

# Homework 1: Autoregressive Models

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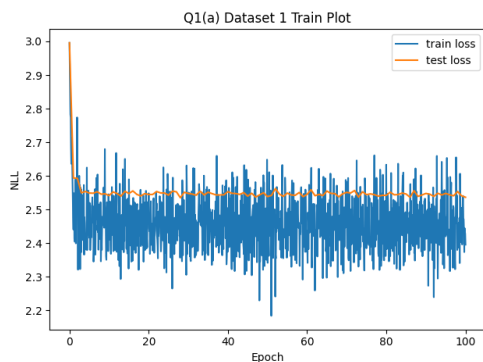
**Deliverable:** This PDF write-up by **Tuesday February 7th, 23:59pm**. Your PDF should be generated by simply replacing the placeholder images of this LaTeX document with the appropriate solution images that will be generated automatically when solving each question. The solution images are automatically generated and saved using the accompanying IPython notebook. Your PDF is to be submitted into Gradescope. This PDF already contains a few solution images. These images will allow you to check your own solution to ensure correctness. Submit this PDF, your iPython notebook, and any other code you wrote to Gradescope!

**Note:** My submission includes this PDF with all the figures and test losses, the iPython notebook I primarily used for prototyping and experimentation, and the `hw1.py` script, which I ran to get final results for most of the questions (mostly question 3 onwards). The notebook has some of the final figures and test losses, while the rest were produced by running the Python script.

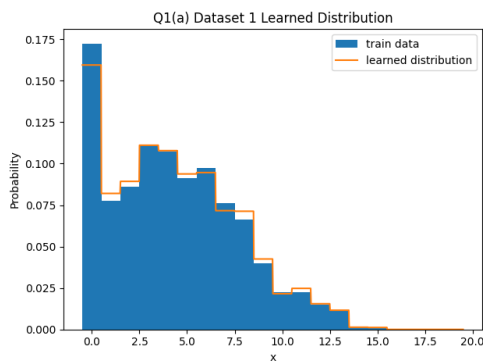
## Question 1: 1D Data

### (a) [10pt] Fitting a Histogram

Final test loss for dataset 1: 2.5365 nats / dim

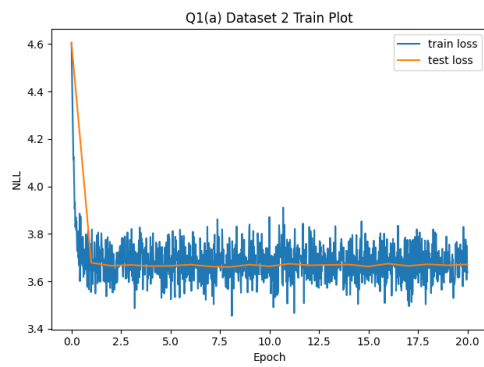


(a) Dataset 1: Training curve

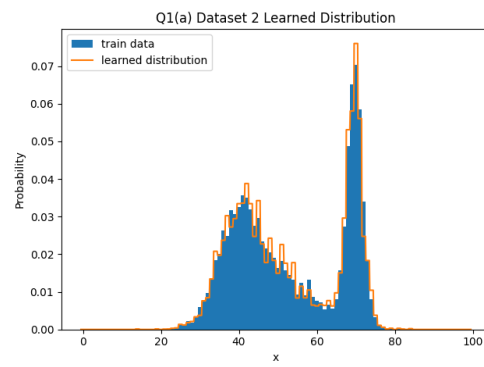


(b) Dataset 1: Learned distribution

Final test loss for dataset 2: 3.6712 nats / dim



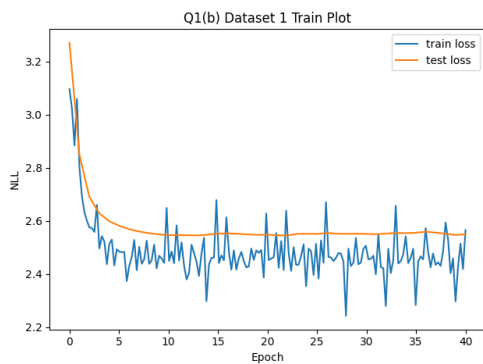
(a) Dataset 2: Training curve



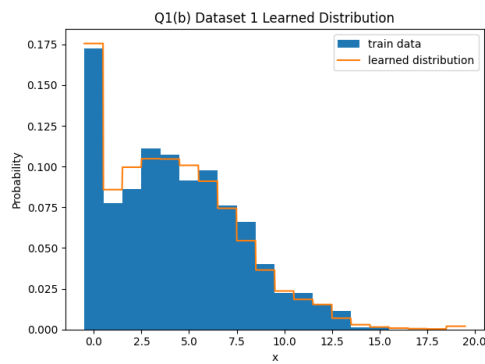
(b) Dataset 2: Learned distribution

**(b) [10pt] Fitting Discretized Mixture of Logistics**

Final test loss for dataset 1: 2.5495 nats / dim

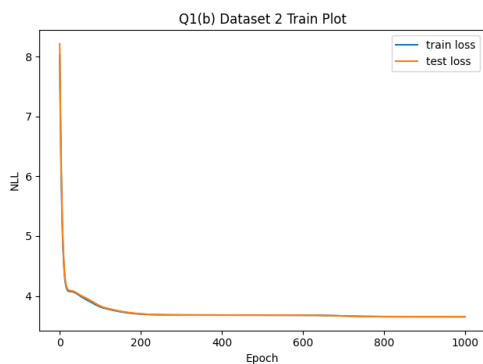


(a) Dataset 1: Training curve

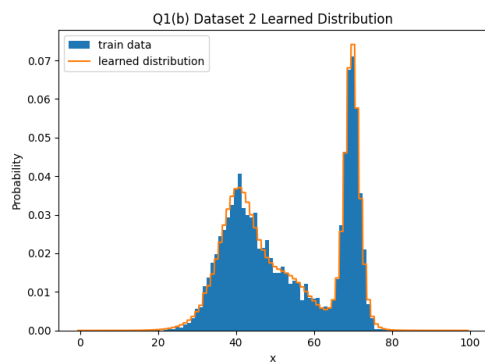


(b) Dataset 1: Learned distribution

Final test loss for dataset 2: 3.6542 nats / dim



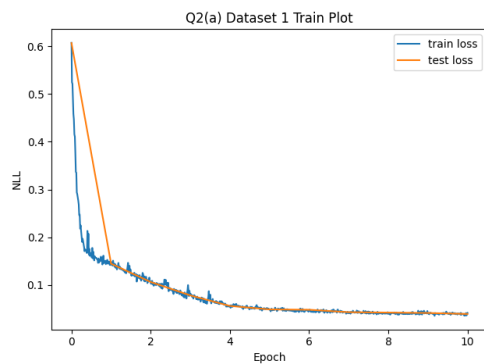
(a) Dataset 2: Training curve



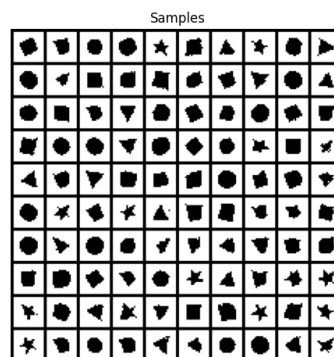
(b) Dataset 2: Learned distribution

**Question 2: PixelCNNs****(a) [15pt] PixelCNNs on Shapes and MNIST**

Final test loss for dataset 1: 0.0396 nats / dim

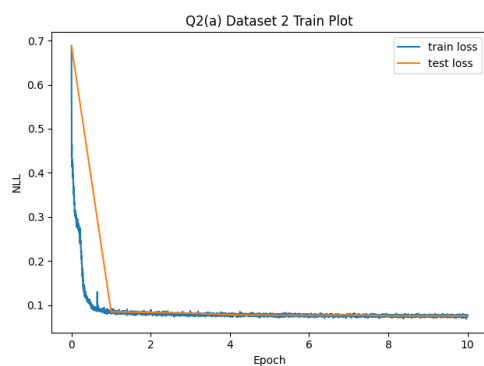


(a) Dataset 1: Training curve

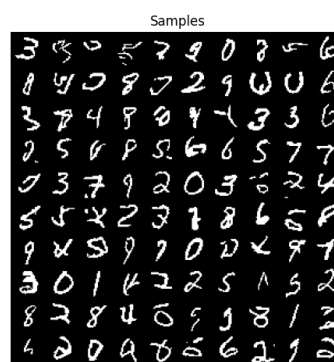


(b) Dataset 1: Samples

Final test loss for dataset 2: 0.0757 nats / dim



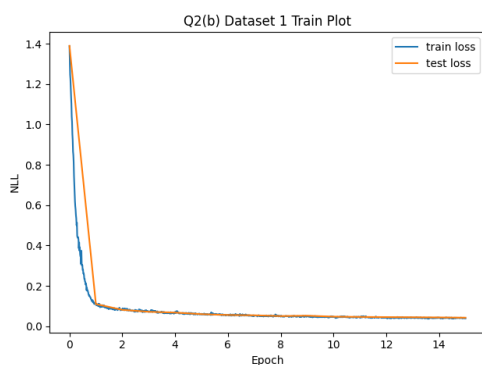
(a) Dataset 2: Training curve



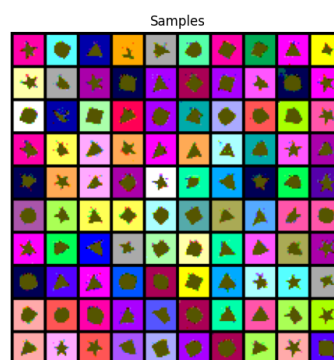
(b) Dataset 2: Samples

## (b) [15pt] PixelCNN on Colored Shapes and MNIST: Independent Color Channels

Final test loss for dataset 1: 0.0425 nats / dim

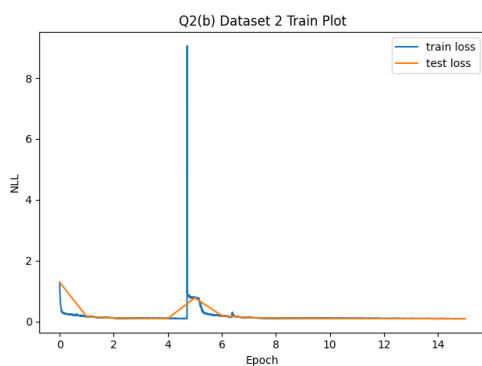


(a) Dataset 1: Training curve

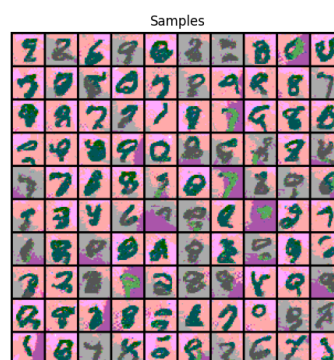


(b) Dataset 1: Samples

Final test loss for dataset 2: 0.0892 nats / dim



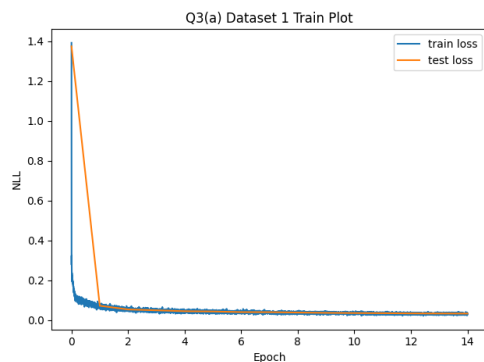
(a) Dataset 2: Training curve



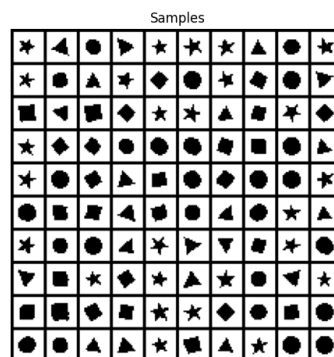
(b) Dataset 2: Samples

**Question 3: Causal Transformer - iGPT****(a) [15pt] Autoregressive Transformer on Shapes and MNIST**

Final test loss for dataset 1: 0.0337 nats / dim

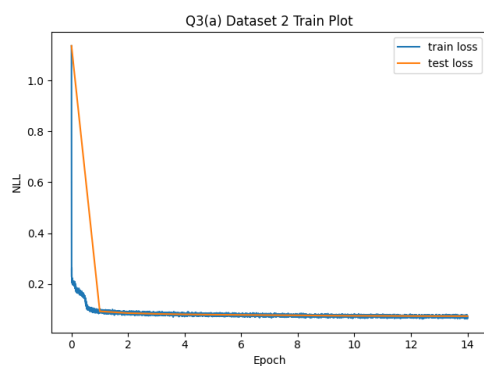


(a) Dataset 1: Training curve

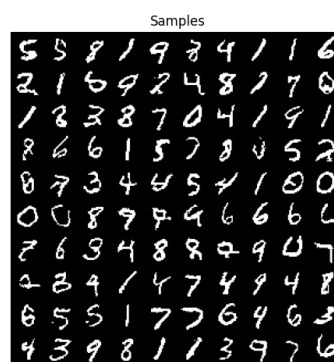


(b) Dataset 1: Samples

Final test loss for dataset 2: 0.0741 nats / dim



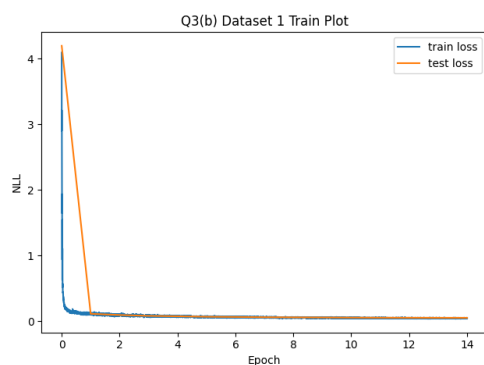
(a) Dataset 2: Training curve



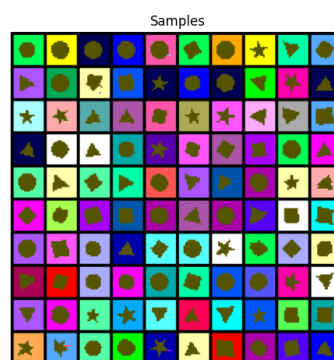
(b) Dataset 2: Samples

## (b) [15pt] Autoregressive Transformer on Colored Shapes and MNIST

Final test loss for dataset 1: 0.0503 nats / dim

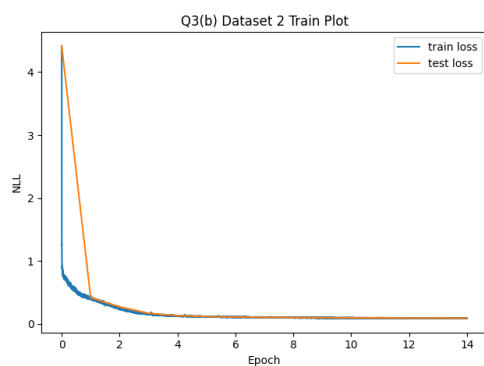


(a) Dataset 1: Training curve



(b) Dataset 1: Samples

Final test loss for dataset 2: 0.0918 nats / dim



(a) Dataset 2: Training curve



(b) Dataset 2: Samples

## (c) [15pt] K,V Caching for Improved Inference

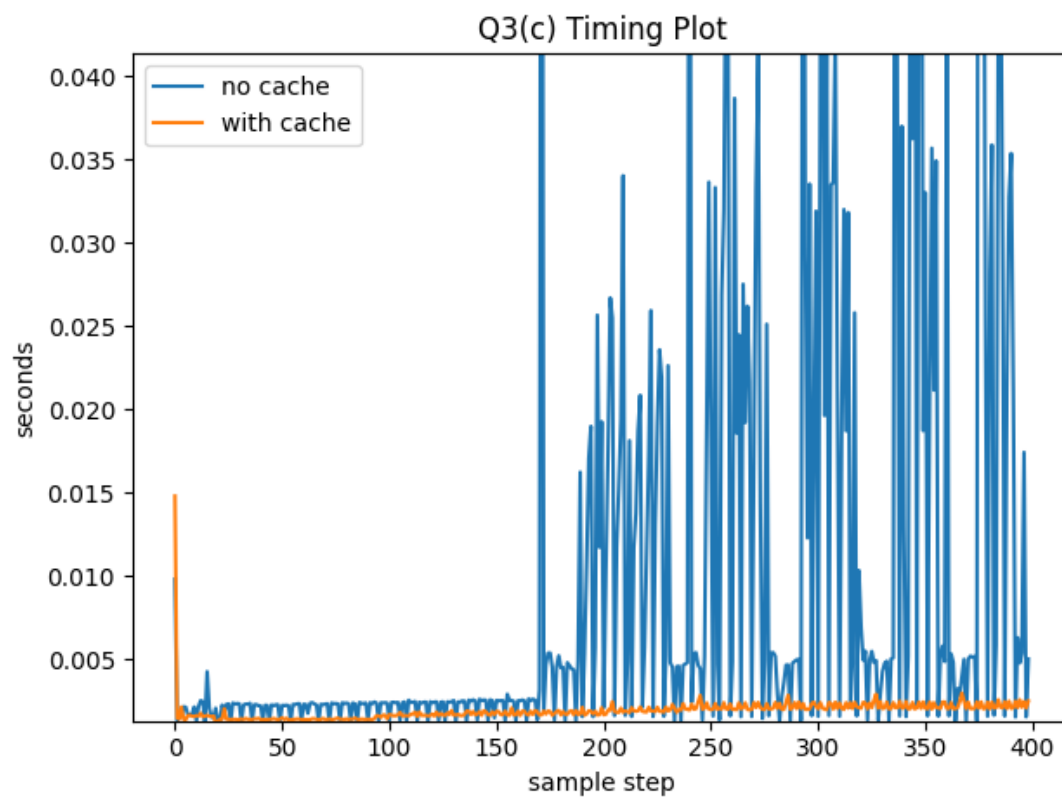
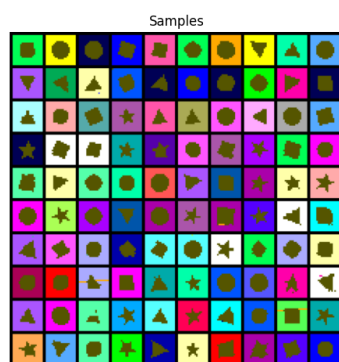
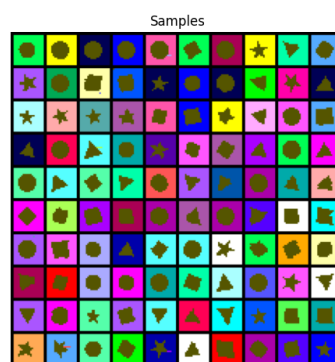


Figure 13: Dataset 2: Inference Speed

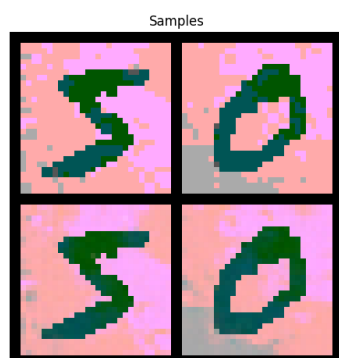


(a) Dataset 2: Samples (no caching)

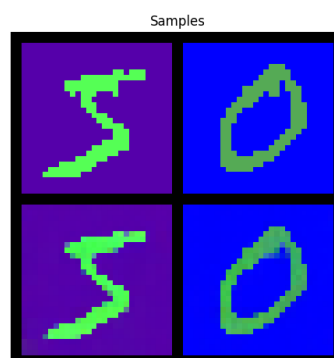


(b) Dataset 2: Samples (caching)



**Question 4: Causal Transformer - Tokenized Images****(a) [5pt] Image Quantization**

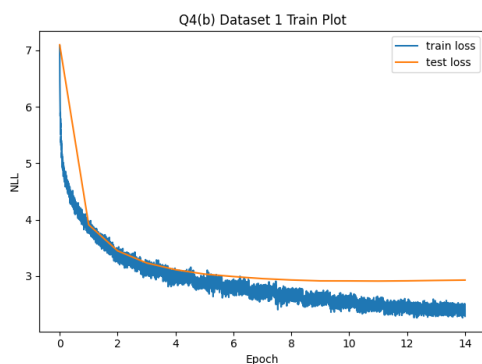
(a) Dataset 1: Quantized Examples



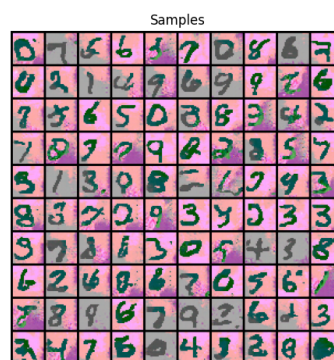
(b) Dataset 2: Quantized Examples

**(b) [15pt] Autoregressive Transformer on Colored Shapes and MNIST with Vector Quantization**

Final test loss for dataset 1: 2.9278 nats / dim

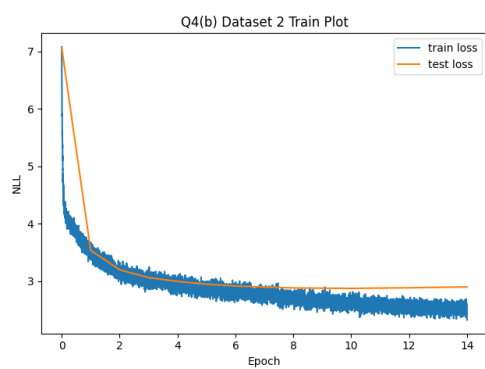


(a) Dataset 1: Training curve

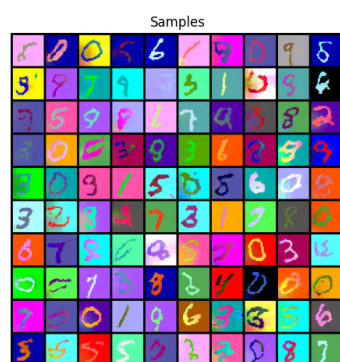


(b) Dataset 1: Samples

Final test loss for dataset 2: 2.9000 nats / dim



(a) Dataset 2: Training curve



(b) Dataset 2: Samples

**Question 5: Causal Transformer - Text****(a) [20pt] Modeling Text**

Final test loss: 1.8461 nats / dim

**Text Samples**

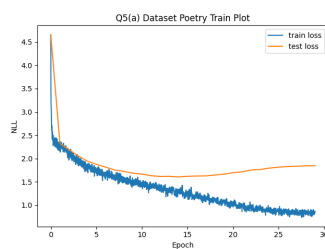
Text Sample 1  
Alas, I come, I my hand all my love.

Text Sample 2  
Orphen S Its it his deeline is to his eye I see  
mortalitous of one any control When Ocean's have  
longing sorrow of forbearth.

Text Sample 3  
Farewed content, many now elpeast, Adieugh thine  
all table bridanches are renneed, And think  
wisher'd wayrds checeefered oft

Text Sample 4  
Shy ender still, sike she worthnd a rooth waste  
With blessed companious, silves, if Ill love  
Not o'clockbird in win

Text Sample 5  
Thou art my winter? I must inferacts their man, But  
plood always not time to sing, for they fight Slow  
I such fair watery and

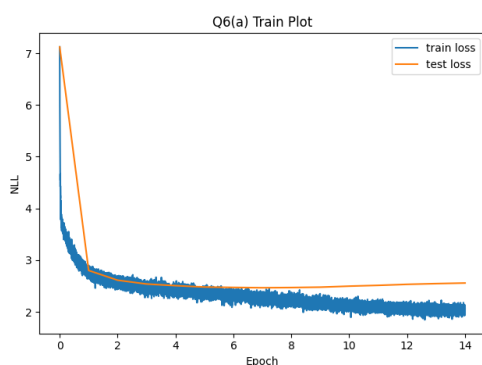


(a) Training curve

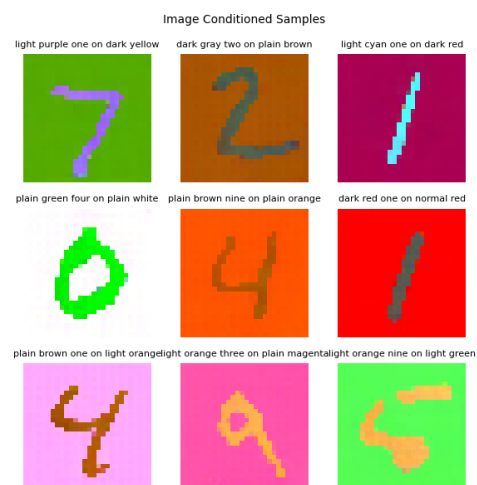
(b) Text samples

**Question 6: Causal Transformer - Multimodal****(a) [20pt] Multimodal Text and Image Generation**

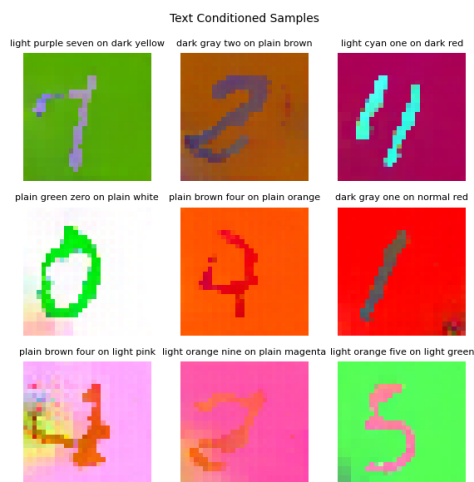
Final test loss: 2.5597 nats / dim



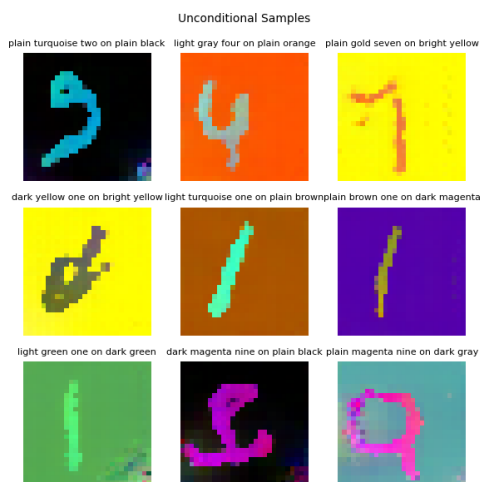
(a) Training curve



(b) Image conditioned samples



(c) Text conditioned samples



(d) Unconditional samples