(6) a) 
$$g_{+1} = \# \circ f (+1) \text{ moves}$$

$$\frac{(g_{+1} + g_{-1})!}{g_{+1}! g_{-1}!} \qquad g_{-1} = \# \circ f (-1) \text{ moves}$$

$$g_{+1} = \# \circ f (+1) \text{ moves}$$

$$g_{+1} = \# \circ f (-1) \text{ moves}$$

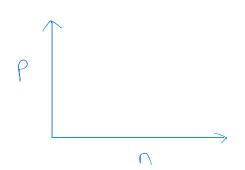
$$i) g_{+1} + g_{-1} = 2n g \implies 2g_{+1} = 2(n+k)$$

gets (i) of pernutations i) 
$$9+1+9-1=2n$$
  $= 29+1=2(n+k)$  of  $(+1) \notin (-1)$  moves i)  $9+1+9-1=2k$   $= 29-1=2(n-k)$ 

$$N(0,2K,2n) = \frac{(2n)!}{(n+K)!(n-K)!}$$

$$\Rightarrow P(\chi_{2n}=2K) = \frac{N(0,2K,2n)}{2^{t=2n}}$$

$$P(2k) = \frac{(2n)!}{2^{2n}(n+k)!(n-k)!} \equiv P$$



$$\Rightarrow ln P = ln [(2n)! ] - ln [(n+k)! ] - ln [(n-k)! ] - 2n ln 2$$

$$n! \approx \sqrt{2\pi n} \left(\frac{A}{e}\right)^n \left(\frac{Stirling's Approximation}\right)$$
 $lnn! \approx ln\sqrt{2\pi n} + nlnn - nlne$ 
 $\approx ln\sqrt{2\pi} + ln(n)' + nlnn - n$ 
 $\approx \frac{1}{2} lnn + nlnn - n + \frac{1}{2} ln 2\pi$ 
 $lnn! \approx lnn\left[\frac{1}{2} + n\right] - n + \frac{1}{2} ln 2\pi$ 
 $(\frac{Stirling's}{seconting for error})$ 

$$ln P = ln [(2n)!] - ln [(n+k)!] - ln [(n-k)!] - 2n ln 2$$

$$ln [(2n)!] = [\frac{1}{2} + 2n] ln (2n) - 2n + \frac{1}{2} ln 2\pi$$

$$ln [(n+k)!] = [\frac{1}{2} + n+k] ln (n+k) - (n+k) + \frac{1}{2} ln 2\pi$$

$$ln [(n-k)!] = [\frac{1}{2} + n-k] ln (n-k) - (n-k) + \frac{1}{2} ln 2\pi$$

$$\ln \Gamma = \left[ \frac{1}{2} + 2n \right] \ln 2n - 2n + \frac{1}{2} \ln 2\pi$$

$$- \left[ \frac{1}{2} + n + k \right] \ln (n + k) + (n + k) - \frac{1}{2} \ln 2\pi$$

$$- \left[ \frac{1}{2} + n - k \right] \ln (n - k) + (n - k) - \frac{1}{2} \ln 2\pi$$

$$- 2n \ln 2$$

let  $\ln(n+k) = \ln[n(1+\frac{k}{n})] = \ln n + \ln(1+\frac{k}{n}) \approx \ln n + \frac{k}{n} - \frac{k^2}{2n^2}$  $\stackrel{?}{\epsilon} \ln(n-k) = \ln[n(1-\frac{k}{n})] = \ln n + \ln(1-\frac{k}{n}) \approx \ln n - \frac{k}{n} - \frac{k^2}{2n^2}$ 

 $\ln P \approx \frac{1}{2} \ln 2n + 2n \ln 2n - \frac{1}{2} \ln 2\pi - 2n \ln 2$   $-\frac{1}{2} \ln n - n \ln n - \frac{1}{2} \ln n - \frac{1}{2} \ln n - \frac{1}{2} \ln \frac{1}{2} + \frac{1}{2} \ln \frac{1}{2} \ln \frac{1}{2} + \frac{1}{2} \ln \frac{1}{2}$ 

 $2 \frac{1}{2} \ln 2n + 2n \ln 2n - \frac{1}{2} \ln 2\pi - 2n \ln 2 - \ln n - 2n \ln n$   $-\frac{2K^2}{n} + \frac{K^2}{2n^2} + \frac{K^2}{n}$ 

 $\frac{1}{2} \ln 2n + 2n \ln 2n - \frac{1}{2} \ln 2\pi - 2n \ln 2 - \ln n - 2n \ln n - \frac{k^{2}}{n} + \frac{1}{2} \left(\frac{k}{n}\right)^{2}$   $\frac{1}{2} \ln 2n + 2n \ln 2n - \frac{1}{2} \ln 2n - 2n \ln 2 - \ln n - 2n \ln n - \frac{k^{2}}{n} + \frac{1}{2} \left(\frac{k}{n}\right)^{2}$   $\frac{1}{2} \ln 2n + 2n \ln 2n - \frac{1}{2} \ln 2n - 2n \ln 2 - \ln n - 2n \ln n - \frac{k^{2}}{n} + \frac{1}{2} \left(\frac{k}{n}\right)^{2}$   $\frac{1}{2} \ln 2n + 2n \ln 2n - \frac{1}{2} \ln 2n - 2n \ln 2 - \ln n - 2n \ln n - \frac{k^{2}}{n} + \frac{1}{2} \left(\frac{k}{n}\right)^{2}$   $\frac{1}{2} \ln 2n + 2n \ln 2n - \frac{1}{2} \ln 2n - 2n \ln 2 - \ln n - 2n \ln n - \frac{k^{2}}{n} + \frac{1}{2} \left(\frac{k}{n}\right)^{2}$   $\frac{1}{2} \ln 2n + 2n \ln 2n - \frac{1}{2} \ln 2n - 2n \ln 2 - \ln n - 2n \ln n - \frac{k^{2}}{n} + \frac{1}{2} \left(\frac{k}{n}\right)^{2}$   $\frac{1}{2} \ln 2n + 2n \ln 2n - \frac{1}{2} \ln 2n - \frac{$ 

$$P(x) = \frac{1}{\sqrt{n\pi}} e^{-\frac{x^2}{4}}$$

$$= \sqrt{\frac{x^2}{4}} e^{-\frac{x^2}{4}}$$

$$= \sqrt{\frac{x^2}{4}} e^{-\frac{x^2}{4}}$$

$$P(x) = \frac{z}{\sqrt{n\pi}} e^{-\frac{x^2}{4}}$$

N= 
$$\frac{(g_{+1}+g_{-1})!}{g_{+1}!g_{-1}!}$$
 Same distribution as previous problems but with different conditions on displacement è time.

$$N = \left[\frac{1}{2}(zt)\right].$$

$$\left(\frac{1}{2}(t+j-i)\right)\left[\frac{1}{2}(t-j+i)\right].$$

$$N = \frac{\{t\}}{\{t+j-i\}} = \left(\frac{t}{2}(t+j-i)\right)$$

$$\left(\frac{1}{2}(t+j-i)\right)$$

8) 
$$N(1,1,2n-2) = \left(\frac{2n-2}{(2n-2+1-1)/2}\right)$$

$$N(1,1,2n-2) = \begin{pmatrix} 2n-2 \\ n-1 \end{pmatrix}$$

$$N\left(-1,1,2n-2\right) = \begin{pmatrix} 2n-2 \\ n \end{pmatrix}$$

$$Nf_{n}(2n) = {2n-2 \choose n-1} - {2n-2 \choose n}$$

$$= \frac{(2n-2)!}{(n-1)!(n-1)!} - \frac{(2n-2)!}{n!(n-2)!}$$

$$= \frac{n!(n-2)!(2n-2)! - (2n-2)!(n-1)!(n-1)!}{n!(n-2)!(n-1)!(n-1)!}$$

$$= \frac{n(n-1)!(n-2)!(2n-2)!-(2n-2)!(n-1)!}{n!(n-2)!(n-1)!(n-1)!}$$

$$= (2n-2)! \left[ \frac{(n-2)! - (n-1)!}{n! (n-2)! (n-0)!} \right]$$

$$= (2n-2)! \left[ \frac{(n-1)!}{n! (n-1)!} - (n-1)! (n-1)! \right]$$

$$= (2n-2)! \left[ \frac{1-n+1}{n! (n-1)!} \right]$$

$$Nfr(2n) = \frac{(2n-2)!}{n! (n-1)!} (2-n)$$

$$= \ln Nfr = \ln (2n-2)! - \ln n! - \ln (n-1)! + \ln (2-n)$$

$$= \ln Nfr = \ln (2n-2)! - \ln n! - \ln (n-1)! + \ln (2-n)$$

$$= \ln Nfr \approx \left[ \frac{1}{2} + 2n - 2 \right] \ln (2n-2) - (2n-2) + \frac{1}{2} \ln 2\pi$$

$$= \left[ \frac{1}{2} + n - 1 \right] \ln (n-1) + (n-1) - \frac{1}{2} \ln 2\pi + \ln (2-n)$$

$$\approx \left[ 2n - \frac{2}{2} \right] \ln (2n-2) - 2n + 2$$

$$= \left[ n + \frac{1}{2} \right] \ln n + \ln$$

$$= \left[ n - \frac{1}{2} \right] \ln (n-1) + \ln - \frac{1}{2} \ln 2\pi + \ln (2-n)$$

$$\lim_{n\to\infty} \operatorname{Nfr}(2n) \approx \lim_{n\to\infty} \frac{2^{2n-3/2}}{\sqrt{2\pi} n^{3/2}} \left(1-\frac{1}{n}\right)^{n-1} e$$

$$\lim_{n\to\infty} \frac{2^{2n-3/2}}{\sqrt{2\pi} n^{3/2}} \lim_{n\to\infty} \left(1-\frac{1}{n}\right)^{n-1} e$$

$$\lim_{N \to \infty} Nfr(2n) \sim \lim_{N \to \infty} \frac{2^{2n-3/2}}{\sqrt{2\pi} n^{3/2}}$$

$$\frac{2n-3/2}{2}$$

$$\frac{2}{2}$$

$$\frac{2}{2}$$

$$\frac{2}{2}$$

$$\frac{2}{2}$$

$$\frac{3}{2}$$