

$$\lambda = 2.0$$

Oppgave 1)  $E(X) = \frac{1}{\lambda} = \underline{\underline{\frac{1}{2}}}$

$$\text{Var}(T) = \frac{1}{\lambda^2} = \frac{1}{2^2} = \underline{\underline{\frac{1}{4}}}$$

Oppgave 2)  $P(X \leq 0.5) = F(0.5) = 1 - e^{-\lambda \cdot t} = 1 - e^{-2 \cdot 0.5} = 1 - e^{-1} = 1 - \frac{1}{e} = \underline{\underline{0.6321}}$

$$P(X \geq 1.5) = e^{-\lambda \cdot t} = e^{-2 \cdot 1.5} = e^{-3} = \frac{1}{e^3} = \underline{\underline{0.0498}}$$

Oppgave 3)  $P(X \leq 2.0) = 1 - e^{-\lambda t} = 1 - e^{-2 \cdot 2} = 1 - e^{-4} = 1 - \frac{1}{e^4} = 0.9817$

$$P(X \geq 1.5) = 0.0498$$

$$P(X \leq 1.5) = 1 - e^{-\lambda t} = 1 - e^{-2 \cdot 1.5} = 1 - e^{-3} = 0.9502$$

Bayes formel  $P(A|B) = \frac{P(A \cap B)}{P(B)}$

$$P(X \leq 2.0 | X \geq 1.5) = \frac{P(1.5 \leq X \leq 2.0)}{P(X \geq 1.5)} = \frac{P(X \leq 2.0) - P(X \leq 1.5)}{P(X \geq 1.5)} = \frac{0.9817 - 0.9502}{0.0498} = \underline{\underline{0.6325}}$$

Oppgave 4)  $Y: \mu = 15, \sigma = 3$

$$Z: \mu = 0, \sigma = 1$$

$$P(Z \leq 1.12) = F(1.12) = G\left(\frac{1.12 - 0}{1}\right) = G(1.12) = \underline{\underline{0.8686}}$$

$$P(Z \geq -1.12) = 1 - G\left(\frac{-1.12 - 0}{1}\right) = 1 - G(-1.12) = 1 - 0.1314 = \underline{\underline{0.8686}}$$

$$P(Y \leq 12) = F(12) = G\left(\frac{12 - 15}{3}\right) = G(-1) = \underline{\underline{0.1587}}$$