

2 **Timing of hadron showers in the CALICE Analog** 3 **Hadronic Calorimeter prototype using steel** 4 **absorber**

The CALICE Collaboration*

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6 **ABSTRACT:** This note presents results obtained with the CALICE Analog Hadronic Calorimeter prototype with steel absorber at the SPS CERN testbeam campaign in July 2015. The analysis presents the timing calibration and includes timing distributions for muon, electron and pion beams. The results are compared to several GEANT 4 version 10.1 physics lists.

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34 1. Introduction

35 Experiments at future lepton colliders require unprecedented jet energy resolution of 3-4% up to
36 250 GeV jet energies. The Particle Flow concept (PFAs) [1] aims to achieve such resolutions by
37 combining measurements of the tracker and calorimeters. This requires exceptional granularity for
38 the calorimeters. The CALICE Collaboration develops, builds and tests such calorimeters to fulfil

the requirements imposed by PFAs. One calorimeter concept is the Analog Hadronic Calorimeter (AHCAL) that consists of scintillator tiles of $3 \times 3 \text{ cm}^2$ readout by Silicon Photomultipliers (SiPMs). Several prototypes with different absorbers, granularity and readout have been tested [2, 3].

Apart from energy measurement, the aspect of precise timing measurement is being investigated. Timing measurements in a calorimeter can be used to reject out of time pile-up events. In addition, the impact of background events on physics measurements such as $\gamma\gamma \rightarrow \text{hadrons}$ background, could be mitigated by using timing information of the calorimeters and trackers [4]. Moreover, time information could be used to improve the energy reconstruction of hadronic showers by distinguishing the electromagnetic and hadronic components of the shower.[5].

The CALICE Analog Hadronic Calorimeter (AHCAL) prototype with steel absorber has been installed in the SPS CERN facilities in July 2015. This prototype was partially instrumented and was comprised of several versions of active readout (SiPM, scintillator material, tile wrapping). The performance of this prototype is not expected to reach the final performance of the engineering prototype. Furthermore, this prototype was operated at a lower clock speed than the design in order to enhance the data taking efficiency at a testbeam with a continuous beam. This limits the timing resolution. For bunched beams at a lepton collider, a 20 times faster clock is foreseen. This note presents the time calibration procedure of the AHCAL and the results obtained in muon, electron and pion beams in an energy range from 10 GeV to 90 GeV, as indicated in Table A1 in the appendix. This analysis is the first of its kind to such a system level and enters new territories for high granular calorimeters.

2. Testbeam Setup

The testbeam setup at CERN in July 2015, at the SPS beamline H2, is shown in figure 1.

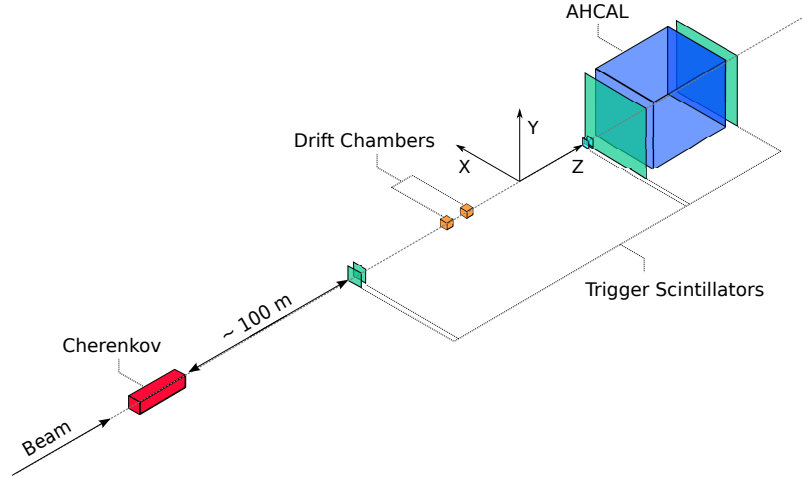


Figure 1: Sketch view of the beamline setup at the CERN SPS H2 beamline in July 2015. The size of the beamline elements is not to scale.

The AHCAL prototype absorber stack is composed of 48 steel plates in which 14 active modules were installed. The two first modules consist of single ECAL Base Units (EBUs) with 4×36

cells of $4.5 \times 0.5 \text{ cm}^2$ size. The ECAL cells of both modules are oriented parallel to the x-axis. The next eight modules consist of single HCAL Base Units (HBUs) with 12×12 cells of $3 \times 3 \text{ cm}^2$ size. The absorber plates have a thickness of 1.7 cm, such that the first 10 modules correspond to a depth of around $10 X_0$ ($\sim 1 \lambda_\pi$). These modules were mainly used as a shower start finder. The last four modules consist of 2 by 2 HBUs providing information about the development of pion showers at different depths. In total, the prototype has 3744 channels. Table 1 provides an overview of the AHCAL layer structure. It uses SiPM technology coupled to scintillator tiles readout by an application specific integrated chip, the SPIROC2b [6]. A diverse variety of SiPMs and tile designs were used in this testbeam, details of the SiPM characteristics can be seen in Table A2. The AHCAL detector was placed on a movable stage in order to be able to scan the detector with muons for calibration runs.

Table 1: Layer structure of the AHCAL in July 2015.

Absorber Slot #	Layer #	Abs. thickness before layer [X_0/λ_π]	Layer size [cm^2]	N_{chn}
1-2	1-2	$\sim 1/0.1$	18×18	288
3-10	3-10	$\sim 1/0.1$	36×36	1152
11	11	$\sim 1/0.1$	72×72	576
13	12	$\sim 2/0.2$	72×72	576
21	13	$\sim 8/0.8$	72×72	576
31	14	$\sim 10/1$	72×72	576

Scintillator plates, $10 \times 10 \text{ cm}^2$ and $50 \times 50 \text{ cm}^2$, placed in front and back of the calorimeter are used as a trigger signal that is provided to the AHCAL DAQ to validate events [7]. Additionally, the coincidence signal from the scintillators is provided directly via charge injection to several channels of the AHCAL in order to provide a reference time of the trigger as shown in Table A3. A Cherenkov detector, at around 100 m upstream, was available to tag incoming particles.

3. Simulation

The AHCAL simulation model is based on the MOKKA [8] framework v08-05-01 and the new DD4HEP [9] framework v00-16, using the GEANT 4 v10.1 simulation [10]. A right-handed coordinate system is used such that the Z-axis points in the beam direction and that the Y-axis is directed upwards. No beamline instrumentation is simulated except for the trigger scintillators in front of and behind the detector. A similar amount of material is achieved by filling the world volume with air and by adding 5.6 mm of lead ($\sim 1 X_0$) directly at the calorimeter front face in order to account for missing upstream material. The beam gun is placed 1 m from the calorimeter front face and it is configured to generate single beam particles with a 2% momentum spread according to the beamline parameters. Muons and electron showers are simulated using the QGSP_BERT_HP physics list. Pion showers are simulated using QGSP_BERT, QGSP_BERT_HP and QBBC physics lists.

The MOKKA and DD4HEP simulations have been checked to give consistent results. In the following, only the results with the DD4HEP simulation are shown.

3.1 Geometry and Digitization

The AHCAL simulation model consists of 32 absorber layers and 14 active modules. Each absorber layer is made of stainless steel 17.2 mm thick. Each active layer is primarily composed of 1 mm steel cassette, 0.7 mm PCB, 2 or 3 mm scintillator strip or tile. The density and composition of the scintillator are taken as default provided in GEANT 4.

The beam profile is generated using a particle gun placed 1 m upstream of the calorimeter front. For muons, a flat beam profile is used and is not expected to impact the MIP response. For electrons and pions, a 2D Gaussian beam is assumed. The mean and sigma of the Gaussian beam are estimated from data using the energy-weighted center of gravity in the x and y-axis.

The digitization of simulated hits is very similar to the previous AHCAL physics prototype [11]. Individual calibration factors obtained from data are used to extract the light yield which is needed to model the statistical fluctuations of photons hitting a SiPM [12]. Saturation effects are also included using a global parameter, the number of pixels available on each SiPM type, as no measurement of the saturation curve is available. Most of the tiles used are wrapped with a reflective foil such that optical crosstalk effects between channels can be neglected. For modules with no wrapping, a default value of 15% for the cross-talk is used based on previous measurements with the AHCAL physics prototype [13]. A variation of the cross-talk parameter between 10% and 18% is used for systematics (see section 6.1). Noise is extracted from muon runs and overlaid onto simulated events. Dead channels and channels without calibration factors (MIP, gain, pedestal) are rejected.

The timing of simulated hits is modeled according to the hit time measurement in the SPIROC2b. The energy from sub-hits, equivalent to a GEANT 4 step, in a cell is integrated over a sliding time window of 15 ns, if the energy sum of the sub-hits in this time window passes the energy threshold, the time of the sub-hit passing the energy threshold is used as the time of the simulated hit. To simulate detector resolution effects, the time of a simulated hit is smeared with a double Gaussian function, with parameters determined from data. In addition, it is convoluted with a Gaussian function with a sigma depending on the number of triggered channels in a chip parametrized from data (see section 5.8).

After the digitization, all simulated hits have the same format as raw data hits and are reconstructed with the same software chain that is used for data. To suppress noise hits, only hits above 0.5 MIP are considered in this study.

3.2 AHCAL Model Validation

Prior to the time analysis, the simulation and digitization are validated. Comparisons of electromagnetic interactions in the AHCAL are done as such interactions should be well described in simulation. Firstly, the simulation must be validated at the lowest hit energies. The comparison of the spectrum of a MIP-like particle traversing the AHCAL is shown in figure 2a. The shape of the spectrum matches relatively well. The simulation is slightly more narrow than the data because of channel-by-channel mis-calibrations that are not fully modeled in the simulation. The figure 2b shows the longitudinal mean energy profile for muon-like tracks in data and simulation. The data is reproduced by the simulations within 3-4%. Channels for which no calibration with MIP-like particles could be determined in data are excluded from the analysis in data and simulation. A

systematic on the energy scale of the calorimeter of 3.6% is applied later on the data when looking at the dependence of the time as a function of the hit energy (see section 6.1).

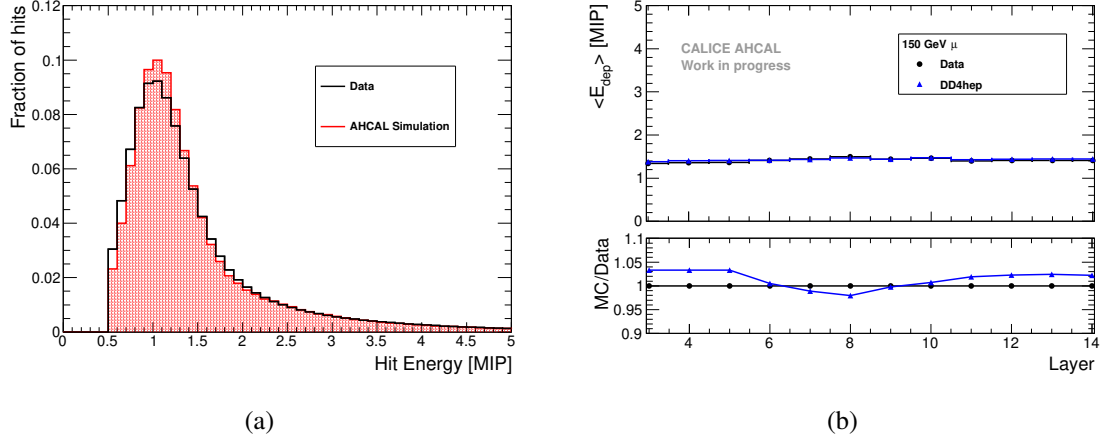


Figure 2: a) Hit Energy Spectra for the complete AHCAL for muon like-track hits for both data and simulation. b) Longitudinal mean energy profile for muon like-track hits in data and the DD4HEP simulation.

The hit energy spectrum has also been checked for electrons. Data and simulation agree rather well within 10% for hit energies below 10 MIPs, which is the range relevant for this analysis.

4. Event Selection

A more detailed description of the selections applied can be read in [14].

4.1 Muon selection

To select muons, an event pre-selection and a track finder [12] selection is performed. A cut on the maximum number of hits (n_{hits}) in the AHCAL is applied at 20 as the number of hits should be around 1 per layer for a MIP-like particle plus the number of noise hits expected in the detector. The track finder algorithm selects AHCAL towers of hits in the same $x : y$ position and it rejects AHCAL towers that contain less than a certain number of hits. In order to select muons, a straight track of at least 7 hits is required in the first ten layers of the AHCAL. Outside of the inner 12x12 tile area, a straight track of at least 2 hits in the last 4 layers is required. In addition, to reject pions showering deep in the detector, no more than 2 hits are allowed per layer to account for some flexibility with noise hits. A summary of the muon selection is shown in Table A4. The selection efficiency is 72.5% for muons, <0.1% for electrons and 5% for pions which is compatible with the fraction of pion traversing the AHCAL without hard interaction.

4.2 Electron selection

Electron events are needed to validate the timing behavior in simulation as well as the detector simulation model. It is important to have a clean sample of electrons to cross-check the timing calibration. An electron selection is performed using the beam instrumentation and the AHCAL layer

information. Events with a Cherenkov tag are used. The energy deposit in the first three AHCAL layers ($E_3 + E_4 + E_5$) must be over 10 MIPs. A box cut on the number of hits (n_{hits}) and the center of gravity in the z-direction (cog_z) is applied. As the number of hits in an electron shower increases with the shower energy, this cut is energy dependent. The energy deposited in the last two layers relative to the energy deposited in the calorimeter ($(E_{13} + E_{14})/\Sigma E$) is required to be under 1% to reject pion showers and to contain the electron shower. The electron selection is summarized in Table A5. The selection efficiencies are shown in Table 2. Even though a significant fraction of pions passes the electron selection at low energies, there is confidence that very little pion contamination is present in the data due to the pure electron beam generation with the beamline.

Table 2: Efficiency of the electron selection for simulated electrons and pions for energies between 10 and 50 GeV. Muons are simulated at 150 GeV. The efficiency is defined as the number of events after selection divided by the number of events before selection and it is estimated from Monte-Carlo. No Cherenkov efficiency is included in the calculation as it is not simulated.

Beam Energy	ϵ_μ	ϵ_e	ϵ_π
10 GeV	<0.1%	96%	15.9%
15 GeV	<0.1%	95.7%	10.1%
20 GeV	<0.1%	95.2%	6.3%
30 GeV	<0.1%	93.9%	2.3%
40 GeV	<0.1%	92.7%	1.2%
50 GeV	<0.1%	91.5%	1.1%

4.3 Pion selection

The goal of the pion selection is to reject punch-through pions, muons and possible electron contamination. The events without a Cherenkov tag are selected. The number of hits per event (n_{hits}) needs to be above 20 to reject most muons or punch-through pions. No cut on the center of gravity in z is done in order not to bias the start of the pion shower. The energy deposited in the two last AHCAL layers relative to the total energy ($(E_{13} + E_{14})/\Sigma E$) must be above 1% in order to ensure that the pion showered and to reject possible electron showers. The number of hits in the two first AHCAL layers ($N_3 + N_4$) must be smaller than 5 to mitigate possible particle contamination from electrons. In addition, multiple particle events were observed in the data. As no beam instrumentation could be used for rejecting these events, a rejection method based on the hit time information was developed. The method is the following: all the hits in an event are ordered in time; For each hit with a time over 50 ns, the number of hits in a timing window of 30 ns after the hit time is counted. If the number of hits is above 5, it is classified as a *late cluster*. The event is rejected if there is at least one late cluster ($n_{Cluster}$). If an event has several particles, the time reference will be given by the first particle. Therefore, all the hits coming from the second particle will be delayed relative to the time reference. These events need to be rejected as they can influence the amount of late hits in the time distribution. The multi-particle event rejection has been checked on simulated data and affects the selection between <0.1% up to 2% from 10 to 90 GeV pions. These multi-particle events are also suppressed in data. The number of events removed varies between 0.1%

184 and 1% depending on the beam energy. However, due to the calorimeter not being fully equipped
185 thus providing limited information, some contamination by multi-particle may remain in the data.
186 The Table A6 shows the selection cuts for the pion data. The selection efficiencies are shown in
187 Table 3

Table 3: Efficiency of the pion selection for beam energies between 10 and 90 GeV. Muons are simulated at 150 GeV. The efficiency is defined as the number of events after selection divided by the number of events before selection and it is estimated from Monte-Carlo. No Cherenkov efficiency is included in the calculation as it is not simulated.

Beam Energy	ϵ_μ	ϵ_e	ϵ_π
10 GeV	<0.1%	<0.1%	29.9%
30 GeV	0.9%	<0.1%	50.3%
50 GeV	0.9%	<0.1%	51.1%
70 GeV	0.9%	<0.1%	51%
90 GeV	0.9%	<0.1%	50.2%

188 5. Timing calibration of the AHCAL

189 In a first step, the muon data is used to determine the parameters for the timing calibration. Muons
190 are used because the process they induce is quasi-instantaneous. In a second step, the calibra-
191 tion is cross-checked using the electron data as also processes induced by EM showers are quasi-
192 instantaneous. This enables a verification of the time calibration procedure and may reveal effects
193 that are not present in the muon data. In the following, the fully calibrated hit time of a channel
194 is referred to as *the time of the first hit* because only the first hit per channel is registered dur-
195 ing a bunch-crossing (multiple hits could occur in a channel but only the first one is kept by the
196 front-end).

197 5.1 Time recording in the SPIROC2b

198 The SPIROC2b ASIC can readout 36 SiPM-channels. It is capable to measure the charge with
199 two gains (high and low gain) and the time for each channel. Each channel is equipped with
200 an analog memory, called memory-cells, with a depth of 16 events to store the energy and time
201 measurement. Additionally, the ASIC can be operated in external or auto-trigger mode with a
202 configurable threshold. The ASIC has two multiplexed TDC voltage ramps to avoid dead time
203 between each clock cycle. The two voltage ramps are common to all channels on the ASIC. The
204 time information provided by the SPIROC2b in the data is in TDC units. The TDC information of
205 each channel can be reconstructed into nanoseconds following the schematic shown in figure 3.

206 In order to determine the ramp slope, the starting point or pedestal of the ramp and the endpoint
207 of the ramp are measured. Since the SPIROC2b has two TDC ramps, each defined by the parity
208 (even or odd) of the clock cycle counter or bunch-crossing ID (BXID), two slopes need to be
209 extracted per chip. The differences between memory-cells lead to offsets in pedestals, thus 16

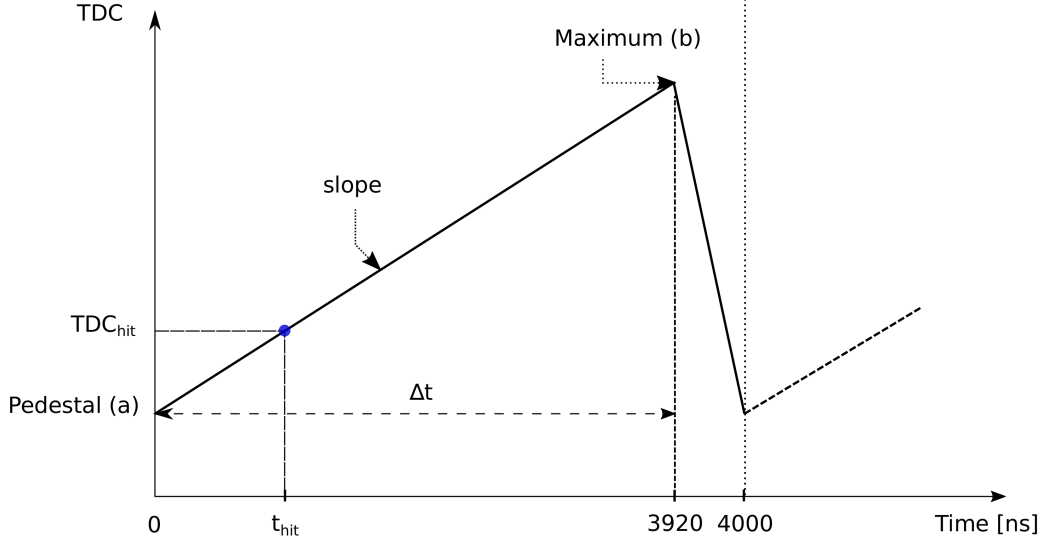


Figure 3: Schematic of the TDC ramp in the SPIROC2b used in testbeam with a slow clock of 250 kHz. The slope of the ramp is $s = (Max - Ped)/\Delta t$.

210 calibration values are needed per channel. The time of the hit in the i -th channel is then calculated
 211 as the following:

$$t_i[ns] = 1/s \times (TDC_i - Ped) \quad (5.1)$$

212 where Ped is the pedestal of the i -th channel in the first memory cell without taking into account
 213 the bunch-crossing parity. The extraction of the slope and the determination of the pedestal is
 214 described in the following sections.

215 5.2 Timing calibration procedure

216 The timing calibration procedure of the AHCAL is quite complex. An overview of the steps per-
 217 formed for the time calibration of each individual AHCAL channel is shown in figure 4.

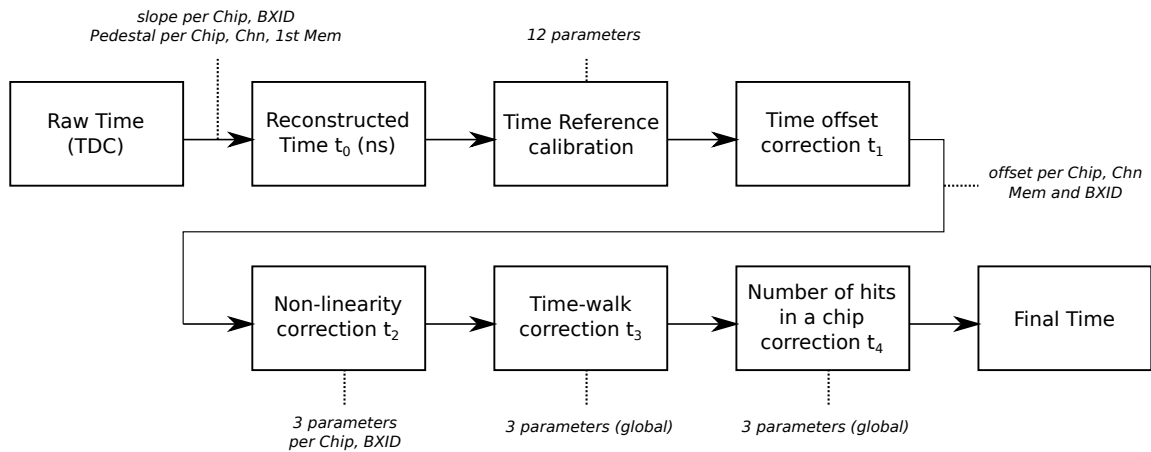


Figure 4: Overall view of the different steps performed for the AHCAL timing calibration. In total, more than 20000 constants are needed.

218 In the following, for each step, the corresponding calibrated time t_i in the figure will be used.

219 5.3 Slope and Pedestal extraction

220 To reconstruct the time in a channel, the TDC value measured needs to be converted into nanosec-
221 onds. The slope is calculated as

$$s [\text{TDC/ns}] = \frac{b - a}{3920} \quad (5.2)$$

222 where s is the TDC ramp slope, b is the endpoint of the TDC ramp and a is the start point of the
223 TDC ramp that is referred to in the following as the pedestal. The total length of the ramp is 3920
224 ns instead of the expected value of 4000 ns due to a deadtime of around 2% [15] induced by the
225 multiplexer that switches between the two TDC ramps.

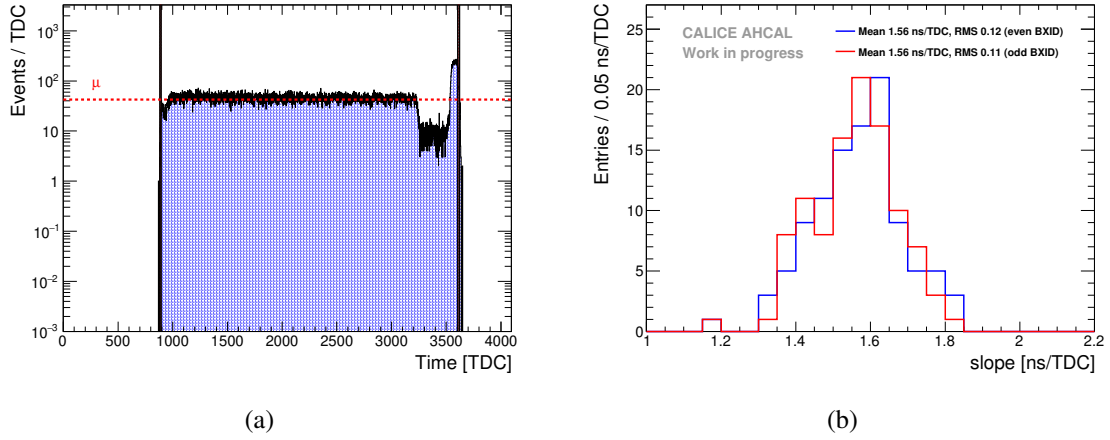


Figure 5: a) TDC spectrum of a typical chip. The vertical black lines indicate the fitted Max and Pedestal parameters for this chip. The horizontal red line represents the mean μ of the histogram on the y-axis used for the determination of the parameter a as the value of the first bin above 30% of μ . The parameter b is extracted as the value of the last bin above 50% of the maximum bin. The extracted parameters are $1/s = 1.44 \pm 0.01$ ns/TDC, $a = 888 \pm 5$ TDC and $b = 3613 \pm 8$ TDC. b) Distribution of the fitted slopes for even and odd bunch-crossing IDs. $\mu_{\text{odd}} = 1.564$ ns/TDC, $\text{RMS}_{\text{odd}} = 0.121$, $\mu_{\text{even}} = 1.556$ ns/TDC, $\text{RMS}_{\text{even}} = 0.113$. In total, 208 TDC slopes were extracted.

226 To first order, the slope of the TDC ramp is assumed to be linear. The parameters a and b
227 are extracted from the TDC spectrum per chip (combining all channels) and BXID parity using
228 only the first memory-cell as shown in figure 5a. The TDC ramp slope does not depend on the
229 memory-cell as the memory-cell only introduce an offset on the parameters a and b . A total of 208
230 slopes have to be extracted for the testbeam setup.

231 The extracted values for the inverse of the slope are shown in figure 5b. They are in the
232 expected range of 1.6 ns per TDC bin due to the limited dynamic range provided by the chip, of
233 around 2500 TDC bins for 4 μs .

234 The same method is used to determine the pedestal for each channel using only the first mem-
235 ory cell without taking into account the bunch-crossing parity. Any time offsets introduced by the
236 other memory cells and the bunch-crossing parity are corrected in section 5.5.

237 5.4 Time reference calibration

238 The channels recording the signal from the trigger scintillators (see Table A3) are calibrated using
 239 the same method described above. This is used later on in the analysis as a time reference (T_{ref})
 240 compared to all channels ($t_{hit} - T_{ref}$). To guarantee the most accurate result, the pedestal value is
 241 extracted for each memory cell. Events are selected by requiring T_{12} , T_{13} and T_{14} to be present. A
 242 cut on the signal amplitude is performed to reject noise hits from these channels. As these channels
 243 receive the trigger coincidence signal at the same time, a timing correction is applied to ensure that
 244 they match in time. It is applied to remove any effects induced by the front-end electronics [16, 15].

245 A 2^{nd} order polynomial correction of $(T_{12} - T_{14})$ and $(T_{13} - T_{14})$ as a function of T_{12} and
 246 T_{13} is performed respectively. However, in this case, T_{14} is not corrected for non-linearity. An
 247 example for the reference trigger T_{12} is shown in figure 6a before and figure 6b after the correction.
 248 The y-axis represent the mean of $(T_{12} - T_{14})$. The two lines are related to the pedestal value that
 249 is dependent on the bunch-crossing parity and was not taken into account in this analysis. One
 250 would expect that the curves are flat independent of T_{12} if no effect are introduced by the front-
 251 end. However, one can notice a slight curvature indicating a non-linear response dependent of the
 252 time of T_{12} .

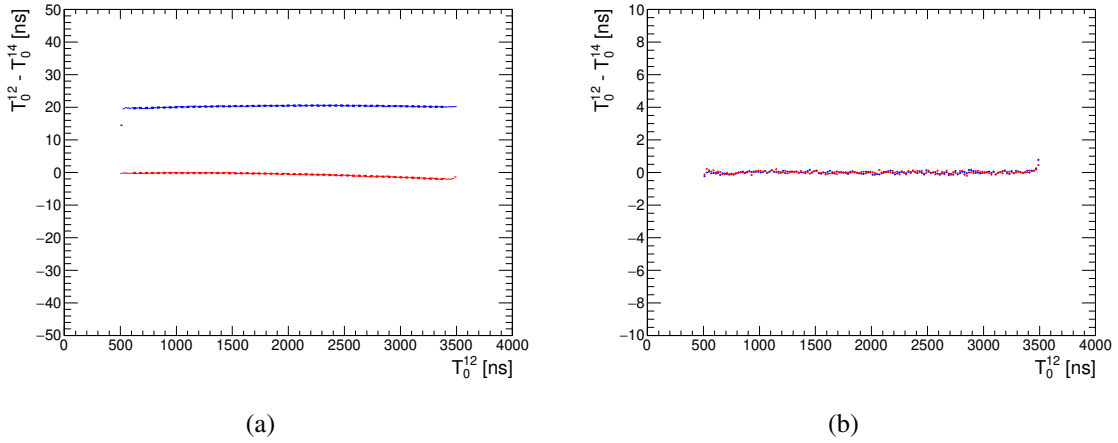


Figure 6: a) Mean of $(T_{12} - T_{14})$ as a function of T_{12} before the correction with a 2^{nd} order polynomial. b) Mean of $(T_{12} - T_{14})$ as a function of T_{12} after the correction.

253 Ideally, the $T_{12} - T_{14}$ and $T_{13} - T_{14}$ distributions should be a Gaussian distribution centered at 0
 254 ns. The figure 7a shows the distribution of $T_{12} - T_{14}$ before and after the correction. The correction
 255 with the 2^{nd} order polynomial corrects for the non-linearity between the time reference channels
 256 as well as it corrects at the same time for the difference of pedestals with the bunch-crossing parity
 257 which was not taken into account at the time of the analysis.

258 Finally, the time reference (T_{ref}) is calculated as the mean of T_{12} , T_{13} and T_{14} per event. To
 259 reject events with a too large time reference uncertainty ($\sigma_{T_{ref}} = \sqrt{\sum_i (T_i - T_{ref})^2 / N}$), a cut of 4 ns
 260 on the time reference uncertainty is applied. The mean uncertainty of the time reference is around
 261 1.39 ns as shown in figure 7b. This resolution from the time reference contributes to the final timing
 262 resolution obtained.

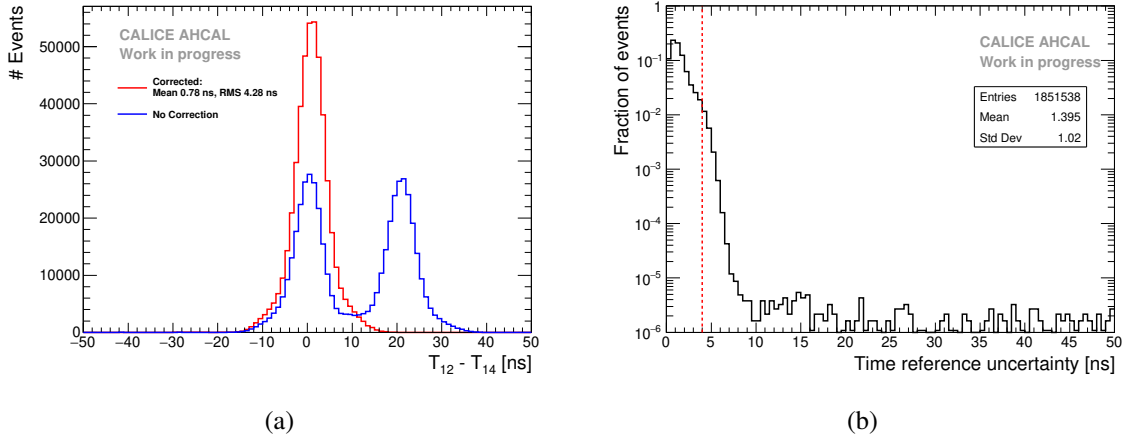


Figure 7: a) Time difference between the trigger channels before and after correction for T_{12} and T_{14} . $\mu_{corrected} = 0.78$ ns, $RMS_{corrected} = 4.28$ ns. The two peaks in blue are due to the fact that the pedestal value is dependent on the bunch-crossing parity. b) Distribution of the time reference uncertainty. The red line represents the cut of 4 ns.

263 5.5 Time offset correction

264 The time reference of the trigger is delayed compared to the muon passing through the detector
 265 because of the length of cables and the trigger electronics logic. Therefore, the time offset of the
 266 time reference is determined from data. The physical process induced by muons is instantaneous,
 267 therefore the difference of the hit time and the time reference for each channel, memory cell and
 268 BXID should be a distribution that is centered at 0 ns.

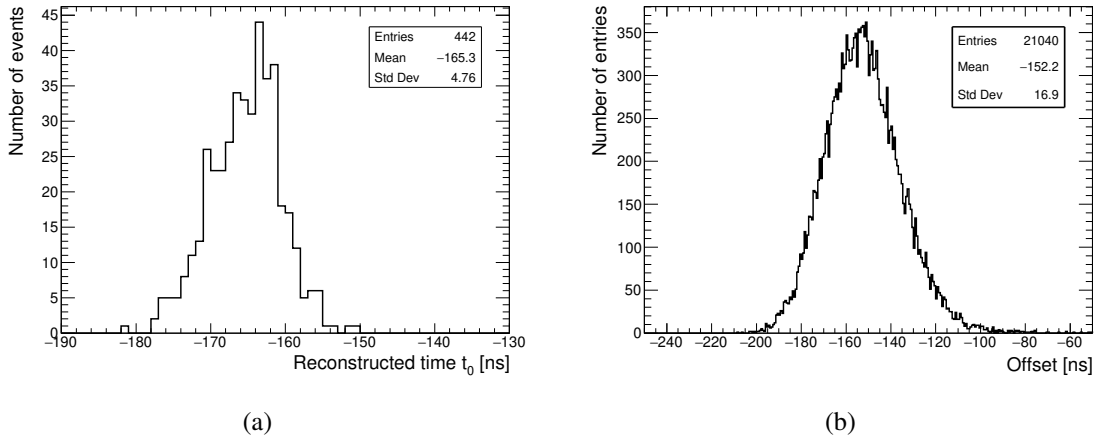


Figure 8: a) Reconstructed time t_0 for a single channel (Chip 236, Chn 21, Mem 01, BXID 1) before correcting for the time offset. An offset of -165.3 ns is determined for this channel. b) Distribution of the time offsets extracted for all chips, channels, memory cells and bunch-crossing. The mean value is around the expected value of -150 ns considering cable length and trigger logic electronics.

269 A procedure has been developed that takes into account delays due to signal propagation and

270 differences in channel pedestals. Only memory-cells containing more than 100 events are consid-
 271 ered. The histogram interval $t_{max} \pm RMS$ where t_{max} corresponds to the time at the center of the
 272 maximum bin, is reduced iteratively, until the RMS of the distribution is smaller than 10 ns. This
 273 value corresponds to more than 3 sigmas of the time reference uncertainty. The mean of the his-
 274 togram is then used as the time offset value. An example of a single channel is shown in figure
 275 8a.

276 In total, 21040 individual offsets are extracted from data. The mean value of the time offset
 277 for all channels is around -150 ns (see figure 8b). This is around the expected value considering
 278 the cabling length and the trigger logic delay. This procedure also corrects for the time of flight of
 279 particles within the detector.

280 5.6 Non-linearity correction

281 The time calibration relies on the linearity of the TDC voltage ramp in the *SPIROC2B*. However,
 282 this assumption is not entirely reliable as shown in subsection 5.4. The voltage slope shows a slight
 283 kink around the middle thus leading to a non-linear ramp. For this, a correction is applied. By
 284 investigating the time t_1 for each chip and BXID parity as a function of the TDC value of the hit,
 285 the shape of the graph indicates how reliable is the assumption of a linear ramp. If the ramp would
 286 be perfectly linear, one would obtain a flat graph. To correct for the non-linearity of the ramp, a 2nd
 287 order polynomial is used. An example of a typical chip is shown in figure 9a. The time resolution
 288 before and after the non-linearity correction are compared in figure 9b, showing an improvement
 289 by about 5%.

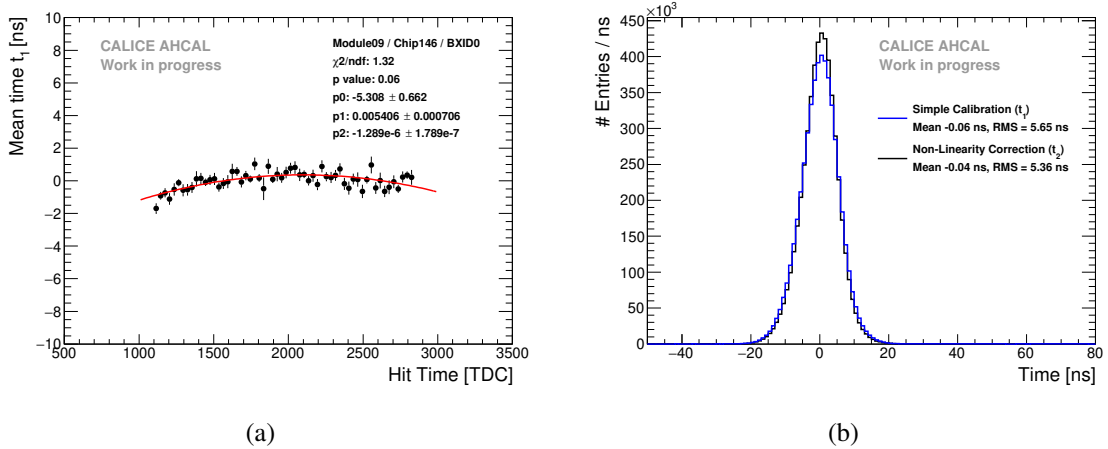


Figure 9: a) Dependence of the mean time t_1 as a function of the raw hit time in TDC units for chip 146 (BXID even) on layer 9. The quadratic fit is slightly curved showing that this chip presents a non-linear TDC ramp. b) Time distribution before (t_1) and after (t_2) the non-linearity correction.

290 5.7 Time-walk correction

291 The time-walk effect is due to the presence of an energy threshold that induces a time shift between
 292 a small amplitude signal and a high amplitude signal. Small amplitude signals will systematically
 293 trigger at a later time than high amplitude signals for a shaper that makes the signals peak at the

294 same time. A time correction $f(E_{hit})$ is determined by looking at the time of the first hit as a
 295 function of the amplitude of the hit as shown in figure 10a. The correction is then applied to the
 296 each hit in the data such as: $t_3 = t_2 - f(E_{hit})$. This may be particularly relevant for late energy
 297 depositions in hadron showers that comes generally from neutrons depositing little energy in the
 298 calorimeter. An improvement of around 3% is achieved on the time resolution of the AHCAL as
 299 shown in figure 10b.

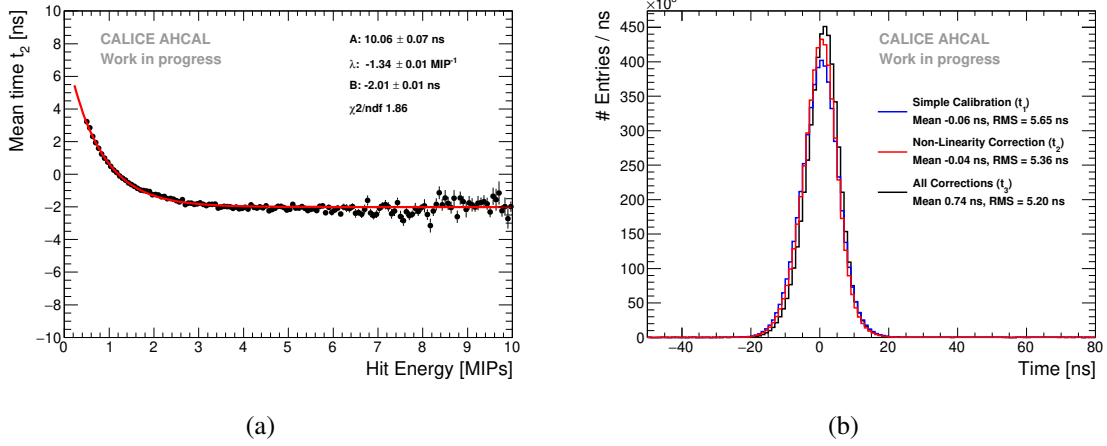
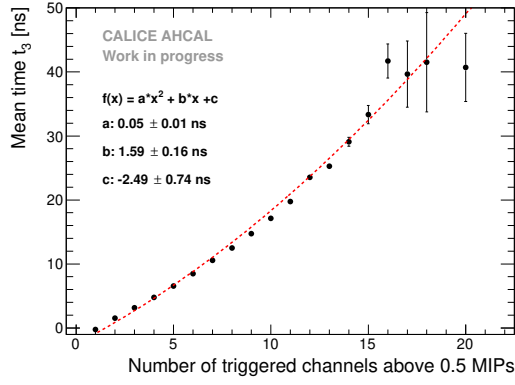


Figure 10: a) t_2 as a function of the hit energy. A difference up to 6 ns is seen between small and large amplitudes. Time-walk correction extracted from data. The fit function is of the form $f(E_{hit}) = A \times e^{-\lambda E_{hit}} + B$, where A is a normalization constant in ns, λ a decay constant in MIP $^{-1}$ and B a time offset in ns. b) Time distribution before (t_1 and t_2) and after (t_3) the time-walk correction. The correction results in an improvement of around 3% on the RMS of the distribution.

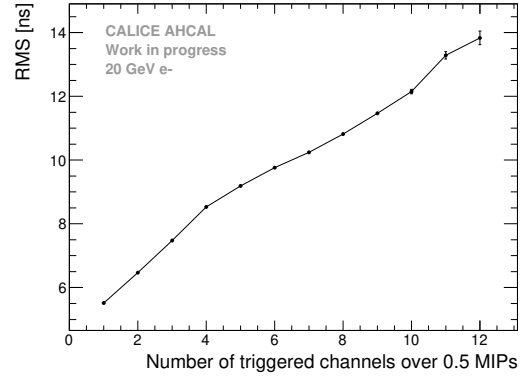
300 5.8 Triggered channel occupancy correction

301 After the time calibration, electrons show a significantly worse time resolution than muons. This
 302 was traced back to events in which many channels are triggered in the same chip. The mean time
 303 t_3 as a function of the number of triggered channels above 0.5 MIP in a chip, $N_{trig/chip}$, is shown
 304 in figure 11a. A time shift of up to 20-40 ns can be seen depending on $N_{trig/chip}$. The cause of the
 305 observed effect is most likely due to an element in the chip called a *delay box* that gets unstable
 306 with a high charge going through the chip. This chip element is responsible for the hold signal of
 307 the TDC ramp in the chip. The hold signal is delayed, and thus a higher TDC ramp value than the
 308 one expected is sampled.

309 This effect not only shifts the mean time t_3 but as well it increases the RMS of the time
 310 distribution as shown in figure 11b for 20 GeV electrons. In order to determine a reliable time
 311 correction, the time correction parameters are determined by combining all the electron data. This
 312 effect may be chip-dependent and the parameters for the correction may differ from chip to chip.
 313 However, the limited amount of data does not allow to determine a correction function for each
 314 chip. In addition, the layers deeper in the calorimeter, which are most interesting for the pion
 315 analysis, are not reached by electrons. Therefore, a global function is used to correct the time in
 316 the data. This effect is parametrized in simulation as explained in section 3.1.



(a)



(b)

Figure 11: a) Mean time t_3 as a function of the number of triggered channels above 0.5 MIP, $N_{trig/chip}$, in a chip. The mean time shift upwards with the increase of triggers leading to large tails in the time distribution. A second order polynomial fit is applied for the time correction shown by the red dashed line. b) RMS of the time distribution for 20 GeV electrons as a function of $N_{trig/chip}$.

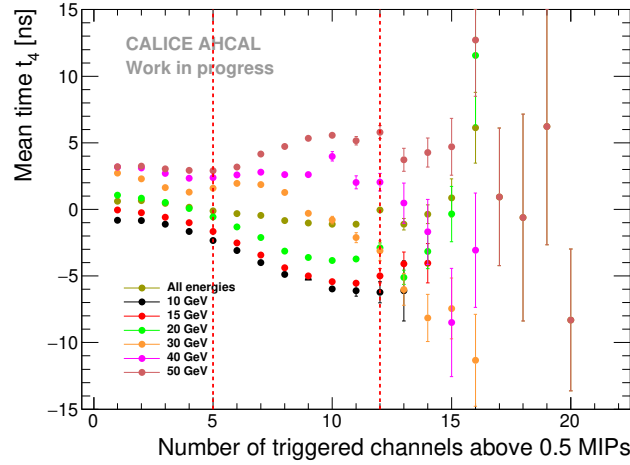


Figure 12: Residuals of the mean time t_4 as a function of the number of triggered channels above 0.5 MIP in a chip after correction. The correction has been applied to all electron samples separately to evaluate the systematic uncertainty. The vertical red lines delimit the three sections used for the systematic uncertainty.

Figure 12 shows the residuals of the mean time t_4 as a function of $N_{trig/chip}$ after the correction. The correction has been applied to all electron samples separately in order to evaluate the systematic uncertainty of the correction. Three ranges in $N_{trig/chip}$ have been defined to estimate the uncertainty. Half of the residual envelope is taken as uncertainty. For $0 < N_{trig/chip} < 5$, a systematic uncertainty of 2 ns is taken, For $5 \leq N_{trig/chip} < 12$, a systematic uncertainty of 5 ns is taken and finally for $N_{trig/chip} \geq 12$, a systematic of 7 ns is taken.

6. Results

6.1 Systematic uncertainties

Systematic uncertainties are evaluated in order to perform a significant assessment of differences observed between data and simulations. The following sources of systematic uncertainty are taken into account for data:

- **Non-Linearity correction:** A correction for the non-linearity of the TDC ramps is determined from data with a limited accuracy, leading to a systematic uncertainty. The residuals of the correction give a systematic uncertainty at the level of 0.2 ns.
- **Time walk correction:** Similarly to the non-linearity correction, the systematic uncertainty obtained from the residuals of the time walk correction in data is in the order of 0.2 ns.
- **Number of triggered channels correction:** The correction in data for $N_{trig/chip}$ results in a residual on the mean time of the first hit as shown in section 5.8. The uncertainty for the mean time of the hit is computed *for each bin of hit energy and hit radius* by weighting according to the fraction of hits in each of the three regions following equation 6.1. As the uncertainties in the three ranges are correlated, a conservative way is to add linearly the uncertainties.

$$\sigma = n_1 \times \sigma_1 + n_2 \times \sigma_2 + n_3 \times \sigma_3 \quad (6.1)$$

with $\sigma_1 = 2$ ns, $\sigma_2 = 5$ ns, $\sigma_3 = 7$ ns, n_1 the fraction of hits for the i -th bin in the region $0 < N_{trig/chip} < 5$, n_2 the fraction of hits for the i -th bin in the region $5 \leq N_{trig/chip} < 12$ and n_3 the fraction of hits for the i -th bin in the region $N_{trig/chip} \geq 12$ and such as $n_1 + n_2 + n_3$ is equal to one in the i -th bin. The resulting systematic uncertainty varies between 2 to 3.9 ns. For the time of first hit distribution, a systematic uncertainty is applied bin-by-bin for electrons and pions in the region of -30 ns to 30 ns. Outside of this region, a systematic error of 50% is taken. This systematic uncertainty is the most dominant over all other uncertainties.

- **AHCAL energy scale:** The energy scale of the AHCAL was determined using the muon dataset. A systematic uncertainty on the MIP scale of around 3.6% was derived by dividing the muon sample in odd and even run numbers and by looking at the average spread of the fitted MIP value for both subsamples. This is converted to an uncertainty in time using the mean time of the first hit as a function of the hit energy using the QGSP_BERT_HP physics list. At 0.5 MIP, this results in an uncertainty of 0.1 ns. For hits above 1 MIP, the uncertainty is below 0.05 ns.

The following systematic uncertainties are taken into account for the simulation:

- **Global time smearing parameters:** A global time smearing parametrization is determined from muon data and is used to smear the time in the simulation. A bin-by-bin systematic uncertainty is applied to the time of first hit distribution in simulation to take into account the difference with a layer-wise time smearing parametrization.

- Time smearing as a function of $N_{trig/chip}$: A smearing parametrization of the width of the time distribution as a function of $N_{trig/chip}$ is obtained from electron data. An error band on the width was obtained by comparing all electron energies. The minimum and maximum borders of the error band are used to derive a systematic uncertainty for the simulation.
- Determination of the offset to $t = 0$: For simulation, the time shift per layer is calculated using a time of flight correction $T_{of} = \frac{z_{layer}}{c}$ with c the speed of light and z_{layer} the z position of a layer. For this, an uncertainty of 3 mm corresponding to the scintillator thickness is taken in z corresponding to 0.01 ns uncertainty in timing.
- Cross-talk: No measurement for optical cross-talk between tiles is available. From previous measurements with the AHCAL physics prototype, the cross-talk value varies between 10% and 18%. The cross-talk value induces a different number of hits in the detector thus has an impact on the width of the time of first hit distribution. The variation of this parameter in the simulation for the modules 4 to 10 is used for systematics.
- Normalisation of the pion dataset: When comparing the number of hits per time bin between data and simulation, there is an uncertainty related to the number of true pion events in the dataset. This number is perfectly known for simulation, however in data, an uncertainty is present due to some possible contamination from multi-particle events after the selection. The cluster time rejection method (see section 4.3) rejects up to 1% of events in the data. A conservative uncertainty of 10% on the data normalization is assigned when comparing data to simulation for the absolute time of first hit distribution of pions.

The systematic uncertainties are added in quadrature for the full systematic uncertainty assuming no correlation between uncertainties. For the mean time of the first hit as a function of the hit energy and as a function of the hit distance to the shower center of gravity, the systematic uncertainty amounts to 0.3 ns for muons and between 2 to 4 ns for electrons and pions. Table 4 summarizes the systematic uncertainties used in the analysis.

6.2 Timing of muon and electron beams

The comparison of the time of first hit distribution for muons between data and simulations is shown in figure 13. The comparison shows that in the range of -20 ns to 20 ns, data and simulation agree well within the uncertainties. In this range the smearing with a double-Gaussian in the simulation describes the data well. However, outside this range, the simulation underestimates the tails. This is probably caused by the noise implementation in simulation that does not perfectly reproduce the data. The time of the first hit distribution has been checked layer-by-layer and compared to simulations. Similarly, the agreement between data and simulations is best in the range of -20 ns to 20 ns and the tails are not perfectly reproduced in simulation.

In order to further validate the time simulation, a comparison with electron data has been done. Figure 14a shows the comparison of the time of first hit distribution for 50 GeV electrons in data and simulation. The simulation is slightly wider than the data. This is caused by the simulation having more hits in a chip than data which can be seen in figure 14b. The simulation lies above the data in the region of 10 to 14 hits per chip. Overall, the simulation describes well the data within

Table 4: Summary of systematic uncertainties.

Uncertainty source	Full uncertainty
Non-linearity correction	0.2 ns
Time-walk correction	0.2 ns
Number of triggered channels correction	2 - 3.9 ns (mean) 1.2 - 2 (RMS) / bin-wise (e/π)
Energy Scale	0.05-0.1 ns
Time of flight offset	0.01 ns (MC)
Cross-talk parameter	10-18% (MC)
Global time smearing parameters	bin-wise (MC)
Number of triggered channels in a chip parametrization	bin-wise (MC)
Multi-particle events	10% (π)
Resulting systematic uncertainties per distribution	
data-MC ToFH distribution (figures 13 to 15b)	bin-wise (e) - bin-wise + 10% (π)
data-MC vs hit energy (figure 16)	0.3 ns (μ) - 2 to 4 ns (e/π)
data-MC vs hit distance to shower CoG (figures 17a to ??)	0.3 ns (μ) - 2 to 4 ns (e/π)

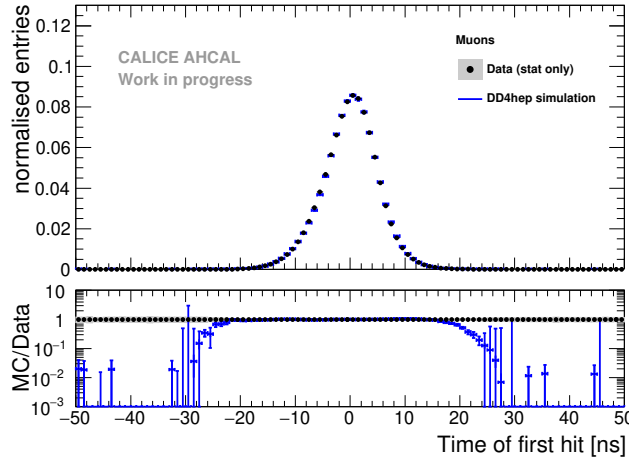
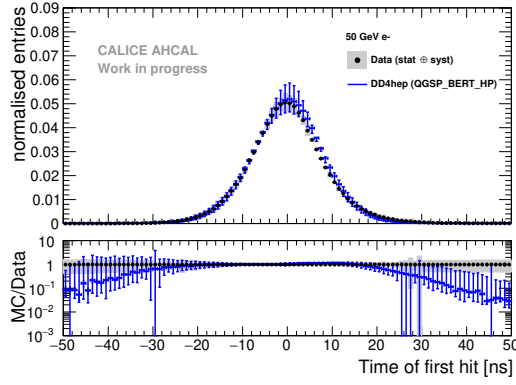


Figure 13: Time of first hit distribution for muons in data and the DD4HEP simulation between -50 and 50 ns. The grey area represents the statistical uncertainty of the data. The error bars of the simulation are obtained by varying the cross-talk parameter between 10% and 18% and taking into account the error of a global time smearing parametrization.

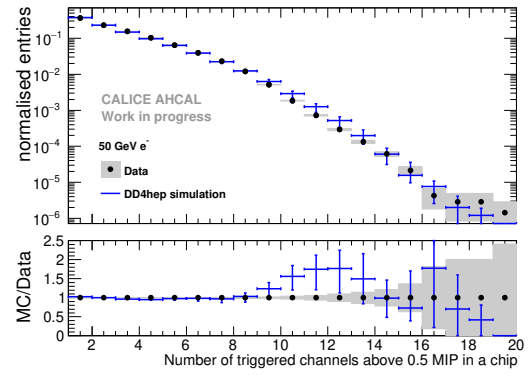
397 statistical and systematic uncertainties in the central region of -30 ns to 30 ns for all energies. The
398 large error bars in the simulation are due to the parametrization of the increase of the width as a
399 function of the number of triggered channels in a chip. However, the description of the tails of the
400 time of the first hit distribution in the simulation is underestimated. Like for muons, this is due to
401 the description of the noise in the simulation that is not perfectly reproduced.

402 6.3 Timing of pion showers

403 Figure 15a shows the time of first hit for muons, 10 GeV electrons and 50 GeV pions. The muon



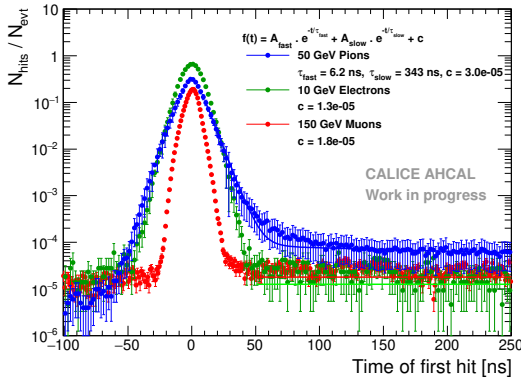
(a)



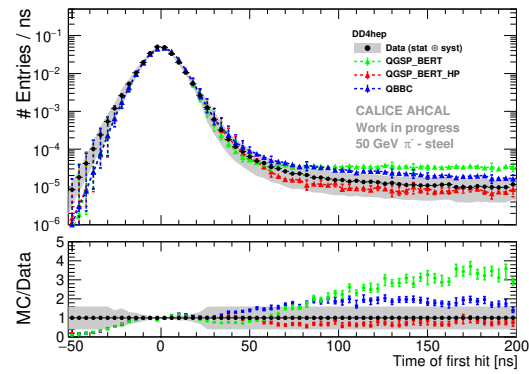
(b)

Figure 14: a) Comparison of the time of first hit between data and the DD4HEP simulation for 50 GeV electrons. The grey area represents the statistical and systematical error of the data. Error bars in simulation are obtained by varying the cross-talk parameter between 10% and 18% and with the uncertainty on parametrization of the width of the time distribution as a function of the number of triggered channels in a chip. b) Comparison of the number of triggered channels per chip between data and simulations for 50 GeV electrons. The grey area represents the statistical error of the data. Error bars in simulation are obtained by varying the cross-talk parameter between 10% and 18%.

404 and electron distributions are centered around 0 ns within a certain time window that is determined
 405 by the intrinsic time resolution of the detector. Isolated hits are present in the tails most likely
 406 caused by SiPM thermal noise.



(a)



(b)

Figure 15: a) Time of first hit for muons, electrons and pions in steel absorber in a range of -100 to 250 ns. The histograms are normalized to the number of events where at least one hit was identified. The errors bars are statistical and systematic uncertainties. The lines represent the fit to the data as explained in the text. b) Comparison of the time of first hit distribution for 50 GeV pions in data and three different physics list for the DD4HEP simulation. The grey and color bands shows the statistical and systematic uncertainties.

The noise level is similar on the left side of the time distribution for muons, electrons and pions giving confidence that the right tail observed between 30 to 50 ns in the pion data is coming from physics and not noise. In the pion data, there is a fast shower component τ_{fast} contributing at times between 10 to 50 ns which changes into a slow shower component τ_{slow} (at around 50 ns). Similarly to the T3B experiment [17], a simple model is used to evaluate the physics processes consisting of the sum of two exponential decays and a constant c ,

$$\frac{1}{N_{evt}} \frac{dN}{dt} = A_{fast} \cdot e^{\frac{-t}{\tau_{fast}}} + A_{slow} \cdot e^{\frac{-t}{\tau_{slow}}} + c$$

where N is the number of hits, N_{evt} the total number of events and A_{fast} and A_{slow} are the amplitudes of the fast and slow component, respectively.

A fast component of 6.21 ± 0.30 ns and a slow component of 343 ± 39 ns are fitted. The time constant of the fast component is in the same order of magnitude as given by the T3B experiment (8 ns). However, due to the time resolution of the AHCAL being in the same order of magnitude, it is difficult to confirm the observation made by T3B. The time constant of the slow component is very different than in the T3B experiment (around 80 ns in steel). It may be due to the contribution of SiPM noise that reduces the sensitivity to the slow component of the shower, and the contribution of multi-particle events. The model may be incomplete as the fitting function does not match well the data in the transition region of 50 to 100 ns but is still within the uncertainties.

Figure 15b shows the distribution of the time of the first hit compared to three different physics lists for 50 GeV pions. For the core of the distribution below 50 ns, all physics lists describe the data within the systematics. The late tail is described best by the QGSP_BERT_HP and QBBC physics lists. The QGSP_BERT physics list without the precision treatment of neutron results in an overestimation of the tail of the distribution by around a factor of 3-4.

The dependence of the time of the first hit on the hit energy is studied in the following. It is expected that there is no hit energy dependence for muon and electron beams. On the other hand, for pions, it is expected that low energy hits mostly coming from neutron signals in the calorimeter are delayed. Figure 16 shows the comparison of the mean time of first hit as a function of the hit energy in data and simulation for 50 GeV pions.

In general, data and all simulations show a rise of the mean time of the first hit towards small hit energies, although the large systematic uncertainties on the data make a firm statement difficult. This behavior is consistent with the expectation that low energy hits are responsible for delayed energy depositions in the calorimeter, most likely due to low energy neutrons from capture and spallation processes, while higher energy deposits occur mostly in the prompt part of the hadron shower. The rise in data is located at hit energies below 1 MIP, while it extends up to 4 MIP in the simulation. A difference is visible between the physics lists mainly between hit energies of 1-3 MIPs, where QGSP_BERT_HP lies below QGSP_BERT and QBBC. In this range, and at higher MIP values, all physics lists agree within the large systematic uncertainties with the data.

The prompt component of a hadron shower is dominated by EM sub-showers and relativistic particles, whereas the delayed component is coming from mostly evaporation and spallation low energy neutrons. It is expected that the former is concentrated near the shower axis, while the latter is spread out laterally as these neutrons can travel far away in the calorimeter before interacting. Therefore, the radial dependence of the time of the first hit of 50 GeV pion showers is studied.

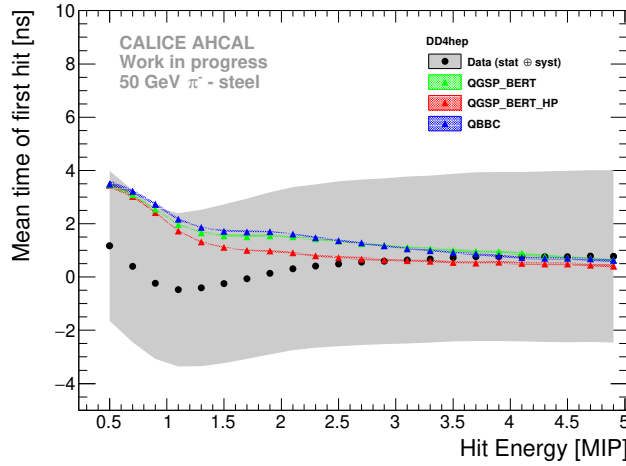


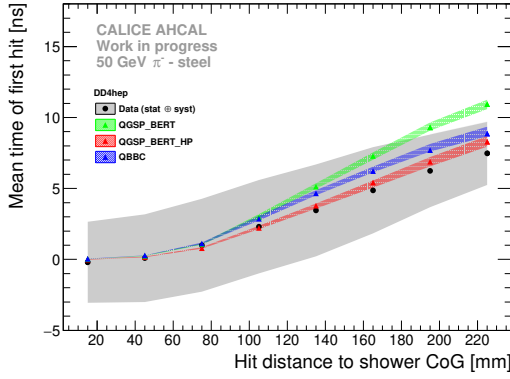
Figure 16: Comparison of the mean time of first hit as a function of the hit energy in data and DD4HEP simulation for 50 GeV pions. The grey and color bands shows the statistical and systematic uncertainties.

It is studied separately for modules 3 to 10 (small modules) and modules 11 to 14 (big modules) as significant differences were found (figure 17). Both distributions show an increase of the mean time of the first hit with the distance to the shower center, but the effect is larger for the small modules, where the mean time of the first hit is around 8 ns at 22 cm, while the large modules show an effect of less than 4 ns at the same distance. For the modules 3 to 10, the QBBC and QGSP_BERT_HP physics lists reproduce well the data within systematics while QGSP_BERT lies above the data at large distances from the center-of-gravity of the shower. For the modules 11 to 14, the QGSP_BERT_HP physics list agrees the best with the data. The QBBC and QGSP_BERT physics lists agree with data up to around 10 cm distance and then both tend to lie above the data for higher distances. The observations for other beam energies are similar. The main difference between the QGSP_BERT_HP and the QGSP_BERT physics list is the detailed neutron tracking in QGSP_BERT_HP. The figures show that without this detailed neutron tracking, too many late energy depositions are created that are spread far away from the shower axis.

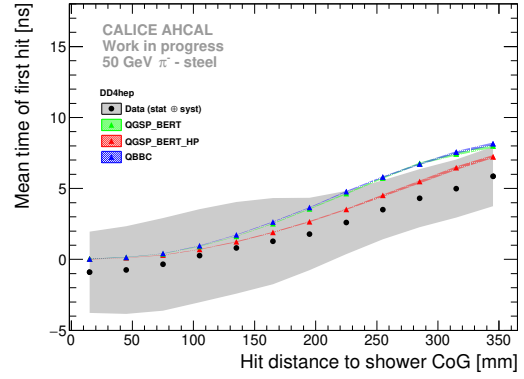
7. Conclusion

In this note, a timing study of hadronic showers with the CALICE AHCAL prototype was presented, using the data taken with steel absorber at the CERN SPS in July 2015 in muon, electron and pion beams between 10 and 90 GeV. This prototype was partially instrumented with several generations of active readout boards which do not reach the final design performance. It was operated at a lower clock speed in order to have a good efficiency in the data taking. Nevertheless, the data collected has been used to develop calibration and correction procedures, to study systematic effects and understand the simulations that reproduce the data and allow for meaningful comparisons with hadron showers.

Firstly, the timing calibration was presented. A time resolution of around 5 ns was achieved with muons and around 8 ns with electrons. The increase of the time resolution for electrons is due



(a) Layers 3 to 10



(b) Layers 11 to 14

Figure 17: Comparison of the time of first hit as a function of the hit distance to the shower axis in data and simulations for 50 GeV pion for the modules 3 to 10 on the left and for modules 11 to 14 on the right. The grey and color bands shows the statistical and systematic uncertainties.

to an electronic effect that increases the time resolution depending on the number of hits within a chip.

Secondly, the study of the time development of pion showers was presented. The late contributions are predominant at a larger radius from the core of the shower and they are consistent with low hit energies below 1 MIP. Comparisons to simulations show that the time structure of pion showers is well reproduced by the GEANT 4 physics lists QGSP_BERT_HP and QBBC. The QGSP_BERT physics list tends to over-estimate the late contribution, showing that a proper treatment of neutrons is needed to reproduce the data to a satisfactory level.

The time resolution obtained in testbeam does not reflect the time resolution that would be obtained in a linear collider scenario. The clock period would be increased from 250 kHz to 5 MHz ($4\mu\text{s}$ to 200 ns, otherwise a running mode called *ILC mode*). This would, theoretically, enable to achieve a single channel time resolution around 150 ps. Further testbeams are planned in order to evaluate the timing performance in ILC mode. Furthermore, many of the short comings in this analysis are related to the hardware poor performance. A better revision of the front-end electronics, especially a redesign of the timing measurement, would have a large impact on the timing performance of the detector. As well, the operation of the detector using similar layers (i.e same front-end revision, same SiPM type...) would facilitate the energy and timing calibration. This has already been demonstrated in a recent large prototype with 22k channels [18].

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Table A1: List of runs taken at SPS in July 2015. The quoted number of events includes not only physics events but also single noise hit events.

Particle	Energy	Runs	# Events
μ^-	50 GeV	24016-24204	120,887,651
	150 GeV	24623-24662	15,534,328
e^-	10 GeV	24531-24576	38,028,438
	15 GeV	24507-24527	7,701,325
	20 GeV	24479-24504	10,498,554
	30 GeV	24454-24475	3,382,943
	40 GeV	24420-24448	2,665,843
	50 GeV	24404-24419	5,933,995
π^-	10 GeV	24266-24272, 24300-24317, 24381-24397	24,311,420
	20 GeV	24398-24400	N/A*
	30 GeV	24259-24299, 24319-24380	10,120,753
	50 GeV	24212-24254, 24325-24357, 24580-24612	10,704,661
	70 GeV	24219-24242, 24365-24374	8,885,407
	90 GeV	24233-24287, 24331-24364	7,955,604

Table A2: List of the different SiPMs used in the CALICE AHCAL in July 2015.

Layer	Producer	Model	Area (mm ²)	Pitch (μ m)	WLS Fibre	Read-out type	N_{px} [10^3]
1	Hamamatsu	S12571_010P	1×1	10	no	Bottom	10
2	Hamamatsu	S10362-11-025O	1×1	25	no	Side	1.6
3	Hamamatsu	S12571-025P	1×1	25	no	SMD	1.6
4-5	Ketek	N/A	2.25×2.25	18	no	Side	12
6-10	CPTA	CPTA	1.28×1.28	40	yes	Side	0.8
11-12	Ketek (UHH)	PM1125NS-SB0	1.2×1.2	25	no	Side	2.3
13-14	SenSL	MicroFB-10020-SMT	1×1	20	no	Side	1.3

*Not analyzed due to limited dataset.

Table A3: List of AHCAL channels used as time reference for this analysis. In this analysis, the time reference signals are defined as T_{11} , T_{12} , T_{13} and T_{14} representing the reference channels on Modules 11, 12, 13 and 14 respectively. In this analysis, T_{12} , T_{13} and T_{14} only are used.

Layer #	Chip Number	Channel	Comments	Name
11	169	29	noisy	T_{11}
11	177	23	broken	-
12	185	29	-	T_{12}
13	201	29	-	T_{13}
13	211	6	broken	-
14	217	23	-	T_{14}

Table A4: Selection cuts for the muon run.

Name	Beam Energy	Cut
Preselection	All	$0 \text{ mm} < cog_z < 800 \text{ mm}$
	All	$0 < n_{hits} < 20$
Track Selection (Modules 1 to 10)	All	n_{hits} in AHCAL tower > 7
	All	n_{hits} in a layer < 3
Track Selection (Modules 11 to 14) outside of inner 12x12 tile area	All	n_{hits} in AHCAL tower > 2
	All	n_{hits} in a layer < 3

Table A5: Selection cuts for each electron run.

Name	Beam Energy	Cut
Event Quality	All	Cherenkov ON
	All	Energy in the first 3 layers of AHCAL ($E_3 + E_4 + E_5$) $> 10 \text{ MIP}$
Electron Selection	10 GeV	$25 < n_{hits} < 75$
	15 GeV	$30 < n_{hits} < 90$
	20 GeV	$40 < n_{hits} < 100$
	30 GeV	$50 < n_{hits} < 110$
	40 GeV	$60 < n_{hits} < 120$
	50 GeV	$70 < n_{hits} < 140$
	All	$cog_z < 250 \text{ mm}$
	All	$-90 \text{ mm} < cog_{x,y} < 90 \text{ mm}$
	All	Energy in last two layers ($E_{13} + E_{14}$) $< 1\% \Sigma E$

Table A6: Selection cuts for the pions run.

Name	Beam Energy	Cut
Event Quality	All	Cherenkov OFF
Pion Selection	All	$n_{hits} > 20$
	All	n_{hits} in the first 2 AHCAL layers $(N_3 + N_4) < 5$
	All	Energy in last two layers $(E_{13} + E_{14}) > 1\% \Sigma E$
Multi Particle Rejection	All	n_{hits} in time window > 5
	All	$n_{Cluster} > 0$