

Local Search for scheduling

Ebrahim Kashkoush

1 Abstract

in this project we try to solve scheduling problem using three Heuristics Local search, Branch and bound and genetic heuristic, we write three unattached projects in each one we use one heuristic, we can get better and faster algorithm by Combine more than one heuristic or by using more complex algorithms like evaluate pairs of chromosomes instead of chromosomes, and use more complex target function in genetic. but the main idea of the project was to learn the basic concept of the following heuristics.

The problem is Scheduling on restricted uniformly related machines. where the Input is An integer number of machines $m \geq 2$. A set of n jobs $J = \{1, 2, \dots, n\}$ where job j has an integer processing time $P_j > 0$ Machines speeds $s_i \in \{1, 2, 4\}$ for $i = 1, 2, \dots, m$, we solve the same problem in the three heuristics

2 Local Search

The local search algorithm It consists of several steps we will Explain the algorithm step by step

2.1 pre preparing(initial solution)

to start running the local search algorithm first we need initial solution. we have as input two file the first file is for tasks where we have on each line task time (integer value), the second file is for machines where each line contains machine speed (integer 1,2,4). from the input we build two vectors the first one hold the tasks and the second hold the machines. after having data structure hold the tasks and the machines we should Hand out the tasks into the machines and make initial solution, so we need greedy algorithm its not important how many the greedy algorithm is good. also if we hand out the task randomly at the end we will have the same result, so for convenience we insert the numbers to minnum heap to sort the tasks and then we Turned on the tasks into machines In a fair way (In a circular) and on each time we give the same amount tasks as the current machine speed value to the machine, for example if we have machine with speed 2 we will give it two task each time, and if the machine speed 4 we will give it 4 tasks each time. we do that while we still have tasks, and when we hand out all the tasks we have an initial solution.

2.2 Local Search for two machines

on this subsection and on the next subsections we will solve small problems and then we will combine all of them together in the last subsection creating the full problem solution.

the current problem is given two machines m_1 and m_2 we want to find the best tasks from m_1 and m_2 that if we swap them between m_1 and m_2 we get the best Improvement to achieve the Goal . so now we should define what is the goal that we want to achieve.

giving two machines m_1 and m_2 where the time of m_1 is X and the time of m_2 is Y . let assume that we chose k tasks from m_1 and r tasks from m_2 now we should evaluate the time after swapping the tasks (simulation) between the two machines by passing k tasks from m_1 to m_2 and removing the k tasks from m_1 ,and the same by passing r tasks from m_2 to m_1 and removing the tasks from m_2 . lets define the time of m_1 after the change is A and the time of m_2 after the change (swapping the tasks) is B . the our goal that we want to achieve:

$(\max\{A,B\} < \max\{X,Y\} \parallel (\max\{A,B\} = \max\{X,Y\} \text{ and } (A+B) < (X+Y))$

that means if we save the best solution and we find new solution by swapping k, r tasks between m_1 and m_2 and that solution better than the best solution for now, we save it as the best solution and we save r, k tasks and then we check the other k, r combination with the new best solution after we check all possible to choose r, k we have the best r, k that by swapping them we achieve our goal NOTE(k and r is constant).

the idea of adding $(\max\{A,B\} = \max\{X,Y\} \text{ and } (A+B) < (X+Y))$ is to give priority to machines with high speed we want to fill machines with high speed also if the final solution still the same $(\max\{A,B\})$, because that help us to find bigger task to swap in the future.

2.3 All possible combination of r, k