

# Equations of the humid air

Here the list of equations governing the physics properties of the humid air:

- vapour pressure parametrization for water :  $p_v$  (vapour pressure of the water) [Pa] as a function of the dry temperature  $T$  [K] [Buck (1981), J. Appl. Meteorol., 20: 1527-1532]

$$p_v(T) = \exp \left[ a_{-1}/T + a_0 + a_1T + a_2T^2 + a_3T^3 + a_4 \log(T) \right] \quad (1)$$

with the following coefficients:

$a_{-1}$	$-5.8002206 \times 10^{+3}$
$a_0$	1.3914993
$a_1$	$-4.8640239 \times 10^{-2}$
$a_2$	$4.1764768 \times 10^{-5}$
$a_3$	$-1.4452093 \times 10^{-8}$
$a_4$	6.5459673

- Relative humidity  $rh$  [no unit] as a function of the dry temperature  $T$  [K], the pressure  $p_0$  [Pa] and the absolute humidity  $ah$  [kg water / kg dry air]:

$$rh = \frac{\mu}{1 - (1 - \mu) \frac{p_v(T)}{p_0}} \text{ where } \mu = \frac{ah}{w} \cdot \left( \frac{p_0}{p_v(T)} - 1 \right) \quad (2)$$

- The previous relation can be inverted in order to express the absolute humidity  $ah$  [kg water / kg dry air] as a function of the dry temperature  $T$  [K], the pressure  $p_0$  [Pa] and the relative humidity  $rh$  [no unit]:

$$ah = \frac{w \cdot \mu}{\frac{p_0}{p_v(T)} - 1} \text{ where } \mu = rh \cdot \frac{p_0 - p_v(T)}{p_0 - rh \cdot p_v(T)} \quad (3)$$

- Specific volume  $v$  as a function of the dry temperature  $T$  [K] and the absolute humidity  $r$  [kg water / kg dry air]:

$$v = \frac{RT \left( 1 + \frac{ah}{w} \right)}{M_a \cdot p_0} \quad (4)$$

- Density  $\rho$  as a function of the specific volume  $v$ :

$$\rho = 1/v \quad (5)$$

- Specific enthalpy  $h$  as function of the dry temperature  $T$  [K] and the absolute humidity  $ah$  [kg water / kg dry air]:

$$h = 2501 \cdot ah + (1.805 \cdot ah + 1.006)(T - 273.15) \quad (6)$$

**Constants:**

$R$	ideal gas constant	8.3144621 J/mol/K
$M_a$	molar mass of dry air	$28.9653 \times 10^{-3}$ kg/mol
$M_w$	molar mass of water	$18.0153 \times 10^{-3}$ kg/mol
$w$	ratio of molar masses	$M_w/M_a$

**Physics observables:**

$ah$	absolute humidity [kg water / kg dry air]
$rh$	relative humidity [no unit]
$h$	specific enthalpy [J / kg dry air]
$v$	specific volume [m <sup>3</sup> / kg dry air]
$\rho$	density [kg dry air / m <sup>3</sup> ]
$T$	dry temperature [K]
$p_v$	vapour pressure of water [Pa]
$p_0$	total pressure [Pa]