# setFTs

Release 0.0.1.0

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**CHAPTER** 

ONE

## **SETFTS**

## 1.1 setFTs package

## 1.1.1 Submodules

## 1.1.2 setFTs.setfunctions module

class setFTs.setfunctions.SetFunction

Bases: abc.ABC

A parent class solely for inheritance purposes

gains(n: int, S0, maximize=True)

Helper function for greedy min/max. Finds element that will increase the set function value the most, if added to an input subset.

## **Parameters**

- **n** (int) groundset size
- **SO** (*np.array of type np.int32 or np.bool*) indicator vector to be improved upon

**Returns** integer index of element that produces the biggest gain if changed to 1 and the corresponding value gain

Return type (np.array,float)

maximize\_greedy(n: int, max\_card: int, verbose=False, force\_card=False)

Greedy maximization algorithm for set functions. (Does not guarantee that the optimal solution is found)

## **Parameters**

- **n** (*int*) groundset size
- max\_card (int) upper limit of cardinality up to which the greedy algorithm should check
- verbose (bool) flag to enable to print gain information for each cardinality
- **force\_card** (*bool*) flag that forces the algorithm to continue until specified max\_card is reached

**Returns** an np.array indicator vector of booleans that maximizes the setfunction and the evaluated setfunction for that indicator

Return type (np.array,float)

minimize\_greedy(n: int, max card: int, verbose=False, force card=False)

Greedy minimization algorithm for set functions does not guarantee that the optimal solution is found

#### **Parameters**

- n (int) groundset size
- max\_card (int) upper limit of cardinality up to which the greedy algorithm should check
- **verbose** (*bool*) flag to enable to print gain information for each cardinality
- **force\_card** (*bool*) flag that forces the algorithm to continue until specified max\_card is reached

**Returns** an array indicator vector of booleans that minimizes the setfunction and the evaluated setfunction for that indicator

Return type (np.array,float)

**class** setFTs.setfunctions.**SparseDSFTFunction**(frequencies: numpy.ndarray[Any,

numpy.dtype[numpy.typing.\_generic\_alias.ScalarType]], coefficients: numpy.ndarray[Any, numpy.dtype[numpy.float64]], model: str, normalization\_flag=False)

Bases: setFTs.setfunctions.SetFunction

export\_to\_csv(name='dsft')

exports the frequencies and coefficients into a csv file

**Parameters name** (str) – name of the newly created file

force\_k\_sparse(k)

creates a k-sparse estimate that only keeps the k largest coefficients

**Parameters k** (*int*) – number of coefficients to keep

**Returns** a sparseDSFTFunction object with only the k largest coefficients

Return type sparseDSFTFunction

**maximize\_MIP**(*C*=1000.0, cardinality\_constraint=None)

utilizes a Mixed Integer Program solver to maximize a set function value

## **Parameters**

- **C** (*int*) parameter for the MIP, if 1000. does not work, try larger values (see https://arxiv.org/pdf/2009.10749.pdf)
- **cardinality\_constraint** (*int* -> *bool*) function that evaluates to true if the cardinality constraint is met. Takes an integer as an input and evaluates to a bool (e.g cardinality\_constraint=lambda x: x == 3)

**Returns** bitvector with the largest function value and associated function value

**Return type** (npt.NDArray[bool],float)

**minimize\_MIP**(*C*=1000.0, cardinality\_constraint=None)

utilizes a Mixed Integer Program solver to minimize a set function value

### **Parameters**

• **C** (*int*) – parameter for the MIP, if 1000. does not work, try larger values (see https://arxiv.org/pdf/2009.10749.pdf)

• **cardinality\_constraint** (*int* -> *bool*) – function that evaluates to true if the cardinality constraint is met. Takes an integer as an input and evaluates to a bool (e.g cardinality constraint=lambda x: x == 3)

**Returns** bitvector with the smallest function value and associated function value

**Return type** (npt.NDArray[bool],float)

## shapley\_values()

Calculates the Shapley Values for all elements in the ground set

Returns an np.array the length of the groundset of shapley values

**Return type** npt.NDArray[float64]

## spectral\_energy(max\_card, flag\_rescale=True)

Calculates the spectral energy for each cardinality

### **Parameters**

- max\_card (int) Maximum Cardinality to consider
- **flag\_rescale** flag indicating whether spectral energy per cardinality should be rescaled to be relative to the total energy

Flag\_rescale bool

**Returns** spectral energy per cardinality

**Return type** List[float]

```
class setFTs.setfunctions.WHTOneHop(n, weights, set_function, model)
```

Bases: setFTs.setfunctions.SetFunction

class setFTs.setfunctions.WrapSetFunction(s: Callable[[numpy.ndarray[Any,

numpy.dtype[numpy.typing.\_generic\_alias.ScalarType]]],
float], n, use\_call\_dict=False, use\_loop=True)

Bases: setFTs.setfunctions.SetFunction

Wrapper class for instantiating set functions with a callable function

```
transform_fast(model='3')
```

fast Fourier transformation algorithm (not advised)

**Parameters model** (str) – basis upon which to calculate the transform see arxiv.org/pdf/2001.10290.pdf for more info

**Returns** a sparseDSFTFunction object of the desired model

**Return type** sparseDSFTFunction

**transform\_sparse**(*model='3'*, *k\_max=None*, *eps=1e-08*, *flag\_print=True*, *flag\_general=True*) sparse Fourier transformation algorithm

**Parameters model** (str) – basis upon which to calculate the Fourier transform

**Returns** a sparseDSFTFunction object of the desired model

**Return type** sparseDSFTFunction

class setFTs.setfunctions.WrapSignal(signal: List[float])

Bases: setFTs.setfunctions.SetFunction

Wrapper class for instantiating set functions with a full list of set function evaluations

## export\_to\_csv(name='sf.csv')

exports the frequencies and coefficients into a csv file

### **Parameters**

- name name of the newly created file ending in .csv
- **type** str

### max()

finds the subset that returns the largest set function value

**Returns** indicator vector that maximizes the set function

**Return type** npt.NDArray[bool]

### min()

finds the subset that returns the smallest set function value

**Returns** indicator vector that minimizes the set function

**Return type** npt.NDArray[bool]

## spectral\_energy(max\_card, flag\_rescale=True)

calculates the normalized coefficients per cardinality

#### **Parameters**

- max\_card (int) maximum cardinality for which to calculate the spectral energy
- **flag\_rescale** (*int*) flag indicating whether to average over all coefficients

Returns normalized coefficient of length max\_card

**Return type** List[float]

## transform\_fast(model='3')

fast Fourier transformation algorithm

**Parameters model** (*str*) – basis upon which to calculate the transform see arxiv.org/pdf/2001.10290.pdf for more info

**Returns** sparseDSFTFunction object of the desired model

**Return type** sparseDSFTFunction

**transform\_sparse**(*model='3'*, *k\_max=None*, *eps=1e-08*, *flag\_print=True*, *flag\_general=True*) sparse Fourier transformation algorithm

### **Parameters**

- model (str) basis upon which to calculate the Fourier transform
- **k\_max** (*int*) max number of coefficients to keep track of during computation
- eps (float of form 1e-i) eps: abs(x) < eps is treated as zero
- **flag\_print** (*bool*) enables verbose mode for more information
- **flag\_general** (bool) enables random one-hop Filtering

Returns a sparseDSFTFunction object of the desired model

**Return type** sparseDSFTFunction

## setFTs.setfunctions.build\_from\_csv(path, model=None)

loads a setfunction from a csv file

## **Parameters**

• **path** (*str*) – path to csv file

• **model** (*str*) – DSFT model to build (None to build set function)

**Returns** SparseDSFTFunction or WrapSignal

 $setFTs.setfunctions.createRandomSparse(n, k, constructor, rand\_sets = < function < lambda >> , rand\_vals = < function < lambda >> )$ 

creates a random k-sparse set function

## **Parameters**

- **n** size of the ground set
- k desired sparsity
- **constructor** a Fourier Sparse SetFunction constructor
- rand\_sets a random zero-one vector generator
- rand\_vals a random Fourier coefficient generator

Returns a fourier sparse set function, the actual sparsity

setFTs.setfunctions.eval\_sf(gt: setFTs.setfunctions.SetFunction, estimate: setFTs.setfunctions.SetFunction, n: int, n\_samples=1000, err\_types=['rel'], custom\_samples=None, p=0.5) evaluation function for setfunction. Compares an estimation to the ground truth

### **Parameters**

- gt a SetFunction representing the ground truth
- estimate a SetFunction
- **n** the size of the ground set
- **n\_samples** number of random measurements for the evaluation
- err\_types List of strings that are mae or relative reconstruction error

Returns error values

Return type List[float]

## 1.1.3 setFTs.plotting module

```
setFTs.plotting.plot_freq_card(sf, plot_type='bar') plot the number of frequencies per cardinality
```

#### **Parameters**

- **sf** (setfunctions.SetFunction) SetFunction object
- plot\_type (str) specifies plot type. Either 'bar' or 'plot

setFTs.plotting.plot\_freq\_card\_multi(sf\_list, label\_list, plot\_type='bar') plot the number of frequencies per cardinality for multiple setfunctions

#### **Parameters**

- **sf\_list** (List[setfunctions.SetFunctions]) list of SetFunction objects
- label\_list (List[str]) list of labels for the setfunctions in corresponding order
- plot\_type (str) specifies plot type. Either 'bar' or 'plot

setFTs.plotting.plot\_max\_greedy(sf\_list, label\_list, n, max\_card) plots the result of the greedy maximization when restricted to each cardinality

#### **Parameters**

- **sf\_list** (List[setfunctions.SetFunctions]) list of SetFunction objects
- label\_list (List[str]) list of labels for the setfunctions in corresponding order
- **n** (int) ground set size
- max\_card (int) maximal cardinality to consider

setFTs.plotting.plot\_max\_mip(ft\_list, label\_list, max\_card) plots the result of the MIP-based maximization when restricted to each cardinality

## **Parameters**

- **ft\_list** (List[setfunctions.SetFunctions]) list of SetFunction objects
- label\_list (List[str]) list of labels for the setfunctions in corresponding order
- max\_card (int) maximal cardinality to consider

setFTs.plotting.plot\_min\_greedy(sf\_list, label\_list, n, max\_card) plots the result of the greedy minimization when restricted to each cardinality

## **Parameters**

- **sf\_list** (*List*[setfunctions.SetFunctions]) list of SetFunction objects
- label\_list (List[str]) list of labels for the setfunctions in corresponding order
- n (int) ground set size
- max\_card (int) maximal cardinality to consider

setFTs.plotting.plot\_min\_mip(ft\_list, label\_list, max\_card)

plots the result of the MIP-based minimization when restricted to each cardinality

### **Parameters**

- **ft\_list** (List[setfunctions.SetFunctions]) list of SetFunction objects
- label\_list (List[str]) list of labels for the setfunctions in corresponding order
- max\_card (int) maximal cardinality to consider

## setFTs.plotting.plot\_minimization\_found(sf, model='3', greedy=False)

plots the minimal value found when performing a minimization algorithm on an eps sparse approximation

#### **Parameters**

- sf (setfunctions.SetFunction) SetFunction object
- model (int) Fourier transformation base to consider
- greedy (bool) flag indicating whether greedy (True) or MIP based algorithm (False) should be used

setFTs.plotting.plot\_minimization\_found\_biggest\_coefs(sf, max\_sparsity, interval, model='3', greedy=False)

plots the minimal value found when performing a minimization algorithm constrained to its biggest coefficients

#### **Parameters**

- sf (setfunctions.SetFunction) SetFunction object
- max\_sparsity (int) maximal sparsity to consider
- interval (int :param model: Fourier transformation base to consider) increment of sparsity
- greedy (bool) flag indicating whether greedy (True) or MIP based algorithm (False) should be used

setFTs.plotting.plot\_reconstruction\_error(sf, n, err\_types=['rel'], model='3', flag\_general=True) plots the reconstruction error when approximated with the sparse algorithm with different eps values

#### **Parameters**

- sf (setfunctions.SetFunction) SetFunction object
- **err\_types** (*List[str]*) list of error calculations to perform
- model (int) Fourier transformation base to consider
- **flag\_general** (*bool*) enables random one hop filtering

setFTs.plotting.plot\_reconstruction\_error\_biggest\_coefs(sf, n, max\_sparsity, interval, err\_types=['rel'], model='3')

plots the reconstruction error when approximated with the sparse algorithm constrained to only the biggest coefs

### **Parameters**

- **sf** (setfunctions.SetFunction) SetFunction object
- **n** (int) ground set size
- max\_sparsity (int) maximal sparsity to consider
- **interval** (*int*) increment of sparsity
- **err\_types** (*List[str]*) list of error calculations to perform
- model (int) Fourier transformation base to consider

 $\verb|setFTs.plotting.plot_scatter| (\textit{sf}, label, max\_card)|$ 

plots the coefficients of a setfunction per cardinality as a scatterplot

## **Parameters**

- sf (setfunctions.SetFunction) SetFunction object
- label (str) name of the setfunction

• max\_card (int) – maximal cardinality to consider

setFTs.plotting.plot\_spectral\_energy(sf, max\_card, flag\_rescale=True, plot\_type='plot') plot the average coefficient for each cardinality

## **Parameters**

- **sf** (setfunctions.SetFunction) SetFunction object
- max\_card (int) maximal cardinality to consider
- **flag\_rescale** (*bool*) flag that enables normalization
- plot\_type (str) specifies plot type. Either 'bar' or 'plot

setFTs.plotting.plot\_spectral\_energy\_multi(sf\_list, label\_list, max\_card, flag\_rescale=True, plot\_type='plot')

plot the average coefficient for each cardinality for multiple set functions

## **Parameters**

- $sf_list(List[setfunctions.SetFunctions]) list of SetFunction objects$
- label\_list (List[str]) list of labels for the setfunctions in corresponding order
- max\_card (int) maximal cardinality to consider
- **flag\_rescale** (*bool*) flag that enables normalization
- plot\_type (str) specifies plot type. Either 'bar' or 'plot

## CHAPTER

## TWO

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