

1. Read in the training data into csr matrix R ;
 2. Read in the testing data into csr matrix T ;
 3. Get k (the latent dimension), λ (the control parameter), maxItrs (the maximum number of iterations allowed) and epsilon (the ratio of objective value change) from the user of your recommender system;
/* learn the factorization model */
 4. Initialize dense factor matrix P and Q (with $1/k$, randomly, or from input)
 5. $t = 0$;
 6. While ($t < \text{maxItrs}$)
 - a. $t++$;
 - b. fix Q and solve for P ; /* $P = \text{LS_closed}(R, P, Q, k, \lambda)$; or $P = \text{LS_gd}(R, P, Q, k, \text{epsilon})$ */
 - c. fix P and solve for Q ; /* $Q = \text{LS_closed}(R^T, Q, P, k, \lambda)$; note: transpose of R ; or $Q = \text{LS_gd}(P^T, Q, P, k, \text{epsilon})$ */
 - d. If $|f(t) - f(t-1)| / f(t-1) < \text{epsilon}$ break; /* $f(t)$ is the value of function f (equation 1 in the optimization sheet) at iteration t */
 7. End
/* generate the recommendations */
 8. $\text{MSE} = 0$; $\text{RMSE} = 0$;
 9. Foreach user u in T
 - a. Foreach item i that u has in T
 - i. $\text{Pred} = P(u, \cdot) * Q(i, \cdot)$; /* dot product */
 - ii. $\text{MSE} += (T(u, i) - \text{pred})^2$;
- $\text{MSE} = \text{MSE} / \text{\# ratings in } T$; /* not # users in T */
- $\text{RMSE} = \text{sqrt}(\text{MSE})$;