Contents

1 Introduction 3 1.1 Introduction to Cryptography 3 1.1.1 Secret-Key Cryptography 3 1.1.2 Public-Key Cryptography 3 1.2 Secure Hardware and Embedded Cryptography 3 1.2.1 The Example of the Smart Card 3 1.2.2 Certification of a Secure Hardware 3 1.2.3 Modern More Complex Devices to Certify 3 1.2.4 Embedded Cryptography Vulnerabilities 3 2 Introduction to Side-Channel Attacks 5 2.1 Introduction to Side-Channel Attacks 6 2.1.1 Historical Overview 6 2.1.2 Terminology and Generalities 6 Target and Leakage Model 6 Points of Interest 6 Simple vs Advanced SCAs 6 Vertical vs Horizontal SCAs 6 Profiled vs Non-Profiled SCAs 6 Side-Channel Algebraic Attacks 6 Distinguishers 6 SCA Metrics 6 2.2 Main Side-Channel Countermeasures 6 2.2.1 Random Delays and Jitter 6 2.2.2 Shuffling 6	Ι	I Context and State of the Art						
1.1.1 Secret-Key Cryptography 3 1.1.2 Public-Key Cryptography 3 1.2 Secure Hardware and Embedded Cryptography 3 1.2.1 The Example of the Smart Card 3 1.2.2 Certification of a Secure Hardware 3 1.2.3 Modern More Complex Devices to Certify 3 1.2.4 Embedded Cryptography Vulnerabilities 3 2 Introduction to Side-Channel Attacks 5 2.1 Introduction to Side-Channel Attacks 5 2.1 Introduction to Side-Channel Attacks 6 2.1.1 Historical Overview 6 2.1.2 Terminology and Generalities 6 Target and Leakage Model 6 Points of Interest 6 Simple vs Advanced SCAs 6 Vertical vs Horizontal SCAs 6 Profiled vs Non-Profiled SCAs 6 Side-Channel Algebraic Attacks 6 Distinguishers 6 SCA Metrics 6 2.2 Main Side-Channel Countermeasures 6 2.2.1 Random Delays and Jitter 6 <	1	Introduction						
1.1.2 Public-Key Cryptography 3 1.2 Secure Hardware and Embedded Cryptography 3 1.2.1 The Example of the Smart Card 3 1.2.2 Certification of a Secure Hardware 3 1.2.3 Modern More Complex Devices to Certify 3 1.2.4 Embedded Cryptography Vulnerabilities 3 2 Introduction to Side-Channel Attacks 5 2.1 Introduction to Side-Channel Attacks 6 2.1.1 Historical Overview 6 2.1.2 Terminology and Generalities 6 Target and Leakage Model 6 Points of Interest 6 Simple vs Advanced SCAs 6 Vertical vs Horizontal SCAs 6 Profiled vs Non-Profiled SCAs 6 Side-Channel Algebraic Attacks 6 Distinguishers 6 SCA Metrics 6 2.2 Main Side-Channel Countermeasures 6 2.2.1 Random Delays and Jitter 6 2.2.2 Shuffling 6 2.2.3 Masking 6 2.3 Higher-Order Attacks 6 2.3.1 Higher-Order Moments Analysis and Combining Functions 6 2.3.2 Profiling Higher-Order Attacks <th></th> <th>1.1</th> <th>Introd</th> <th>uction to Cryptography</th> <th>3</th>		1.1	Introd	uction to Cryptography	3			
1.2 Secure Hardware and Embedded Cryptography 3 1.2.1 The Example of the Smart Card 3 1.2.2 Certification of a Secure Hardware 3 1.2.3 Modern More Complex Devices to Certify 3 1.2.4 Embedded Cryptography Vulnerabilities 3 2 Introduction to Side-Channel Attacks 5 2.1 Introduction to Side-Channel Attacks 6 2.1.1 Historical Overview 6 2.1.2 Terminology and Generalities 6 Target and Leakage Model 6 Points of Interest 6 Simple vs Advanced SCAs 6 Vertical vs Horizontal SCAs 6 Profiled vs Non-Profiled SCAs 6 Side-Channel Algebraic Attacks 6 Distinguishers 6 SCA Metrics 6 2.2 Main Side-Channel Countermeasures 6 2.2.1 Random Delays and Jitter 6 2.2.2 Shuffling 6 2.2.3 Masking 6 2.3 Higher-Order Attacks 6 2.3.1 Higher-Order Moments Analysis and Combining Functions 6 2.3.2 Profiling Higher-Order Attacks 6 2.4 Thesis Contribution and Organ			1.1.1	Secret-Key Cryptography	3			
1.2.1 The Example of the Smart Card 3 1.2.2 Certification of a Secure Hardware 3 1.2.3 Modern More Complex Devices to Certify 3 1.2.4 Embedded Cryptography Vulnerabilities 3 2 Introduction to Side-Channel Attacks 5 2.1 Introduction to Side-Channel Attacks 6 2.1.1 Historical Overview 6 2.1.2 Terminology and Generalities 6 Target and Leakage Model 6 Points of Interest 6 Simple vs Advanced SCAs 6 Vertical vs Horizontal SCAs 6 Profiled vs Non-Profiled SCAs 6 Side-Channel Algebraic Attacks 6 Distinguishers 6 SCA Metrics 6 2.2 Main Side-Channel Countermeasures 6 2.2.1 Random Delays and Jitter 6 2.2.2 Shuffling 6 2.2.3 Masking 6 2.3 Higher-Order Attacks 6 2.3.1 Higher-Order Moments Analysis and Combining Functions 6 2.3.2 Profiling With Masks Knowledge 6 Profiling without Masks Knowledge 6 Profiling without Masks Knowledge			1.1.2	Public-Key Cryptography	3			
1.2.1 The Example of the Smart Card 3 1.2.2 Certification of a Secure Hardware 3 1.2.3 Modern More Complex Devices to Certify 3 1.2.4 Embedded Cryptography Vulnerabilities 3 2 Introduction to Side-Channel Attacks 5 2.1 Introduction to Side-Channel Attacks 6 2.1.1 Historical Overview 6 2.1.2 Terminology and Generalities 6 Target and Leakage Model 6 Points of Interest 6 Simple vs Advanced SCAs 6 Vertical vs Horizontal SCAs 6 Profiled vs Non-Profiled SCAs 6 Side-Channel Algebraic Attacks 6 Distinguishers 6 SCA Metrics 6 2.2 Main Side-Channel Countermeasures 6 2.2.1 Random Delays and Jitter 6 2.2.2 Shuffling 6 2.2.3 Masking 6 2.3 Higher-Order Attacks 6 2.3.1 Higher-Order Moments Analysis and Combining Functions 6 2.3.2 Profiling With Masks Knowledge 6 Profiling without Masks Knowledge 6 Profiling without Masks Knowledge		1.2	Secure	Hardware and Embedded Cryptography	3			
1.2.3 Modern More Complex Devices to Certify 3 1.2.4 Embedded Cryptography Vulnerabilities 3 2 Introduction to Side-Channel Attacks 5 2.1 Introduction to Side-Channel Attacks 6 2.1.1 Historical Overview 6 2.1.2 Terminology and Generalities 6 Target and Leakage Model 6 Points of Interest 6 Simple vs Advanced SCAs 6 Vertical vs Horizontal SCAs 6 Profiled vs Non-Profiled SCAs 6 Side-Channel Algebraic Attacks 6 Distinguishers 6 SCA Metrics 6 2.2 Main Side-Channel Countermeasures 6 2.2.1 Random Delays and Jitter 6 2.2.2 Shuffling 6 2.2.3 Masking 6 2.3.1 Higher-Order Attacks 6 2.3.2 Profiling Higher-Order Attacks 6 Profiling with Masks Knowledge 6 Profiling without Masks Knowledge 6 Profiling without Masks Knowledge 6 <				The Example of the Smart Card	3			
1.2.4 Embedded Cryptography Vulnerabilities 3 2 Introduction to Side-Channel Attacks 5 2.1 Introduction to Side-Channel Attacks 6 2.1.1 Historical Overview 6 2.1.2 Terminology and Generalities 6 Target and Leakage Model 6 Points of Interest 6 Simple vs Advanced SCAs 6 Vertical vs Horizontal SCAs 6 Profiled vs Non-Profiled SCAs 6 Side-Channel Algebraic Attacks 6 Distinguishers 6 SCA Metrics 6 2.2 Main Side-Channel Countermeasures 6 2.2.1 Random Delays and Jitter 6 2.2.2 Shuffling 6 2.2.3 Masking 6 2.3.1 Higher-Order Attacks 6 2.3.2 Profiling Higher-Order Attacks 6 Profiling with Masks Knowledge 6 Profiling without Masks Knowledge 6 Profiling without Masks Knowledge 6 2.4.1 Foreword of this Thesis: Research of Points of Interest 6 2.4.2 Dimensionality Reduction Approach 6			1.2.2	Certification of a Secure Hardware	3			
2 Introduction to Side-Channel Attacks 5 2.1 Introduction to Side-Channel Attacks 6 2.1.1 Historical Overview 6 2.1.2 Terminology and Generalities 6 Target and Leakage Model 6 Points of Interest 6 Simple vs Advanced SCAs 6 Vertical vs Horizontal SCAs 6 Profiled vs Non-Profiled SCAs 6 Side-Channel Algebraic Attacks 6 Distinguishers 6 SCA Metrics 6 2.2 Main Side-Channel Countermeasures 6 2.2.1 Random Delays and Jitter 6 2.2.2 Shuffling 6 2.2.3 Masking 6 2.3.1 Higher-Order Attacks 6 2.3.2 Profiling Higher-Order Attacks 6 Profiling with Masks Knowledge 6 Profiling without Masks Knowledge 6 2.4 Thesis Contribution and Organization 6 2.4.2 Dimensionality Reduction Approach 6			1.2.3	Modern More Complex Devices to Certify	3			
2.1 Introduction to Side-Channel Attacks62.1.1 Historical Overview62.1.2 Terminology and Generalities6Target and Leakage Model6Points of Interest6Simple vs Advanced SCAs6Vertical vs Horizontal SCAs6Profiled vs Non-Profiled SCAs6Side-Channel Algebraic Attacks6Distinguishers6SCA Metrics62.2 Main Side-Channel Countermeasures62.2.1 Random Delays and Jitter62.2.2 Shuffling62.2.3 Masking62.3 Higher-Order Attacks62.3.1 Higher-Order Moments Analysis and Combining Functions62.3.2 Profiling Higher-Order Attacks6Profiling with Masks Knowledge6Profiling without Masks Knowledge6Profiling without Masks Knowledge62.4.1 Foreword of this Thesis: Research of Points of Interest62.4.2 Dimensionality Reduction Approach6			1.2.4	Embedded Cryptography Vulnerabilities	3			
2.1.1 Historical Overview 6 2.1.2 Terminology and Generalities 6 Target and Leakage Model 6 Points of Interest 6 Simple vs Advanced SCAs 6 Vertical vs Horizontal SCAs 6 Profiled vs Non-Profiled SCAs 6 Side-Channel Algebraic Attacks 6 Distinguishers 6 SCA Metrics 6 2.2.1 Random Delays and Jitter 6 2.2.2 Shuffling 6 2.2.3 Masking 6 2.3.1 Higher-Order Attacks 6 2.3.2 Profiling Higher-Order Attacks 6 Profiling with Masks Knowledge 6 Profiling without Masks Knowledge 6 2.4.1 Foreword of this Thesis: Research of Points of Interest 6 2.4.2 Dimensionality Reduction Approach 6	2	Intr	oductio	on to Side-Channel Attacks	5			
2.1.2 Terminology and Generalities 6 Target and Leakage Model 6 Points of Interest 6 Simple vs Advanced SCAs 6 Vertical vs Horizontal SCAs 6 Profiled vs Non-Profiled SCAs 6 Side-Channel Algebraic Attacks 6 Distinguishers 6 SCA Metrics 6 2.2 Main Side-Channel Countermeasures 6 2.2.1 Random Delays and Jitter 6 2.2.2 Shuffling 6 2.2.3 Masking 6 2.3.1 Higher-Order Attacks 6 2.3.2 Profiling Higher-Order Attacks 6 Profiling with Masks Knowledge 6 Profiling without Masks Knowledge 6 2.4 Thesis Contribution and Organization 6 2.4.1 Foreword of this Thesis: Research of Points of Interest 6 2.4.2 Dimensionality Reduction Approach 6		2.1	Introd	uction to Side-Channel Attacks	6			
Target and Leakage Model Points of Interest Simple vs Advanced SCAs Vertical vs Horizontal SCAs Profiled vs Non-Profiled SCAs Side-Channel Algebraic Attacks Distinguishers SCA Metrics 2.2 Main Side-Channel Countermeasures 2.2.1 Random Delays and Jitter 2.2.2 Shuffling 2.2.3 Masking 3.3 Higher-Order Attacks 46 2.3.1 Higher-Order Moments Analysis and Combining Functions 2.3.2 Profiling Higher-Order Attacks Profiling with Masks Knowledge Profiling without Masks Knowledge 3.4 Thesis Contribution and Organization 3.4.1 Foreword of this Thesis: Research of Points of Interest 3.4.2 Dimensionality Reduction Approach 3.5 G			2.1.1	Historical Overview	6			
Target and Leakage Model Points of Interest Simple vs Advanced SCAs Vertical vs Horizontal SCAs Profiled vs Non-Profiled SCAs Side-Channel Algebraic Attacks Distinguishers SCA Metrics 2.2 Main Side-Channel Countermeasures 2.2.1 Random Delays and Jitter 2.2.2 Shuffling 2.2.3 Masking 3.3 Higher-Order Attacks 46 2.3.1 Higher-Order Moments Analysis and Combining Functions 2.3.2 Profiling Higher-Order Attacks Profiling with Masks Knowledge Profiling without Masks Knowledge 3.4 Thesis Contribution and Organization 3.4.1 Foreword of this Thesis: Research of Points of Interest 3.4.2 Dimensionality Reduction Approach 3.5 G			2.1.2	Terminology and Generalities	6			
Points of Interest 6 Simple vs Advanced SCAs 6 Vertical vs Horizontal SCAs 6 Profiled vs Non-Profiled SCAs 6 Side-Channel Algebraic Attacks 6 Distinguishers 6 SCA Metrics 6 2.2 Main Side-Channel Countermeasures 6 2.2.1 Random Delays and Jitter 6 2.2.2 Shuffling 6 2.2.3 Masking 6 2.3 Higher-Order Attacks 6 Profiling Higher-Order Attacks 6 Profiling with Masks Knowledge 6 Profiling without Masks Knowledge 6 Profiling without Masks Knowledge 6 Profiling without Masks Knowledge 6 2.4.1 Foreword of this Thesis: Research of Points of Interest 6 2.4.2 Dimensionality Reduction Approach 6				••	6			
Simple vs Advanced SCAs Vertical vs Horizontal SCAs Profiled vs Non-Profiled SCAs Side-Channel Algebraic Attacks Distinguishers SCA Metrics 2.2 Main Side-Channel Countermeasures 2.2.1 Random Delays and Jitter 2.2.2 Shuffling 2.2.3 Masking 3.3 Higher-Order Attacks 2.3.1 Higher-Order Moments Analysis and Combining Functions 2.3.2 Profiling Higher-Order Attacks Profiling with Masks Knowledge Profiling without Masks Knowledge Profiling without Masks Knowledge 3.4.1 Foreword of this Thesis: Research of Points of Interest 4.4.2 Dimensionality Reduction Approach 6					6			
Vertical vs Horizontal SCAs 6 Profiled vs Non-Profiled SCAs 6 Side-Channel Algebraic Attacks 6 Distinguishers 6 SCA Metrics 6 2.2 Main Side-Channel Countermeasures 6 2.2.1 Random Delays and Jitter 6 2.2.2 Shuffling 6 2.2.3 Masking 6 2.3 Higher-Order Attacks 6 2.3.1 Higher-Order Moments Analysis and Combining Functions 6 2.3.2 Profiling Higher-Order Attacks 6 Profiling with Masks Knowledge 6 Profiling without Masks Knowledge 6 Profiling without Masks Knowledge 6 Profiling without Masks Knowledge 6 Profile Scontribution and Organization 6 2.4.1 Foreword of this Thesis: Research of Points of Interest 6 2.4.2 Dimensionality Reduction Approach 6					6			
Side-Channel Algebraic Attacks Distinguishers SCA Metrics 6 SCA Metrics 6 2.2 Main Side-Channel Countermeasures 6 2.2.1 Random Delays and Jitter 6 2.2.2 Shuffling 6 2.2.3 Masking 6 2.3 Higher-Order Attacks 6 2.3.1 Higher-Order Moments Analysis and Combining Functions 7 2.3.2 Profiling Higher-Order Attacks Profiling with Masks Knowledge Profiling without Masks Knowledge 6 Profiling without Masks Knowledge 6 Profiling without Masks Knowledge 6 2.4 Thesis Contribution and Organization 6 2.4.1 Foreword of this Thesis: Research of Points of Interest 6 2.4.2 Dimensionality Reduction Approach 6					6			
Distinguishers				Profiled vs Non-Profiled SCAs	6			
Distinguishers				Side-Channel Algebraic Attacks	6			
SCA Metrics 6 2.2 Main Side-Channel Countermeasures 6 2.2.1 Random Delays and Jitter 6 2.2.2 Shuffling 6 2.2.3 Masking 6 2.3 Higher-Order Attacks 6 2.3.1 Higher-Order Moments Analysis and Combining Functions 6 2.3.2 Profiling Higher-Order Attacks 6 Profiling with Masks Knowledge 6 Profiling without Masks Knowledge 6 2.4 Thesis Contribution and Organization 6 2.4.1 Foreword of this Thesis: Research of Points of Interest 6 2.4.2 Dimensionality Reduction Approach 6					6			
2.2.1 Random Delays and Jitter					6			
2.2.1 Random Delays and Jitter		2.2	Main S	Side-Channel Countermeasures	6			
2.2.2Shuffling62.2.3Masking62.3Higher-Order Attacks62.3.1Higher-Order Moments Analysis and Combining Functions62.3.2Profiling Higher-Order Attacks6Profiling with Masks Knowledge6Profiling without Masks Knowledge62.4Thesis Contribution and Organization62.4.1Foreword of this Thesis: Research of Points of Interest62.4.2Dimensionality Reduction Approach6					6			
2.2.3 Masking 6 2.3 Higher-Order Attacks 6 2.3.1 Higher-Order Moments Analysis and Combining Functions 6 2.3.2 Profiling Higher-Order Attacks 6 Profiling with Masks Knowledge 6 Profiling without Masks Knowledge 6 2.4 Thesis Contribution and Organization 6 2.4.1 Foreword of this Thesis: Research of Points of Interest 6 2.4.2 Dimensionality Reduction Approach 6			2.2.2		6			
2.3 Higher-Order Attacks62.3.1 Higher-Order Moments Analysis and Combining Functions62.3.2 Profiling Higher-Order Attacks6Profiling with Masks Knowledge6Profiling without Masks Knowledge62.4 Thesis Contribution and Organization62.4.1 Foreword of this Thesis: Research of Points of Interest62.4.2 Dimensionality Reduction Approach6			2.2.3		6			
2.3.1 Higher-Order Moments Analysis and Combining Functions		2.3	Highe		6			
2.3.2 Profiling Higher-Order Attacks			_		6			
Profiling with Masks Knowledge			2.3.2	•	6			
Profiling without Masks Knowledge								
2.4 Thesis Contribution and Organization								
2.4.1 Foreword of this Thesis: Research of Points of Interest 6 2.4.2 Dimensionality Reduction Approach 6		2.4	Thesis					
2.4.2 Dimensionality Reduction Approach 6								
			2.4.2					
Linear Methods for First-Order Attacks 6				Linear Methods for First-Order Attacks	6			
Kernel Methods for Higher-Order Attacks 6								
2.4.3 Neural Network Approach 6			2.4.3					
Toward Getting Rid of Information-Loosing Preprocessing 6				* *				

3	Introduction to Machine Learning				
	3.1	Basic Concepts of Machine Learning	7		
		3.1.1 The Task, the Experience and the Performance	7		
		3.1.2 Supervised, Semi-Supervised, Unsupervised Learning	7		
		3.1.3 Training, Validation and Test Sets	7		
		3.1.4 Underfitting, Overfitting and Regularization	7		
		3.1.5 Data Augmentation	7		
		3.1.6 No Free Lunch Theorem	7		
	3.2	Machine Learning Applications in Side-Channel Context	7		
	0.2	3.2.1 Profiled Attack as a Classification Problem	7		
		Support Vector Machine	7		
		Random Forest	7		
		Neural Networks	7		
II	Co	ontributions	9		
4	Poir	nts of Interest	11		
	4.1	Motivations	11		
		4.1.1 The Curse of Dimensionality	11		
	4.2	Selection on Points of Interest: Classical Statistics	11		
	4.3	Related Issues: Leakage Detection and Leakage Assessment	11		
	4.4	Generalized SNR for Multi-Variate Attacks	11		
	4.5	Observations Leading to Take a Dimensionality Reduction Approach .	11		
5	Line	ear Dimensionality Reduction	13		
	5.1	Introduction	13		
		5.1.1 Principal Component Analysis	13		
		5.1.2 Linear Discriminant Analysis	13		
		5.1.3 Projection Pursuits	13		
	5.2	Principal Component Analysis	13		
		5.2.1 Statistical Point of View	13		
		5.2.2 Geometrical Point of View	13		
	5.3	Application of PCA in SCAs	13		
		5.3.1 Original vs Class-Oriented PCA	13		
		5.3.2 The Choice of the Principal Components	13		
	5.4	Linear Discriminant Analysis	13		
	0.1	5.4.1 Statistical Point of View	13		
		5.4.2 Geometrical Point of View	13		
	5.5	Application of LDA in SCAs	13		
	0.0	5.5.1 The Small Sample Size problem	13		
6	Vor	nal Dimanajanality Paduatian	15		
6		nel Dimensionality Reduction	15		
	6.1	Motivation			
		6.1.1 Higher-Order Version of Projection Paracuite	15		
	()	Higher-Order Version of Projection Pursuits	15		
	6.2	Kernel Function and Kernel Trick	15		
	()	6.2.1 Local Kernel Functions as Similarity Metrics	15		
	6.3	Kernel Discriminant Analysis	15		
	6.4	Experiments over Atmega328P	15		
		6.4.1 The Regularization Problem	15		

	6.5	6.4.2 The Multi-Class Trade-Off	15 15 15 15 15 15 15
7	Con	volutional Neural Networks against Jitter-Based Countermeasures	17
•	7.1	Moving from Kernel Machines to Neural Networks	17
	7.2	Misalignment of Side-Channel Traces	17
	7.2	7.2.1 The Necessity and the Risks of Applying Realignment Techniques	17
		7.2.2 Analogy with Image Recognition Issues	17
	7.3	Convolutional Layers to Impose Shift-Invariance	17
	7.3	Data Augmentation for Misaligned Side-Channel Traces	17
	7.5	Experiments against Software Countermeasures	17
	7.6	Experiments against Artificial Hardware Countermeasures	17
	7.7	Experiments against Real-Case Hardware Countermeasures	17
8	KD	A vs Neural Networks Approach for HO-Attacks	19
O	8.1	Simulated Experiment for Profiled HO-Attacks	19
	0.1	8.1.1 The Simulations	19
		8.1.2 Comparison between KDA and MLP	19
	8.2	Real-Case Experiments over ARM Cortex-M4	19
9	Sian	nese Neural Networks for Collision Attacks	21
	9.1	Introduction	21
	9.2	Siamese Neural Networks	21
		9.2.1 Distances and Loss Functions	21
		9.2.2 Relation with Kernel Machines	
	9.3	Collision Attacks with Siamese NNs	
		9.3.1 Experimental Results	21
10	Con	clusions and Perspectives	23
		Summary	23
		Strengthen Embedded Security: the Main Challenge for Machine Learning Applications	23