Augmented Panel Data Models with Staggered Adoption

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Summary

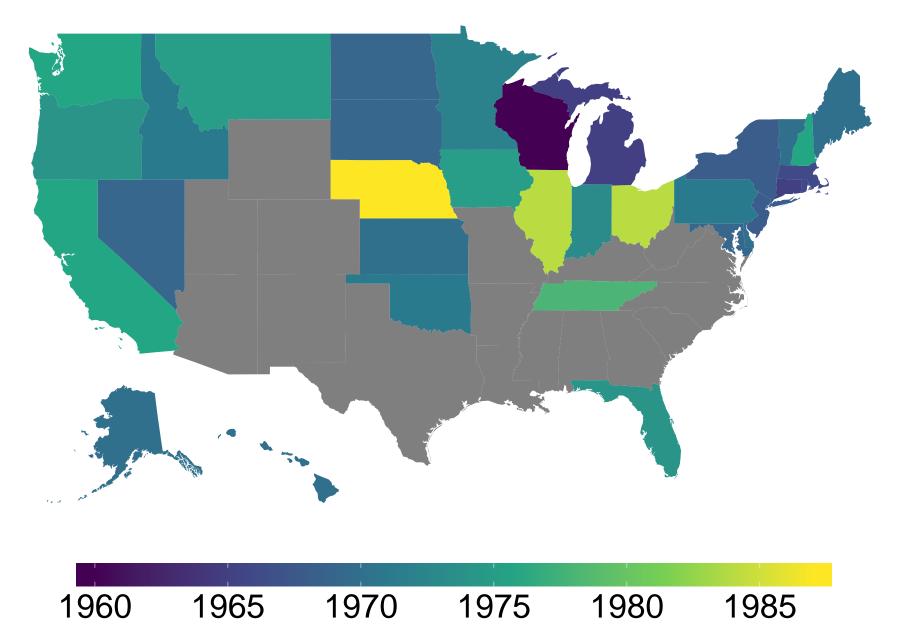
- Often, jurisdictions adopt policies over time
- Differences in Differences (DiD) is a workhorse, but parallel trends isn't always reasonable
- Synthetic Control Method (SCM) is more flexible, but designed for a single treatment time
- We extend SCM to staggered adoption setting, partially pool across times, and combine with DiD

Mandatory Collective Bargaining

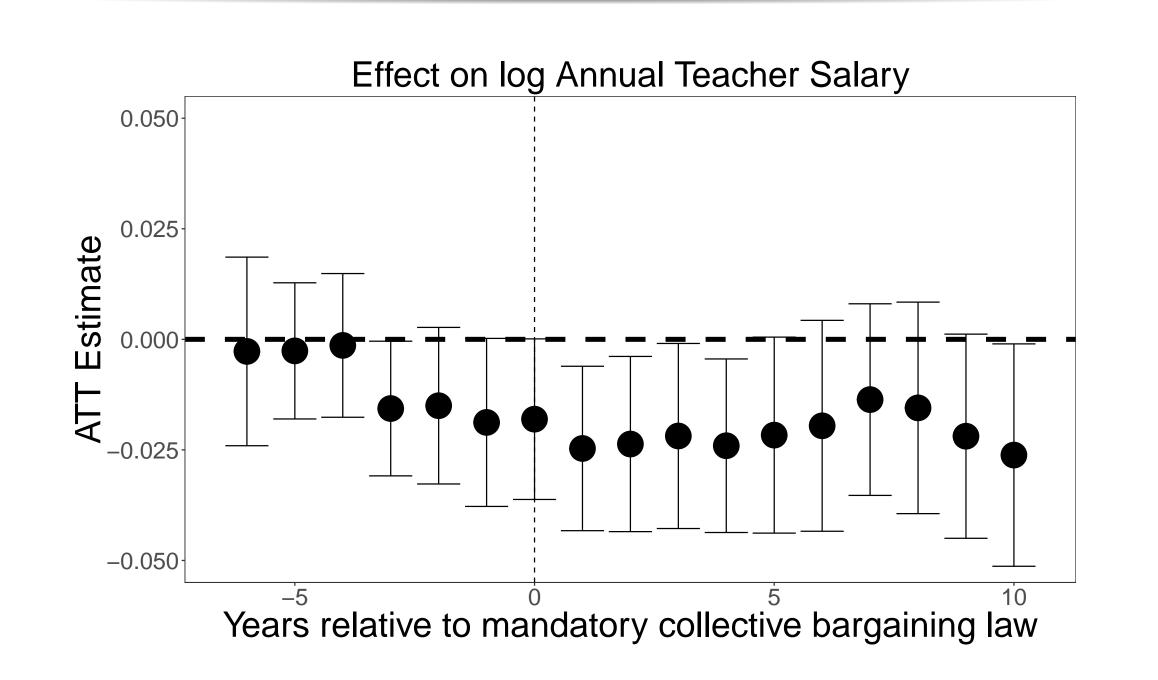
Do public sector unions influence public spending? **Data**: Mandatory collective bargaining laws [1]

- Study period: 1959 to 1997
- 33 states mandate bargaining with public unions
- 10 states allow but do not require, 7 prohibit
- Evaluate effect on average teacher salaries

Year of Mandatory Collective Bargaining Law



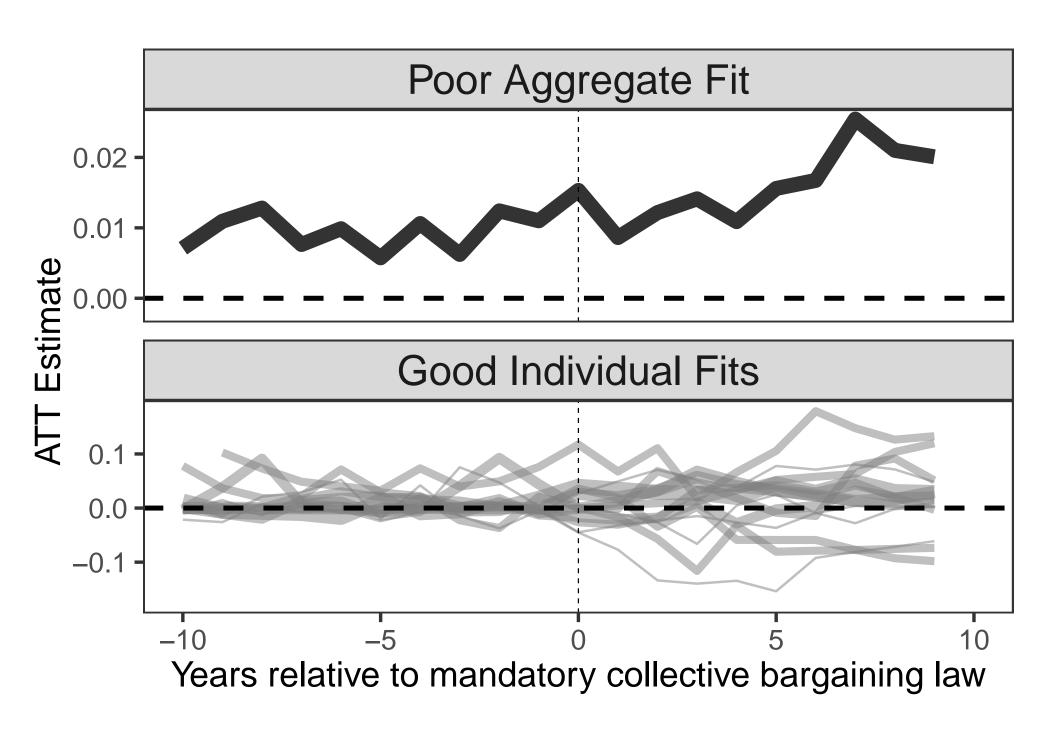
Non-parallel trends



No parallel trends? No problem!

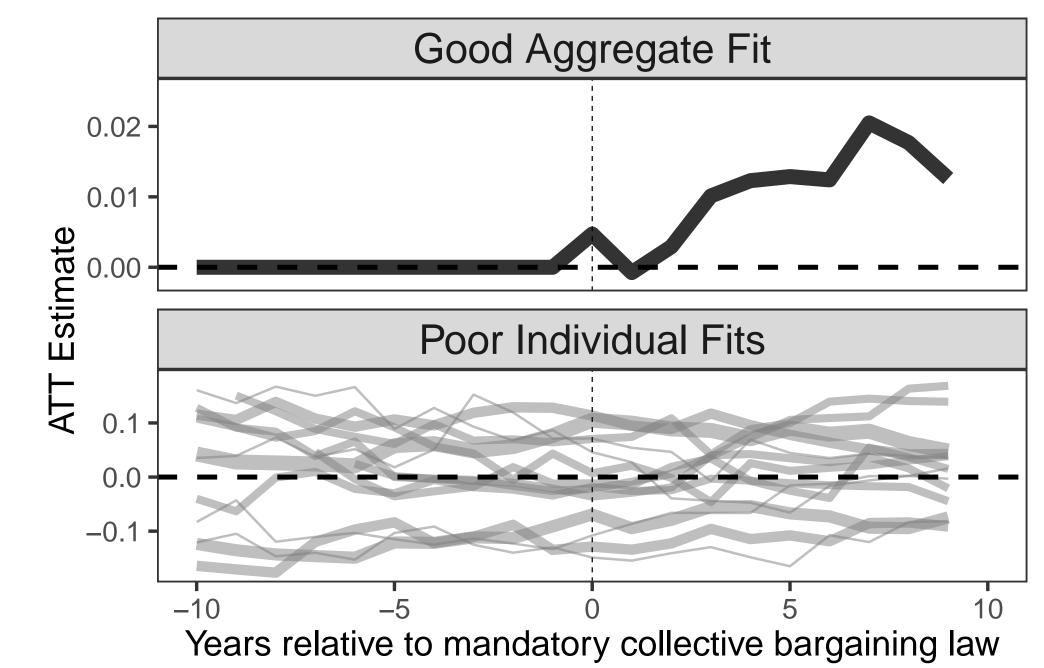
Separate SCM

Fit many separate synthetic controls

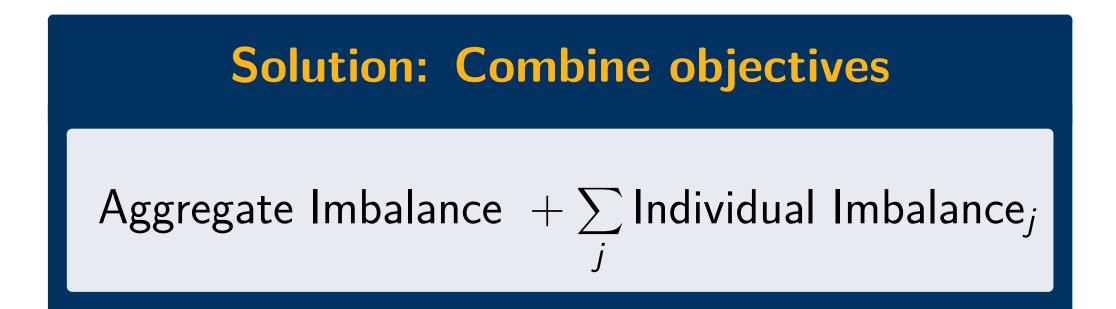


Aggregated SCM

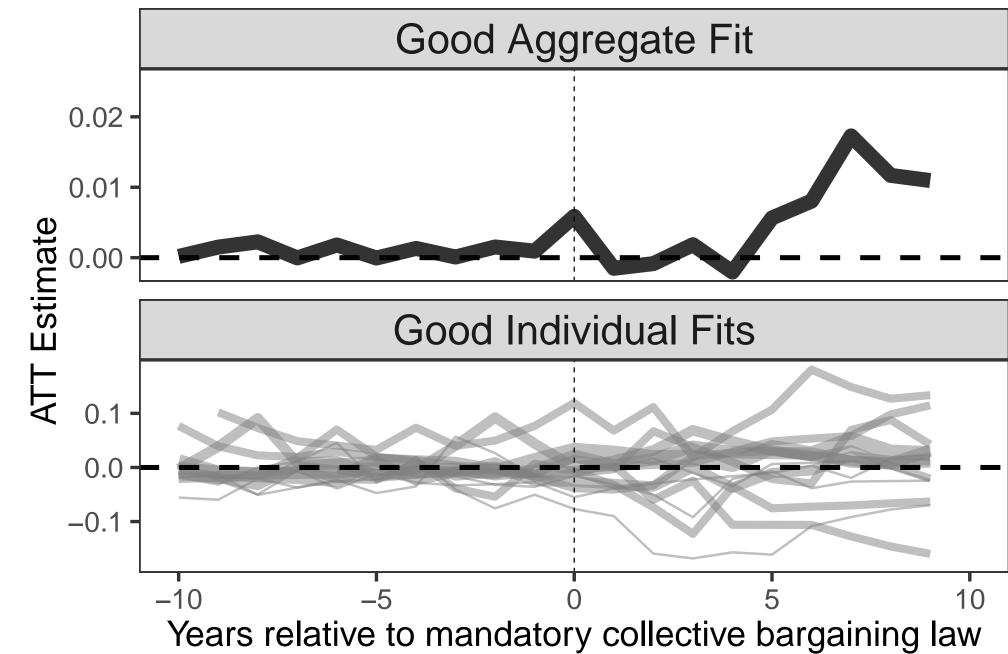
Fit a single aggregated synthetic control

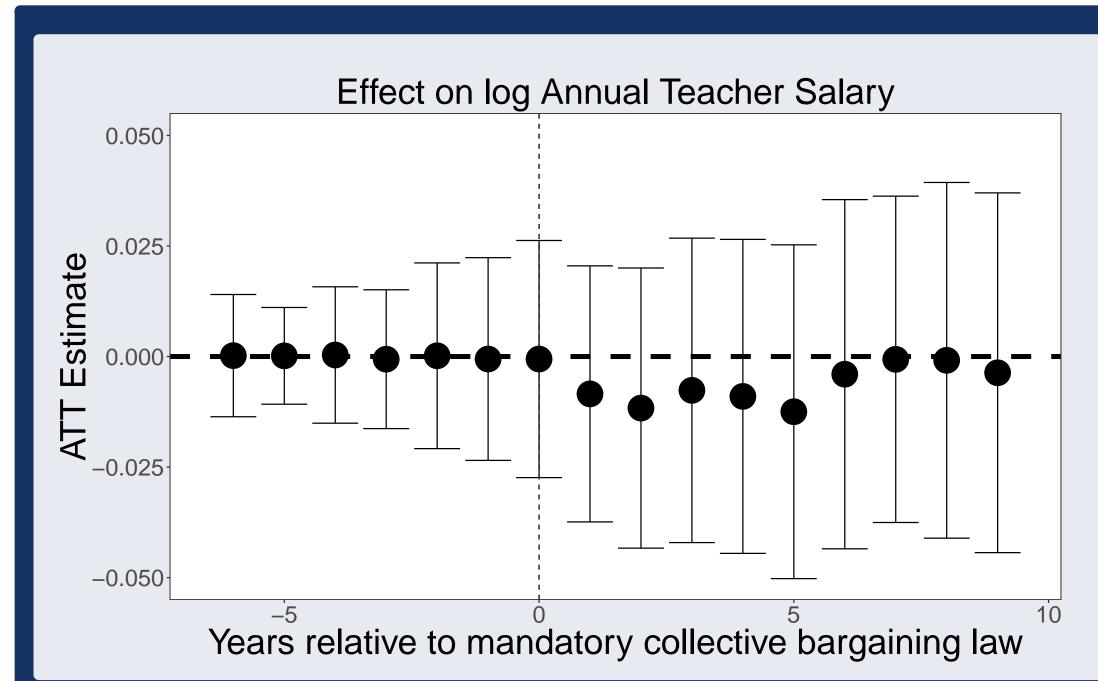


Partially Pooled SCM



- Move continuously between both solutions
- Trades off individual fit and aggregate fit
- Dual view as partial pooling across adoption times





Combining Weighting and DiD

Augment w/pre-period average: weighted DiD [2]

$$\frac{1}{T_{j}} \sum_{t'=1}^{T_{j}} \left[\frac{1}{N_{1j}} \sum_{W_{i}=j} (Y_{it} - Y_{it'}) - \sum_{W_{i}=0} \hat{\gamma}_{ij} (Y_{it} - Y_{it'}) \right]$$

- Adjust for non-parallel trends
- Balance residuals after unit/time fixed effects
- Add fixed effects and weighted residuals
- Key assumption: conditional parallel trends [3, 4]

Hierarchical Generalized Propensity Score

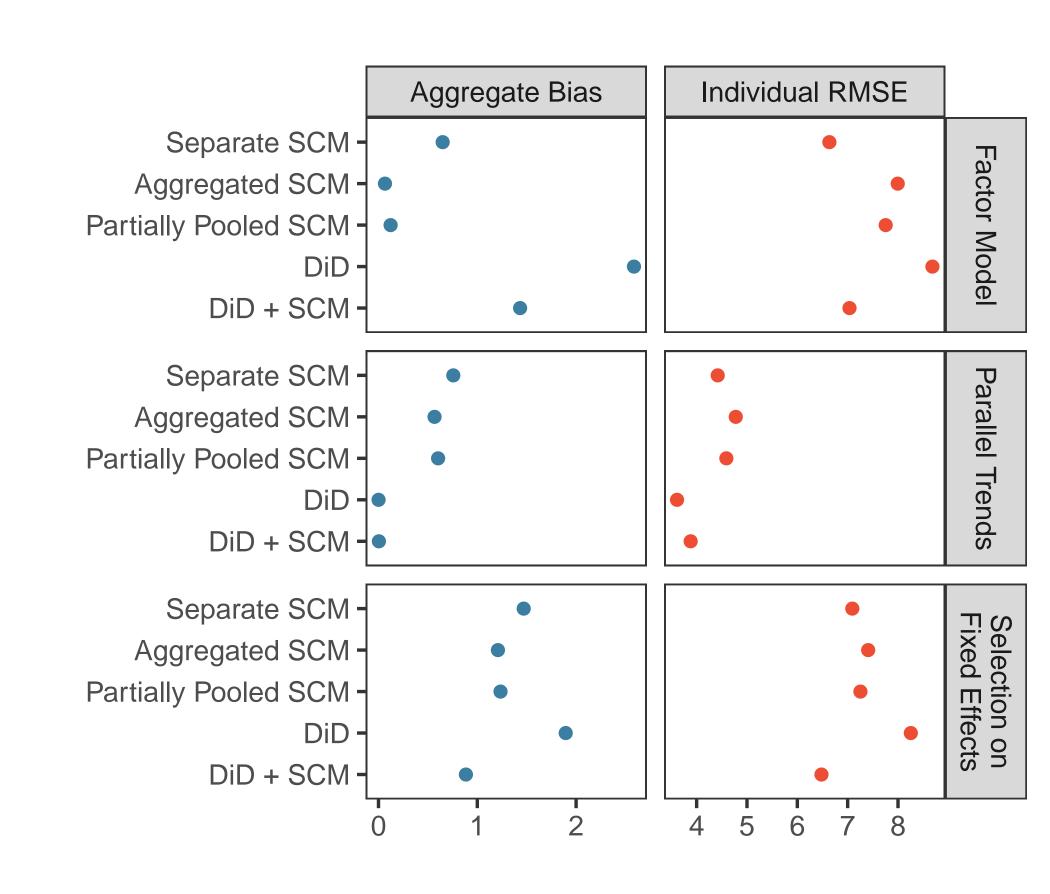
- Lagrangian dual \Rightarrow implicit p-score estimate
- Selection on lagged outcomes
- Separate parameters β_i for treatment time T_i

$$\log \frac{P(W_i = j \mid Y_{i(T_j - K)}, \dots, Y_{iT_j})}{P(W_i = 0 \mid Y_{i(T_j - K)}, \dots, Y_{iT_j})} = \alpha_j + \sum_{\ell=1}^K \beta_{\ell j} Y_{i(T_j - \ell)}$$

- Hierarchical propensity score model
- Shrinkage to a global model w/params μ_{β}

$$eta_{j\ell} \sim \mathcal{N}\left(\mu_{eta\ell}, \sigma_{eta}^2
ight) \ \mu_{eta\ell} \sim \mathcal{N}\left(0, \sigma_{\mu}^2
ight).$$

Data Calibrated Simulation Study



References

- [1] A. S. Paglayan, "Public-sector unions and the size of government," *American Journal of Political Science*, vol. 63, no. 1, pp. 21–36, 2019.
- [2] E. Ben-Michael, A. Feller, and J. Rothstein, "The Augmented Synthetic Control Method." 2018.
- [3] A. Abadie, "Semiparametric difference-in-differences estimators," *The Review of Economic Studies*, vol. 72, no. 1, pp. 1–19, 2005.
- [4] C. Hazlett and Y. Xu, "Trajectory balancing: A general reweighting approach to causal inference with time-series cross-sectional data," 2018.
- [5] A. Abadie, A. Diamond, and J. Hainmueller, "Synthetic Control Methods for Comparative Case Studies: Estimating the Effect of California's Tobacco Control Program," *Journal of the American Statistical Association*, vol. 105, no. 490, pp. 493–505, 2010.



• Standard DiD analysis \Rightarrow non-parallel trends!