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Simulating Concurrent Behaviors with Worst-Case Cost Bounds *

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Abstract

Modern software systems are increasingly being developed for deployment on a range of architectures. For this purpose, it is interesting to capture aspects of low-level deployment concerns in high-level modeling languages. In this paper, an executable object-oriented modeling language is extended with resource-restricted deployment components. To analyze model behavior a formal methodology is proposed to assess resource consumption, which balances the scalability of the method and the reliability of the obtained results. The approach applies to a general notion of resource, including traditional cost measures (e.g., time, memory) as well as concurrency-related measures (e.g., requests to a server, spawned tasks). The main idea of our approach is to combine reliable (but expensive) worst-case cost analysis of statically predictable parts of the model with fast (but inherently incomplete) simulations of the concurrent aspects in order to avoid the state-space explosion. The approach is illustrated by the analysis of memory consumption.

1 Introduction

Software systems today are increasingly being developed to be highly configurable, not only with respect to the functionality provided by a specific instance of the system but also with respect to the targeted deployment architecture. An example of a development method is software product line engineering [19]. In order to capture and analyze the intended deployment variability of such

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software, formal models need to express and range over different deployment scenarios. For this purpose, it is interesting to reflect aspects of low-level deployment in high-level modeling languages. As our first contribution, in this paper, we propose a notion of resource-restricted deployment component for an executable modeling language based on concurrent objects [7, 10, 13, 20, 23]. The main idea of resource-restricted deployment components is that they are parametric in the amount of resources they make available to their concurrently executing objects. This way, different deployment scenarios can be conveniently expressed at the modeling level and a model may be analyzed for a range of deployment scenarios.

As our main contribution, we develop a novel approach for estimating the resource consumption of this kind of resource-constrained concurrent executions which is reasonably reliable and scalable. Resource consumption is in this sense a way of understanding and debugging the model of the deployment components. Our work is based on a general notion of resource, which can be any function that associates a cost unit to the program statements. Traditional resources are execution steps, time and memory, but one may also consider more concurrency-related resources like the number of tasks spawned along the execution, the number of requests to a server, etc.

The two main approaches to estimating resource consumption of a program execution are static cost analysis and dynamic simulation (or monitoring). Efficient simulation techniques can analyze model behavior in different deployment scenarios, but simulations are carried out for particular input data. Hence, they cannot guarantee the correctness of the model. Due to the non-determinism of concurrent execution and the choice of inputs, possible errors may go undetected in a simulation. Static cost (or resource usage) analysis aims at automatically inferring a program's resource consumption statically, i.e., without running the program. Such analysis must consider all possible execution paths and ensures soundness, i.e., it guarantees that the program never exceeds the inferred resource consumption for any input data. While cost analysis for sequential languages exists, the problem has not yet been studied in the concurrent setting, partly due to the inherent complexity of concurrency: the number of possible execution paths can be extremely large and the resulting outcome nondeterministic. Statically analyzing the concurrent behaviors of our resourcerestricted models requires a full state space exploration and quickly becomes unrealistic.

In this paper, we propose to combine simulations with static techniques for cost analysis, which allows classes of input values to be covered by a single simulation. The main idea is to apply cost analysis to the sequential computations while simulation handles the concurrent system behavior. Our method is developed for an abstract behavioral specification language ABS, simplifying Creol [10,13], which contains a functional level where computations are sequential and an concurrent object-oriented level based on concurrent objects. This separation allows a concise and clean formalization of our technique. The combination of simulation and static analysis, as proposed in this paper, suggests a middle way between full state space exploration and simulating single paths,

which gives interesting insights into the behavior of concurrent systems.

Paper organization. Section 2 describes the syntax and semantics of the ABS modeling language and introduces our running example. Section 3 discusses the worst-case cost bounds calculation of the functional parts of ABS. Section 4 introduces deployment components, which model resource-containing runtime entities, and Section 5 presents the results of applying the technique to the running example. Finally, Section 6 discusses related work and Section 7 concludes the paper with a discussion of extensions of our presented technique.

2 A Language for Distributed Concurrent Objects

Our method is presented for ABS, an abstract behavioral specification language for distributed concurrent objects (simplifying Creol [10, 13] by excluding, e.g., class inheritance and dynamic class upgrades). Characteristic features of ABS are that: (1) it allows abstracting from implementation details while remaining executable; i.e., a functional sub-language over abstract data types is used to specify internal, sequential computations; and (2) it provides flexible concurrency and synchronization mechanisms by means of asynchronous method calls, release points in method definitions, and cooperative scheduling of method activations.

Intuitively, concurrent ABS objects have dedicated processors and live in a distributed environment with asynchronous and unordered communication. All communication is between named objects, typed by interfaces, by means of asynchronous method calls. (There is no remote field access.) Calls are asynchronous as the caller may decide at runtime when to synchronize with the reply from a call. Method calls may be seen as triggers of concurrent activity, spawning new activities (so-called *processes*) in the called object. Active behavior, triggered by an optional *run* method, is interleaved with passive behavior, triggered by method calls. Thus, an object has a set of processes to be executed, which stem from method activations. Among these, at most one process is *active* and the others are *suspended* in a process pool. Process scheduling is non-deterministic, but controlled by *processor release points* in a cooperative way.

An ABS model defines interfaces, classes, datatypes, and functions, and has a main method to configure the initial state. Objects are dynamically created instances of classes; their declared attributes are initialized to arbitrary type-correct values, but may be redefined in an optional method *init*. This paper assumes that models are well-typed, so method binding is guaranteed to succeed.

The functional level of ABS defines data types and functions, as shown in Fig. 1. In data type declarations Dd, a data type D has at least one constructor Cons, which has a name Co and a list of types T for its arguments. Function declarations F consist of a return type T, a function name fn, a list of variable declarations \overline{x} of types \overline{T} , and an expression e. Expressions e include

```
Definitions.
Syntactic categories.
I in Interface type
                                             Dd
                                                    ::=
                                                              data D = Cons;
D in Data type
                                           Cons
                                                               Co[(\overline{T})] \mid (Cons \mid Cons)
x in Variable
                                                              \mathbf{def}\ T\ fn(\overline{T\ x}) = e;
                                                     ::=
e in Expression
                                               T
                                                     ::=
                                                              I \mid D
b in Bool Expression
                                                              b \mid x \mid t \mid \mathtt{this} \mid Co[(\overline{e})] \mid fn(\overline{e}) \mid \mathtt{case} \ e \ \{\overline{br}\}\
                                                     ::=
t \ {\rm in} \ {\sf Ground} \ {\sf Term}
                                                              Co[(\bar{t})] \mid \mathtt{null}
br in Branch
                                               br
                                                              p \Rightarrow e;
p in Pattern
                                                    ::=
                                                             |x| t | Co[(\overline{p})]
                                                p
```

Figure 1: ABS syntax for the functional level. Terms \overline{e} and \overline{x} denote possibly empty lists over the corresponding syntactic categories, and square brackets [] optional elements. Boolean expressions b include comparison by equality, greater- and less-than operators.

Boolean expressions b, variables x, (ground) terms t, the (read-only) variable **this** which refers to the object's identifier, constructor expressions $Co(\overline{e})$, function expressions $fn(\overline{e})$, and case expressions **case** e $\{\overline{br}\}$. Ground terms t are constructors applied to ground terms $Co(\overline{t})$, and **null**. Case expressions have a list of branches $p \Rightarrow e$, where p is a pattern. The branches are evaluated in the listed order. Patterns include wild cards _, variables x, terms t, and constructor patterns $Co(\overline{p})$. Remark that expressions may refer to object references.

Example 1 Consider a polymorphic data type for sets and a function in which checks if e is an a member of the set ss.

The concurrent object level of ABS is given in Fig. 2. Here, an interface IF has a name I and method signatures Sg. A class implements a list of interfaces, specifying types for its instances; a class CL has a name C, interfaces \overline{I} , class parameters and state variables x of type T, and methods M (The attributes of the class are both its parameters and state variables). A method signature Sg declares the return type T of a method with name m and formal parameters \overline{x} of types \overline{T} . M defines a method with signature Sg, a list of local variable declarations \overline{x} of types \overline{T} , and a statement s. Statements may access attributes of the current class, locally defined variables, and the method's formal parameters.

Right hand side expressions rhs include object creation \mathbf{new} $C(\overline{e})$, method calls, and (pure) expressions e. Statements are standard for assignment x := rhs, sequential composition $s_1; s_2$, and \mathbf{skip} , \mathbf{if} , \mathbf{while} , and \mathbf{return} constructs. $\mathbf{release}$ unconditionally releases the processor, suspending the active process. In \mathbf{await} g, the guard g controls processor release and consists of Boolean conditions b and return tests x? (see below). If g evaluates to false, the

```
Definitions.
Syntactic categories.
C, m \text{ in Names}
                                                         interface I\{\overline{Sg}\}
                                          IF
                                                 ::=
q in Guard
                                                          class C[(\overline{Tx})] [implements \overline{I}] { \overline{Tx}; \overline{M}}
s \ {\rm in} \ {\sf Statement}
                                          Sg
                                                 ::=
                                                          T m (\overline{T x})
                                                         Sg == \overline{T x}; \{s\}
                                           M
                                                 ::=
                                                         b \mid x? \mid g \land g \mid g \lor g
                                                 ::=
                                                          s; s \mid x := rhs \mid release \mid await g \mid return e
                                                         if b then \{s\} [else \{s\}] | while b\{s\} | skip
                                         rhs
                                                 ::=
                                                         e \mid \mathtt{new} \ C[(\overline{e})] \mid [e]! m(\overline{e}) \mid x.\mathtt{get}
```

Figure 2: ABS syntax for the concurrent object level.

processor is released and the process suspended. When the processor is idle, any enabled process from the object's pool of suspended processes may be scheduled. Explicit signaling is therefore redundant. Like expressions e, guards g are side-effect free.

Communication in ABS is based on asynchronous method calls, denoted $o!m(\overline{e})$. (Local calls are written $!m(\overline{e})$.) After asynchronously calling $x:=o!m(\overline{e})$, the caller may proceed with its execution without blocking on the call. Here x is a future variable, o is an object (an expression typed by an interface), and \overline{e} are expressions. A future variable x refers to a return value which has yet to be computed. There are two operations on future variables, which control external synchronization in ABS. First, a return test x? evaluates to false unless the reply to the call can be retrieved. (Return tests are used in guards.) Second, the return value is retrieved by the expression $x.\mathtt{get}$, which blocks all execution in the object until the return value is available. The statement sequence $x:=o!m(\overline{e})$; $v:=x.\mathtt{get}$ encodes a blocking, synchronous call, abbreviated $v:=o.m(\overline{e})$, whereas the statement sequence $x:=o!m(\overline{e})$; await x?; $v:=x.\mathtt{get}$ encodes a non-blocking, preemptable call, abbreviated await $v:=o.m(\overline{e})$.

Example 2 Consider a model of a book shop where clients can order a list of books for delivery to a country. Clients connect to the shop by calling the getSession method of an Agent object. An Agent hands out Session objects from a dynamically growing pool. Clients call the order method of their Session instance, which calls the getInfo and confirmOrder methods of a Database object shared between the different sessions. Session objects return to the agent's pool after an order is completed. (The full model is available in Appendix B)

```
interface Agent { Session getSession(); Unit free(Session session);}
interface Session {
    OrderResult order(List<Bname> books, Cname country);}
interface Database {
    DatabaseInfo getInfo(List<Bname> books, Cname country);
    Bool confirmOrder(List<Bname> books); }
class DatabaseImp(Map<Bname,Binfo> bDB, Map<Cname,Cinfo> cDB)
implements Database {
    DatabaseInfo getInfo(List<Bname> books, Cname country) {
    Map<Bname,Binfo> bOrder:=EmptyMap; Pair<Cname,Cinfo> cDestiny;
    bOrder:=getBooks(bDB, books); cDestiny:=getCountry(cDB, country);
```

In the model, a DatabaseImp class stores and handles the information about the books available in the shop (in the bDB map) as well as information about the delivery countries (in the cDB map). This class has a method getInfo; given an order with a list of books and a destination country, the getInfo method extracts information about book availability from bDB and shipping information from cDB by means of function calls getBooks(bDB, books) and getCountry(cDB, country) The result from method call has type DatabaseInfo, with a constructor of the form: Info(bOrder, cDestiny).

2.1 Operational Semantics

The operational semantics of ABS is presented as a transition system in an SOS style [18]. Rules apply to subsets of configurations (the standard context rules are not listed). For simplicity we assume that configurations can be reordered to match the left hand side of the rules (i.e., matching is modulo associativity and commutativity as in rewriting logic [17]). A run is a possibly nonterminating sequence of rule applications. When auxiliary functions are used in the semantics, these are evaluated in between the application of transition rules in a run.

Configurations cn are sets of objects, invocation messages, and futures. The associative and commutative union operator on configurations is denoted by whitespace and the empty configuration by ε . These configurations live inside curly brackets; in the term $\{cn\}$, cn captures the entire configuration. An object is a term ob(o, C, a, p, q) where o is the object's identifier and C its class, a an attribute mapping representing the object's fields, p an active process, and q a pool of suspended processes. A process p consists of a mapping l of local variable bindings and a list s of statements, denoted by $\{l|s\}$ when convenient. In an invocation message invoc (o, f, m, \overline{v}) , o is the callee, f the future to which the call's result is returned, f the method name, and f the call's actual parameter values. A future fut(f, v) has a identifier f and a reply value f (which is f when the future's reply value has not been received). Values are object and future identifiers, Boolean expressions, and null (as well as expressions in the functional language). For simplicity, classes are not represented explicitly in the semantics, but may be seen as static tables.

Evaluating Expressions. Denote by $\sigma(x)$ the value bound to x in a mapping σ and by $\sigma_1 \circ \sigma_2$ the composition of mappings σ_1 and σ_2 . Given a substitution σ and a configuration cn, denote by $\llbracket e \rrbracket_{\sigma}^{cn}$ a confluent and terminating reduction system which reduces expressions e to data values. Let $\llbracket x? \rrbracket_{\sigma}^{cn} = \text{true}$ if $\llbracket x \rrbracket_{\sigma}^{cn} = f$ and $fut(f, v) \in cn$ for some value $v \neq \bot$, otherwise $\llbracket x? \rrbracket_{\sigma}^{cn} = \text{false}$. The remaining cases are fairly straightforward, looking up values for declared variables in σ . For brevity, we omit the reduction system for the functional level of ABS (for details, see Appendix A) and simply denote by $\llbracket e \rrbracket_{\sigma}^{\varepsilon}$ the evaluation of a guard or expression e in the context of a substitution σ and a state configuration cn (the state configuration is needed to evaluate future variables). The

reduction of an expression always happens in the context of a given process, object state, and configuration. Thus, $\sigma = a \circ l$ (the composition of the fields a and the local variable bindings l), and cn the current configuration of the system (ignoring the object itself).

Transition Rules. Transition rules of the operational semantics transform state configurations into new configurations, and are given in Fig. 3. We assume given functions $bind(o, f, m, \overline{v}, C)$ which returns a process resulting from the method activation of m in a class C with actual parameters \overline{v} , callee o and associated future f; init(C) which returns a process initializing instances of class C; and $atts(C, \overline{v}, o, n)$ which returns the initial state of an instance of class C with class parameters \overline{v} , identity o, and deployment component n. The predicate fresh(n) asserts that a name n is globally unique (where n may be an identifier for an object or a future). Let idle denote any process $\{l|s\}$ where s is an empty statement list. Finally, we define different assignment rules for side effect free expressions (assign1 and assign2), object creation (new-object), method calls (async-call), and future dereferencing (read-fut). Rule skip consumes a skip in the active process. Here and in the sequel, the variable s will match any (possibly empty) statement list. Rules assign1 and assign2 assign the value of expression e to a variable x in the local variables l or in the fields a, respectively. Rules cond1 and cond2 branch the execution depending on the value obtained by evaluating the expression e. (We omit the standard rule for while)

Process Suspension and Activation. Three operations are used to manipulate a process pool q: enqueue(p,q) adds a process p to q, $q \setminus p$ removes the process p from q, and select(q,a,cn,t) selects a process from q (if q is empty, this is the idle process or no process is ready [13]). The actual definitions of these operations are left undefined; different definitions correspond to different scheduling policies for processes. Let \emptyset denote the empty pool. Rule release suspends the active process to the process pool, leaving the active process idle. Rule await1 consumes the await statement if the guard evaluates to true in the current state of the object, rule await2 adds a release statement in order to suspend the process if the guard evaluates to false. Rule activate selects a process from the process pool for execution if this process is ready to execute, i.e., if it would not directly be resuspended or block the processor [13].

Communication and Object Creation. Rule async-call sends an invocation message to o' with the unique identity f (by the condition $\operatorname{fresh}(f)$) of a new future, the method name m, and actual parameters \overline{v} . Note that the return value of the new future f is undefined (i.e., \bot). Rule bind-mtd consumes an invocation method and places the process corresponding to the method activation in the process pool of the callee. Note that a reserved local variable 'destiny' is used to store the identity of the future associated with the call. Rule return places the return value into the call's associated future. Rule read-fut dereferences the future f in the case where $v \ne \bot$. Note that if this attribute is \bot the reduction in this object is blocked. Finally, new-object creates a new object with a unique identifier o'. The object's fields are given default values by $\operatorname{atts}(B, \overline{v}, o', n)$, extended with the actual values \overline{v} for the class parameters and o' for this. In order to instantiate the remaining attributes, the process p is loaded (we assume

$$\begin{array}{c} \text{(BIND-MTD)} \\ ob(o,C,a,\{l|\text{skip};s\},q) \\ \rightarrow ob(o,C,a,\{l|s\},q) \\ \\ \hline \\ c(\text{ASSIGN1}) \\ x \in \text{dom}(l) \quad v = \llbracket e \rrbracket_{(aol)}^{\varepsilon} \\ \hline \\ ob(o,C,a,\{l|x:=e;s\},q) \\ \rightarrow ob(o,C,a,\{l|x:=e;s\},q) \\ \hline \\ c(\text{ASSIGN2}) \\ \hline \\ x \in \text{dom}(a) \quad v = \llbracket e \rrbracket_{(aol)}^{\varepsilon} \\ \hline \\ ob(o,C,a,\{l|x:=e;s\},q) \\ \hline \\ c(\text{ASSIGN2}) \\ \hline \\ x \in \text{dom}(a) \quad v = \llbracket e \rrbracket_{(aol)}^{\varepsilon} \\ \hline \\ ob(o,C,a,\{l|x:=e;s\},q) \\ \hline \\ c(\text{DODD}1) \\ \hline \\ \llbracket e \rrbracket_{(aol)}^{\varepsilon} \\ \hline \\ ob(o,C,a,\{l|s;s\},q) \\ \hline \\ c(\text{COND1}) \\ \hline \\ else \ s_2 \ fi; s\}, q) \\ \hline \\ c(\text{COND2}) \\ \hline \\ c(\text{DOD}1) \\ \hline \\ else \ s_2 \ fi; s\}, q) \\ \hline \\ c(\text{COND2}) \\ \hline \\ c(\text{DOD}1) \\ \hline \\ else \ s_2 \ fi; s\}, q) \\ \hline \\ c(\text{COND2}) \\ \hline \\ c(\text{DOD}1) \\ \hline \\ c(\text{COND2}) \\ \hline \\ c(\text{DOD}1) \\ \hline \\ c(\text{DOD}1) \\ \hline \\ (\text{COND2}) \\ \hline \\ c(\text{DOD}1) \\ \hline \\ c(\text{DOD}1) \\ \hline \\ (\text{DOD}1) \\ \hline \\ (\text{COND2}) \\ \hline \\ c(\text{DOD}1) \\ \hline \\ c(\text{DOD}1) \\ \hline \\ (\text{DOD}1) \\ \hline \\ (\text{DOD}2) \\ \hline$$

Figure 3: ABS Semantics

that this process reduces to idle if init(B) is unspecified in the class definition, and that it asynchronously calls run if the latter is specified).

3 Worst-Case Cost Bounds

The goal of this section is to infer worst-case upper bounds (UBs) from the (sequential) functions in our sub-language. This problem has been intensively studied since the seminal paper on cost analysis [22]. Thus, instead of a formal development, we illustrate the main steps of the analysis on the running example.

Size of terms. The cost of a function that traverses a term t usually depends on the size of t, and not on the concrete data structure to which t is bound. For instance, the cost of executing dom(map) (which returns the domain of a map) depends on the size of map (the number of elements). Therefore, in order to infer worst-case UBs, we first need to define the meaning of size of a term. This is done by using norms [6]. A norm is a function that maps terms to their size. For instance, the term-size norm calculates the number of type constructors in a given term, and is defined as $|Co(t_1,\ldots,t_n)|_{ts}=1+\sum_{i=1}^n|t_i|_{ts}$, and, the term-depth norm calculates the depth of the term, and is defined as $|Co(t_1,\ldots,t_n)|_{td}=1+\max(|t_1|_{td},\ldots,|t_n|_{td})$. Consider the book shop model described in Ex. 2; the database uses maps for storing information; a Map<A, B> has two constructors |Ins(Pair<A, B>, Map<A, B>) and |EmptyMap| (to represent empty maps). For storing the information of a book sold by the shop, the model uses a constructor of the form |BInfo(Bquantity, Bweight, Bbackordertime)| (A more detailed description of this data type can be found in Appendix B). For a term:

 $t=\inf(\text{"b1",BInfo}(5,1,2)),\inf(\text{Pair}(\text{"b2",BInfo}(1,2,5)),\text{EmptyMap}))$ which can represent the database of books in the shop, we have that $|t|_{ts}=15$ and $|t|_{td}=5$. Note that we count strings and numbers as type constructors. Norms map a given variable x to itself in order to account for the size of the term to which x is bounded. Any norm can be used in the analysis, depending on the used data structures, w.l.o.g., we will use the term-size norm.

Size relations. The getBooks function (called from method getInfo in Ex. 2) returns a sub-database (of booksDB) which contains only those books in books:

```
def Map getBooks(Map booksDB, List books) = case books {
    Nil => EmptyMap;
    Cons(b,t) => case in(dom(booksDB),b) {
        False => getBooks(booksDB,t);
        True => Ins(Pair(b,lookup(booksDB,b)),getBooks(booksDB,t)); };};
```

Function dom returns the set of keys of the mapping provided as argument, in is the one of Ex. 1, and, lookup returns the value that corresponds to the provided key in the provided mapping. Observe that the return value of dom is passed on to function in. Since the cost of in is part of the total cost of getBooks, we need to express its cost in terms of booksDB. This is possible only if we know which is the relation between the returned value of dom and its input value booksDB. This *input-output* relation (or a post-condition) is a conjunction of (linear) constraints that describe a relation between the sizes

of the input parameters of the function and its return value, w.r.t. the selected norm. E.g., $ret \leq map$ is a possible post-condition for function dom, where map is the size of its input parameter and ret is the size of the returned term. We apply existing techniques [5] to infer such relations for our functional language. In what follows, we assume that \mathcal{I}_P includes a post-conditions $\langle fn(\bar{x}), \psi \rangle$ for each function, where ψ is a conjunction of (linear) constraints over \bar{x} and ret.

Cost Model. Cost analysis is typically parametric on the notion of cost model \mathcal{M} , i.e., on the resource that we want to measure [2]. Informally, a cost model is a function that maps instructions to costs. Traditional cost models are: (1) number of instructions, which maps all instructions to 1, i.e., $\mathcal{M}(b) = 1$ for all instructions b; and (2) memory consumption, which can be defined as $\mathcal{M}_h(x = t) = \mathcal{M}_h(t) = mem(t)$ where $mem(Co(t_1, \ldots, t_n)) = \text{Co} + \sum_{i=1}^n mem(t_i)$ and mem(x) = 0. For any other instruction b we let $\mathcal{M}_h(b) = 0$. The symbol Co represents the amount of memory required for constructing a term of type Co. Note that we estimate only the memory required for storing terms.

Upper bounds. In order to make the presentation simpler, we assume functions are normalized such that nested expressions are flattened using **let** bindings. Using this normal form, the evaluation of an expression e consists in evaluating a sequence of sub-expressions of the form $y = fn(\bar{x}), y = t, match(y, t), fn(\bar{x}), t$ or x. We refer to such sequence as an execution path of e. In a static setting, since variables are not assigned concrete values, and due to the use of **case**, an expression e might have several execution paths. We denote the set of all execution paths of e by paths(e). This set can be constructed from the abstract syntax tree of e. Clearly, when estimating the cost of executing an expression e we must consider all possible execution paths. In practice, we generate a set of (recursive) equations where each equation accounts for the cost of one execution path. Then, the solver of [1] is used in order to obtained a closed-form UB.

Definition 1 Given a function **def** T $fn(\overline{T}x) = e$, its cost relation (CR) is defined as follows: for each execution path $p \equiv b_1, \ldots, b_n \in paths(e)$, we define an equation $\langle fn(\bar{x}) = \sum_{i=1}^n \mathcal{M}(b_i) + fn_{i_1}(\bar{x}_{i_1}) + \cdots + fn_{i_k}(\bar{x}_{i_k}), \wedge_{i=1}^n \varphi_i \rangle$ where $fn_{i_1}(\bar{x}_{i_1}), \ldots, fn_{i_k}(\bar{x}_{i_k})$ are all function calls in p; and $\varphi_i \equiv y = |t|_{t_s}$ if $b_i \equiv y = t$, and $\varphi_i \equiv \psi[ret/y]$ if $b_i \equiv y = f(\bar{x})$ and $\langle f(\bar{x}), \psi \rangle \in \mathcal{I}_P$, otherwise $\varphi_i = true$. The CR system of a given program the set of all CRs of its functions.

Example 3 The following is the *CR* of getBooks w.r.t the cost model *mem*:

```
\begin{array}{lll} getBooks(a,b) & = & \mathsf{EmptyMap} & \{b=1\} \\ getBooks(a,b) & = & dom(a) + in(d,e) + getBooks(a,g) & \{b=1 + e + g, d \leq a, d \geq 1, e \geq 1, g \geq 1\} \\ getBooks(a,b) & = & \mathsf{Pair} + \mathsf{Ins} + dom(a) + in(d,e) & \{b=1 + e + g, d \leq a, d \geq 1, e \geq 1, g \geq 1\} \\ & + & lookup(a,e) + getBooks(a,g) & \{b=1 + e + g, d \leq a, d \geq 1, e \geq 1, g \geq 1\} \\ \end{array}
```

The first equation can be read as "the memory consumption of getBooks is one EmptyMap constructor if the size of b is 1". Equations for functions in, lookup

and dom are not shown due to space limitations and have resp. constant, zero and linear memory consumptions. Solving the above $\it CR$ results in the UB

```
getBooks(a,b) = \mathsf{EmptyMap} + \mathsf{nat}(\tfrac{b-1}{2}) * (\mathsf{nat}(\tfrac{a-1}{4}) * \mathsf{Ins} + \mathsf{EmptySet} + \max(\mathsf{True}, \mathsf{False}))
```

Replacing, for example, ${\sf EmptyMap},$ ${\sf Ins},$ ${\sf True}$ and ${\sf False}$ by 1 results in

$$getBooks(a,b) = 1 + \mathsf{nat}(\frac{b-1}{2}) * (2 + \mathsf{nat}(\frac{a-1}{4}))$$

4 Deployment components

Deployment components make quantifiable deployment-level resources explicitly available in the modeling language. A deployment component allows the logical execution environment of concurrent objects to be mapped to a model of physical resources, by specifying an abstract execution context which is shared between a number of concurrently executing objects. The resources available to a deployment component are shared between the component's objects. An object may get and return resources from and to its deployment component. In this way, the deployment components impose an execution context with resource restrictions on the concurrently executing objects contained within.

Resource-restricted deployment components are integrated in the modeling language as follows. Let variables x of type Component refer to deployment components and allow deployment components to be statically created by the statement x:=component(r) in the main method, which allocates a given quantity of resources r to the component x (capturing the resource constraint of x). Resources are modeled by a data type Resource which extends the natural numbers with an "unbounded resource" ω . Resource allocation and usage is captured by resource addition and subtraction, where $\omega + n = \omega$ and $\omega - n = \omega$.

Concurrent objects residing on components, may grow dynamically. All objects are created inside a deployment component. The syntax for object creation is extended with an optional clause to specify the targeted deployment component in the expression $\mathbf{new}\ C\ (\overline{e})\ @\ x$. This expresses that the new C object will reside in the component x. Objects generated without an @ clause reside in the same component as their parent object. Thus the behavior of an ABS model which does not statically declare additional deployment components can be captured by a root deployment component with ω resources.

Example 4 Consider the book shop model described in Ex. 2 instantiated inside deployment components:

```
Component c := component(200);
Database db := new DataBaseImp(...) @ c;
Agent agent := new AgentImp(db) @ c;
```

The Session objects created and handed out by the Agent object will then be created inside c as well, without further changes to the model.

The *execution* inside a component d with r resources can be understood as follows. An object o residing in d may execute a transition step with cost c if

Rule	$\cos t$	free
ASSIGN1, ASSIGN2	cost(e)	vp - v
Read-Fut	max(cost(e), v)	0
BIND-MTD	$P + \overline{v} $	$-(P+ \overline{v})$
Async-Call	$\cot(\overline{e}) + f $	0
New-Object-Create	$O + P + \overline{v} $	$-(O+P+ \overline{v})$

Table 1: The non-trivial cost functions of memory-constrained ABS semantics. All identifiers are the same as in the corresponding rule of Figure 3, except vp (old value of a variable), |v| (size of term v), P (size of a process), O (size of an object).

- o can execute the step in a context with unbounded resources, and
- $c \le r$; i.e., the cost of executing the step does not exclude the transition in an execution context restricted to r resources.

After the execution of the transition step, the object may return free resources to its deployment component. Thus, for each transition rule the resources needed to apply this rule to a state t, resulting in a state t', can be characterized in terms of two functions over the state space, one computing the cost of the transition form t to t' and one computing the free resources after the transition. The allocation and return of resources for objects in a deployment component will depend on the specific cost model \mathcal{M} for the considered resource, so the exact definitions of $cost_{\mathcal{M}}(t,t')$ and $free_{\mathcal{M}}(t,t')$ depend on \mathcal{M} .

Example 5 Table 1 shows the $cost_{\mathcal{M}}(t,t')$ and $free_{\mathcal{M}}(t,t')$ functions for the memory cost model of the ABS semantics, using the symbols of Figure 3. There are some subtle details in these functions – for example, message invocations and future variables are considered to be outside any one deployment component, so the memory required to execute the READ-FUT rule can be larger than evaluating the future variable expression e since the deployment component must have enough memory to accommodate the incoming value v. Also, object creation affects two places, so was split into two rules, similar to method invocation.

Semantics of Resource Constrained Execution. Let \mathcal{M} be a cost model. The operational semantics of \mathcal{M} -constrained execution in deployment components is defined as a small-step operational semantics, extending the semantics of ABS given in Sec. 2.1 to resource-sensitive runtime configurations for \mathcal{M} . We assume given functions $cost_{\mathcal{M}}(t,t')$ and $free_{\mathcal{M}}(t,t')$.

Let \longrightarrow denote the single-step reduction relation of the ABS semantics, defined in Sec. 2.1. A resource-constrained run of an ABS model consists of zero or more applications of a transition relation $\longrightarrow_{\mathcal{M}}$, which is defined by the context rule given in Fig. 4. Runtime configurations are extended with the representation of deployment components comp(id, r), where id is the identifier of the component and r its currently available resources. Each object has a

$$\begin{array}{c} (\text{Context}) \\ mycomp(o) = id \\ o \ \overline{msg} \longrightarrow o' \ \overline{msg'} \ \overline{config'} \end{array} \begin{array}{c} cost_{\mathcal{M}}(o \ \overline{msg}, o' \ \overline{msg'} \ \overline{config'}) \leq r \\ r' = r + free_{\mathcal{M}}(o \ \overline{msg}, o' \ \overline{msg'} \ \overline{config'}) \end{array} \\ \overline{\{comp(id,r) \ o \ \overline{msg} \ \overline{config}\}} \longrightarrow_{\mathcal{M}} \overline{\{comp(id,r') \ o' \ \overline{msg'} \ \overline{config} \ \overline{config'} \ \}}$$

Figure 4: An operational semantics for resource-constrained deployment components

$$\frac{x \in \text{dom}(l) \quad v = \llbracket e \rrbracket_{(a \circ l)}^{\varepsilon} \quad vp = l(x) \quad \text{cost}(e) \leq r \quad \text{mycomp}(o) = dc}{dc(r) \ ob(o, C, a, \{l|x := e; s\}, q)} \\ \rightarrow dc(r + |vp| - |v|) \ ob(o, C, a, \{l[x \mapsto v]|s\}, q)$$

Figure 5: Resource-aware assignment rule, with an object ob and deployment component dc. The assignment statement is only executed if e can be evaluated with the current r, which is adjusted afterwards.

field mycomp, instantiated to its deployment component at creation time (we omit the redefined object creation rule). Let \overline{config} denote a set of objects and futures. The context rule expresses how an object o may evolve to o' given a set of invocation messages \overline{msg} in the context of a deployment component with r available resources. Since o may consume an invocation message and create new objects, futures, or invocation messages, the right hand side of the rule returns o' with a possibly different set of messages \overline{msg}' and a configuration \overline{config}' .

5 Simulation and Experimental Results

To validate the approach presented in this paper, the interpreter for the ABS language was augmented with a resource constraint model simulating systems with limited memory. The semantics of the ABS interpreter is given in rewriting logic [17] and is executable on the Maude platform [9]. Observe that operational semantics in an SOS style, like the rule of Fig. 4 for adding resource constraints to an existing operational semantics, leads to a significant amount of backtracking in an actual simulation. For this purpose, we do not use this rule directly in our interpreter. Instead, the costs of Table 1 are used to directly extend the transition rules of ABS which evaluate expressions (from Fig. 3). The extension to the ABS operational semantics is illustrated in Figure 5, which shows the modified interpreter rule for assignment to local variables. An assignment to a variable x can only proceed if the cost of evaluating the right-hand side e of the assignment statement is less than the currently free memory r. In this case, xis rebound to the new value v, and r is adjusted using Table 1 (in this case, the difference between v and the previous value vp). All other rules involving evaluating expressions are modified in the same way.

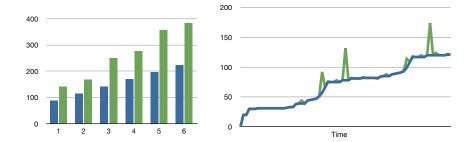


Figure 6: Final and highest temporary memory use as a function of the size of input (left) and memory use during execution (right).

Simulation Results. Deployment component declarations were added to the book shop model described in Ex. 2, restricting the memory available to the server parts of it. The used cost functions calculating memory usage of all functions in the model, were computed as described in Sec. 3 (The table containing UBs for all functions in the book shop model can be found in Appendix C).

When a deployment component was instantiated with too little memory, the expected effect (a deadlock in the simulation) was observed. To obtain quantitative results, the current memory r and peak memory usage $r + \cos(s)$ were recorded during evaluation of rules potentially having an effect on resources. By adding this instrumentation to the interpreter, it becomes possible to visualize various aspects of the memory behavior of a model.

Figure 6 shows some results. We recorded peak memory usage and memory use at the end of the simulation for various input sizes (in this case, how often to run book orders of constant size), the results can be seen in the left chart. The right chart shows the memory use over time of one single run of the model. The "peaks" of transient memory usage occur during updates of the book database, which is modeled as a function.

6 Related Work

Static inference of cost for sequential programming languages has recently received considerable attention. A cost analysis for Java bytecode has been developed in [2], for C++ in [11], and for functional programs in [12]. Our approach for inferring cost for the functional part of ABS is based on [2], which follows the classical approach of [22] to cost analysis. Inference of worst-case UBs on the memory usage of Java like programs in the presence of garbage collection has been studied in [4]. The analysis accounts for memory that is freed by garbage collection, and thus infer more tight and realistic bounds. The analysis support several GC scheme. The analysis of [12] supports inference of memory usage, and accounts for memory freed due destructive matching. In [15] live

heap space analysis for a concurrent language has been proposed. However it uses a very limited model of shared memory. Recently, in [3] a cost analysis for X10 programs [8] has been developed. The analysis infers UBs on the number of maximum tasks that can be running in parallel. The concurrency primitives in the X10 language are similar to the ABS, though X10 is not based on concurrent objects.

Formal resource modeling happens mainly in the embedded domain. For example, Verhoef et al. [21] use the timed VDM++ to model processing time, schedulability and bandwidth resources for distributed embedded systems, but their approach is less general and not used for memory consumption. Johnsen et al. modeled processing resources in the context of deployment components in previous work [14], but this work does not use cost analysis methods. There is not much work combining static cost analysis and simulation to analyze resource usage. However, Künzli et al. [16] combine exact simulation and arrival curves to model processing costs, decreasing the needed simulation time by using arrival curves in their simulations to abstract from some of the components in a SystemC model of specific hardware. In contrast, we use cost analysis to generalize simulations on abstract, formally defined object-oriented models.

7 Discussion

Software is increasingly being developed to be configured for different architectures, which may be restricted in the resources they provide to the software. Therefore, it is interesting to capture aspects of low-level deployment concerns at the abstraction level of a software modeling language. In this paper, we have shown how a formally defined executable concurrent object-oriented modeling language can be extended with a notion of deployment component, which imposes a resource-constraint on the execution of objects in the model.

In order to validate the behavior of the resource-restricted model, we propose to combine static cost analysis with simulations. This combination is achieved by applying static cost analysis to the sequential parts of the modeling language, for which practical cost analysis methods exist, while using simulation for the concurrent part, for which static approaches would lead to a state-space explosion. Thus, the complexity of applying static cost analysis to concurrent executions is avoided, and, in addition, we obtain better results than concrete simulations because the sequential parts of the model are simulated by the worst-case bounds. The technique is demonstrated for memory consumption analysis on an example. The analysis of memory consumption considered here could be strengthened by allowing explicit scheduling and garbage collection policies to be included in the model. This is left for future work.

Another interesting issue is how resource analysis carries over from executable models to generated code. A code generator from ABS to Java is under development that translates user defined abstract data types in ABS into object structures. Hence, the symbolic UBs inferred for memory consumption of the ABS models corresponds to bounds on the number of objects in the correspond-

ing Java code. Note that it might not be possible to find similar correlations for other cost models such as the number of execution steps. Another line of interesting future work is to set up actual measurements on generated code and use these results to profile our analysis approach for a given cost model.

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$$\begin{split} \llbracket b \rrbracket_{\sigma} &= b \\ \llbracket x \rrbracket_{\sigma} &= \sigma(x) \\ \llbracket t \rrbracket_{\sigma} &= t \\ \llbracket Co(\overline{e}) \rrbracket_{\sigma} &= Co(\llbracket e \rrbracket_{\sigma}) \\ \end{split}$$

$$\llbracket fn(\overline{e}) \rrbracket_{\sigma} &= \left\{ \begin{array}{c} \llbracket e_{fn} \rrbracket_{\overline{x} \mapsto \overline{t}} & \text{if } \overline{e} = \overline{t} \\ \llbracket fn(\llbracket e \rrbracket_{\sigma}) \rrbracket_{\sigma} & \text{otherwise} \end{array} \right. \\ \llbracket \text{case } e \ \{ \overline{br} \} \rrbracket_{\sigma} &= \llbracket \text{case2} \ \llbracket e \rrbracket_{\sigma} \ \{ \overline{br} \} \rrbracket_{\sigma} \\ \llbracket \text{case2} \ t \ \{ p \to e; \overline{br} \} \rrbracket_{\sigma} &= \left\{ \begin{array}{c} \llbracket e \rrbracket_{\sigma \circ match(p,t)} & \text{if } match(p,t) \neq \bot \\ \llbracket \text{case2} \ t \ \{ \overline{br} \} \rrbracket_{\sigma} & \text{otherwise} \end{array} \right. \end{split}$$

Figure 7: The evaluation of functional expressions.

A Operational Semantics for ABS Functional Expressions

The evaluation $\llbracket e \rrbracket_{\sigma}$ of functional expressions e, given in Figure 7, takes place in the context of a substitution σ (i.e., the object state and the local variable bindings of the method activation) and is defined inductively over the data types of the functional sublanguage. Let the syntactic category t consist of ground terms; i.e., constructor terms and built-in constants such as, e.g., null and object names.

For simplicity, we let function eveluation be strict. Thus, for every (user defined) function definition $\operatorname{def} T fn(\overline{T} x) = e_{fn}$, the evaluation of a function call $\llbracket fn(\overline{e}) \rrbracket_{\sigma}$ reduces to the evaluation of the corresponding expression $\llbracket e_{fn} \rrbracket_{\overline{x} \mapsto \overline{t}}$ when the arguments \overline{e} have already been reduced to ground terms \overline{t} . (Note the change in scope. Since functions are defined independently of the context where they are used, we here assume that the expression e does not contain free variables and the substitution σ does not apply in the evaluation of e.)

In the case of pattern matching, variables in the pattern p may be bound to ground terms in the term t. Thus the substitution context for evaluating the right hand side e of the branch $p \to e$ extends the current substitution σ with bindings that occurred during the pattern matching. Let the function match(p,t) return a substitution σ such that $\sigma(p)=t$ (if there is no match, it returns the empty substitution \bot).

```
interface Session {
           OrderResult order(List<Bname> books, Cname country);}
2
   interface Database {
           DatabaseInfo getInfo(List<Bname> books, Cname country);
4
           Bool confirmOrder(List<Bname> books); }
   interface Agent { Session getsession(); Unit free(Session session);}
6
   class SessionImp(Agent agent, Database db) implements Session {
      ShippingCost shippingcost := 0; ShippingTime shippingtime := 0;
9
10
      OrderResult result := OrderFail; Bool updatedb := False;
      List<Bname> availableBooks := Nil;
11
12
13
      OrderResult order(List<Bname> books, Cname country) {
         DatabaseInfo preresult := InfoFail ;
14
         preresult := db.getInfo(books,country);
15
16
         if (preresult != InfoFail) {
            shippingCost := calculatecost(calculateweight(getBookMap(
17
                            preresult)), countryshipcost (info(
                            getCountryinfo(preresult))));
19
            shippingTime := calculatetime(getBookMap(preresult),
20
                            countryshiptime(info(
21
                            getCountryinfo(preresult))));
22
23
            availableBooks := map2list(getBookMap(preresult));
            updatedb := db.confirmOrder(availableBooks);
24
            if (updatedb) {
25
26
                   result := Result(availableBooks,
                              shippingCost, shippingTime);}
27
            else {result := OrderFail;};
29
30
        else {result := OrderFail;}; agent.free(this);
        return result;
31
32
   }
33
```

Figure 8: A book shop example in ABS.

B Case Study: Book Shop

This case study models a book shop where clients can order a list of books for delivery to a given destination country. As a result of such an order, the book shop will return a confirmation with the list of the availableBooks from the order, as well as the shippingTime and the shippingCost of the order. Figure 8 and Figure 9 show the implementation of this model in ABS (ignoring the implementation details of the functional language).

The database db of this model stores the information about the collection of books which can be sold in the book shop. For the representation of this table in the database, the model uses a map of the form Map<Bname, Binfo> where Bname is the key of the map and the name of the book, and Binfo is a constructor of the form Bookinfo (Bquantity, Bweight, Bbackordertime), where Bquantity stores the number of available copies of the book in the book shop, Bweight stores the weight per unit of these copies and Bbackordertime stores the extra shipping time needed in case there is no available copy of this book. Furthermore, the database db stores the information about the countries

```
class DatabaseImp(Map<Bname,Binfo> bDB, Map<Cname,Cinfo> cDB)
   implements Database {
2
3
      Map<Bookname, Bookinfo> booksDB := bDB;
4
      DatabaseInfo getInfo(List<Bname> books, Cname country) {
        DatabaseInfo result := InfoFail;
6
        Map<Bname,Binfo> myorder := EmptyMap ;
7
        List<Bname> mybooks := Nil;
        mybooks := books ; myorder := getBooks(booksDB, books) ;
9
10
        result := Info(myorder, Pair(country, lookup(cDB, country)));
        return result;
11
12
13
      Bool confirmOrder(List<Bookname> books) {
14
15
        booksDB := updateBooks(booksDB, books);return True;
16
17
18
   class AgentImp(Database db) implements Agent {
19
20
     List<Session> sessions := Nil;
21
     Unit free(Session session) {sessions := appendright(sessions, session);}
22
23
     Session getsession() {
^{24}
25
      Session session;
26
      if (isEmpty(sessions)) {session := new SessionImp(this,db); }
      else {session := head(sessions); sessions := tail(sessions); }
27
28
      return session; }
29
```

Figure 9: A book shop example in ABS (continuation).

to which the shop can deliver books. For this table the model uses map of the form Map<Cname, Cinfo>, where Cname is the key of the map and the name of the country, and Cinfo is a constructor of the form Countryinfo (Cshiptime, Cshipcost) where Cshiptime is the shipping time needed for delivering an order to this country and Cshipcost is the cost per kilogram for delivering an order to this country.

When a client wants to make an order; it connects to the book shop by calling the getSession method of an Agent object. An Agent hands out Session objects from a dynamically growing pool. Clients call the order method of their Session instance; the order method has as parameters a list of books (from the order) and a destination country; this method extracts the availableBooks (books that the book shop can sell), and calculates the shippingTime and the shippingCost of the order; in the order method the preresult variable is of the type DatabaseInfo which has a constructor of the form Info (Map<Bname, Binfo>, Pair<Cname, Cinfo>); the function calculatetime calculates the shipping time taking into account the Cshiptime of the destination country and the Bbackordertime of the books in preresult (in case there are not enough copies available for one or more of the books); the function calculatecost calculates the cost of the order taking into account the Cshipcost of the destination country and the Bweight

of the books in preresult; the map2list function extract the list of books in preresult; the confirmOrder method returns a Boolean which confirms if the necessary updates have been done in the database db. If confirmOrder returns True, the order method will return the list of the availableBooks, the shipping time, and the shipping cost to the Client. Otherwise, the order will fail. After completing the order, the session object is added to the agent's pool again.

In the implementation of the Database class, the getInfo method has as parameters a list of books (from the order) and a destination country; the getInfo method extracts the full information about the available books from the order (books that the book shop can sell), using the getBooks function, as well the necesary computation to get the destination country. The getInfo method returns the collected information in a data type DatabaseInfo. The confirmOrder method has as parameter a list of availableBooks (copies that are going to be sold and shipped to a destination country). The method updates bDB by decreasing the number of available copies (Bquantity) according to the availableBooks list.

In the Agent class, the attribute sessions stores a list of Session objects. When a client requests a Session, the Agent takes a session from the available sessions if possible, otherwise it creates a new session. The method free inserts a session in the sessions list (of the Agent), and is called by the session itself upon completion of an order. Section 4 shows how to run this case study using a memory deployment component.

C UBs for all functions in the running example

Figure 10 lists the upper bounds on memory consumption for all functions of the book shop case study. For simplicity, the cost model that has been used counts 1 for any type construct.

```
= 1 + \mathsf{nat}(\frac{a-1}{2})
set(a)
contains(a, b)
lookup(a, b)
list(a)
head(a)
tail(a)
                             =  nat(\frac{a-1}{2})
concatenate(a,b)
appendright(a,b) = 2 + nat(\frac{a-1}{2})
isEmpty(a)
map(a)
                             = 1 + \mathsf{nat}(\frac{a-1}{2})
                             = 2 + \mathsf{nat}(\frac{a-3}{2})
shuffle(a)
chose(a)
                              = 0
choseN(a,b)
                             = 1 + \mathsf{nat}(b)
info(a)
                          = 1 + \mathsf{nat}(\frac{a-1}{4})
domain(a)
                           = 1 + \mathsf{nat}(\frac{a-1}{4})
map2list(a)
                             = 2 * \mathsf{nat}(\frac{a-1}{4})
concatMap(a, b)
bookweight(a)
                              = 0
countryshiptime(a) = 0
country ship cost(a)
getBookMap(a)
getCountryinfo(a)
calculateweight(a)
calculatecost(a, b)
                           = 0
calculate time(a, b)
                             = 1 + \operatorname{nat}(\frac{b-1}{2}) * (2 + \operatorname{nat}(\frac{a-1}{4}))
getBooks(a, b)
updateBooks(a,b) \qquad = \quad \mathsf{nat}(\tfrac{b-1}{2}) * (4 + \mathsf{nat}(\tfrac{a-1}{2}) * (2 + 2 * \mathsf{nat}(\tfrac{a-3}{4})) + 2 * \mathsf{nat}(\tfrac{a}{4} - 2))
updateBook(a,b,c) \quad = \quad 3 + \mathsf{nat}(\tfrac{a-1}{2}) * (2 + 2 * \mathsf{nat}(\tfrac{a+c}{4} - 1)) + 2 * \mathsf{nat}(\tfrac{a-b+C}{4} - 2)
```

Figure 10: Upper bounds for the functions of the book shop.