ECON899. Problem set 1

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1 Problem

Agents solve the value function

$$\begin{split} V(K,Z) &= \max_{K',C} \log(C) + \beta \mathbb{E}[V(K',Z')|Z] \\ \text{s.t. } C &= ZK^{\theta} + (1-\delta)K - K' \\ &= \max_{K'} \ \log(ZK^{\theta} + (1-\delta)K - K') + \beta \left[Pr(Z' = Z^{g}|Z)V(K',Z^{g}) + Pr(Z' = Z^{b}|Z)V(K',Z^{b}) \right] \end{split}$$

Where $Z^g=1.25$ and $Z^b=0.2$ with the following transition matrix:

$$\Pi = \begin{bmatrix} 0.977 & 0.023 \\ 0.074 & 0.926 \end{bmatrix}$$

2 Results

Q2.

Our results and graphs are coming from our Julia code. For each value of Z the value function is indeed increasing in capital K (Figure 2.1, left). It is also concave in capital since the value function changes are decreasing in capital.

Q3.

The decision rules are also increasing in K and Z (Figure 2.1, right).

We also calculate the change in the decision rules K'(K, Z) - K for both states of Z (Figure 2.2). We find that the savings is a decreasing function in the current capital level for the bad shock realization, while for the good shock realization it is a non-monotonic function

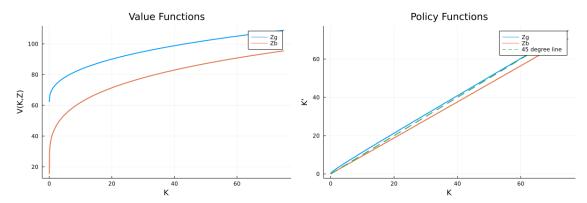


Figure 2.1: Value and policy functions for good and bad technology shocks.

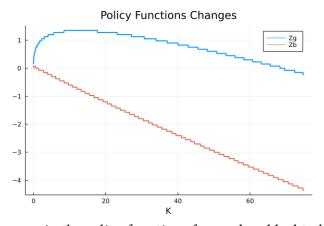


Figure 2.2: Changes in the policy functions for good and bad technology shocks.

in capital. The savings is an increasing function in the productivity shock, and in good conditions people want to invest more in tomorrow's capital, especially at low values of capital.

Comparing times

Julia solves the model in 1.179602393 seconds, and with parallelizing Julia solves the model in 3.450236762 seconds. Fortran solves the model in 362.828003 seconds. It seems to take too much time, but the results obtained from Fortran coincides with the results from Julia.