

Integrated assessment modelling - Big and small

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- We want to explore possible climate/transition futures
 - → We need models
 - The godfather of climate economic models: DICE
 - However: limitations
- Alternative strategies
 - Include macro-finance into climate economic models
 - Include climate/transition into neoclassical macro models
 - Include climate/transition into non-neoclassical macro models

- Integrated Assessment Models (IAMs)
 - Integrate economy, energy and climate
 - Going beyond DICE
- Analytical IAMs
 - Small-scale models rooted in econ
 - Useful to explore new grounds (e.g. uncertainty)
 - Incorporating insights from financial modelling
- Large-scale numerical IAMs
 - Diversified family of numerical models (including CGEs)
 - Going granular on technologies/regions/sectors
 - Intermodel comparison exercises → IPCC scenarios
 - Spatial IAMs

Analytical IAMs

- By ‘analytical’ IAMs, we refer to a family of models
 - Integrating economy and climate/transition small-scale (without granularity of large numerical IAMs) and with simplified functions
 - Aimed at deriving analytical conclusions (e.g. a formula for the optimal carbon price) or at investigating specific mechanisms
 - Rooted into neoclassical growth theory
 - Used to introduce new advancements and features (e.g. Epstein-Zin preferences, stochastic uncertainty, learning)
 - While analytical, they also often offer numerical simulations
 - Usually published in econ journals (while large IAMs often appear on interdisciplinary ones)

Analytical IAMs interests

- Find efficient transition/policy paths
 - Can be in a cost-benefit setting with climate damages (see [Golosov et al., 2014](#) in Econometrica).. .. or in a cost-effectiveness one, i.e. looking for least-cost paths (see [Lemoine and Rudik, 2017](#) in AER)
- Introduce uncertainty and learning
 - ‘Recursive IAMs’: focus on uncertainty ([Cai & Lontzek, 2018](#) in JPE; [van den Bremer & van der Ploeg, 2021](#) in AER)
 - Deterministic models or Monte Carlo simulations not enough
 - We need to find optimal paths under uncertainty (i.e. behaviour should respond to uncertainty and its resolution)
 - Stochastic elements: Brownian and Poisson processes
- Incorporate insights from macro and finance
 - Ongoing efforts build on modelling approaches borrowed from macro/financial economics (e.g. Epstein-Zin preferences)
 - Overlaps with E-DSGE and asset pricing models (Lecture 9)

- Logarithmic utility function ($\eta = 1$)

$$U_t(C_t) = \ln C_t$$

- Cobb-Douglas production function (pre-damage output)

$$\tilde{Y}_t = A_t K_t^\alpha N_t^{1-\alpha-\nu} E_t^\nu$$

where K : capital; N :labour; E : energy composite

- CES energy function with oil, coal and clean sources

$$E_t = \left(\kappa_{\text{coal}} E_{\text{coal},t}^\rho + \kappa_{\text{oil}} E_{\text{oil},t}^\rho + \kappa_{\text{clean}} E_{\text{clean},t}^\rho \right)^{\frac{1}{\rho}}$$

- Fossil emissions E^f increase CO2 atmospheric concentration S

$$(S_t - \bar{S}) = \sum_{s=0}^{t+T} (1 - d_s) E_{t-s}^f$$

with $1 - d_s$ amount of carbon in atmosphere at time s

- Carbon cycle: a share φ_I remains forever; $1 - \varphi_0$ decays immediately; the rest decays at rate φ

$$1 - d_s = \varphi_L + (1 - \varphi_L)\varphi_0(1 - \varphi)^s$$

- Damages proportional to output

$$Y_t = (1 - D_t)\tilde{Y}$$

- Damage function of CO2 concentration

$$1 - D_t = e^{-\gamma(S_t - \bar{S})}$$

with γ defining climate damage strength (lower γ , higher loss)

- Planning problem:

$$\max \mathbb{E} \sum_{t=0}^{\infty} \beta^t U(C_t)$$

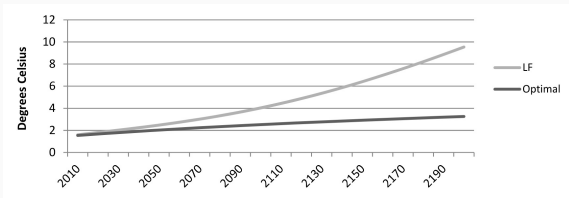
- Assuming constant savings rate, the marginal damage from emissions is a function of (i) discounting (ii) damage coefficient (iii) atmospheric carbon depreciation structure

$$\Lambda_t^s = Y_t \left[\mathbb{E} \sum_{j=0}^{\infty} \beta^j \gamma_{t+j} (1 - d_j) \right]$$

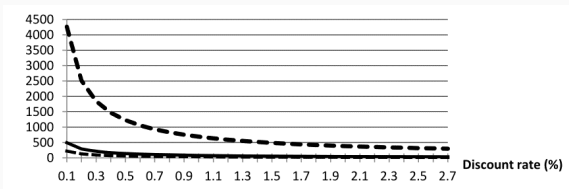
- Decentralized equilibrium: Pigouvian carbon tax equal to Λ^s
- Optimal carbon tax grows at the growth rate of the economy

Golosov et al. (2014) numerical results

- Numerical simulations
 - Stochastic uncertainty around true value of γ



Optimal vs laissez-faire temperature. Source: [Golosov et al. \(2014\)](#)



Optimal tax rates (\$ per ton of carbon at 70\$tn output) before uncertainty is resolved (solid) and after (dashed: γ_L and γ_H). Source: [Golosov et al. \(2014\)](#)

Alternative: put constraint and find efficient path

- Hotelling structure applicable
 - Hotelling rule: optimal net price ('Hotelling rent') of an exhaustible resources grows at the rate of interest
 - Remaining allowable CO2 emissions (carbon budget) are like an exhaustible resource
 - Many regions (e.g. Europe) don't run cost-benefit analysis (\rightarrow SCC) but focus on keeping T below a target
- Optimal carbon price is a function of interest rate (or SDR)
 - $P_t = e^{\rho t} P_0$ (continuous time)
 - $P_t = \left(\frac{1}{1+\rho}\right)^t P_0$ (discrete time)
- Risk-adjusted interest rate is what we're interested in
 - [Gollier et al. \(2024\)](#): 3.5%
 - If it's too high, it means that, for a specific carbon budget, price today is too low

- CO2 concentration M increases with net emissions ($E - A$) and decreases with decay

$$\dot{M}(t) = E - A(t) - \delta (M(t) - M_{\text{pre}})$$

- Concentration generates forcing F but this translates into temperature change with some inertia (greater ϕ , lower inertia)

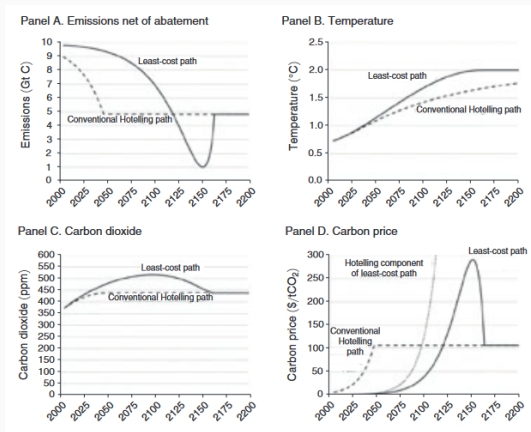
$$\dot{T}(t) = \phi [sF(M(t)) - T(t)]$$

- Planner minimises abatement costs $C(A)$

$$\min_{A(t)} \int_{t_0}^{\infty} e^{-r(t-t_0)} C(A(t)) dt$$

Lemoine and Rudik (2017) results

- Least-cost path targeting \bar{T} different from Hotelling path constraining emissions
- Overshoot of atmospheric concentration allowed
- Postpone climate policies



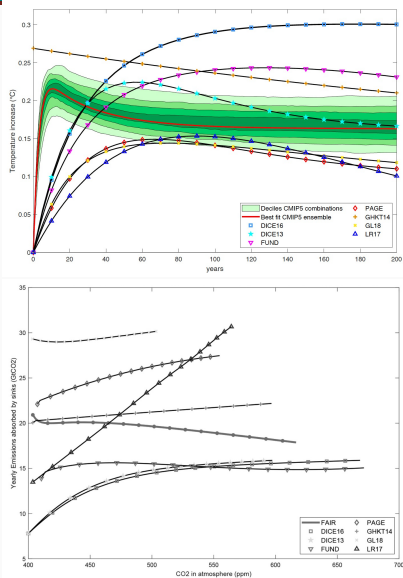
Least-cost and Hotelling trajectories with a 2° temperature target. Source: [Lemoine et al. \(2017\)](#)

Are IAMs getting climate dynamics right? (i)

- Dietz et al. (2021) take six prominent IAMs
 - DICE, FUND and PAGE; Golosov et al. (2014) on Ecta; Lemoine and Rudik (2017) on AER; Gerlagh and Liski (2018) on EconJ
 - Compare them with climate science models from CMIP5
- First experiment: how does T react to an emission impulse?
 - We know from climate science: rapid increase and stable afterwards
- Second experiment: how does CO₂ absorption change when concentration increases?
 - We know from climate science: absorption decreases when concentration rises

Are IAMs getting climate dynamics right? (ii)

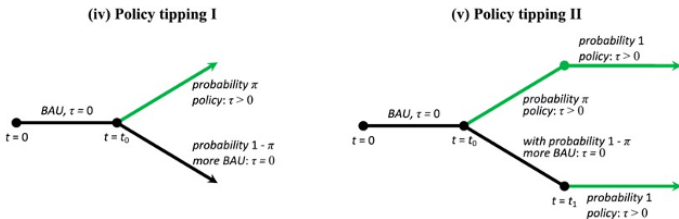
- IAMs tend to follow slower temperature response trajectories, and not include decline in sinks absorption capacity
- → Optimal carbon prices too low
- → Optimal carbon prices too sensitive to discount rates



Source: Dietz et al. (2021)

Stranding: van der Ploeg & Rezai (2020) in JEEM

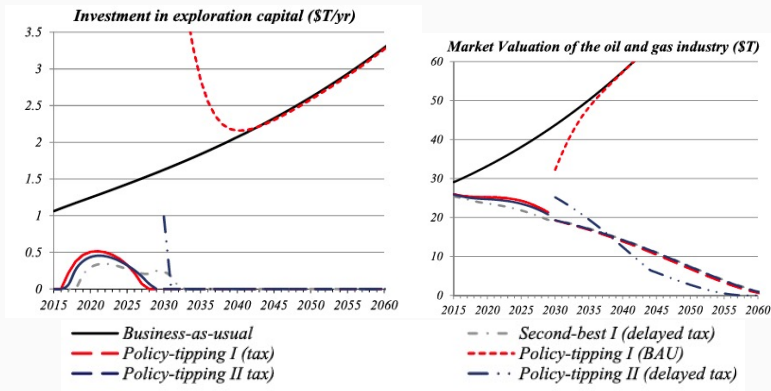
- Focus on the fossil fuel sector
 - A single type of capital to work with: extraction capital k
 - No underutilisation of capital allowed
- Market valuation of fossil firms given by future profits
 - They decide investments by maximising $V^R \equiv \int_0^\infty e^{-rt} \Pi^R$
- Policy tipping setting:



Source: van der Ploeg & Rezai (2020)

van der Ploeg & Rezai (2020): Results

- Uncertainty (and its resolution) affect transition profiles
 - I might go to zero but K continues to operate
 - $\rightarrow V$ moves more smoothly



Source: van der Ploeg & Rezai (2020)

- Cobb-Douglas production function with abatement costs Λ and damages Ω

$$Y = AL^{1-\alpha}K^{\alpha}\Lambda\Omega$$

- Two types of capital stocks with different productivities
 - Abatement takes place via structural change $K_d \rightarrow K_c$
 - Negative dirty investments possible ('stranding')
 - Adjustment costs in both investments and disinvestments
- Emissions function of dirty capital

$$E = \psi_t K_d$$

- Damages are a function of temperature T , itself a function of cumulative emissions S (with ζ : TCRE coefficient)

$$\Omega = \exp\left(-\frac{\gamma}{2}T^2\right)$$

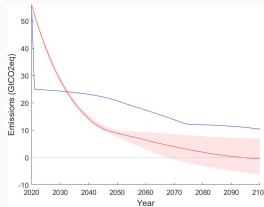
- Abatement cost function of abatement μ and MAC slope φ

$$\Lambda = \exp\left(-\frac{\varphi_t}{2}\mu^2\right)$$

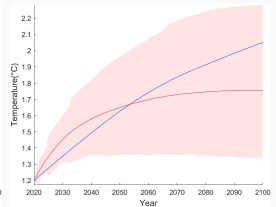
- Clean technology costs fall over time
 - Exogenous component: spillovers from general tech progress: AI, nanotechnology, etc.
 - Endogenous component: MAC parameters evolve as a function of cumulative abatement M (learning)
- Sources of uncertainty
 - Brownian motions on temperature, capital stocks and productivity
 - T -dependent Poisson jumps on productivity (macro disasters)
- Epstein-Zin-Weil recursive preferences

Campiglio, Dietz and Venmans (2024) results (i)

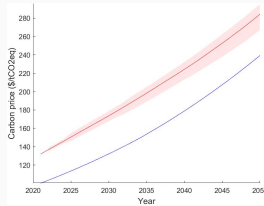
- CB carbon price:
\$133 → \$283
(2050)
- CB disinvestment:
\$4.8 tn. (33% lost)
- Not considering
inertia, learning and
uncertainty gives
incorrect
suggestions



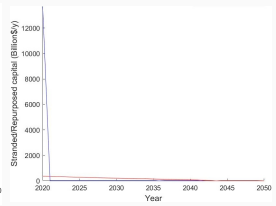
(a) Emissions E



(b) Temperature T



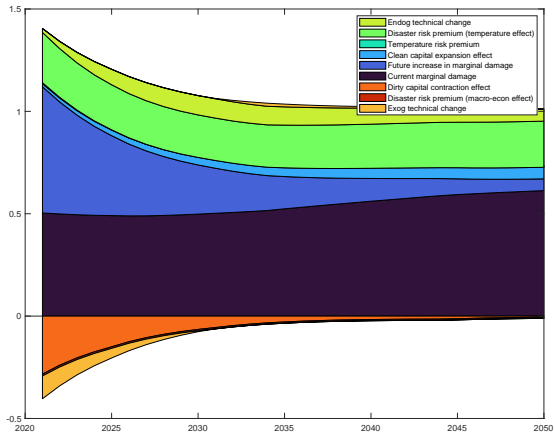
(c) Carbon price p



(d) Dirty capital disinvestment R

Comparison with 'straw man' model. **Red:** cost-benefit.
Blue: without inertia, learning and uncertainty. Source:
Campiglio et al. (2024)

Campiglio, Dietz and Venmans (2024) results (ii)



Optimal carbon price decomposition results. Y-axis is scaled in percent of the absolute price. Source: [Campiglio et al. \(2024\)](#)

Strengths and weaknesses of analytical IAMs

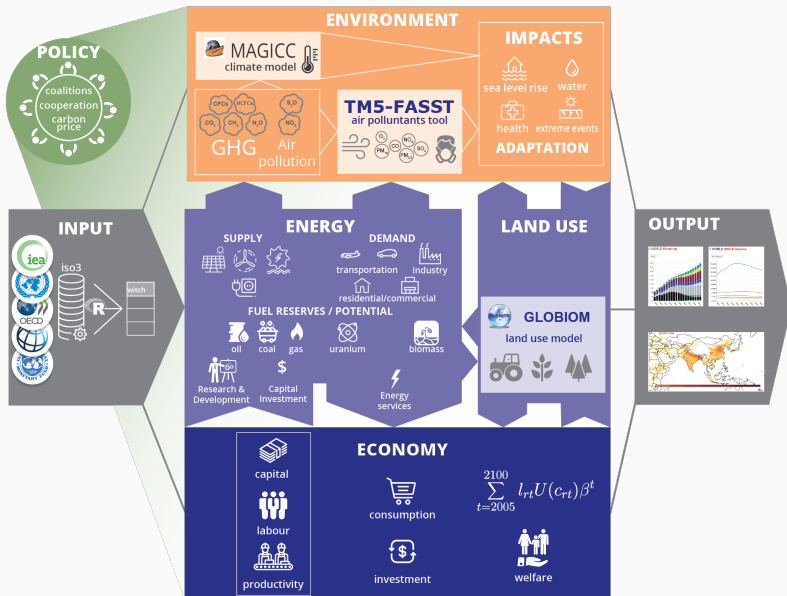
- They are useful, in that they
 - offer interesting new insights, especially on uncertainty-related matters, which would not be possible in large-scale numerical models
 - provide analytical conclusions (more generally valid than numerical ones)
 - develop a bridge between climate economics and macro/finance modelling
- At the same time, they
 - are by definition constrained in their complexity and need to be simple

Large-scale numerical IAMs

Large-scale numerical IAMs

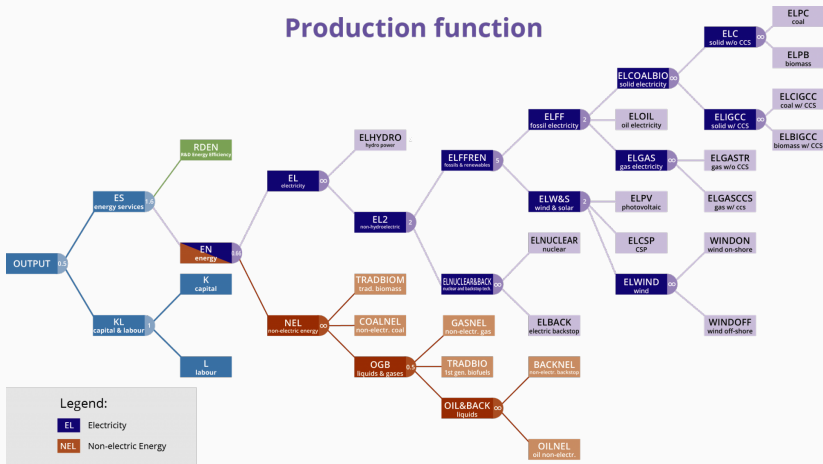
- Common features across models
 - Multiple regions
 - Cooperative/non-cooperative behaviour; coalitions
 - Equity issues (burden-sharing, transfers)
 - Detailed energy sources/technologies and pollutants
 - Small climate modules (or links to larger climate models)
 - Economic modules also tend to be simple (or absent)
 - Exception: CGE models (are they IAMs?)
- But large variability across models
 - Partial vs general equilibrium
 - Simulation vs optimization
 - Recursive dynamic (myopic) vs intertemporal optimization (foresight)
 - Different representation of climate impacts, non-energy sectors, land use, regions..

An example: The WITCH model



The WITCH production function

Production function



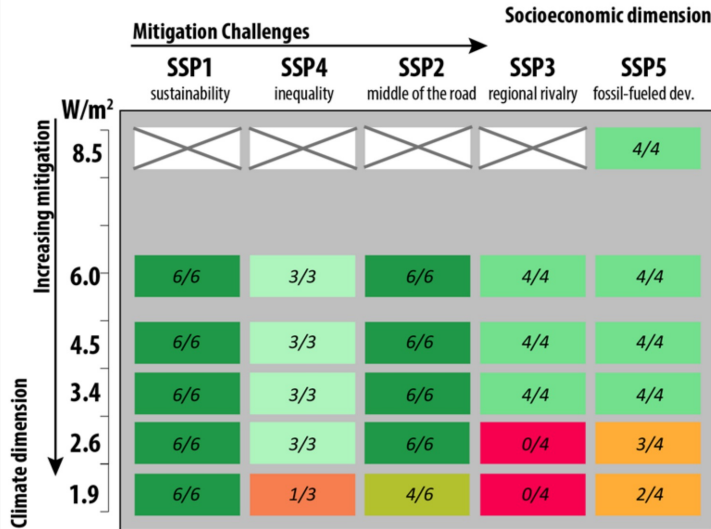
Source: WITCH website

- More details in the [WITCH documentation](#)

Many other large IAMs exist

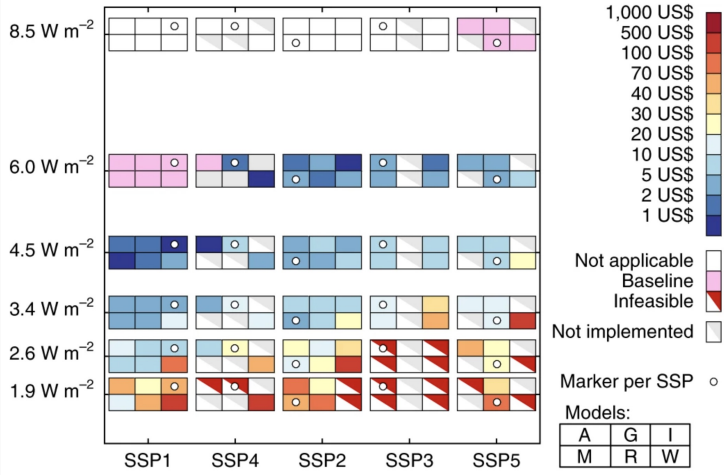
- Other notable models:
 - [MESSAGE model](#) (IIASA, Austria)
 - [GCAM model](#) (JGCRI, United States)
 - [IMAGE](#) (PBL, Netherlands)
 - [REMIND model](#) (PIK, Germany)
 - [IMACLIM](#) (CIRED, France)
 - [E3ME](#) (Cambridge Econometrics, United Kingdom)
 - An overview: see the [IAM Consortium Wiki paper](#)
- Inter-model comparison exercises
 - Run the same scenarios and compare results
 - e.g. [Rogelj et al. \(2018\)](#): can we achieve 1.5°C? using six IAMs

SSP/RCP combinations



In cells: numbers of models with feasible scenarios. Source: Rogelj et al. (2018)

Optimal carbon prices per RCP/SSP



Average global average carbon prices over 2020–2100 (discounted to 2010 with a 5% rate). A: AIM/CGE; G: GCAM4; I: IMAGE; M: MESSAGE-GLOBIOM; R: REMIND-MagPIE; W: WITCH-GLOBIOM. Source: [Rogelj et al. \(2018\)](#)

Fossil stranding using TIAM-UCL

- TIAM-UCL regional model:
 - Partial equilibrium model with detailed representation of energy sources and systems
 - Driven by minimisation of energy system NPV costs to 2100
- What is the optimal geographical distribution of unburnable carbon in a 2° scenario?

Table 1 | Regional distribution of reserves unburnable before 2050 for the 2 °C scenarios with and without CCS

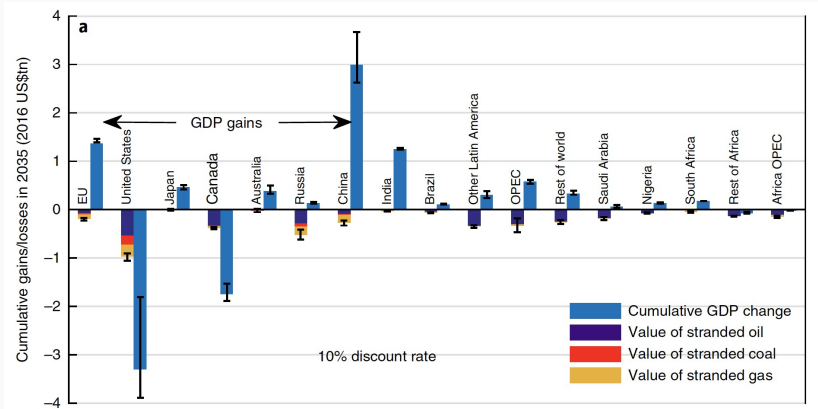
Country or region	2 °C with CCS						2 °C without CCS					
	Oil		Gas		Coal		Oil		Gas		Coal	
	Billions of barrels	%	Trillions of cubic metres	%	Gt	%	Billions of barrels	%	Trillions of cubic metres	%	Gt	%
Africa	23	21%	4.4	33%	28	85%	28	26%	4.4	34%	30	90%
Canada	39	74%	0.3	24%	5.0	75%	40	75%	0.3	24%	5.4	82%
China and India	9	25%	2.9	63%	180	66%	9	25%	2.5	53%	207	77%
FSU	27	18%	31	50%	203	94%	28	19%	36	59%	209	97%
CSA	58	39%	4.8	53%	8	51%	63	42%	5.0	56%	11	73%
Europe	5.0	20%	0.6	11%	65	78%	5.3	21%	0.3	6%	74	89%
Middle East	263	38%	46	61%	3.4	99%	264	38%	47	61%	3.4	99%
OECD Pacific	2.1	37%	2.2	56%	83	93%	2.7	46%	2.0	51%	85	95%
ODA	2.0	9%	2.2	24%	10	34%	2.8	12%	2.1	22%	17	60%
United States of America	2.8	6%	0.3	4%	235	92%	4.6	9%	0.5	6%	245	95%
Global	431	33%	95	49%	819	82%	449	35%	100	52%	887	88%

FSU, the former Soviet Union countries; CSA, Central and South America; ODA, Other developing Asian countries; OECD, the Organisation for Economic Co-operation and Development. A barrel of oil is 0.159 m³; % Reserves unburnable before 2050 as a percentage of current reserves.

Source: [McGlade and Ekins \(2015\)](#)

- Combination of E3ME (macroeconometrics), FTT (diffusion) and GENIE (Earth systems) models
- Two stranding drivers: 2°C climate policy or technological diffusion
 - Fossil stranding can happen even without policies
 - Drop in demand for fossil fuels (→ can trigger a 'sell out')
- Focus on geographical distribution of fossil stranding and macro implications
 - Net importers (e.g China, EU) may benefit from dynamics
 - Producers (Russia, US, Canada) will lose out
 - Global NPV wealth loss of US\$1-4 trillion

Fossil stranded assets across regions



Cumulative GDP changes and discounted fossil fuel value loss to 2035 - 2 °C sell-out scenario vs IEA projections. Source: [Mercure et al. \(2018\)](#)

Strengths and weaknesses of numerical IAMs

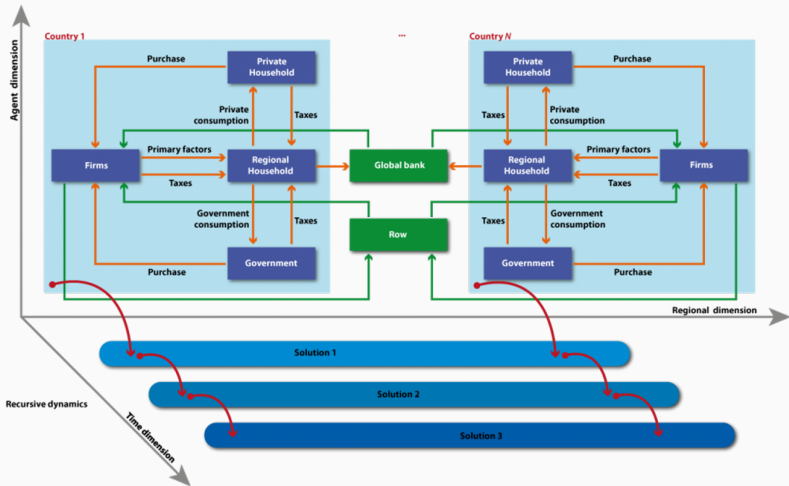
- IAMs are very useful
 - Granular representation of technologies, calibrated on real data, multi-regional perspective
 - Inter-model comparison gives us idea of uncertainty ranges
- However
 - Doubts about theoretical foundations
 - Economic modules usually very small and simple
 - Difficult to introduce macro and financial components into modelling frameworks

Computable General Equilibrium (CGE) models

- Start from actual data capturing economic inter-dependencies
 - Input-Output (IO) tables
 - Social Accounting Matrices (SAM) also include institutional accounts
 - e.g. [GTAP Database](#)
- Define a set of behavioural rules
 - Profit maximisation or cost minimisation by firms
 - Welfare maximisation by households
 - e.g. [GTAP model](#)
- Calibrate parameters on available data
 - E.g. Armington elasticity (of substitution between products of different countries)
- Introduce a change
 - E.g. a change in taxes or border tariffs
 - Observe how the system reacts to the change in prices

- They can adapted to include energy/environment
 - Impact of mitigation policies (carbon tax) or climate impacts
 - Multi-sectoral dimension is important (structural change)
 - Multi-regional dimension is important (trade impacts)
- Stylized representation of macro-financial dimension
 - All savings aggregated into a global banks that reallocates them according to relative returns
 - Crowding-out assumption (exogenous money)
- Example: ICES model (CMCC Venice)
 - Recursive model generating a sequence of static equilibria under myopic expectations
 - Derived from GTAP-E model
 - Cost-minimizing firms, representative household and government

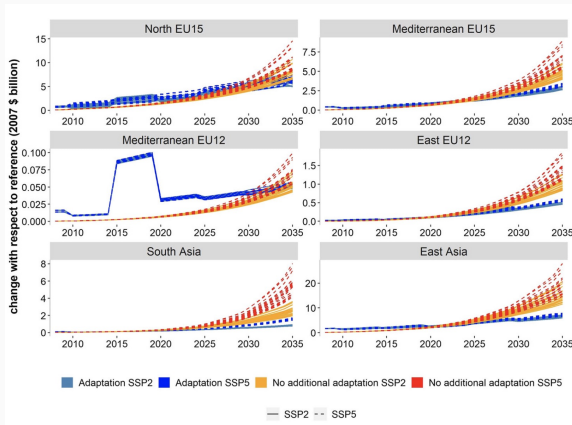
An example: the ICES model



ICES model structure. Source: [ICES website](#)

An application: Public deficit and adaptation to sea level rise

- Public spending in SLR adaptation increases deficits in the short-term but avoids larger deficits in the longer-term
- Note: total crowding-out of investments assumed



- Clear advantages, as they
 - Capture inter-sectoral and inter-regional exchanges in a dynamic setting
- However, they
 - Rely on unrealistic market clearing assumptions (in the real world, we have inefficiencies and underutilisation)
 - Given these assumptions, it's hard to introduce further macro/financial dimensions

Spatial IAMs

- Spatial IAMs (S-IAMs)
 - Climate change impacts diversified across space (see Lecture 2)
 - Migration/trade as adaptation mechanism
 - Recent literature using developments in spatial economics (see [Desmet and Rossi-Hansberg, 2024](#))
- Two-dimensional space
 - Latitude and Longitude
 - $1^\circ \times 1^\circ$ grids: 64,800 cells (locations r) in the globe
 - Data on population, output, temperature
 - Harder to split sectors: agriculture vs non-agriculture

- Location-specific utility for agent j function of consumption C , local amenities a , preference for location ϵ and possibly access cost to location ('migration costs') m

$$U_t^j(r) = a_t(r) C_t(r) \epsilon_t^j(r) m_t^j(r)^{-1}$$

- Local amenities can be made a function of climate change T and affected by congestion (too many people L)

$$a_t(r) = \bar{a}(r, T_t) L_t(r)^{-\lambda}$$

- Consumption combines goods from different industries i , each with several varieties (firms) ω

$$C_t(r) = \prod_{i=1}^I \left(\int_0^1 c_{it}^\omega(r)^\rho d\omega \right)^{\frac{\chi_i}{\rho}}$$

with ρ : elast. of sub. btw varieties; χ_i : exp. share of good i

- Firm/variety production q in industry i is a Cobb-Douglas function of k inputs with (T -affected) productivity z

$$q_{it}^{\omega}(r) = z_{it}^{\omega}(r) \prod_k F_{kit}(r)^{\mu_{ki}}$$

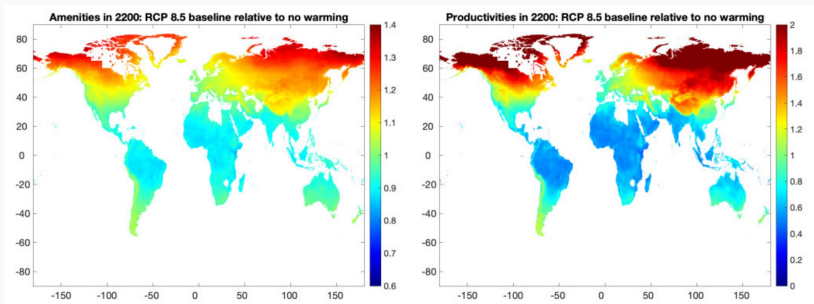
- Production inputs
 - Labor, land, energy and others
 - Capital stocks usually missing
 - Example from [Cruz and Rossi-Hansberg \(2024\)](#)

$$q_t^{\omega}(r) = \phi_t^{\omega}(r)^{\gamma_1} z_t^{\omega}(r) (L_t^{\omega}(r)^{\chi} e_t^{\omega}(r)^{1-\chi})^{\mu}$$

with ϕ : innovation

Desmet and Rossi-Hansberg (2024) results

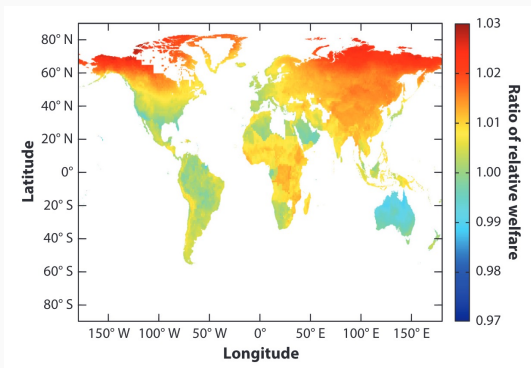
- Climate change has strongly diversified impacts across space



Ratio between amenities and productivities in 2200, RCP8.5 climate change scenario vs no climate change. Source: [Cruz and Rossi-Hansberg \(2024\)](#)

Desmet and Rossi-Hansberg (2024) results

- Adaptation by migrating, changing production structure, etc.
- Migration costs affect local welfare under climate change
 - Oceania/LAC: depopulation affects innovation attractiveness
 - Africa: depopulation reduces congestion



Ratio between welfare in baseline and scenario with 25% higher migration costs.

Source: [Desmet and Rossi-Hansberg \(2024\)](#)

Conclusions

Conclusions

- Integrated Assessment Models
 - Integrating climate and economic systems
- Small-scale analytical IAMs
 - Simplify complexity to reach analytical conclusions and/or..
 - ..incorporating dimensions from macro/finance (e.g. uncertainty)
 - Mostly rooted in economics
- Large-scale numerical IAMs
 - Capture granular dimensions across technologies/sectors/space..
 - Integrated Assessment Models (IAMs)
 - Computable General Equilibrium (CGE) models
 - Spatial IAMs