

## **Computer Vision**

**Exercise Session 1** 

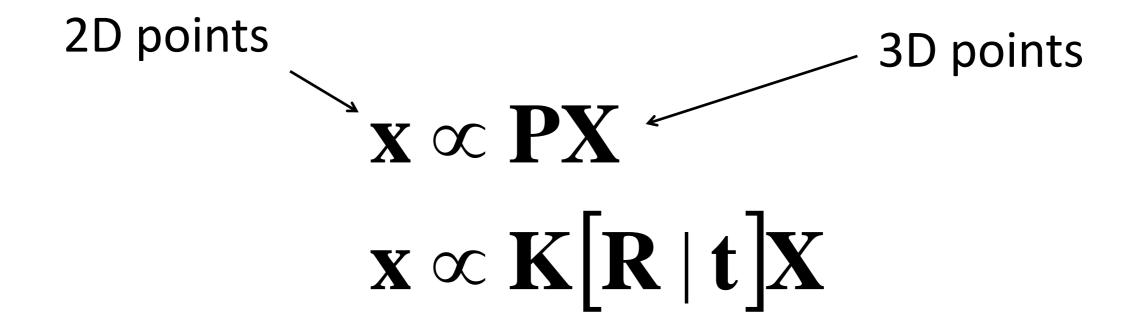




#### **Camera Calibration**

- Intrinsic parameters

  - Radial distortion coefficients



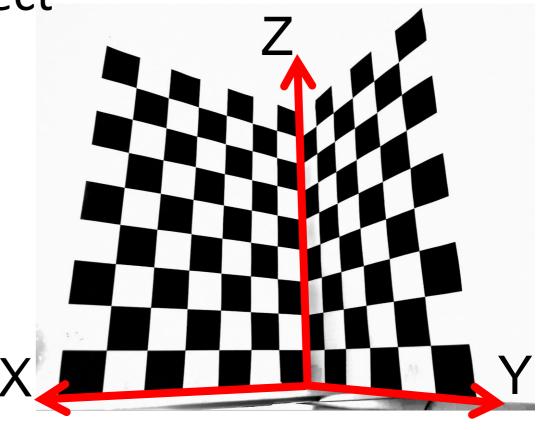


#### **Camera Calibration**

- Taking calibration pictures (optional)
  - You can use the provided image for tasks 1 3
- Use your own camera

Build your own calibration object

- Print checkerboard patterns
- Stich to two orthogonal planes





#### **Camera Calibration**

- 4 Tasks:
  - Data normalization
  - Direct Linear Transform (DLT)
  - Gold Standard algorithm
  - Bouguet's Calibration Toolbox
- Use the same settings for all tasks!
- Good reference:
   Multiple View Geometry in computer vision
   (Richard Hartley & Andrew Zisserman)





#### **Data normalization**

- Shift the centroid of the points to the origin
- Scale the points so that the mean distance to the origin is 1.
- Determine **P**using normalized points.
- Determine  $\mathbf{P} = \mathbf{T}^{-1}\hat{\mathbf{P}}\mathbf{U}$

$$\mathbf{T} = \begin{bmatrix} S_{2D} & C_{x} \\ S_{2D} & C_{y} \\ 1 \end{bmatrix}^{-1}$$

$$\mathbf{U} = \begin{bmatrix} S_{3D} & C_{x} \\ S_{3D} & C_{x} \\ S_{3D} & C_{z} \\ 1 \end{bmatrix}$$

## **Direct Linear Transform (DLT)**

$$\mathbf{AP} = \begin{bmatrix} \mathbf{w}_i \mathbf{X}_i^T & 0^T - \mathbf{x}_i \mathbf{X}_i^T \\ 0^T - \mathbf{w}_i \mathbf{X}_i^T & \mathbf{y}_i \mathbf{X}_i^T \end{bmatrix} \begin{pmatrix} \mathbf{P}^1 \\ \mathbf{P}^2 \\ \mathbf{P}^3 \end{pmatrix} = 0$$

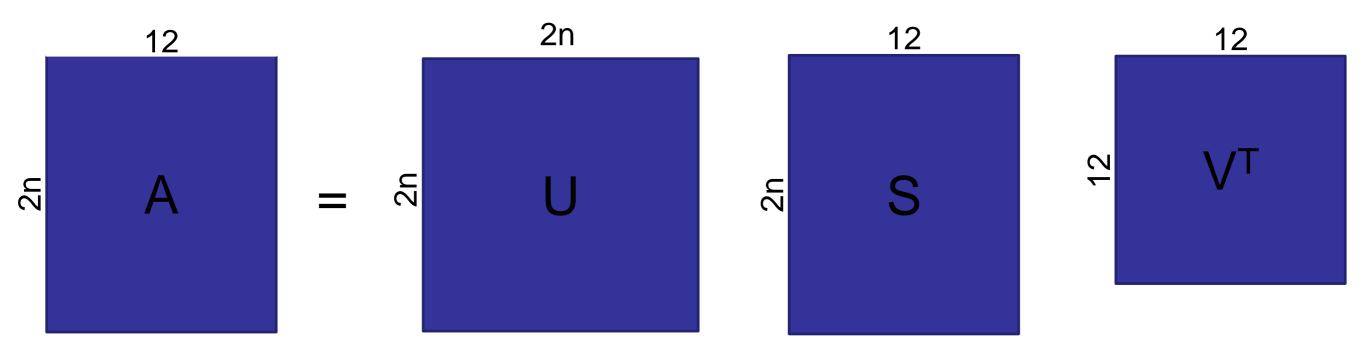
$$=\begin{bmatrix} X_{ix} & X_{iy} & X_{iz} & 1 & 0 & 0 & 0 & 0 & -x_{i}X_{ix} & -x_{i}X_{iy} & -x_{i}X_{iz} & -x_{i} \\ 0 & 0 & 0 & 0 & -X_{ix} & -X_{iy} & -X_{iz} & -1 & y_{i}X_{ix} & y_{i}X_{iy} & y_{i}X_{iz} & y_{i} \end{bmatrix} \begin{bmatrix} P_{1,1} \\ P_{1,2} \\ \vdots \\ P_{3,3} \\ P_{3,4} \end{bmatrix}$$





#### **Direct Linear Transform (DLT)**

Singular Value Decomposition

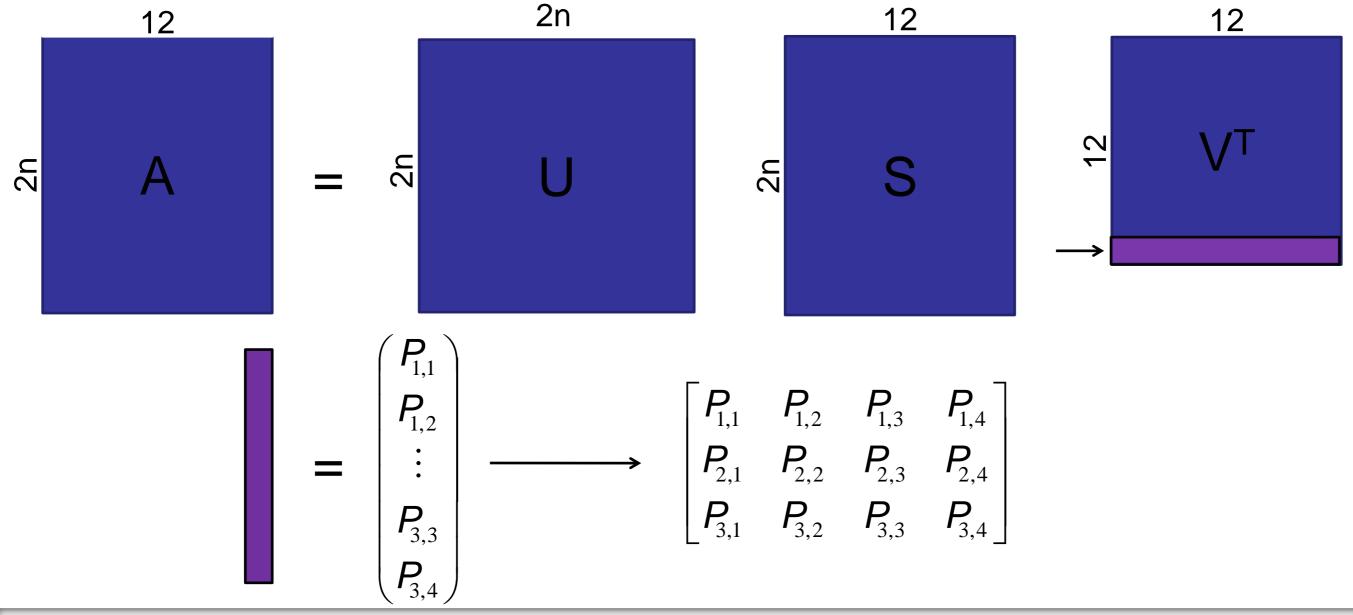






## **Direct Linear Transform (DLT)**

Singular Value Decomposition





## Camera Matrix Decomposition (K and R)

$$P = K[R|t] = [KR|-KR]$$

- K is upper triangular
- R is orthonormal
- QR decomposition A = QR
  - Q is orthogonal
  - R is upper triangular





## Camera Matrix Decomposition (K and R)

$$\mathbf{P} = \mathbf{K} [\mathbf{R} \mid \mathbf{t}] = [\mathbf{K} \mathbf{R} \mid -\mathbf{K} \mathbf{R} \mathbf{C}]$$

$$M = KR$$

$$\mathbf{M}^{-1} = \mathbf{R}^{-1} \mathbf{K}^{-1}$$

- Run QR-decomposition on the inverse of the left 3x3 part of P
- Invert both result matrices to get K and R





# Camera Matrix Decomposition (C)

The camera center is the point for which

$$PC = 0$$

■ This is the right null vector of P (→ SVD)

# **Gold Standard Algorithm**

- Normalize data
- Run DLT to get initial values
- Compute optimal  $\hat{\mathbf{P}}$  by minimizing the sum of squared reprojection errors

$$\min_{\hat{\mathbf{P}}} \sum_{i=1}^{N} d(\hat{\mathbf{x}}_{i}, \hat{\mathbf{P}}\hat{\mathbf{X}}_{i})^{2}$$

Denormalize  $\hat{\mathbf{P}}$ 



#### Minimization in MATLAB

- fminsearch
  - See code framework
- Isqnonlin
  - nonlinear least-squares

Vectorize your parameters





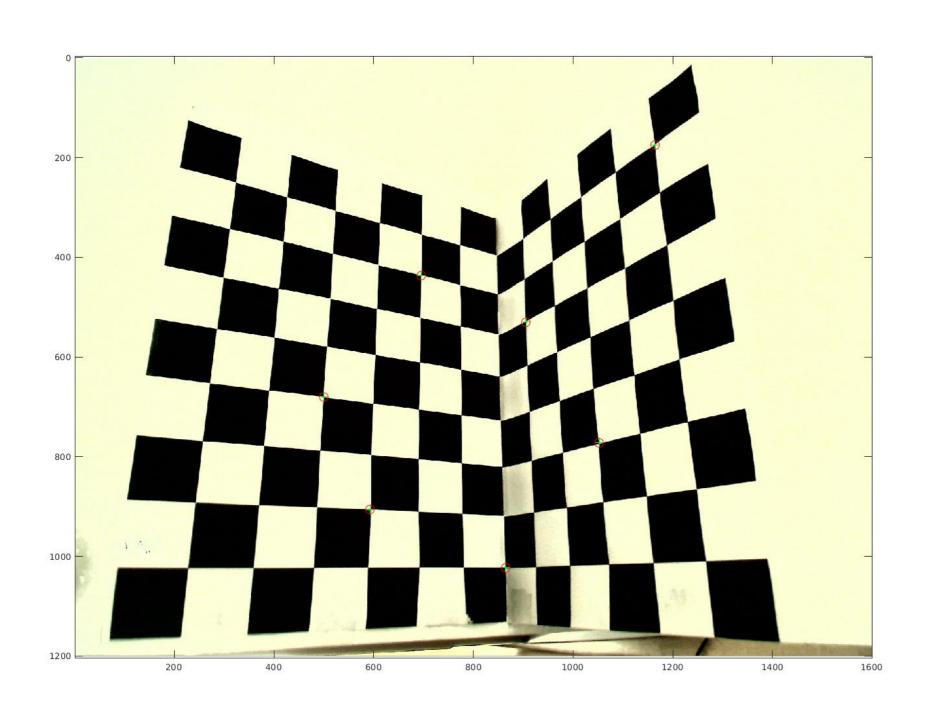
#### Hand-in

- Source code
- Matlab .mat-file with hand-clicked 3D-2D correspondences
- Image used for calibration (optional)
  - Use the same camera with the same settings for all tasks!
- Visualize hand-clicked points and reprojected 3D points
- Discuss values of intrinsic parameters
- Discuss average reprojection errors of all methods





#### Hand-in



Reprojection of the the 3D points



