

CSE232 HW2 2022

1)

Truth Table

Numbers	A	B	C	D	a	b	c	d	e	f	g
0	0	0	0	0	1	1	1	1	1	1	0
1	0	0	0	1	0	1	1	0	0	0	0
2	0	0	1	0	1	1	0	1	1	0	1
3	0	0	1	1	1	1	1	1	0	0	1
4	0	1	0	0	0	1	1	0	0	1	1
5	0	1	0	1	1	0	1	1	0	1	1
6	0	1	1	0	1	0	1	1	1	1	1
7	0	1	1	1	1	1	1	0	0	0	0
8	1	0	0	0	1	1	1	1	1	1	1
9	1	0	0	1	1	1	1	1	0	1	1

K-MAP FOR a

AB\CD	00	01	11	10
00	1	0	1	1
01	0	1	1	1
11	x	x	x	x
10	1	1	x	x

$$a = C + BD + A + B'D'$$

$$a = \sum m(0, 2, 3, 5, 6, 7, 8, 9) + \sum d(10, 11, 12, 13, 14, 15)$$

↓ don't care conditions

K-MAP FOR b

AB\CD	00	01	11	10
00	1	1	1	1
01	1	0	1	0
11	x	x	x	x
10	1	1	x	x

$$b = C'D' + CD + B'$$

$$b = \sum m(0, 1, 2, 3, 4, 7, 8, 9) + \sum d(10, 11, 12, 13, 14, 15)$$

K-MAP FOR c

AB\CD	00	01	11	10
00	1	1	1	0
01	1	1	1	1
11	x	x	x	x
10	1	1	x	x

$$c = C' + D + B$$

$$c = \sum m(0, 1, 2, 3, 4, 5, 6, 7, 8, 9) + \sum d(10, 11, 12, 13, 14, 15)$$

K-MAP FOR d

AB\CD	00	01	11	10
00	1	0	1	1
01	0	1	0	1
11	x	x	x	x
10	1	1	x	x

$$d = A + CD' + A'B'C + BC'D + B'D'$$

$$d = \sum m(0, 2, 3, 5, 6, 8, 9) + \sum d(10, 11, 12, 13, 14, 15)$$

K-MAP FOR e

AB\CD	00	01	11	10
00	1	0	0	1
01	0	0	0	1
11	x	x	x	x
10	1	0	x	x

$$e = CD' + B'D'$$

$$e = \sum m(0, 2, 6, 8) + \sum d(10, 11, 12, 13, 14, 15)$$

K-MAP FOR f

AB\CD	00	01	11	10
00	1	0	0	0
01	1	1	0	1
11	x	x	x	x
10	1	1	x	x

$$f = C'D' + A + BC' + BD'$$

$$f = \sum m(0, 4, 5, 6, 8, 9) + \sum d(10, 11, 12, 13, 14, 15)$$

K-MAP FOR g

AB\CD	00	01	11	10
00	0	0	1	1
01	1	1	0	1
11	x	x	x	x
10	1	1	x	x

$$g = BC' + A + CD' + B'C$$

$$g = \sum m(2, 3, 4, 5, 6, 8, 9) + \sum d(10, 11, 12, 13, 14, 15)$$

2)

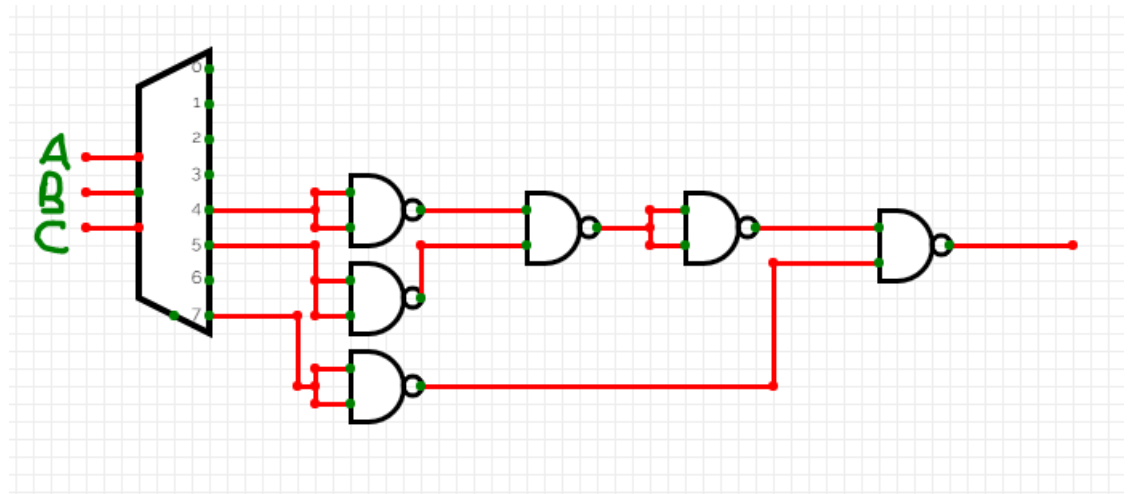
a)

$$F(A, B, C) = AB'C + AB' + AC$$

$$AB'C + AB'C + AB'C' + ABC + AB'C$$

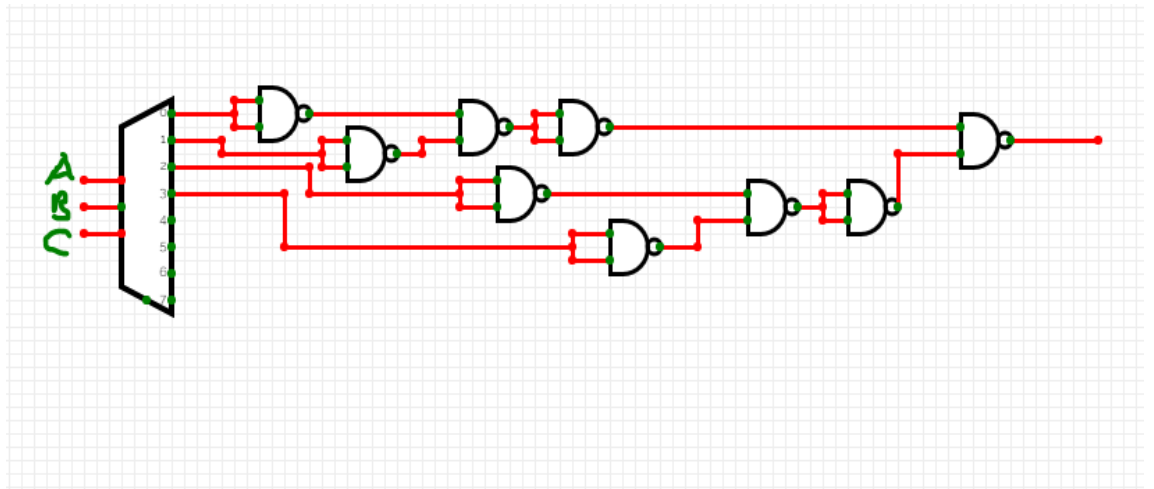
$$AB'C + AB'C' + ABC$$

$$D_5 + D_4 + D_7$$



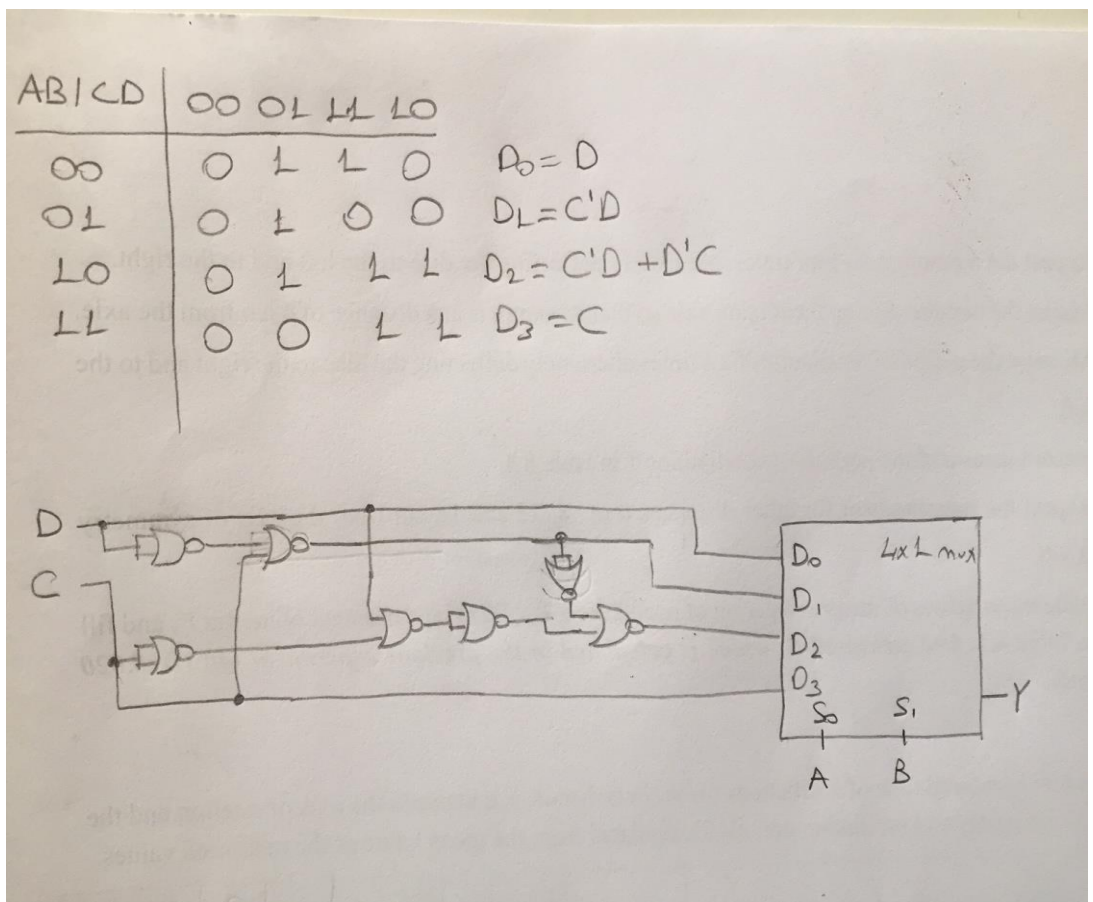
b)

$$\begin{aligned}
 F(A, B, C) &= (A' + B' + C')(A' + B')(A' + C) \\
 &= (A'A' + A'B' + A'B + \underbrace{B'B}_0 + A'C' + B'C')(A' + C) \\
 &= (A' + A'B' + A'B + A'C + B'C')(A' + C) \\
 &= (A'(\underbrace{1 + B' + B + C}_1) + B'C')(A' + C) \\
 &= (A' + B'C')(A' + C) \\
 &= A'A' + A'C + A'B'C' + \underbrace{B'C'C'}_0 \\
 &= A'(\underbrace{1 + C + B'C'}_1) = A' \\
 &\quad \swarrow \quad \searrow \\
 &\quad D_0 \quad D_1 \quad D_2 \quad D_3
 \end{aligned}$$



3)

a)



b)

