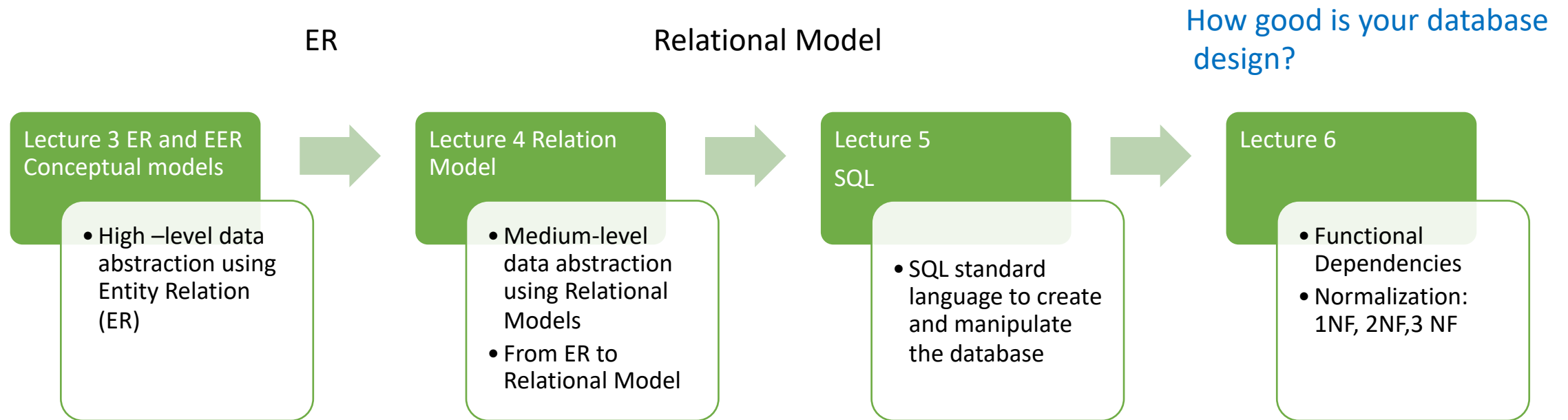


Lecture 5. Functional Dependencies and Normalization (Chapter 14)

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Connection to previous lectures



Outline

- Functional Dependencies
- Normalization:
 - 1NF,
 - 2NF,
 - 3NF,
 - Boyce-Codd NF
 - Multivalued Dependencies and 4NF, 5NF

Informal Guidelines for Relation Databases

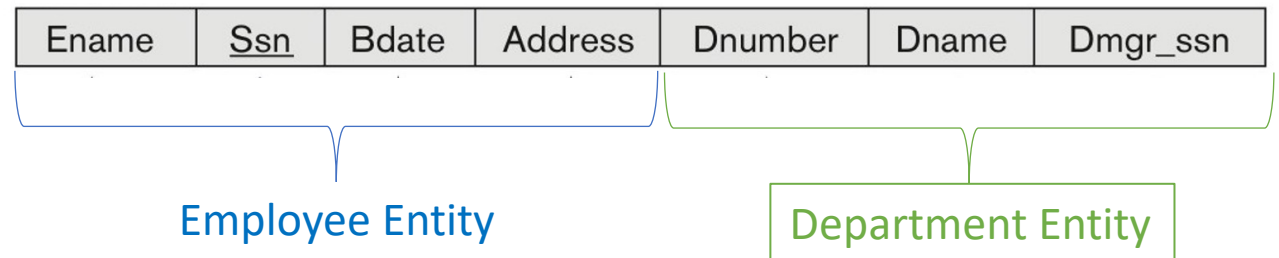
- **Guideline1. Making sure that the semantics of attributes is clear in the schema:** Do not combine attributes from multiple entities and relationships into a single table. If a relation schema corresponds to one entity or one relation, it is straightforward to explain its meaning. But if the relationship corresponds to a mixture of multiple entities (non-binary relationships), the relation can not be easily explained.

Bad design

Example:

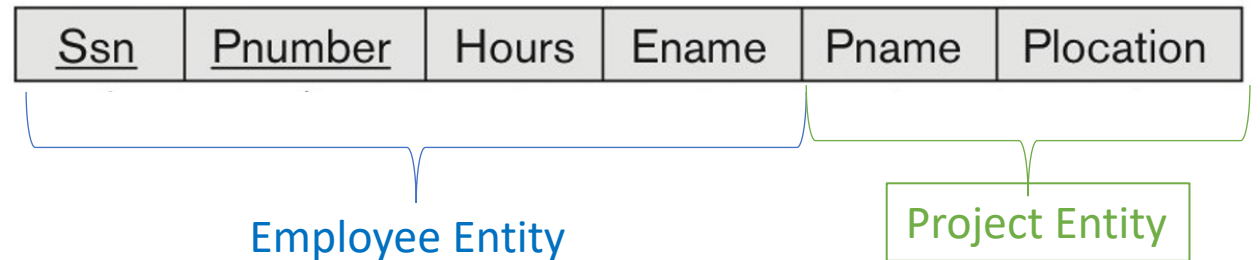
(a)

Employee_Department



(b)

Employee_Project



A simplified COMPANY relational database schema.

Better design according the Guideline 1

| EMPLOYEE | | | | | F.K. |
|----------|------------|-------|---------|---------|------|
| Ename | <u>Ssn</u> | Bdate | Address | Dnumber | |

P.K.

| DEPARTMENT | | | F.K. |
|------------|----------------|----------|------|
| Dname | <u>Dnumber</u> | Dmgr_ssn | |

P.K.

| DEPT_LOCATIONS | | F.K. |
|----------------|------------------|------|
| <u>Dnumber</u> | <u>Dlocation</u> | |

P.K.

| PROJECT | | | | F.K. |
|---------|----------------|-----------|------|------|
| Pname | <u>Pnumber</u> | Plocation | Dnum | |

P.K.

| WORKS_ON | | | F.K. | F.K. |
|------------|----------------|-------|------|------|
| <u>Ssn</u> | <u>Pnumber</u> | Hours | | |

P.K.

Informal Guidelines for Relation Databases

- **Guideline 2. Reducing the redundant information in tuples:** design the relation schema/database so that *no insertion, deletion, or modification anomalies* are present in the entities/tables. If anomalies are present, note them clearly and make sure that the programs (e.g., Python program) that updates the database will operate correctly.

Example

Redundancy

Employee_Department

| Ename | Ssn | Bdate | Address | Dnumber | Dname | Dmgr_ssn |
|----------------------|-----------|------------|--------------------------|---------|----------------|-----------|
| Smith, John B. | 123456789 | 1965-01-09 | 731 Fondren, Houston, TX | 5 | Research | 333445555 |
| Wong, Franklin T. | 333445555 | 1955-12-08 | 638 Voss, Houston, TX | 5 | Research | 333445555 |
| Zelaya, Alicia J. | 999887777 | 1968-07-19 | 3321 Castle, Spring, TX | 4 | Administration | 987654321 |
| Wallace, Jennifer S. | 987654321 | 1941-06-20 | 291 Berry, Bellaire, TX | 4 | Administration | 987654321 |
| Narayan, Ramesh K. | 666884444 | 1962-09-15 | 975 FireOak, Humble, TX | 5 | Research | 333445555 |
| English, Joyce A. | 453453453 | 1972-07-31 | 5631 Rice, Houston, TX | 5 | Research | 333445555 |
| Jabbar, Ahmad V. | 987987987 | 1969-03-29 | 980 Dallas, Houston, TX | 4 | Administration | 987654321 |
| Borg, James E. | 888665555 | 1937-11-10 | 450 Stone, Houston, TX | 1 | Headquarters | 888665555 |

Redundancy

Redundancy

Employee_Project

| Ssn | Pnumber | Hours | Ename | Pname | Plocation |
|-----------|---------|-------|----------------------|-----------------|-----------|
| 123456789 | 1 | 32.5 | Smith, John B. | ProductX | Bellaire |
| 123456789 | 2 | 7.5 | Smith, John B. | ProductY | Sugarland |
| 666884444 | 3 | 40.0 | Narayan, Ramesh K. | ProductZ | Houston |
| 453453453 | 1 | 20.0 | English, Joyce A. | ProductX | Bellaire |
| 453453453 | 2 | 20.0 | English, Joyce A. | ProductY | Sugarland |
| 333445555 | 2 | 10.0 | Wong, Franklin T. | ProductY | Sugarland |
| 333445555 | 3 | 10.0 | Wong, Franklin T. | ProductZ | Houston |
| 333445555 | 10 | 10.0 | Wong, Franklin T. | Computerization | Stafford |
| 333445555 | 20 | 10.0 | Wong, Franklin T. | Reorganization | Houston |
| 999887777 | 30 | 30.0 | Zelaya, Alicia J. | Newbenefits | Stafford |
| 999887777 | 10 | 10.0 | Zelaya, Alicia J. | Computerization | Stafford |
| 987987987 | 10 | 35.0 | Jabbar, Ahmad V. | Computerization | Stafford |
| 987987987 | 30 | 5.0 | Jabbar, Ahmad V. | Newbenefits | Stafford |
| 987654321 | 30 | 20.0 | Wallace, Jennifer S. | Newbenefits | Stafford |
| 987654321 | 20 | 15.0 | Wallace, Jennifer S. | Reorganization | Houston |
| 888665555 | 20 | Null | Borg, James E. | Reorganization | Houston |

Identifying Anomalies

Looking at the example (Employee_Department) shown on slide 6 we can identify the following anomalies

| Operation | Anomaly |
|----------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Insert new department into Employee_Department Table. | If not employee currently worked in the new department, we can't insert the new department information without violating the database schema. This is an insertion anomaly because it restricts the ability to add a certain information without having related data already present. |
| The employee with ssn '888665555' stopped working in this company and we want to delete him. | Deleting this employee will lose the information about "Headquarters" department. This is a deletion anomaly because removing data about employee also removes information about department and department manager. |
| We need to update the department name from "Research" to "Research and Innovation". | To update this change consistently, we would need to modify each row where "Research" department is listed. This is an update anomaly because it requires multiple records updates instead of once to keep our database consistent. |

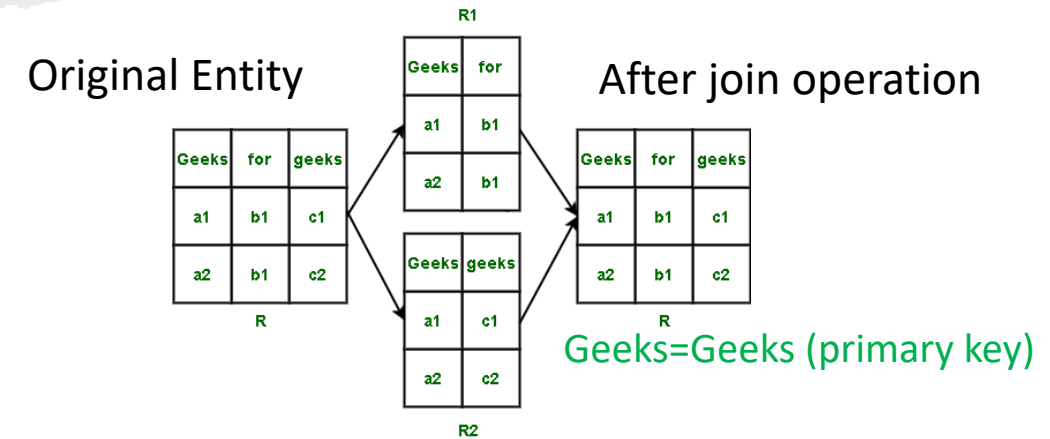
Informal Guidelines for Relation Databases

- **Guidelines 3: Reducing NULL values in tuples/rows:** As far as possible, avoid placing attributes in a base relation whose values may frequently be NULL. If NULL are unavoidable, make sure that they apply in exceptional cases only and do not apply to a majority of tuples/rows in the table.
- For example:
 - if only 15% of employees have individual offices, there is little justification for including an attribute Office_number in the EMPLOYEE table; an additional table Employee_Offices (Essn,Office_number) can be created to include rows/tuples for only the employees with individual offices.

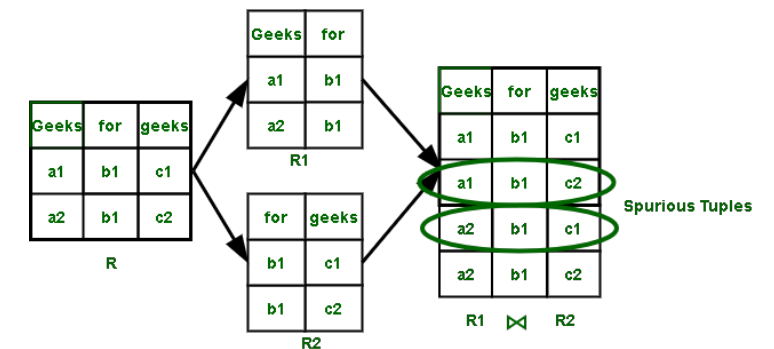
Informal Guidelines for Relation Databases

- **Guideline 4. Disallowing the possibility of generating spurious tuples/rows in table:**
 - Spurious tuples/rows are those rows in a table, which occur as a result of natural joining two tables in wrong manner (more rows than the original set of rows). They are extra (rows) which might not be required. Natural join is implicit join statement on the common columns with the same names in the two tables being joined.
 - Design relation tables so that they can be joined with equality conditions on attributes that are appropriately related (primary key, foreign key) pairs in a way that guarantees that no spurious rows are generated
 - Avoid tables that contain matching attributes that are not (foreign key, primary key) combinations because joining on such attributes may produce spurious rows.
- Solution: the equality condition on primary key or foreign keys should be applied.

Example 1 No Spurious Rows



Example 2 Generated Spurious Rows



for=for (not primary
key/foreign key)

Functional Dependencies (1)

- A *functional dependency* (FD) is a relationship between two attributes, typically between the primary key (PK) and other non-key attributes within a table.
- For any relation ***R (or table)***, attribute *Y* is functionally dependent on attribute *X* (usually the PK), if for every valid instance of *X*, that value of *X* uniquely determines the value of *Y*. This relationship is indicated by the representation below :
- $X \rightarrow Y$
- The left side (*X*) is called the *determinant*, and the right side (*Y*) is the *dependent*.
- Example using Employee_Project table (on slide 6):

| Example | Explanation |
|--------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------|
| $Ssn \rightarrow Ename$ | The value of an employee's social security number (Ssn) uniquely determines the employee name (Ename) |
| $Pnumber \rightarrow \{Pname, Plocation\}$ | The values of a project's number (Pnumber) uniquely determines the project name (Pname) and location (Plocation) |
| $\{Ssn, Pnumber\} \rightarrow Hours$ | A combination of Ssn and Pnumber values uniquely determines the number of hours the employee currently works on the project per week (Hours) |

Functional Dependencies (2)

- A functional dependency is a **property of the table R** , not of a particular table state r of R .
- Therefore, an FD **cannot** be inferred automatically from a given relation state r but must be defined explicitly by someone who knows the semantics of the attributes of R . All we can say is that a certain FD **may** exist if it holds in that particular state r .
- Hence, we can identify a certain FD which **does not hold** if there are rows which show the violation of such an FD.

Example. A table $R(A,B,S,D)$ at particular state r_1

| A | B | C | D |
|----|----|----|----|
| a1 | b1 | c1 | d1 |
| a1 | b2 | c2 | d2 |
| a2 | b2 | c2 | d3 |
| a3 | b3 | c4 | d3 |

FD may hold:

$B \rightarrow C$; $C \rightarrow B$; $\{A,B\} \rightarrow C$; $\{A,B\} \rightarrow D$; $\{C,D\} \rightarrow B$

FD do not hold:

$A \rightarrow B$ (row 2 violates this constrain);

$B \rightarrow A$ (row 3 violates this constrain);

$D \rightarrow C$ (row 4 violates it)

Functional Dependencies (2)

- Example 2 A state of TEACH table

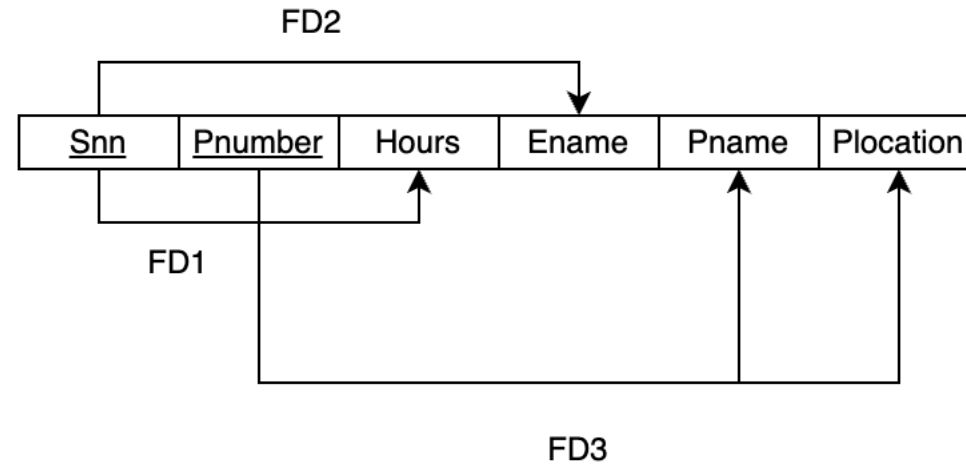
Which FDs may hold?

| Teacher | Course | Book |
|---------|------------------|----------|
| Erik | Programming | Bartam |
| Erik | Database | Martin |
| Alice | Networks | Hoffman |
| Amanda | Machine Learning | Horowitz |

Which FDs do not hold?

Functional Dependencies (3)

- FDs can be displayed on the diagram as follow:



FD1: {Snn, Pnumber} → Hours

FD2: Snn → Ename

FD3: Pnumber → {Pname, Plocation}

Using Armstrong's Axioms rules to identify FDs

- **Reflexive Rule:**

- A set of attributes always determines itself or any of its subsets
- $X \supseteq Y, \text{ then } X \rightarrow Y$
- Example: if $\{A\} \rightarrow \{A\}$, then $\{A\} \rightarrow \{A, B, C\}$. Also called trivial dependencies

If $\{\text{fname}\} \subseteq \{\text{fname}, \text{lname}\}$ then $\{\text{fname}, \text{lname}\} \rightarrow \{\text{fname}\}$

StudentId \rightarrow Name

StudentId, **Name** \rightarrow Name. This dependency is trivial, because adding Name attribute does not bring a new value

- **Augmentation Rule:**


- If $X \rightarrow Y$ holds, then $XZ \rightarrow YZ$ also holds for any set of attributes Z
- Example: if $\{A\} \rightarrow \{B\}$ then $\{A, C\} \rightarrow \{B, C\}$

If $\{\text{Dno}\} \rightarrow \{\text{Dname}\}$ then $\{\text{Dno}, \text{Lname}\} \rightarrow \{\text{Dname}, \text{Lname}\}$ That is adding attributes to dependencies, does not change the basic dependencies

Using Armstrong's Axioms rules to identify FDs

- **Transitive Rule:**

- If $X \rightarrow Y$ and $Y \rightarrow Z$, then $X \rightarrow Z$
- Example: If $\{A\} \rightarrow \{B\}$ and $\{B\} \rightarrow \{C\}$ then $\{A\} \rightarrow \{C\}$

$\{\text{SSN}\} \rightarrow \{\text{Dno}\}$
 $\{\text{Dno}\} \rightarrow \{\text{Dname}\}$  $\{\text{SSN}\} \rightarrow \{\text{Dname}\}$

- **Decomposition Rule:**

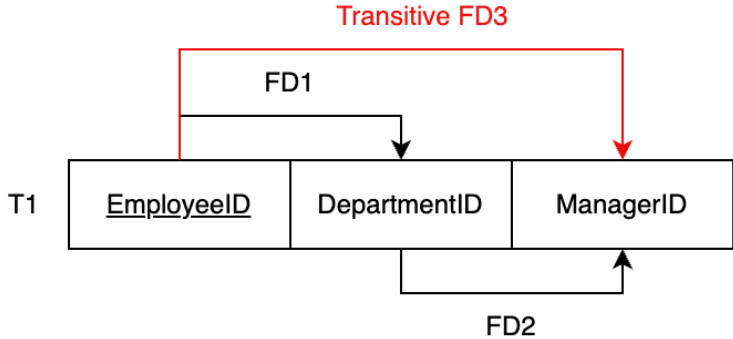
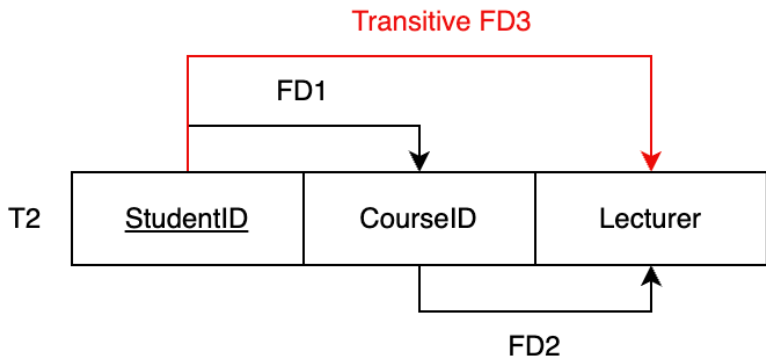
- If $X \rightarrow \{Y, Z\}$, then $X \rightarrow Y$ and $X \rightarrow Z$
- Example: $\{A, B\} \rightarrow \{C\}$, then $\{A, B\} \rightarrow \{A\}$ and $\{A, B\} \rightarrow \{B\}$

How to Apply Armstrong's Axioms

- Start with the given dependencies.
- Apply Armstrong's Axioms
- Repeat until no new FDs can be inferred
- Verify Dependencies against the data to ensure they hold true

Transitive FDs

- Transitive dependencies occur when an attribute depends on another attribute that is not its primary key.

| Example | Transitive FDs | |
|---------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------|
| 1 |  <p>Diagram illustrating transitive dependencies in table T1. The table has attributes <u>EmployeeID</u>, DepartmentID, and ManagerID. FD1 is a functional dependency from EmployeeID to DepartmentID. FD2 is a functional dependency from DepartmentID to ManagerID. FD3 is a transitive functional dependency from EmployeeID to ManagerID, indicated by a red arrow and the label 'Transitive FD3'.</p> | Attribute ManagerID depends on DepartmentID (not primary key) and EmployeeID (primary key) |
| 2 |  <p>Diagram illustrating transitive dependencies in table T2. The table has attributes <u>StudentID</u>, CourseID, and Lecturer. FD1 is a functional dependency from StudentID to CourseID. FD2 is a functional dependency from CourseID to Lecturer. FD3 is a transitive functional dependency from StudentID to Lecturer, indicated by a red arrow and the label 'Transitive FD3'.</p> | Attribute Lecturer depends on CourseID (not primary key) and StudentID (primary key) |

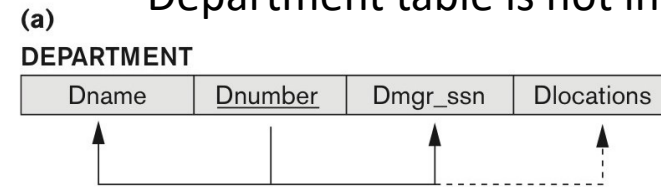
Methodology for testing and improving Relation Database

- Using the Normalization of Relations
- The normalization process take a relation database (or schema) through a series of tests to *certify* whether it satisfies **a certain normal form**.
- All the tables in a database can be in one of the normal forms.
- There are six normal forms, but we will look at the first three, which are:
 - First normal norm (1NF)
 - Second normal norm (2NF)
 - Third normal norm (3NF)
- The **normal form** of a table refers to the highest normal form condition that it meets, and hence indicates the degree to which it has been normalized

First Normal Form(1NF)

- 1NF disallows *relations within relations*, or *relations as attribute values within rows*. The only attribute values permitted by 1NF are **single atomic (or indivisible) values**.
- Example:
 - The domain of Dlocation attribute contains atomic values or single-valued (e.g., Houston), but some rows can have a set of these values (when one department has several locations). In this case, Dlocation is not functionally dependent on the primary key Dnumber.
 - Normalization to 1NF:** remove the attribute Dlocations that violates 1NF and place it in a separate table called DEPT_LOCATIONS with primary key Dnumber of DEPARTMENT. The primary key of this newly formed table is the combination {Dnumber,Dlocation}

Department table is not in 1NF



Sample state of table DEPARTMENT

(b)

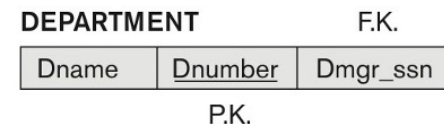
DEPARTMENT

| Dname | <u>Dnumber</u> | Dmgr_ssn | Dlocations |
|----------------|----------------|-----------|--------------------------------|
| Research | 5 | 333445555 | {Bellaire, Sugarland, Houston} |
| Administration | 4 | 987654321 | {Stafford} |
| Headquarters | 1 | 888665555 | {Houston} |

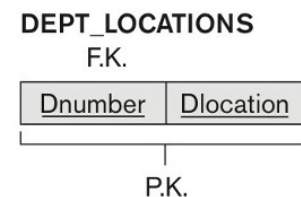
(c) DEPARTMENT is not in 1NF version with redundancy

DEPARTMENT

| Dname | <u>Dnumber</u> | Dmgr_ssn | <u>Dlocation</u> |
|----------------|----------------|-----------|------------------|
| Research | 5 | 333445555 | Bellaire |
| Research | 5 | 333445555 | Sugarland |
| Research | 5 | 333445555 | Houston |
| Administration | 4 | 987654321 | Stafford |
| Headquarters | 1 | 888665555 | Houston |



F.K.



DEPARTMENT and DEPT_LOCATIONS in 1NF form

Normalizing nested relations to 1NF

Normalizing nested relations into 1NF.

(a) Schema of the EMP_PROJ relation with a *nested relation* attribute PROJS.

(b) Sample extension of the EMP_PROJ relation showing nested relations within each tuple.

(c) Decomposition of EMP_PROJ into relations EMP_PROJ1 and EMP_PROJ2 by propagating the primary key.

(a)

| EMP_PROJ | | Projs | |
|----------|-------|---------|-------|
| Ssn | Ename | Pnumber | Hours |

(b)

| EMP_PROJ | | | |
|-----------|----------------------|---------|-------|
| Ssn | Ename | Pnumber | Hours |
| 123456789 | Smith, John B. | 1 | 32.5 |
| | | 2 | 7.5 |
| 666884444 | Narayan, Ramesh K. | 3 | 40.0 |
| 453453453 | English, Joyce A. | 1 | 20.0 |
| | | 2 | 20.0 |
| 333445555 | Wong, Franklin T. | 2 | 10.0 |
| | | 3 | 10.0 |
| | | 10 | 10.0 |
| | | 20 | 10.0 |
| 999887777 | Zelaya, Alicia J. | 30 | 30.0 |
| | | 10 | 10.0 |
| 987987987 | Jabbar, Ahmad V. | 10 | 35.0 |
| | | 30 | 5.0 |
| 987654321 | Wallace, Jennifer S. | 30 | 20.0 |
| | | 20 | 15.0 |
| 888665555 | Borg, James E. | 20 | NULL |

(c)

EMP_PROJ1

| Ssn | Ename |
|-----|-------|
|-----|-------|

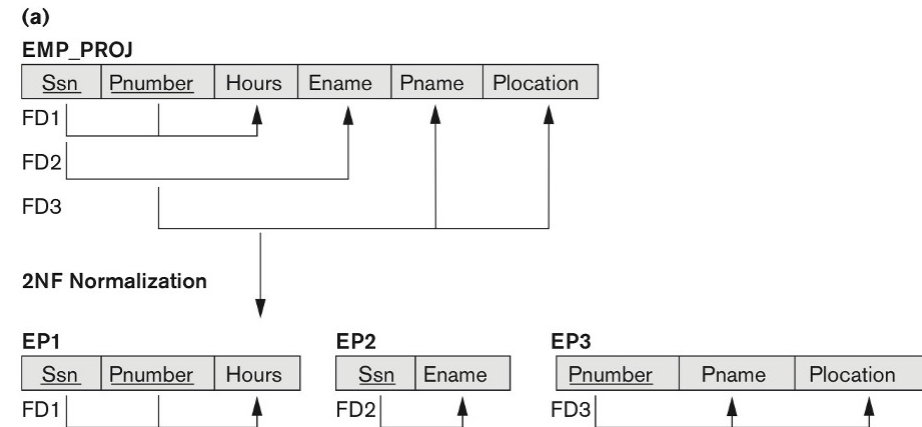
EMP_PROJ2

| Ssn | Pnumber | Hours |
|-----|---------|-------|
|-----|---------|-------|

Second Normal Form(2NF)

- A database (relation schema) R is in 2NF if every nonprime attribute A in R is **fully functionally dependent** on the primary key of R .
- **Fully functionally dependent** means PK are single-valued attribute or is a composite PK, then each non-key attribute must be fully dependent on the entire PK and not on a subset of the PK (i.e., there must be no partial dependency).
- **Normalization to 2NF:**
 - The relation must first be in 1NF. We can not jump from non 1NF to 2NF without first to normalize to 1NF. So, non NF \rightarrow 1NF \rightarrow 2NF
 - Decompose and set up a new table for each partial key with its dependent attribute(s).

Normalizing EMP_PROJ into 2NF relations



Third Normal Form (3NF)

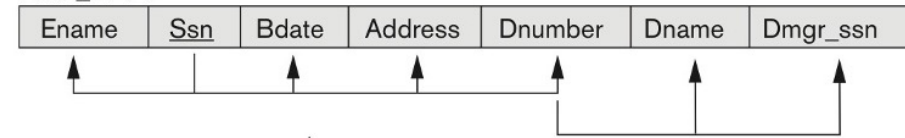
- A database (relation schema) R is in 3NF if it satisfies 2NF and no non-prime attribute of R is transitively dependent on the primary key.
- More precisely: a non-key attribute may not be functionally dependent on another non-key attribute.
- **Normalization to 3NF:**
 - The relation must first be in 2NF. We can not jump from non 1NF to 3NF without first to normalize to 2NF. So, non 1NF \rightarrow 1NF \rightarrow 2NF \rightarrow 3NF
 - Decompose and set up a relation that includes the nonkey attribute(s) that functionally determine(s) other nonkey attribute(s).

Example: EMP_DEPT in 2NF form.

Hence it has non-key attributes FDs. Non-key attribute Dnumber uniquely identifies other non-key attributes Dname and Dmgr_ssn. Thus violate the 3NF constraint

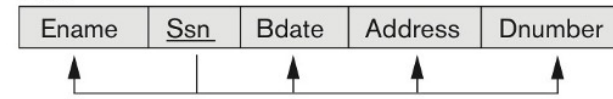
(b)

EMP_DEPT

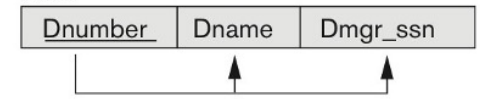


3NF Normalization

ED1



ED2



ED1 table have single-valued primary key Ssn which uniquely identifies all other attributes. No FDs between non-key Attributes
Same for ED2

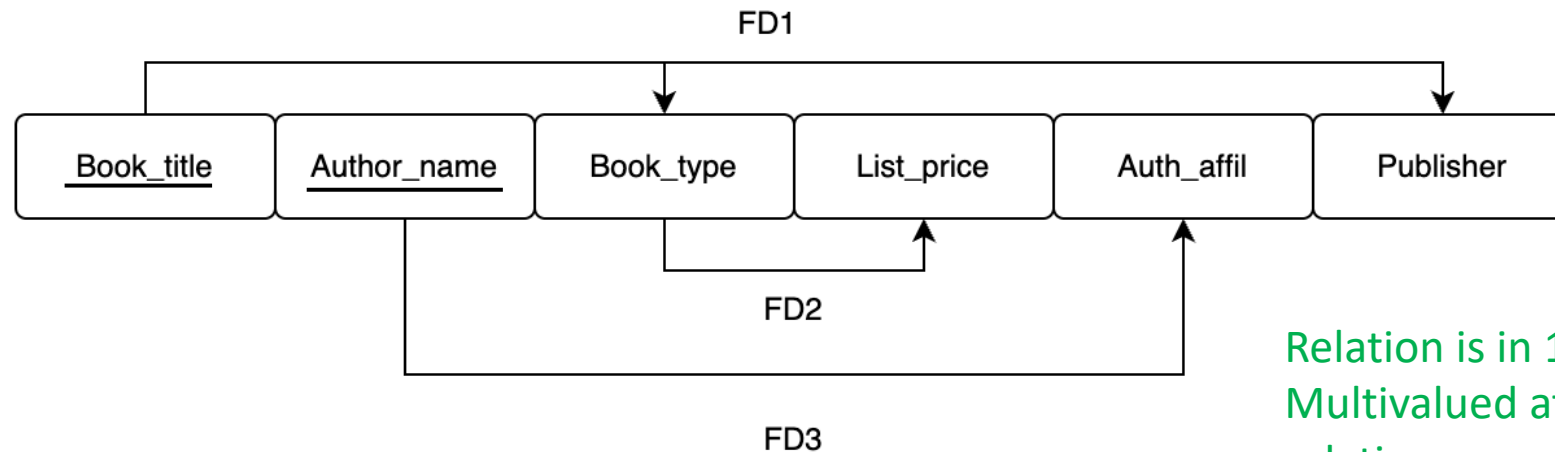
Summary of Three Normal Forms

Table 14.1 Summary of Normal Forms Based on Primary Keys and Corresponding Normalization

| Normal Form | Test | Remedy (Normalization) |
|--------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| First (1NF) | Relation should have no multivalued attributes or nested relations. | Form new relations for each multivalued attribute or nested relation. |
| Second (2NF) | For relations where primary key contains multiple attributes, no nonkey attribute should be functionally dependent on a part of the primary key. | Decompose and set up a new relation for each partial key with its dependent attribute(s). Make sure to keep a relation with the original primary key and any attributes that are fully functionally dependent on it. |
| Third (3NF) | Relation should not have a nonkey attribute functionally determined by another nonkey attribute (or by a set of nonkey attributes). That is, there should be no transitive dependency of a nonkey attribute on the primary key. | Decompose and set up a relation that includes the nonkey attribute(s) that functionally determine(s) other nonkey attribute(s). |

Example 1 : Book Store

- Consider the following relation for published books:



Relation is in 1NF, because it is no Multivalued attributes, and nested relations

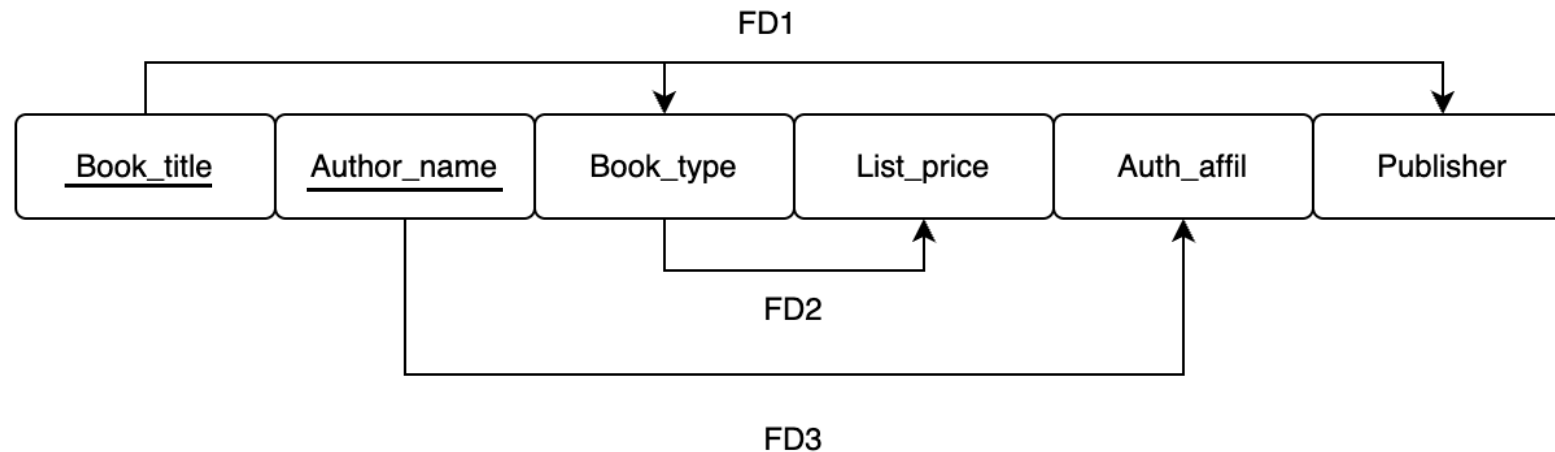
What normal form is the relation?

Check if it is in 1NF:

- Is there multivalued attribute? May be List_price, but we do not see the data and thus can not confirm that this attribute is multivalued.
- Is there nested relations? No, we do not see the data, thus we assume that there is no nested relations

Example 1 : Book Store

- Consider the following relation for published books:

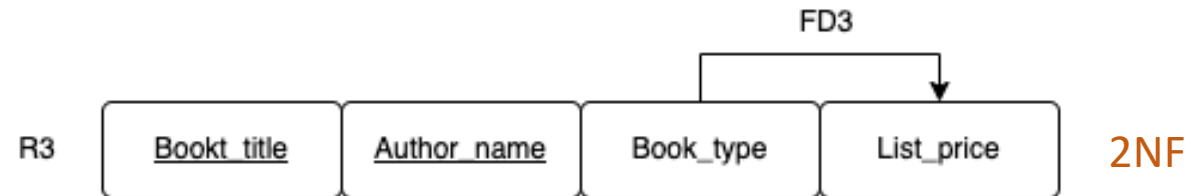
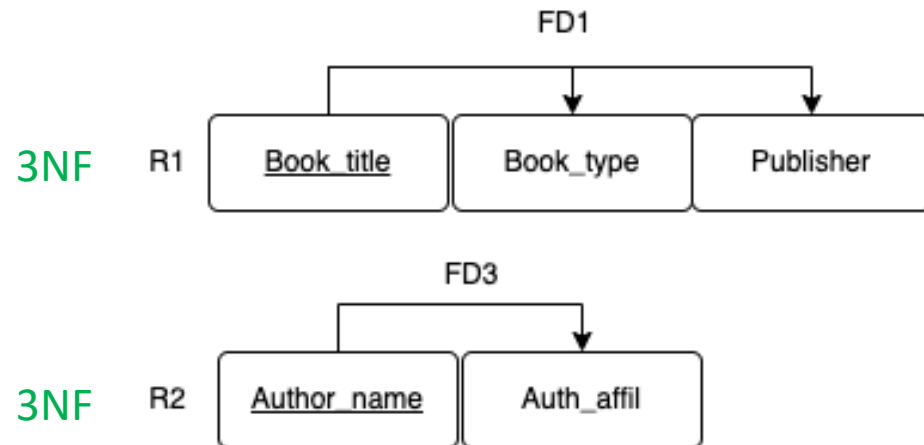


Check if it is in 2NF:

- Is relation contains a composite key? Yes: Book_title and Author_name
- Is there dependencies exist between non-key attribute and part of key attribute? Yes, FD1, FD3

Relation is **not in 2NF**, because it has dependencies between non-key attribute and part of the primary key, such as FD1 and FD3.

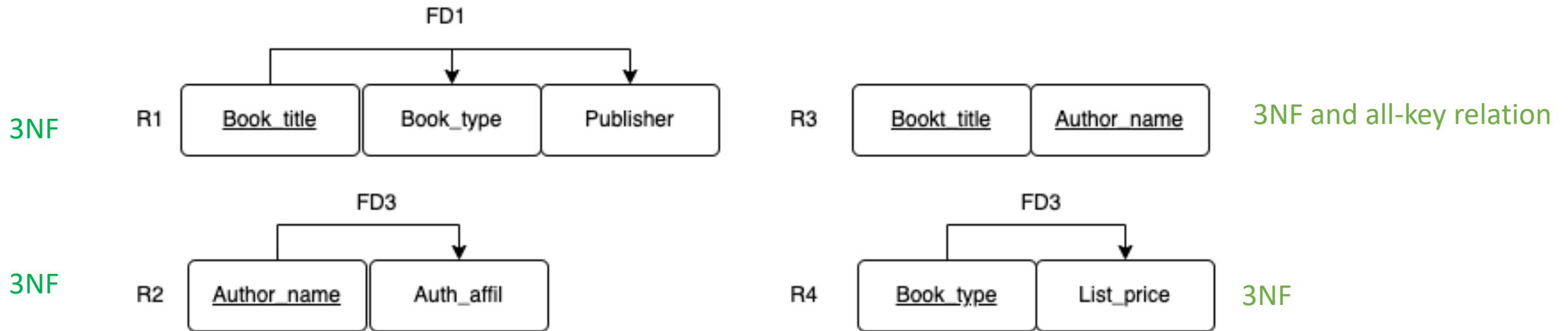
Decompose to 2NF



R3 relation is in 2NF, and not in 3NF because it has Dependencies between non-key attribute and another non-key attribute which is FD3

Relations R1 –R2 are in 3NF, because all non-key attributes depend on the entire primary key, and not transitive dependencies.

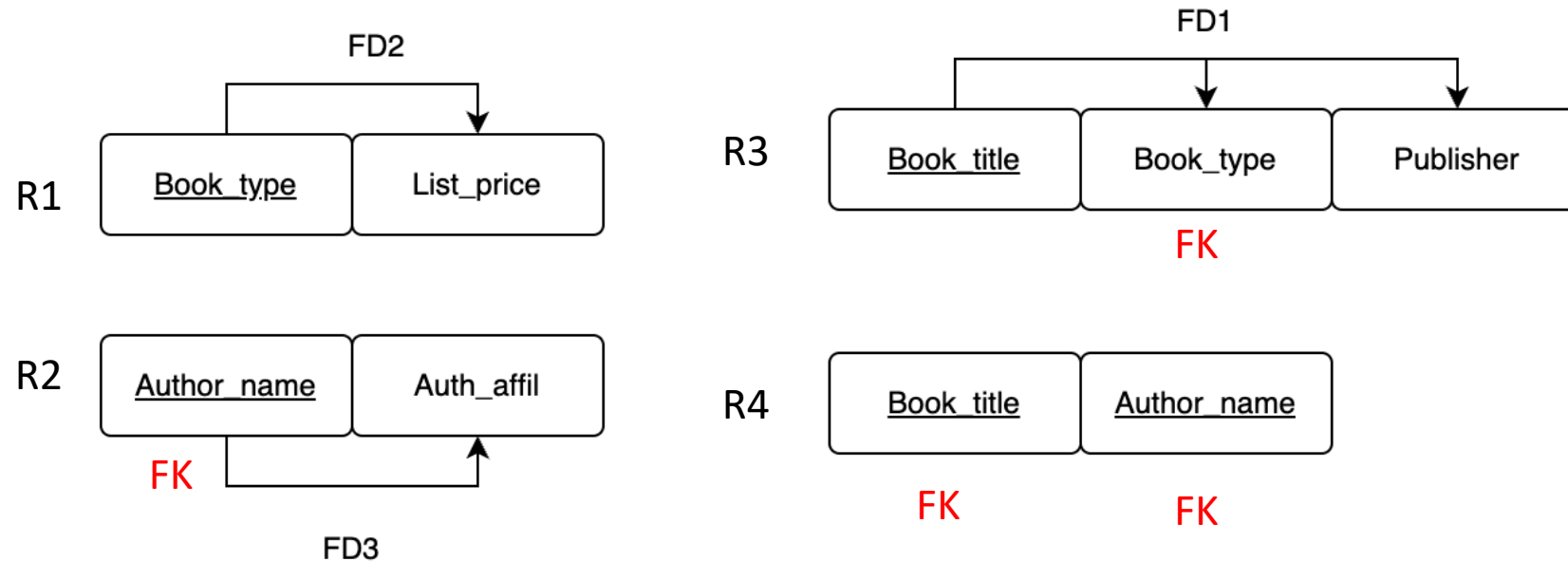
Decompose to R3 to 3NF



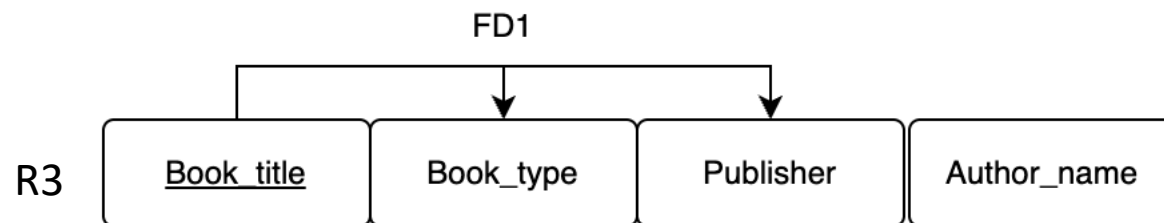
Relations R1 – R4 are in 3NF, because all non-key attributes depend on the entire primary key, and not transitive dependencies.

How to check if the decomposition is correct?

You need to compose back to the original table in ONF using inner join

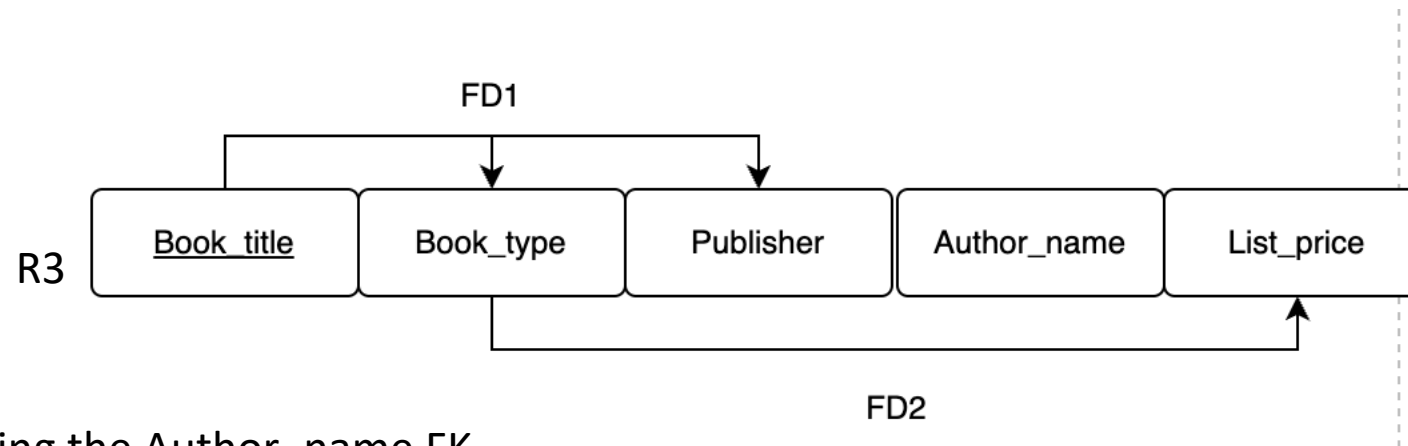


Step 1: Join R3 and R4 using the Book_title FK

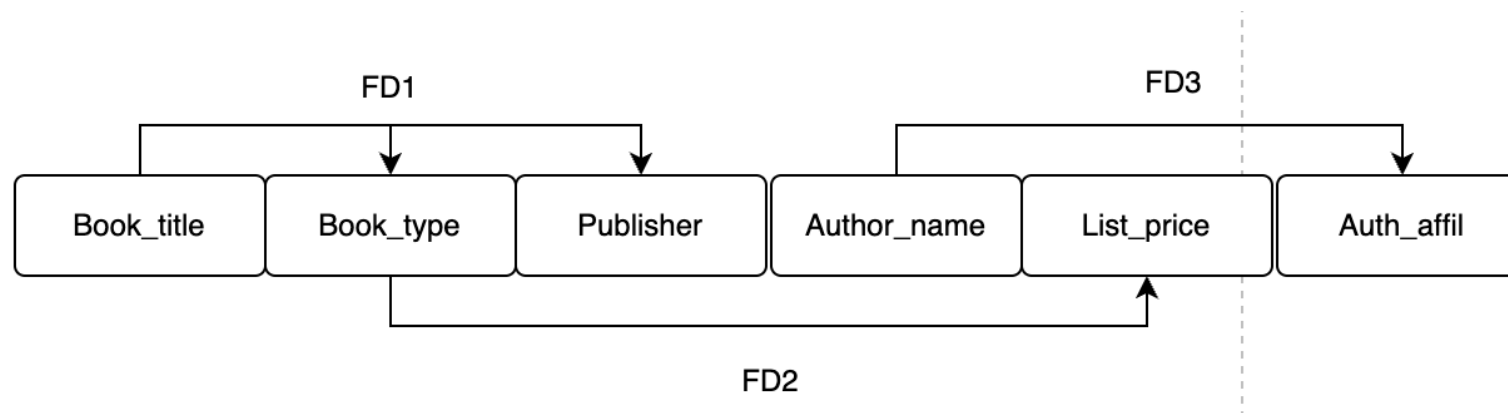


Compose back to ONF

Step 2: Join R1 and R3 using the Book_title FK



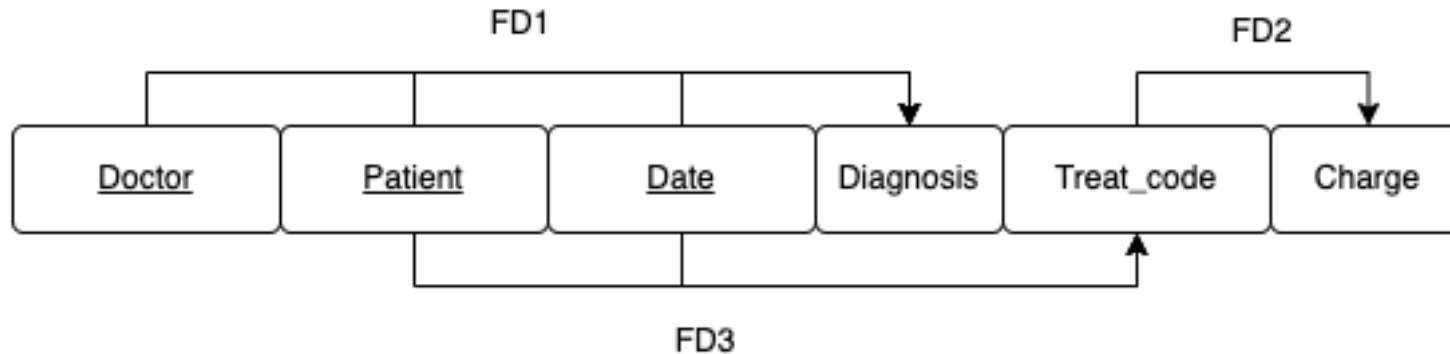
Step 3: Join R2 and R3 using the Author_name FK



This is original
relation in ONF
(slide 24)

Example 2: Hospital visit

The relation is in 1NF because there is no nested relations, and all attributes are atomic



What normal form is the relation?

Composite primary key: Doctor, Patient, Date

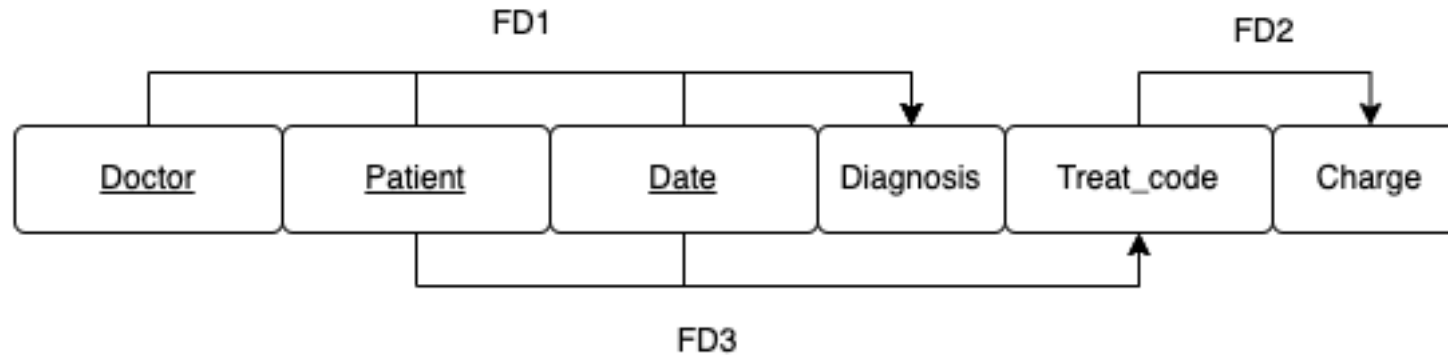
Check if it is in 1NF:

- Is there multivalued attribute?
- Is there nested relations?

Perhaps Diagnosis, hence we do not see the data therefore is not possible to confirm that there are multivalued attributes. We assume that all attributes are atomic

No, there is no data to confirm this

Example 2: Hospital visit



Composite primary key: Doctor, Patient, Date

Check if it is in 2NF:

- Is there dependencies exist between non-key attribute and part of key attribute??

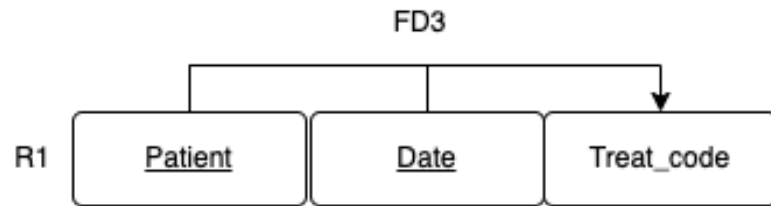
Yes, FD3

The relation is not in 2NF, because of FD3

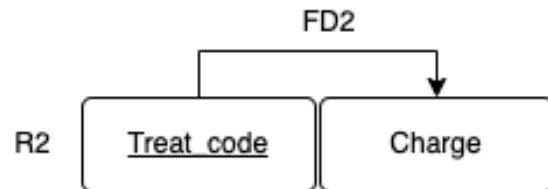
Normalize to 2NF

Create a new relation for FD3 and FD2

3NF



3NF

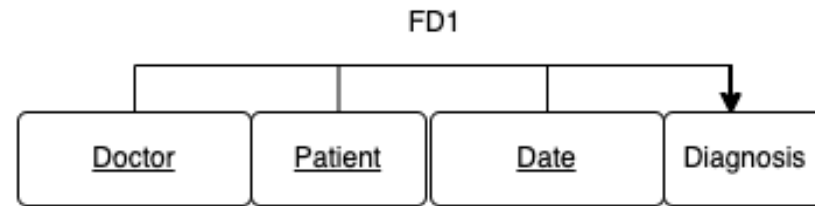


Check if it is in 3NF:

- Is there dependencies exist between non-key attribute and another non-key attribute?

Yes,

R3

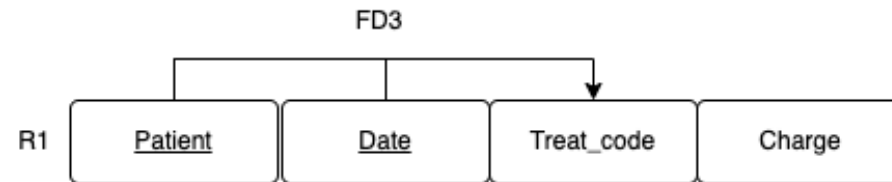


3NF

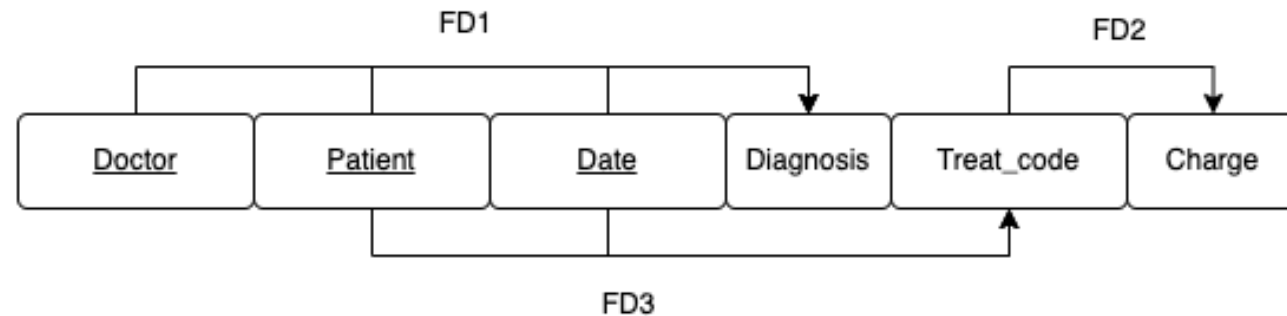
All relations in 3NF

Compose back to original table in 1NF

Step1: Join R1 and R2 on key: Treat_code



Step 2: Join the result with R3 on key Patient, Date

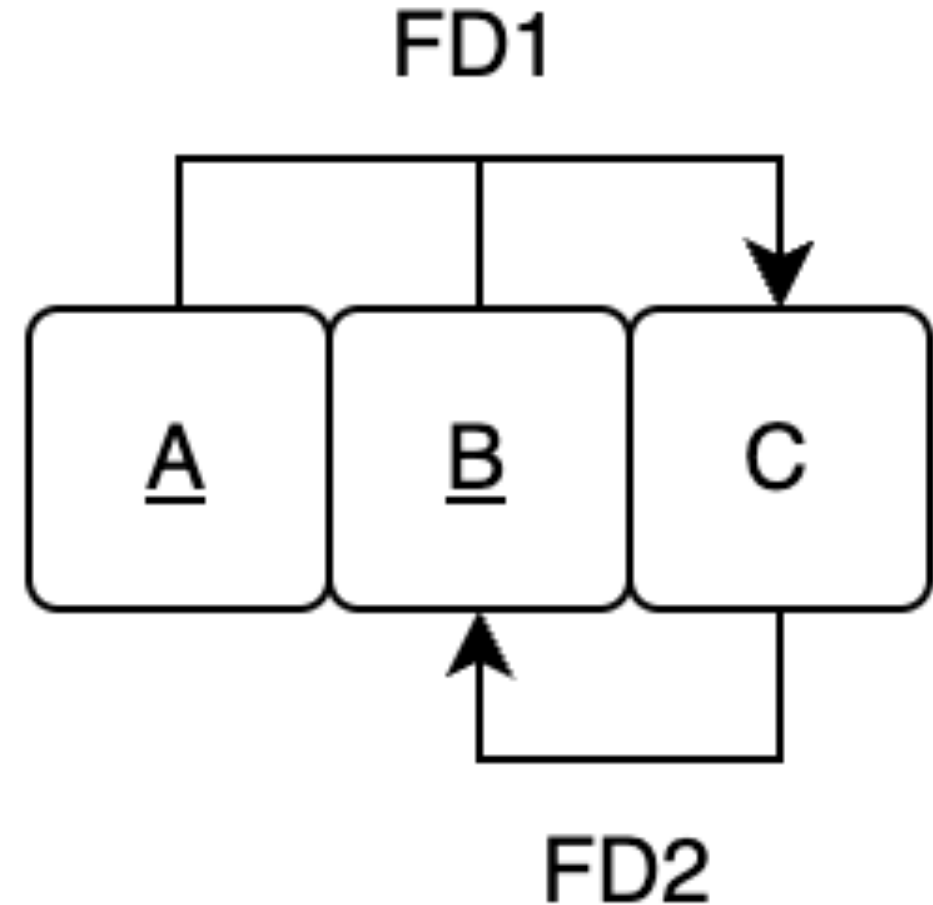


Break 10 min

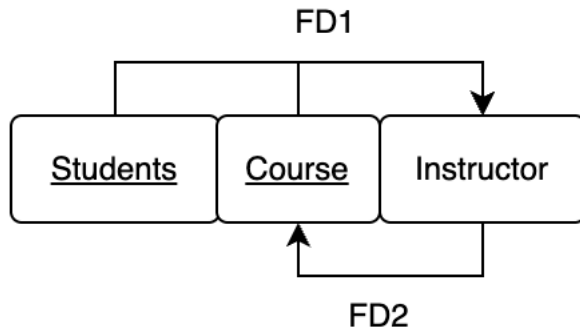
Relation is in BCNF if whenever a *nontirival functional dependencies* $X \rightarrow A$ holds in R, then X is a superkey of R

Boyce-Codd Normal Form (BCNF)

In 3NF, but not in BCNF



Example



| N | Student | Course | Instructor |
|---|---------|-------------|------------|
| 1 | Narayan | Database | Mark |
| 2 | Smith | Database | Navathe |
| 3 | Smith | Informatics | Ammar |
| 4 | Smith | Math | Schulman |
| 5 | Wallace | Database | Mark |
| 6 | Wallace | Informatics | Ahamad |
| 7 | Wong | Database | Omiecinski |
| 8 | Zelaya | Database | Navathe |
| 9 | Narayan | Informatics | Ammar |

Possible decompositions:

Option 1: R1 (Student, Instructor) and R2 (Student, Course)

Option 2: R1 (Course, Instructor) and R2 (Course, Student)

Option 3: R1 (Instructor, Course) and R2 (Instructor, Student)

Two properties of decomposition:

- Functional dependencies preserving property
- Nonadditive join property

Possible decompositions:

Option 1: $R1 \cap R2 \mapsto (R1-R2): \text{Student} \mapsto \text{Instructor}$

Option 2: $R1 \cap R2 \mapsto (R1-R2): \text{Course} \mapsto \text{Instructor}$

Option 3: $R1 \cap R2 \mapsto (R1-R2): \text{Instructor} \mapsto \text{Course}$

FD2

Multivalued Dependency (MVD) and Fourth Normal Form

- MVD describes relationships between sets of attributes

| <u>Employee Name</u> | <u>Project Name</u> | <u>Dependent Name</u> |
|----------------------|---------------------|-----------------------|
| Smith | X | John |
| Smith | Y | Anna |
| Smith | X | Anna |
| Smith | Y | John |

All-key relation is always in BCNF, it has no FDs

Employee_name \twoheadrightarrow Project_Name | Dependent_Name

4NF

| <u>Employee Name</u> | <u>Project Name</u> |
|----------------------|---------------------|
| Smith | X |
| Smith | Y |

4NF

| <u>Employee Name</u> | <u>Dependent Name</u> |
|----------------------|-----------------------|
| Smith | John |
| Smith | Anna |

MVD Example

| <u>Manufacturer</u> | <u>Color</u> | <u>Fuel</u> |
|---------------------|--------------|-------------|
| Volvo | Green | diesel |
| Audi | Grey | Bensin |
| Volvo | White | diesel |
| Toyota | White | Bensin |
| Toyota | White | diesel |
| Toyota | Grey | Bensin |
| Ford | White | Etanol |
| Ford | Red | Etanol |

Relation is in 3NF and BCNF, all-key relation

Adding a new color means we need to repeat Manufacturer and Color attribute three times for each fuel type: Bensin, Diesel, etanol.

Available colors must be independent from available fuel types.

Manufacturer has a set of colors and set of fuel which cause the **multivalued dependencies**.

$\{\text{Manufacturer}\} \twoheadrightarrow \{\text{Color}\}$

$\{\text{Manufacturer}\} \twoheadrightarrow \{\text{Fuel}\}$

Manufacturer attribute is not a key, it is a part of the key.
Key is composite: Manufacturer, Color, Fuel

MVD Example

R1

| <u>Manufacturer</u> | <u>Color</u> |
|---------------------|--------------|
| Volvo | Green |
| Audi | Grey |
| Volvo | White |
| Toyota | White |
| Toyota | Grey |
| Ford | White |
| Ford | Red |

R2

| <u>Manufacturer</u> | <u>Fuel</u> |
|---------------------|-------------|
| Volvo | diesel |
| Audi | Bensin |
| Toyota | Bensin |
| Toyota | diesel |
| Ford | Etanol |

We can add a new color without violating insert constraint

Fifth Normal Form

| <u>Person</u> | <u>Brand</u> | <u>Flavor</u> |
|---------------|--------------|---------------|
| Adam | Sia Glass | Vanilla |
| Adam | Sia Glass | Chocolate |
| Adam | Magnum | Vanilla |
| Jessica | GB Glace | Strawberry |
| Jessica | GB Glace | Orange |
| Amanda | GB Glace | Chocolate |
| Amanda | ICA glass | Strawberry |
| Amanda | ICA glass | Mint |
| Amanda | Sia Glass | Chocolate |
| Amanda | Sia Glass | Strawberry |
| Amanda | Sia Glass | Mint |

5NF



Person N:M Brand
Brand N:M Flavor
Person N:M Flavor

Amanda likes now Sia Glass

| <u>Person</u> | <u>Brand</u> |
|---------------|--------------|
| Adam | Sia Glass |
| Adam | Magnum |
| | |

| <u>Brand</u> | <u>Flavor</u> |
|--------------|---------------|
| Sia Glass | Vanilla |
| Magnum | Vanilla |
| | |

| <u>Person</u> | <u>Flavor</u> |
|---------------|---------------|
| Amanda | Chocolate |
| Amanda | Strawberry |
| | |

Key terms (for Exam)

- A ***functional dependency(FD)*** is a constraint between two sets of attributes from the database.
- A ***normalization*** is a process to determining how much redundancy exists in a database. This process involves analysis of relational schema based on their functional dependencies and primary key to minimizing redundancy, insertions, edition, and update anomalies.
- There are six normal forms, but only three most commonly used are: 1NF, 2NF, and 3NF
- The understanding of table 14.1 (slide 20)

Video Tutorial

- <https://www.youtube.com/watch?v=VFuAwSoMatw&list=PLyp-1WQY32mN6U6PUq9c977X9vyHxtohd&index=2>