

# The DICE model and its discontents

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- Complex dynamic problem
  - How will we be able to ensure a rapid and smooth low-carbon transition?
  - Multiple macro-financial implications/requirements
- We want to explore possible futures
  - → We need prospective models
  - Some key building blocks of climate-economy interactions
- Today: the DICE model
  - The 'godfather' of climate economic modelling
  - or.. 'the model that everyone loves to hate'

## The DICE model structure

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# The ‘dynamic integrated climate economy’ (DICE) model

- Start: 1992 paper on Science
- Latest version:
  - DICE2023 with [Lint Barrage](#)
  - [See code](#) available in both GAMS and Excel
  - Good reading: 2017 paper on [PNAS](#)
- 2018 Nobel Prize in Economics
  - “for integrating climate change into long-run macroeconomic analysis”
  - Nobel lecture ([video](#)) ([AER article](#))



William Nordhaus (1941-)

# Social welfare function

- Social welfare is the discounted sum of the future stream of population-weighted instantaneous utilities:

$$W = \sum_{t=1}^T \frac{U(c_t)L_t}{(1 + \rho)^t}$$

- $U(c)$ : utility as a function of per capita consumption
- $L$ : population
- $\rho$ : Pure rate of social time preference
  - Also called 'rate of time impatience' or 'time discount rate'
  - Set to 2.2% in DICE; to 0.1% in the Stern Review
  - Choosing this value has ethical implications: how do we treat future generations compared to the present ones?

# Utility function

- Isoelastic utility function

$$U(c_t) = \frac{c_t^{1-\varphi}}{1-\varphi}$$

- $\varphi$ : Elasticity of marginal utility of consumption (set to 0.9)
  - It can be interpreted as a measure of relative intergenerational inequality aversion
  - The intertemporal elasticity of substitution is  $\frac{1}{\varphi}$
  - Coincides with risk aversion here, but different concepts (see Epstein and Zin preferences)
- Remember Lecture 6:  $SDR = \rho + \varphi g$ 
  - Given values for  $\rho$  and  $\varphi$ , discount rate in DICE roughly 4.6% in first period and declines to 3.4% in 2100

- Cobb-Douglas production function

$$Y_t = A_t K_t^\gamma L_t^{1-\gamma}$$

- $Y$ : Gross output (before damages and mitigation)
- $A$ : TFP parameter
  - TFP increases exogenously at a declining growth rate
  - Hicks-neutral technological progress, i.e.  $\frac{K}{L}$  is not affected
- $K$ : Capital stock (endogenous)
- $L$ : Population
  - $L$  grows asymptotically to 10.8 billion
  - Population = labour
- $\gamma$ : elasticity of output with respect to the capital (set to 0.3)

- DICE2023 includes three types of emissions:
- CO2 industrial emissions (already present)
  - Function of production  $Y$
  - $\sigma$ : Carbon intensity, with  $\sigma_{2015} \approx 0.29$
  - $\sigma$  decreases exogenously, first rapidly (-1.5% per year) then more slowly (approaching -0.5%)
- Land use CO2 emissions (new)
  - Exogenous decline by 10% per time period
- non-CO2 GHG emissions (new)
  - Abateable fraction of non-CO2 emissions  $\approx 12\%$  of CO2 emissions

$$E_{base,t} = \sigma_t Y_t + E_{land,t} + E_{nonCO2,t}$$



- Emissions can be abated
  - $\mu$ : Emission reduction rate (or 'control rate')
  - New in DICE2023: carbon price as additional control option
  - $\mu$  set to 0.05 in baseline scenario (\$6/tCO<sub>2</sub>)

$$E_t = (1 - \mu_t)E_{base,t}$$

- Abating emissions is costly → Abatement cost function

$$\Lambda = \theta_{1,t}\mu_t^{\theta_2}$$

- $\theta_1$  is a function of the price of the backstop technology
- $\theta_2 = 2.6$

# Backstop technology

- Backstop technology concept
  - Set of technologies capable of replacing fossil fuels (renewables, CCS, CDR, nuclear fusion, etc.)
- Exogenous decrease in time

$$p_{b,t} = p_0(1 - g_b)^t$$

- with  $p_{b,2050} = 515\$/\text{tCO}_2$  taken from larger IAMs ([ENGAGE](#))
  - $g_b = 1\%$  in 2020-2050,  $g_b = 0.1\%$  after 2050
- Calibrate  $\theta_{1,t}$  so that MAC equals  $p_{b,t}$  when  $\mu = 1$ 
  - $\rightarrow \theta_{1,t} = \frac{p_{b,t}\sigma}{\theta_2}$
  - $\rightarrow$  Net-zero emissions in 2020 would cost  $\approx 11\%$  of output (2.7% in 2100)

# Climate damages

- DICE2023 climate module is an adaption of the [FAIR model](#).  
In a nutshell
  - Emissions affect GHG atmospheric concentration →  
Concentration affects radiative forcing → Radiative forcing  
causes increase in temperatures
- Finally, temperature creates damages

$$\Omega_t = \psi_1 T_{AT,t} + \psi_2 T_{AT,t}^2$$

- where  $\Omega$  is the damage ratio (damages/GDP)
- with  $\psi_1 = 0$  and  $\psi_2 = 0.003467$
- Based on recent estimates (see [Piontek et al. \(2021\)](#) from  
Lecture 2 + Estimates of tipping point damages (see [Dietz et al. \(2021\)](#) + adjustment for non-market damages
- → 3.1% of GDP lost at 3°C; 7% at 4.5°C

## Macro accounting variables

- Net output is equal to gross output less damages and abatement costs

$$Q_t = \frac{(1 - \Lambda_t) Y_t}{1 + \Omega_t}$$

- Net output is allocated between consumption and investments

$$Q_t = C_t + I_t$$

- Investments contribute to accumulating capital stock

$$K_{t+1} = (1 - \delta_K) K_t + I_t$$

with depreciation rate  $\delta = 10\%$

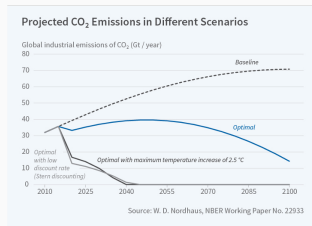
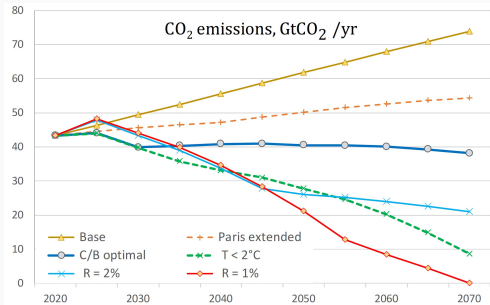
## DICE numerical results

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# Scenarios

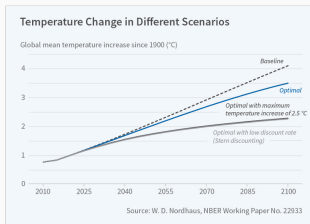
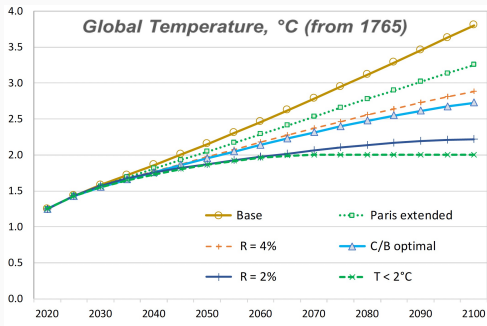
- No controls
  - $\mu$  set to zero for entire simulation
- Baseline (or 'BAU')
  - Extension of current policies
  - Carbon price=\$6/tCO<sub>2</sub> in 2020, increasing 1% per year)
- Paris-extended
  - Updated NDCs to 2030 achieved
  - $\mu$  increases  $\approx 0.5\%$  per year after 2030
- Cost-benefit optimal
  - $\mu$  is a decision variable
  - Trade-off between abatement and damage costs
- Temperature-limited
  - Additional temperature constraint to CB run (e.g. 2°C)
- Change in parameters
  - Higher/lower discount rate
  - Higher/lower damage coefficient

# DICE results - Emission paths



Source: Nordhaus and Barrage (2023) (left) Nordhaus (2017) (right)

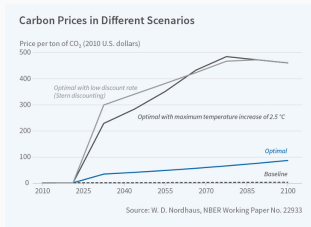
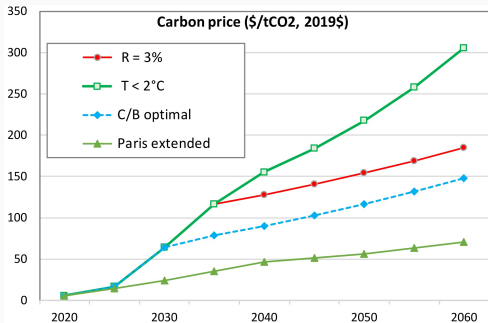
# DICE results - Temperature paths



Source: Nordhaus and Barrage (2023) (left) Nordhaus (2017) (right)

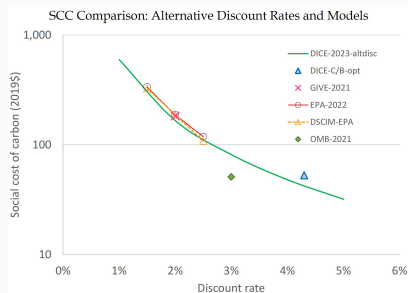
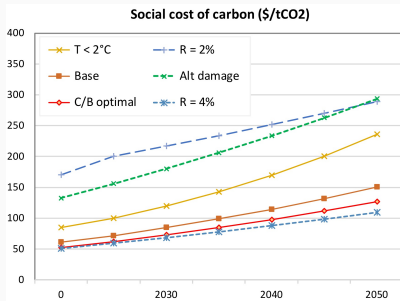


# DICE results - Carbon price paths



Source: Nordhaus and Barrage (2023) (left) Nordhaus (2017) (right)

# DICE results - Social Cost of Carbon



DICE 2023-altdisc: alternative constant discount rates; DICE- C/B-opt: C/B optimal scenario with average 2020 – 2050 discount rate; GIVE-2021: estimate from GIVE model; EPA-2022: US Environmental Protection Agency; DSCIM-EPA estimates specific to damage module based on DSCIM framework; OMB-2021: US Office of Management and Budget. Source: [Nordhaus and Barrage \(2023\)](#)

## Moving beyond DICE

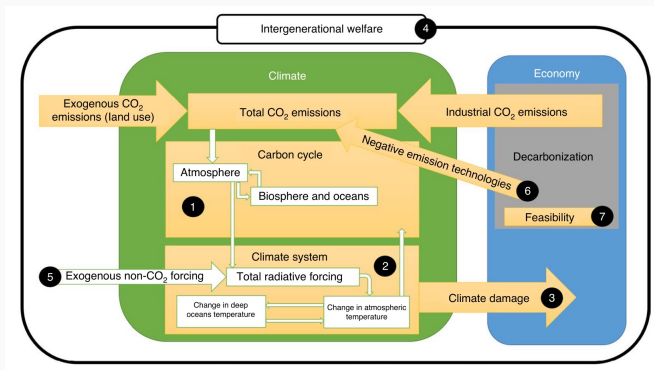
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# Strengths and limitations

- In climate econ, the DICE model is both the most followed..
  - The first to do it: benchmark for everyone else
  - Simple and following standard econ setting
  - Open-access: play for yourself
  - Most papers compare their results to DICE
- .. and the most criticised
  - Simplistic setting
  - No regional disaggregation (although RICE model)
  - Shaky empirical foundations (e.g. damage function)
  - No inertia: just turn up  $\mu$  and get abatement; but really, painful structural change  $K_d \rightarrow K_c$
  - Technological change is exogenous, no learning
  - Entirely deterministic: no uncertainty

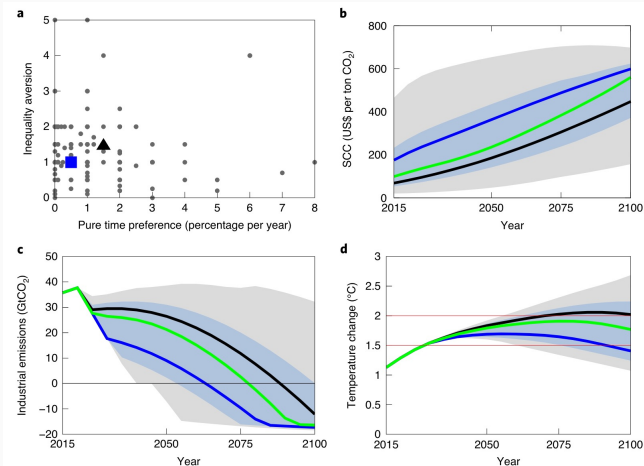
# First strategy: Improve DICE

- See for instance [Hansel et al. 2020](#)
  - Note: some of these improvements were included in DICE2023



Updates to DICE2016: 1) carbon cycle based on FAIR model; 2) update of energy balance model; 3) damage estimate revised to Howard and Sterner (2017); 4) expert views on intergenerational welfare; 5) non-CO<sub>2</sub> forcing; 6) earlier availability of NETs; 7) constraints on maximum rate of decarbonization. Source: [Hansel et al. 2020](#)

# Hansel et al. 2020 results



a) Experts' judgements on discounting parameters ( $n = 173$ ); Black triangle: DICE2016 values; Blue square: median expert view; b-d) climate policy pathways; black: updated DICE; blue: median expert view; green: median expert path. Source: Hansel et al. 2020

## Second strategy: use something else

- Other pioneering medium-scale models
  - **FUND model** by Richard Tol and collaborators
  - PAGE model by Chris Hope and collaborators
  - DICE, FUND and PAGE are used to calculate SCC in US
- Two main evolutions from this first generation
  - Go big: large-scale numerical models with multiple regions and detailed representation of technologies
  - Go small: simplified models aimed at deriving analytical solutions

## Addendum: An application to climate finance

- What would be the impact of climate change on asset values?
  - Value at Risk (VaR): potential portfolio loss over a given time horizon, at a given probability
- Starting point: DICE 2010
  - Modified climate damages: on both growth and capital stocks
- Some assumption
  - Asset values = NPV of discounted cash flows
  - Corporate earnings constant % of GDP → same growth rates
  - Debt and equity perfect substitutes

**Table 1 | The present value at risk of global financial assets from climate change between 2015 and 2100—the climate VaR.**

| Emissions scenario                                       | 1st pctl. | 5th   | Mean  | 95th  | 99th   |
|--|-----------|-------|-------|-------|--------|
| BAU (expected warming of 2.5 °C in 2100)                 | 0.46%     | 0.54% | 1.77% | 4.76% | 16.86% |
| Mitigation to limit warming to 2 °C with 2/3 probability | 0.35%     | 0.41% | 1.18% | 2.92% | 9.17%  |

Source: [Dietz et al. \(2016\)](#)