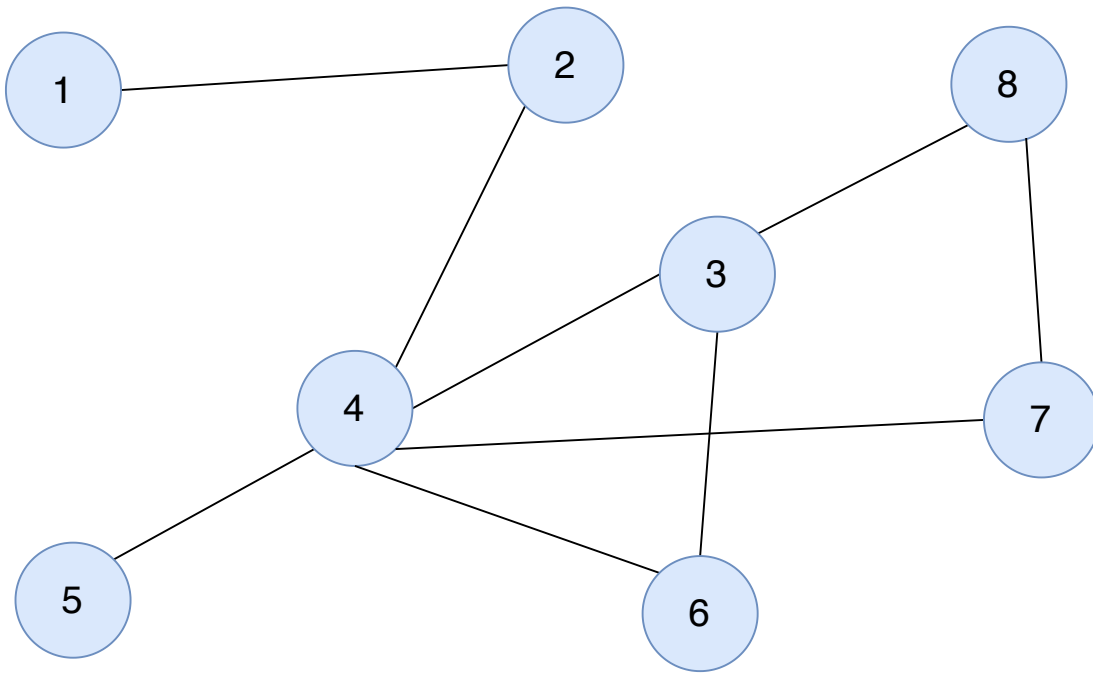


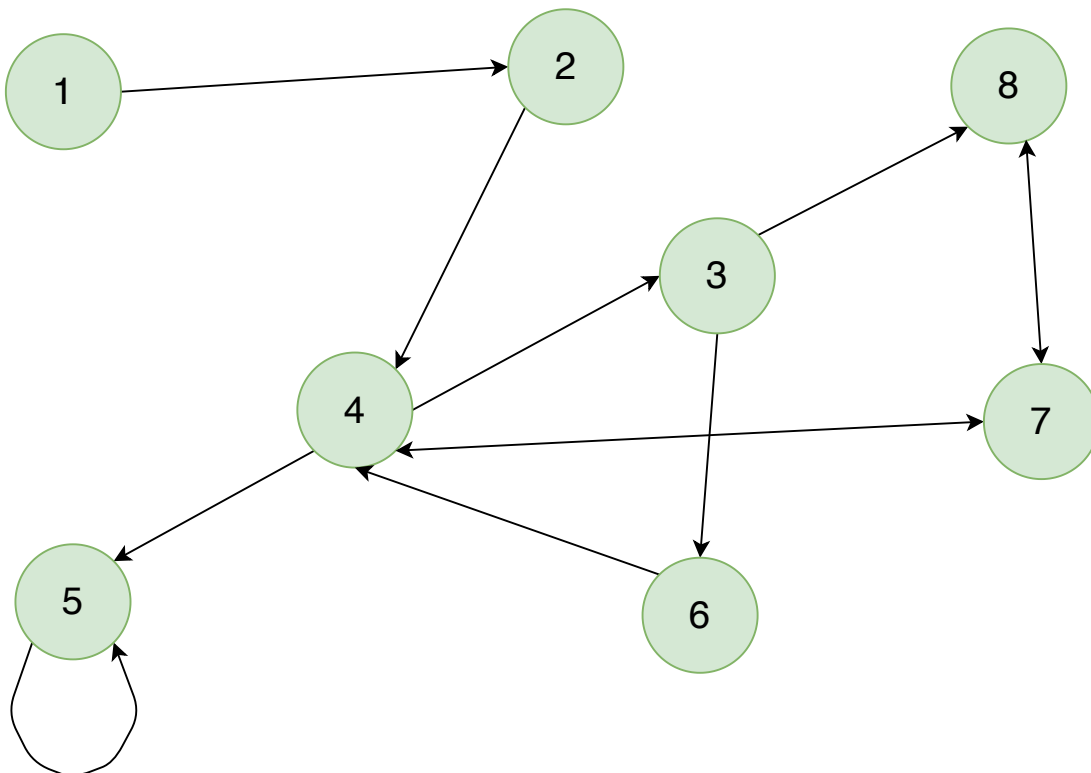
Graph Theory

Undirected Graph



Example:
Friends on Facebook

Directed Graph

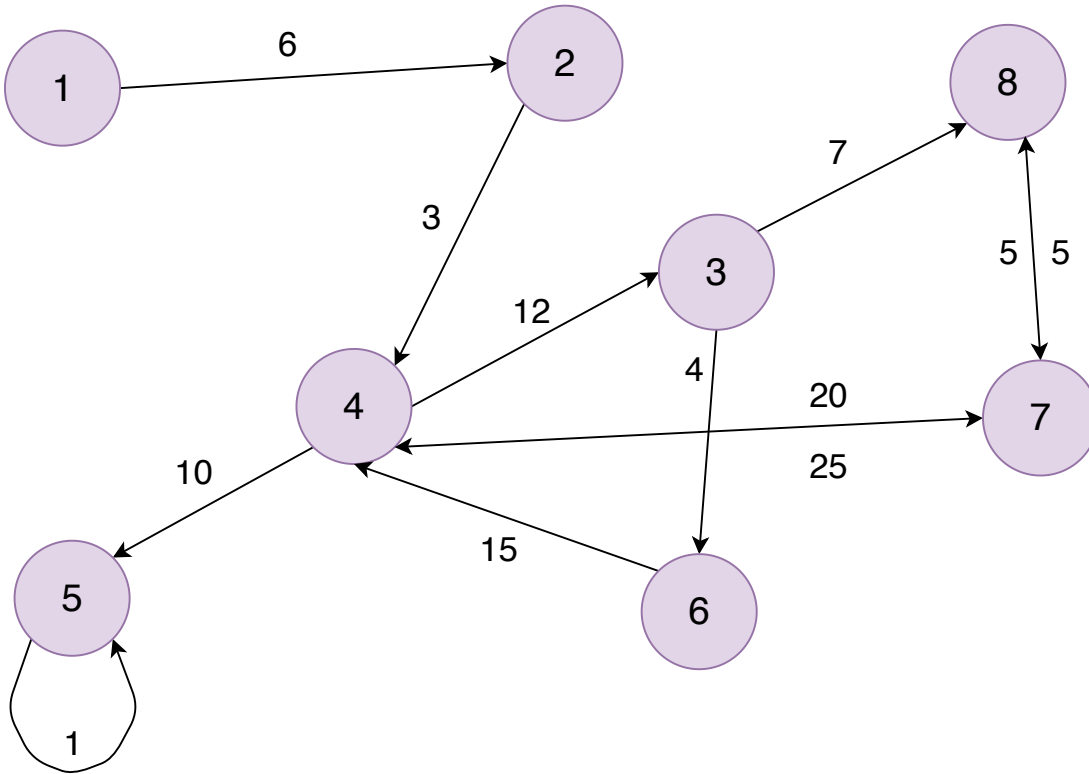


Example:
Followers on instagram
People giving each other gifts
Roads with 1 way streets

Weighted Graph

(Can Be **Undirected** or **Directed**)

Example:
Roads with Traffic



Other Types of Graphs

Tree

Rooted Tree

In-Tree (anti-arborescence)

Out-Tree (arborescence)

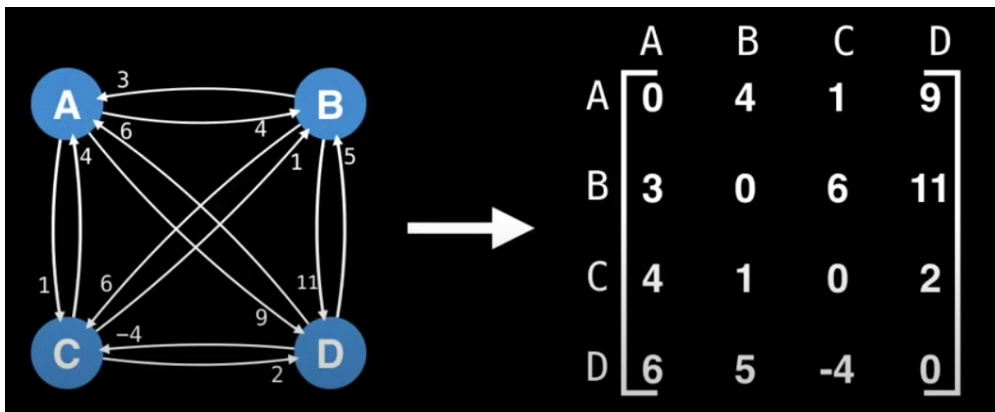
Directed Acyclic Graph (DAGs)

Bipartite Graph

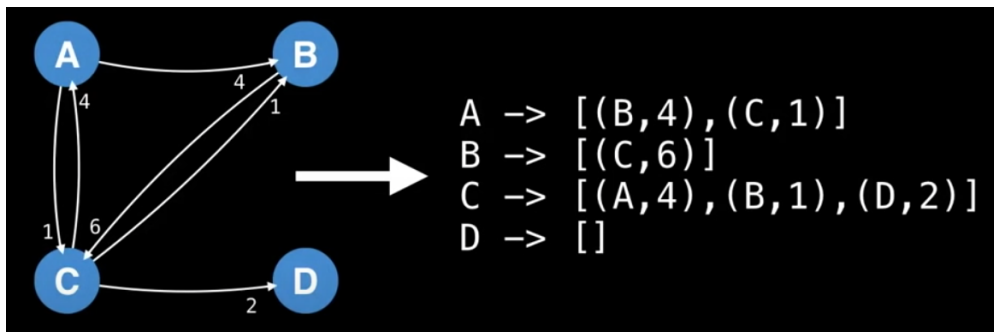
Complete Graph

How To Represent a Graph

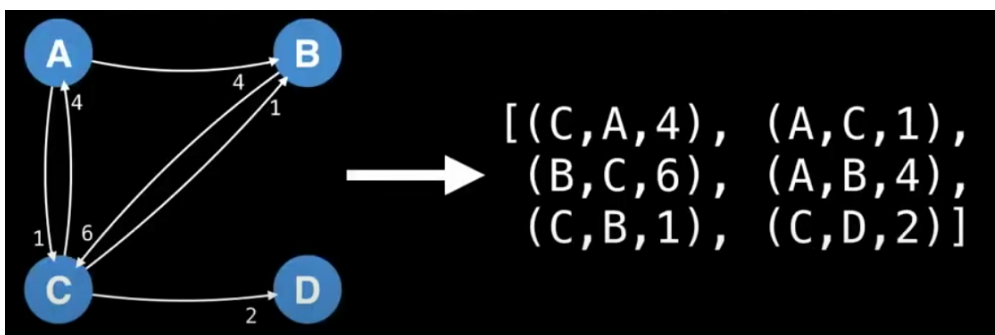
Adjacent Matrix



Adjacent List



Edge List



There are many different ways to represent a graph. The representation of a graph will always depend on its size, its type, whether it is directed, whether it is weighted, and more. For an undirected graph, I use a dictionary to represent the nodes.

Algorithms Used For Graphs

Depth-first search	(Connectivity)
Breadth-first search	(Connectivity)
Dijkstra's	(Shortest path)
A*	(Shortest path)
Bellman-Ford	(Shortest path) Or (Detect Negative Cycles)
Floyd-Warshall	(Shortest path) Or (Detect Negative Cycles)
Tarjan's	(Strongly Connected Components)
Kosaraju's	(Strongly Connected Components)
Held-Karp	(approximation) <small>Used to solve Traveling Salesman Problems (TSPs)</small>
Branch and Bound	(approximation) <small>Used to solve Traveling Salesman Problems (TSPs)</small>
Kruskal's	(Finding Minimum Spanning Trees (MSTs))
Prim's	(Finding Minimum Spanning Trees (MSTs))
Boruvka's	(Finding Minimum Spanning Trees (MSTs))
Ford-Fulkerson	(Network Flow: Max Flow)
Edmonds-Karp	(Network Flow: Max Flow)
Dinic's	(Network Flow: Max Flow)