algorithm for computing the closure
  - Start with closure =  $Z$
  - If  $X \rightarrow Y$  is in  $\mathcal{F}$  and  $X$  is already in the closure, then also add  $Y$  to the closure
  - Repeat until no new attributes can be added

# A more complex example

Assuming a user can only join a group once

*UserJoinsGroup (uid, uname, twitterid, gid, fromDate)*

- Assume that there is a one-to-one correspondence between our users and Twitter accounts
- *uid* → *uname, twitterid*
- *twitterid* → *uid*
- *uid, gid* → *fromDate*

Not a good design, and we will see why shortly

# Example of computing closure

- $\{gid, twitterid\}^+ = ?$
- $twitterid \rightarrow uid$ 
  - Add  $uid$
  - Closure grows to  $\{gid, twitterid, uid\}$
- $uid \rightarrow uname, twitterid$ 
  - Add  $uname, twitterid$
  - Closure grows to  $\{gid, twitterid, uid, uname\}$
- $uid, gid \rightarrow fromDate$ 
  - Add  $fromDate$
  - Closure is now **all attributes in *UserJoinsGroup***

$\mathcal{F}$  includes:

$uid \rightarrow uname, twitterid$

$twitterid \rightarrow uid$

$uid, gid \rightarrow fromDate$

# Using attribute closure

Given a relation  $R$  and set of FD's  $\mathcal{F}$

- Does another FD  $X \rightarrow Y$  follow from  $\mathcal{F}$ ?
    - Compute  $X^+$  with respect to  $\mathcal{F}$
    - If  $Y \subseteq X^+$ , then  $X \rightarrow Y$  follows from  $\mathcal{F}$
  - Is  $K$  a key of  $R$ ?
    - Compute  $K^+$  with respect to  $\mathcal{F}$
    - If  $K^+$  contains all the attributes of  $R$ ,  $K$  is a super key
    - Still need to verify that  $K$  is *minimal* (how?)
      - Hint: check the attribute closure of its proper subset.
      - i.e., Check that for no set  $X$  formed by removing attributes from  $K$  is  $K^+$  the set of all attributes
- Ask professor to go over this

# Rules of FD's

- Armstrong's axioms
  - **Reflexivity**: If  $Y \subseteq X$ , then  $X \rightarrow Y$ 
    - $\text{uid, uname} \rightarrow \text{uid}$  Trivial dependency
  - **Augmentation**: If  $X \rightarrow Y$ , then  $XZ \rightarrow YZ$  for any  $Z$ 
    - $\text{uid} \rightarrow \text{uname}$
    - $\text{uid, gid} \rightarrow \text{uname, gid}$
  - **Transitivity**: If  $X \rightarrow Y$  and  $Y \rightarrow Z$ , then  $X \rightarrow Z$ 
    - $\text{Twitterid} \rightarrow \text{uid}$
    - $\text{uid} \rightarrow \text{uname}$
    - $\text{Twitterid} \rightarrow \text{uname}$



# Rules of FD's

- Armstrong's axioms
  - **Reflexivity**: If  $Y \subseteq X$ , then  $X \rightarrow Y$
  - **Augmentation**: If  $X \rightarrow Y$ , then  $XZ \rightarrow YZ$  for any  $Z$
  - **Transitivity**: If  $X \rightarrow Y$  and  $Y \rightarrow Z$ , then  $X \rightarrow Z$
- Rules derived from axioms
  - **Splitting**: If  $X \rightarrow YZ$ , then  $X \rightarrow Y$  and  $X \rightarrow Z$
  - **Combining**: If  $X \rightarrow Y$  and  $X \rightarrow Z$ , then  $X \rightarrow YZ$
- Using these rules, you can prove or disprove an FD given a set of FDs

# Non-key FD's

- Consider a non-trivial FD  $X \rightarrow Y$  where  $X$  is **not** a super key
  - Since  $X$  is not a super key, there are some attributes (say  $Z$ ) that are not functionally determined by  $X$

$X$	$Y$	$Z$
$a$	$b$	$c_1$
$a$	$b$	$c_2$
...	...	...

That  $a$  should be mapped to  $b$  is recorded multiple times:  
**redundancy, update/insertion/deletion anomaly**

# Example of redundancy

*UserJoinsGroup* (*uid*, *uname*, *twitterid*, *gid*, *fromDate*)

- *uid* → *uname*, *twitterid*

(... plus other FD's)

Issue with this table is that we have the users and the groups together.

<i>uid</i>	<i>uname</i>	<i>twitterid</i>	<i>gid</i>	<i>fromDate</i>
142	Bart	@BartJSimpson	dps	1987-04-19
123	Milhouse	@MilhouseVan_	gov	1989-12-17
857	Lisa	@lisasimpson	abc	1987-04-19
857	Lisa	@lisasimpson	gov	1988-09-01
456	Ralph	@ralphwiggum	abc	1991-04-25
456	Ralph	@ralphwiggum	gov	1992-09-01
...	...	...	...	...

# Decomposition

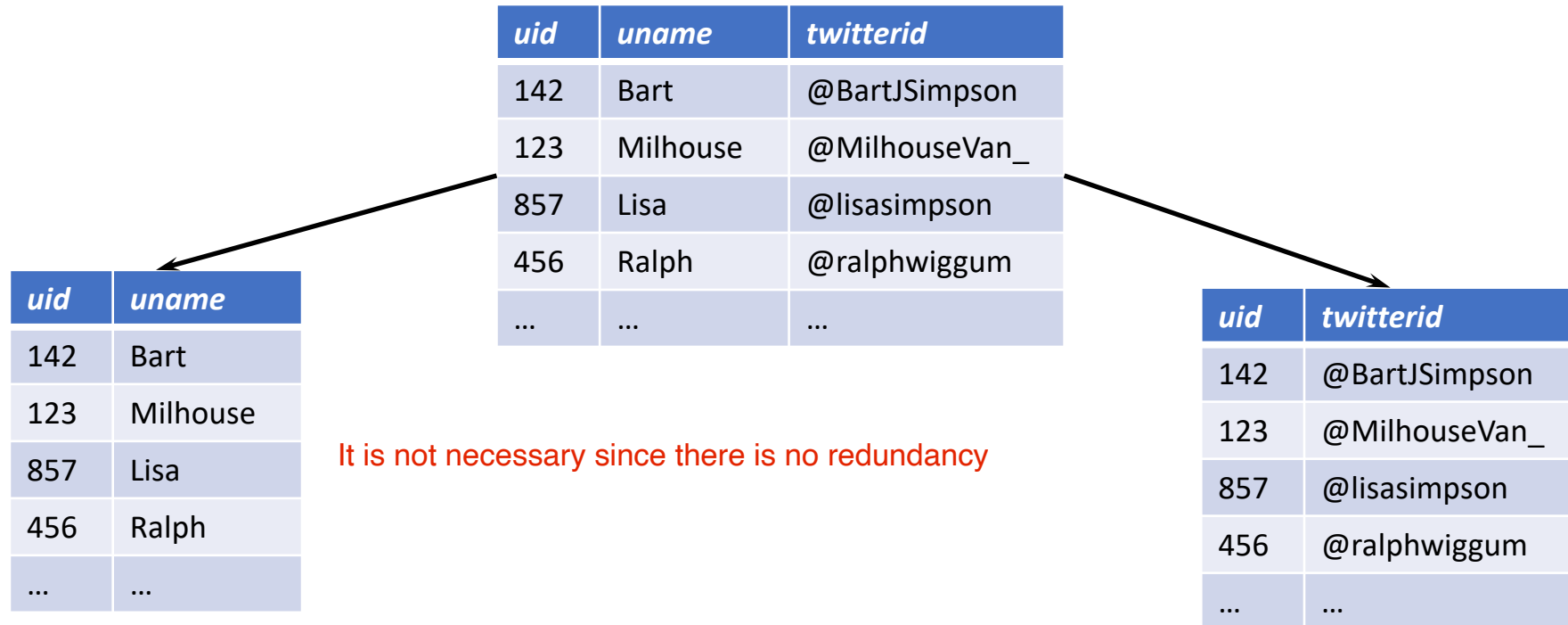
<i>uid</i>	<i>uname</i>	<i>twitterid</i>	<i>gid</i>	<i>fromDate</i>
142	Bart	@BartJSimpson	dps	1987-04-19
123	Milhouse	@MilhouseVan_	gov	1989-12-17
857	Lisa	@lisasimpson	abc	1987-04-19
857	Lisa	@lisasimpson	gov	1988-09-01
456	Ralph	@ralphwiggum	abc	1991-04-25
456	Ralph	@ralphwiggum	gov	1992-09-01
...	...	...	...	...

<i>uid</i>	<i>uname</i>	<i>twitterid</i>
142	Bart	@BartJSimpson
123	Milhouse	@MilhouseVan_
857	Lisa	@lisasimpson
456	Ralph	@ralphwiggum
...	...	...

<i>uid</i>	<i>gid</i>	<i>fromDate</i>
142	dps	1987-04-19
123	gov	1989-12-17
857	abc	1987-04-19
857	gov	1988-09-01
456	abc	1991-04-25
456	gov	1992-09-01
...	...	...

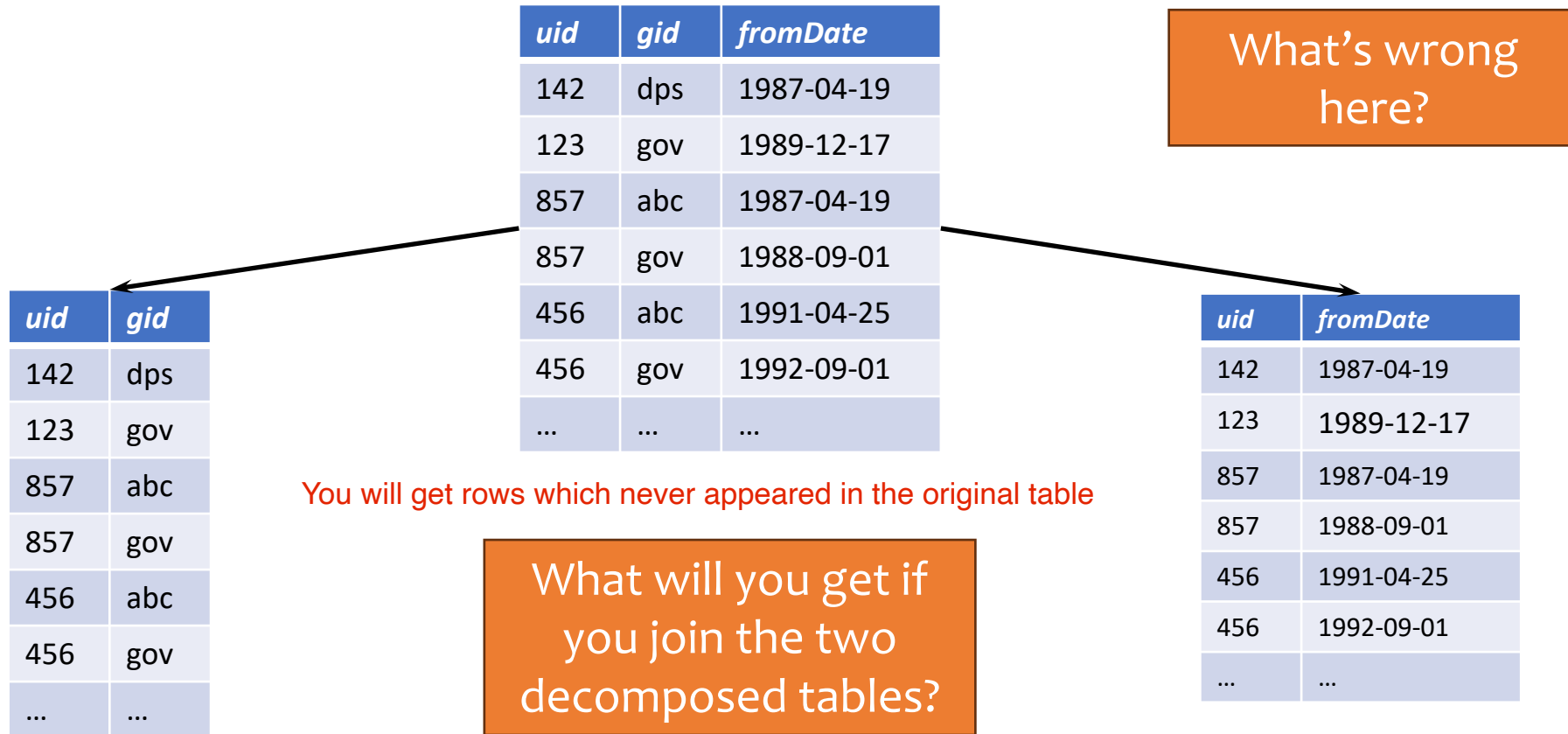
- Eliminates redundancy
- To get back to the original relation: ⋈

# Unnecessary decomposition



- Fine: join returns the original relation
- Unnecessary: no redundancy is removed; schema is more complicated

# Bad decomposition



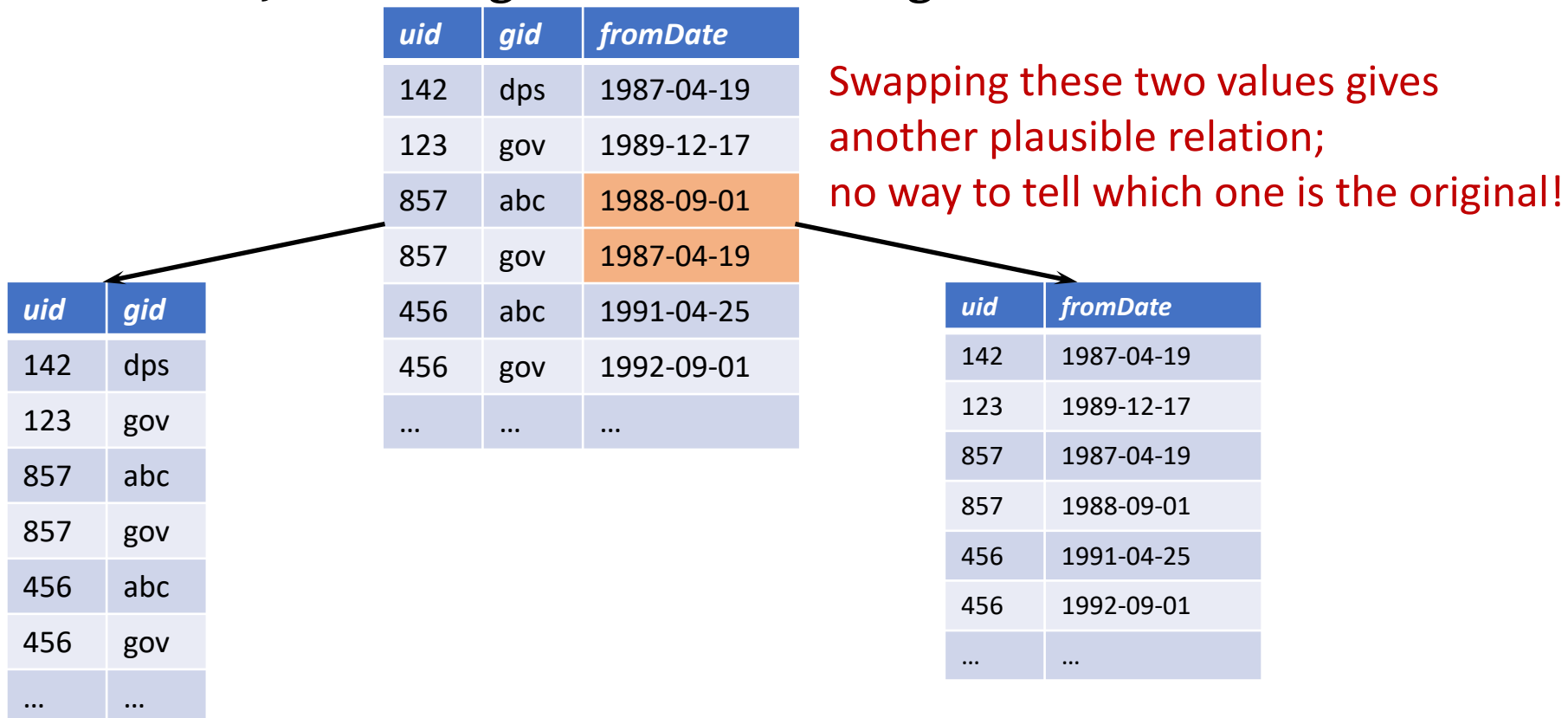
- Association between *gid* and *fromDate* is lost
- Join returns more rows than the original relation

# Lossless join decomposition

- Decompose relation  $R$  into relations  $S$  and  $T$ 
  - $attrs(R) = attrs(S) \cup attrs(T)$
  - $S = \pi_{attrs(S)}(R)$
  - $T = \pi_{attrs(T)}(R)$
- The decomposition is a **lossless join decomposition** if, given known constraints such as FD's, we can guarantee that  $R = S \bowtie T$
- Any decomposition gives  $R \subseteq S \bowtie T$  (why?)
  - A **lossy** decomposition is one with  $R \subset S \bowtie T$

# Loss? But I got more rows!

- “Loss” refers not to the loss of tuples, but to the loss of information
  - Or, the ability to distinguish different original relations





# Questions about decomposition

- When to decompose
- How to come up with a correct decomposition (i.e., lossless join decomposition)

# An answer: BCNF

- A relation  $R$  is in **Boyce-Codd Normal Form** if
  - For every non-trivial FD  $X \rightarrow Y$  in  $R$ ,  $X$  is a super key
  - That is, all FDs follow from “key  $\rightarrow$  other attributes”
- When to decompose
  - As long as some relation is not in BCNF
- How to come up with a correct decomposition
  - Always decompose on a BCNF violation (details next)
  - ☞ Then it is guaranteed to be a lossless join decomposition!

# Example

Is this table in BCNF?

<i>uid</i>	<i>uname</i>	<i>twitterid</i>	<i>gid</i>	<i>fromDate</i>
142	Bart	@BartJSimpson	dps	1987-04-19
123	Milhouse	@MilhouseVan_	gov	1989-12-17
857	Lisa	@lisasimpson	abc	1987-04-19
857	Lisa	@lisasimpson	gov	1988-09-01
456	Ralph	@ralphwiggum	abc	1991-04-25
456	Ralph	@ralphwiggum	gov	1992-09-01
...	...	...	...	...

⇒ **Not** in BCNF

*FD1: uid → uname, twitterid*

*FD2: twitterid → uid*

*FD3: uid, gid → fromDate*

Consider FD1: uid it is **not** a key

Since uid does not work as a key, you have a violation

What is the key?

{uid, gid}

# BCNF decomposition algorithm

- Find a **BCNF violation**
  - That is, a non-trivial FD  $X \rightarrow Y$  in  $R$  where  $X$  is **not** a super key of  $R$
- Decompose  $R$  into  $R_1$  and  $R_2$ , where
  - $R_1$  has attributes  $X \cup Y$
  - $R_2$  has attributes  $X \cup Z$ , where  $Z$  contains all attributes of  $R$  that are in neither  $X$  nor  $Y$
- Repeat until all relations are in BCNF

# BCNF decomposition example

FD1:  $uid \rightarrow uname, twitterid$   
FD2:  $twitterid \rightarrow uid$   
FD3:  $uid, gid \rightarrow fromDate$

*UserJoinsGroup* ( $uid, uname, twitterid, gid, fromDate$ )

BCNF violation:  $uid \rightarrow uname, twitterid$

*User* ( $uid, uname, twitterid$ )

$uid \rightarrow uname, twitterid$   
 $twitterid \rightarrow uid$

BCNF

Not trivial since we have that  
 $uid$  determines another  
attribute?

*Member* ( $uid, gid, fromDate$ )

$uid, gid \rightarrow fromDate$

BCNF

# Another example

FD1:  $uid \rightarrow uname, twitterid$   
FD2:  $twitterid \rightarrow uid$   
FD3:  $uid, gid \rightarrow fromDate$

*UserJoinsGroup* (*uid*, *uname*, *twitterid*, *gid*, *fromDate*)

BCNF violation:  $twitterid \rightarrow uid$

*UserId* (*twitterid*, *uid*)

BCNF

*UserJoinsGroup'* (*twitterid*, *uname*, *gid*, *fromDate*)

$twitterid \rightarrow uname$   
 $twitterid, gid \rightarrow fromDate$

BCNF violation:  $twitterid \rightarrow uname$

BCNF violation since *twitterid* does not serve as a key

*UserName* (*twitterid*, *uname*)

BCNF

*Member* (*twitterid*, *gid*, *fromDate*)

BCNF

# Why is BCNF decomposition lossless

Review this slide

Given non-trivial  $X \rightarrow Y$  in  $R$  where  $X$  is **not** a super key of  $R$ , need to prove:

- Anything we project always comes back in the join:

$$R \subseteq \pi_{XY}(R) \bowtie \pi_{XZ}(R)$$

- Sure; and it doesn't depend on the FD
- Anything that comes back in the join must be in the original relation:

$$R \supseteq \pi_{XY}(R) \bowtie \pi_{XZ}(R)$$

- Proof will make use of the fact that  $X \rightarrow Y$

# BCNF = no redundancy?

- *User (uid, gid, place)*

- A user can belong to multiple groups
- A user can register places she's visited
- Groups and places have nothing to do with other

- FD's? No dependencies since the keys are all the attributes?

- None

- BCNF?

- Yes

- Redundancies?

- Tons!

We will always need to insert a copy of the group for each place they visit with the group

<i>uid</i>	<i>gid</i>	<i>place</i>
142	dps	Springfield
142	dps	Australia
456	abc	Springfield
456	abc	Morocco
456	gov	Springfield
456	gov	Morocco
...	...	...



# Multivalued dependencies

- A **multivalued dependency** (**MVD**) has the form  $X \twoheadrightarrow Y$ , where  $X$  and  $Y$  are sets of attributes in a relation  $R$
- $X \twoheadrightarrow Y$  means that whenever two rows in  $R$  agree on all the attributes of  $X$ , then we can swap their  $Y$  components and get two rows that are also in  $R$

$X$	$Y$	$Z$
$a$	$b_1$	$c_1$
$a$	$b_2$	$c_2$
$a$	$b_2$	$c_1$
$a$	$b_1$	$c_2$
...	...	...

# MVD examples

*User (uid, gid, place)*

- $uid \twoheadrightarrow gid$
- $uid \twoheadrightarrow place$ 
  - Intuition: given *uid*, *gid* and *place* are “independent”
- $uid, gid \twoheadrightarrow place$ 
  - Trivial:  $LHS \cup RHS = \text{all attributes of } R$
- $uid, gid \twoheadrightarrow uid$ 
  - Trivial:  $LHS \supseteq RHS$

Since the place a person visits is independent of the groups they are with, we can swap the places

# Complete MVD + FD rules

Review this slide

- FD reflexivity, augmentation, and transitivity
- MVD complementation:  
If  $X \twoheadrightarrow Y$ , then  $X \twoheadrightarrow \text{attrs}(R) - X - Y$  Ask professor if he would recommend going through the textbook questions  
Ask what other sources he would recommend
- MVD augmentation:  
If  $X \twoheadrightarrow Y$  and  $V \subseteq W$ , then  $XW \twoheadrightarrow YV$
- MVD transitivity:  
If  $X \twoheadrightarrow Y$  and  $Y \twoheadrightarrow Z$ , then  $X \twoheadrightarrow Z - Y$
- Replication (FD is MVD):  
If  $X \rightarrow Y$ , then  $X \twoheadrightarrow Y$
- Coalescence:  
If  $X \twoheadrightarrow Y$  and  $Z \subseteq Y$  and there is some  $W$  disjoint from  $Y$  such that  $W \rightarrow Z$ , then  $X \rightarrow Z$

*Try proving things using these!?*

# An elegant solution: chase

- Given a set of FD's and MVD's  $\mathcal{D}$ , does another dependency  $d$  (FD or MVD) follow from  $\mathcal{D}$ ?
- Procedure
  - Start with the “if-part” of  $d$ , and treat them as “seed” tuples in a relation
  - Apply the given dependencies in  $\mathcal{D}$  repeatedly
    - If we apply an FD, we infer equality of two symbols
    - If we apply an MVD, we infer more tuples
  - If we infer the “then-part” of  $d$ , we have a **proof**
  - Otherwise, **if nothing more can be inferred**, we have a **counterexample**

# Proof by chase

- In  $R(A, B, C, D)$ , does  $A \twoheadrightarrow B$  and  $B \twoheadrightarrow C$  imply that  $A \twoheadrightarrow C$ ?

Ask professor to go through  
this proof after class

Have:

<i>A</i>	<i>B</i>	<i>C</i>	<i>D</i>
<i>a</i>	<i>b</i> <sub>1</sub>	<i>c</i> <sub>1</sub>	<i>d</i> <sub>1</sub>
<i>a</i>	<i>b</i> <sub>2</sub>	<i>c</i> <sub>2</sub>	<i>d</i> <sub>2</sub>
$A \twoheadrightarrow B$			
<i>a</i>	<i>b</i> <sub>2</sub>	<i>c</i> <sub>1</sub>	<i>d</i> <sub>1</sub>
<i>a</i>	<i>b</i> <sub>1</sub>	<i>c</i> <sub>2</sub>	<i>d</i> <sub>2</sub>
$B \twoheadrightarrow C$			
<i>a</i>	<i>b</i> <sub>2</sub>	<i>c</i> <sub>1</sub>	<i>d</i> <sub>2</sub>
<i>a</i>	<i>b</i> <sub>2</sub>	<i>c</i> <sub>2</sub>	<i>d</i> <sub>1</sub>
$B \twoheadrightarrow C$			
<i>a</i>	<i>b</i> <sub>1</sub>	<i>c</i> <sub>2</sub>	<i>d</i> <sub>1</sub>
<i>a</i>	<i>b</i> <sub>1</sub>	<i>c</i> <sub>1</sub>	<i>d</i> <sub>2</sub>

Need:

<i>A</i>	<i>B</i>	<i>C</i>	<i>D</i>
<i>a</i>	<i>b</i> <sub>1</sub>	<i>c</i> <sub>2</sub>	<i>d</i> <sub>1</sub>
<i>a</i>	<i>b</i> <sub>2</sub>	<i>c</i> <sub>1</sub>	<i>d</i> <sub>2</sub>



# Another proof by chase

- In  $R(A, B, C, D)$ , does  $A \rightarrow B$  and  $B \rightarrow C$  imply that  $A \rightarrow C$ ?

Have:

<i>A</i>	<i>B</i>	<i>C</i>	<i>D</i>
<i>a</i>	<i>b</i> <sub>1</sub>	<i>c</i> <sub>1</sub>	<i>d</i> <sub>1</sub>
<i>a</i>	<i>b</i> <sub>2</sub>	<i>c</i> <sub>2</sub>	<i>d</i> <sub>2</sub>

Need:

$$c_1 = c_2 \text{ ✌}$$

$$A \rightarrow B \quad b_1 = b_2$$

$$B \rightarrow C \quad c_1 = c_2$$

In general, with both MVD's and FD's,  
chase can generate both new tuples and new equalities

# Counterexample by chase

- In  $R(A, B, C, D)$ , does  $A \twoheadrightarrow BC$  and  $CD \rightarrow B$  imply that  $A \rightarrow B$ ?

Have:

<i>A</i>	<i>B</i>	<i>C</i>	<i>D</i>
<i>a</i>	<i>b</i> <sub>1</sub>	<i>c</i> <sub>1</sub>	<i>d</i> <sub>1</sub>
<i>a</i>	<i>b</i> <sub>2</sub>	<i>c</i> <sub>2</sub>	<i>d</i> <sub>2</sub>
<i>a</i>	<i>b</i> <sub>2</sub>	<i>c</i> <sub>2</sub>	<i>d</i> <sub>1</sub>
<i>a</i>	<i>b</i> <sub>1</sub>	<i>c</i> <sub>1</sub>	<i>d</i> <sub>2</sub>

$A \twoheadrightarrow BC$

Need:

$$b_1 = b_2 \text{ } \downarrow$$

Review this with professor

Counterexample!

If *b*<sub>2</sub> and *b*<sub>1</sub> have different values, then you can not have that  $A \rightarrow B$

# 4NF

- A relation  $R$  is in **Fourth Normal Form (4NF)** if
  - For every non-trivial MVD  $X \twoheadrightarrow Y$  in  $R$ ,  $X$  is a superkey
  - That is, all FD's and MVD's follow from “key  $\rightarrow$  other attributes” (i.e., no MVD's and no FD's besides key functional dependencies)
- 4NF is stronger than BCNF
  - Because every FD is also an MVD



# 4NF decomposition algorithm

- Find a **4NF violation**
    - A non-trivial MVD  $X \twoheadrightarrow Y$  in  $R$  where  $X$  is **not** a superkey
  - Decompose  $R$  into  $R_1$  and  $R_2$ , where
    - $R_1$  has attributes  $X \cup Y$
    - $R_2$  has attributes  $X \cup Z$  (where  $Z$  contains  $R$  attributes not in  $X$  or  $Y$ )
  - Repeat until all relations are in 4NF
- 
- Almost identical to BCNF decomposition algorithm
  - Any decomposition on a 4NF violation is lossless

# 4NF decomposition example

Is the key not  
uid, gid, and place?

*User (uid, gid, place)*

4NF violation:  $uid \twoheadrightarrow gid$

<i>uid</i>	<i>gid</i>	<i>place</i>
142	dps	Springfield
142	dps	Australia
456	abc	Springfield
456	abc	Morocco
456	gov	Springfield
456	gov	Morocco
...	...	...

*Member (uid, gid)*

4NF

<i>uid</i>	<i>gid</i>
142	dps
456	abc
456	gov
...	...

*Visited (uid, place)*

4NF

<i>uid</i>	<i>place</i>
142	Springfield
142	Australia
456	Springfield
456	Morocco
...	...

# Third Normal Form (3NF)

- R with FDs  $F$  is in **3NF** if, for all  $X \rightarrow Y$  in  $F^+$ 
  - $Y \in X$  (called a *trivial* FD), or
  - $X$  is a superkey of R, **or**
  - $Y$  is part of some **candidate key** (not superkey!) for R

Candidate key?

- If R is in BCNF, obviously in 3NF.
- If R is in 3NF, some redundancy is possible.
- It is a compromise, used when BCNF not achievable
  - (e.g., no “good” decomp, or performance considerations).
  - *Lossless-join, dependency-preserving decomposition of R into a collection of 3NF relations always possible.*

# Summary

- Philosophy behind BCNF, 4NF:  
Data should depend on the key,  
the whole key,  
and nothing but the key!
  - You could have multiple keys though
- Other normal forms
  - 3NF: More relaxed than BCNF; will not remove redundancy if doing so makes FDs harder to enforce
  - 2NF: Slightly more relaxed than 3NF
  - 1NF: All column values must be atomic

