AMD **Accelerated** Parallel Processing TECHNOLOGY

SAMPLE

Gaussian LU Decomposition

1 Overview

1.1 Location

`$<AMDAPPSDKSamplesInstallPath>\samples\opencl\cl\1.x`

1.2 How to Run

See the *Getting Started* guide for how to build samples. You first must compile the sample.

Use the command line to change to the directory where the executable is located. The default executables are placed in `$<AMDAPPSDKSamplesInstallPath>\samples\opencl\bin\x86` for 32-bit builds and `$<AMDAPPSDKSamplesInstallPath>\samples\opencl\bin\x86_64\` for 64-bit builds.

Type the following command(s).

1. `LUDecomposition`
   This uses the Gaussian LU decomposition algorithm to determine the factorization of a random square matrix, which is the product of a lower triangular matrix and and upper triangular matrix. Default option is x = 16.
2. `LUDecomposition -h`
   This prints the help message.

1.3 Command Line Options

Table 1 lists, and briefly describes, the command line options.

Table 1 Command Line Options

Short Form	Long Form	Description
`-h`	`--help`	Shows all command options and their respective meaning.
	`--device`	Devices on which the program is to be run. Acceptable values are `cpu` or `gpu`.
`-q`	`--quiet`	Quiet mode. Suppresses all text output.
`-e`	`--verify`	Verify results against reference implementation.
`-t`	`--timing`	Print timing.
	`--dump`	Dump binary image for all devices.
	`--load`	Load binary image and execute on device.
	`--flags`	Specify compiler flags to build the kernel.
`-p`	`--platformId`	Select deviceId to be used (0 to N-1, where N is the number of available devices).
`-d`	`--deviceId`	Select deviceId to be used (0 to N-1, where N is the number of available devices).

Short Form	Long Form	Description
-v	--version	AMD APP SDK version string.
-x	--dimension	Actual dimension of input matrix.
-i	--iterations	Number of iterations for kernel execution.

2 Description

The sample calculates LU Decomposition of a random square matrix using basic Gaussian LU Decomposition Algorithm.

Let *A* be a square matrix. An **LU decomposition** is a decomposition of the form

A = ***L U***

where ***L*** and ***U*** are the lower and upper triangular matrices (of the same size), respectively. This means that *L* has only zeros above the diagonal and *U* has only zeros below the diagonal. For a 3X3 matrix it becomes

$$[A] = [L][U] = \begin{bmatrix} 1 & 0 & 0 \\ \ell_{21} & 1 & 0 \\ \ell_{31} & \ell_{32} & 1 \end{bmatrix} \begin{bmatrix} u_{11} & u_{12} & u_{13} \\ 0 & u_{22} & u_{23} \\ 0 & 0 & u_{33} \end{bmatrix}$$

3 Algorithm

The algorithm used is a naïve Gaussian elimination algorithm. It is a recursive algorithm that treats a matrix n-1 times recursively. The algorithm makes all elements in a column below diagonal zero in each successive step.

The operation performed in the k^{th} step makes all elements of the k^{th} column below the diagonal zero using basic matrix algebra.

At the end of n-1 steps, an upper triangular matrix (U) is obtained from the original matrix. The multipliers used in each step are grouped into a lower triangular matrix (L).

4 Implementation Details

The basic requirement of the algorithm is that one step must be completed before starting the next step. To enforce this global behavior each step of the n-1 steps are performed one after other by different calls to the kernel. The matrix need not be transferred each time because of the persistent model of the global memory. So all the kernels modify the same buffer, one after other without the overhead of bringing the data in global buffers again & again. Double is used for better precision and vectorized reads are writes performed for efficiency. In addition LDS is used to store the multipliers for each step which reduced the memory fetches and eliminate redundant calculation.

5 References

- www.cse.illinois.edu/courses/cs554/notes/06_lu.pdf

- http://mathworld.wolfram.com/GaussianElimination.html
- http://www.math-linux.com/spip.php?article51

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