

# Learning Java by Design Examples

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PROJECT 10: INDEXING

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ACTIVITY 1

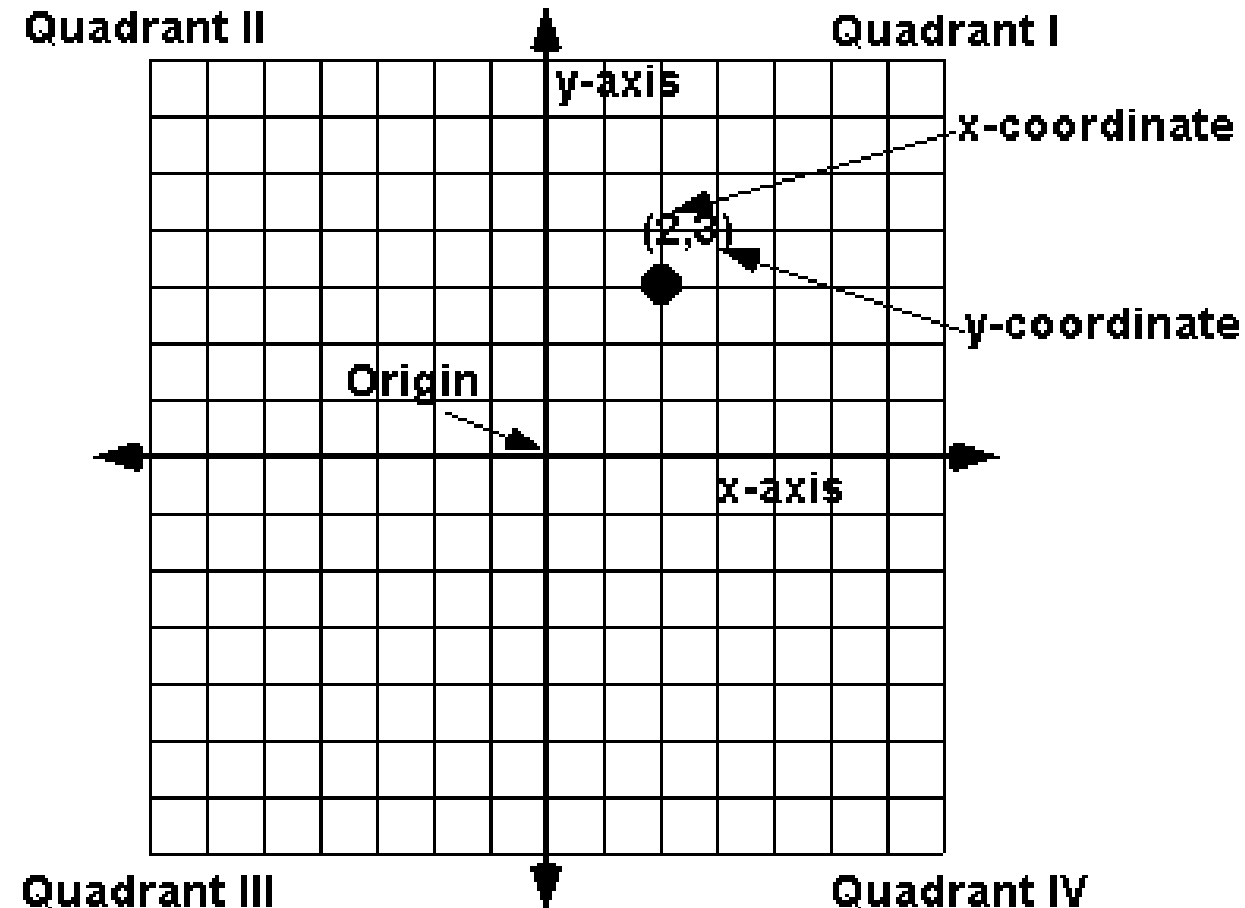
# Discrete Space

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# Cartesian Coordinate

## Continuous Space





# Base and local index

$n-i$	-8	-7	-6	-5	-4	-3	-2	-1	0
$b+i$	4	5	6	7	8	9	10	11	12
$i$	0	1	2	3	4	5	6	7	8

$$\begin{aligned}\text{Index} &= \text{Base} + \text{local\_Index} \\ &= b + i\end{aligned}$$

$$\begin{aligned}\text{Index} &= \text{Length} - \text{local\_neg\_Index} \\ &= n - i\end{aligned}$$

$$\text{Base} = b = 4, \text{ Length} = n = a.\text{length}$$



# Indexing for ASCII code

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- Total number of ASCII letters:  $'Z' - 'A' + 1$  (alphabet size)
- Indexing for a letter ('B'):  $'A' + ('B' - 'A')$
- Traversing through the whole alphabet:  $'A' + i$ ;  $i$  is from 0 to 25
- Letter indexing is also used for histogram:  $a['X' - 'A']$  to store the number of occurrence for the letter 'X'



Sum up an array of 8 elements with index from the last element to the first.

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Write a program to sum up

```
Int[] a = {1, 2, 3, 4, 5, 6, 7, 8};
```

starting from 8 down to 1 with proper indexing.

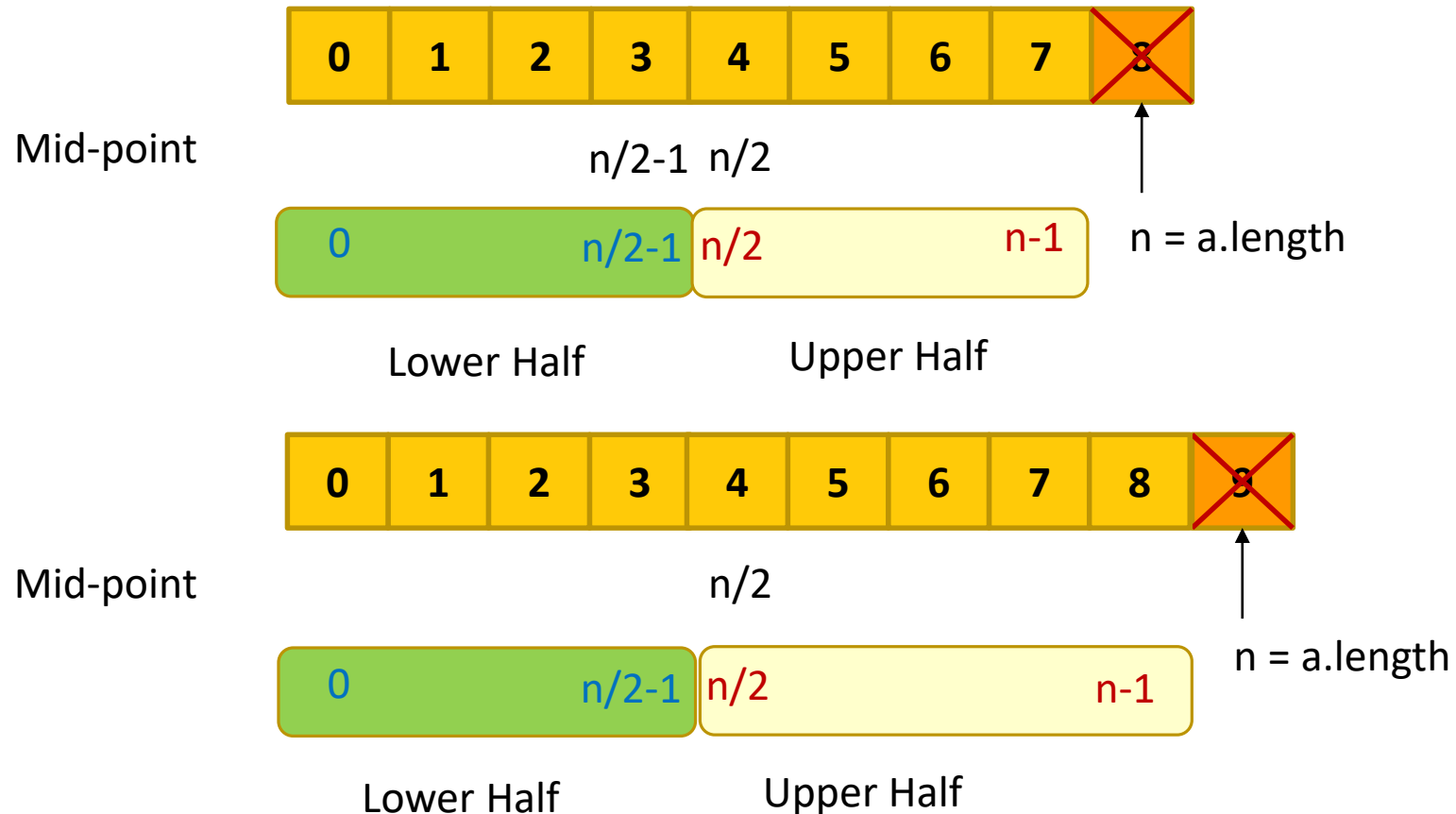
ACTIVITY 2

# Half an Array

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# Divide an array into half







## Activity 2:

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Divide an index space from 0 to  $n-1$  (totally  $n$  elements) into two halves. If  $n$  is odd, the first half should be shorter.

Write a program and enter a number  $n$  from console. Print the first half with letter “\*”, the second half with letter “#”. If  $n$  is odd, “\*” should be one less than “#”.

```
BlueJ: Terminal Window - Project10_Indexing
Options
Enter a number:11
*****#####
```

```
BlueJ: Terminal Window - Project10_Indexing
Options
Enter a number:10
*****#####
*****#####
```

ACTIVITY 3

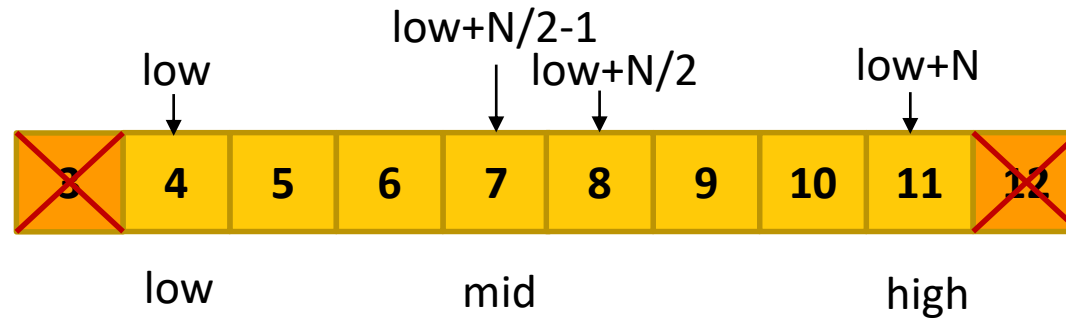
# Binary Search

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# low and high

$low + N/2$  is high middle  
( $low + high$ ) is low middle

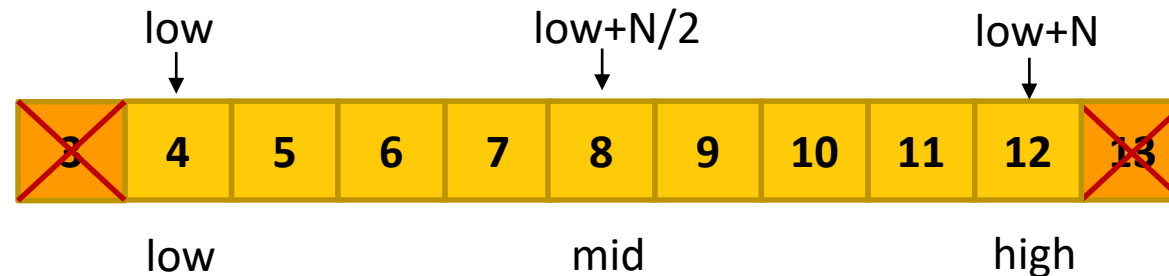


$mid$  is the end of first half

$$N = \text{Length} = \text{high} - \text{low} + 1 = \text{high} - (\text{low} - 1) = 11 - 4 + 1 = 11 - 3 = 8$$

$$\text{mid} = (\text{low} + \text{high}) / 2 = (2 * \text{low} + N - 1) / 2 = \text{low} + (N - 1) / 2$$

$$\text{First Half} = [\text{low}, \text{low} + N/2 - 1], \text{Second Half} = [\text{low} + N/2, \text{low} + N - 1]$$



$$\text{Length} = \text{high} - \text{low} + 1 = \text{high} - (\text{low} - 1) = 11 - 4 + 1 = 11 - 3 = 8$$

$$\text{mid} = (\text{low} + \text{high}) / 2$$



# Activity 4:

index	0	1	2	3	4	5	6	7
a[]	3	8	12	16	23	27	34	38

low                      mid      mid+1                      high

low      mid      high

low      high

Find the index for the key=28.  
If it is not found, return -1.

$\text{mid} = (\text{low} + \text{high}) / 2$   
*Note: low middle is used in here.*

Stop when found

(When  $\text{high} == \text{low}$ , stop return whatever)

# Activity 3: Find the index of a key value in an Array

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Write a program to find the index of a search key. If not found, return -1. Try the following two arrays.

Pre-condition, the array is already sorted.

```
static int[] a = {3, 8, 12, 16, 23, 34, 37, 38};  
static int[] b = {3, 8, 12, 16, 23, 34, 37, 38, 60};
```

ACTIVITY 4

# Pyramid Problem

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## Activity 3:

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### **NumberPyramid**

Using nested loops, print the following.

-----1-----

-----333-----

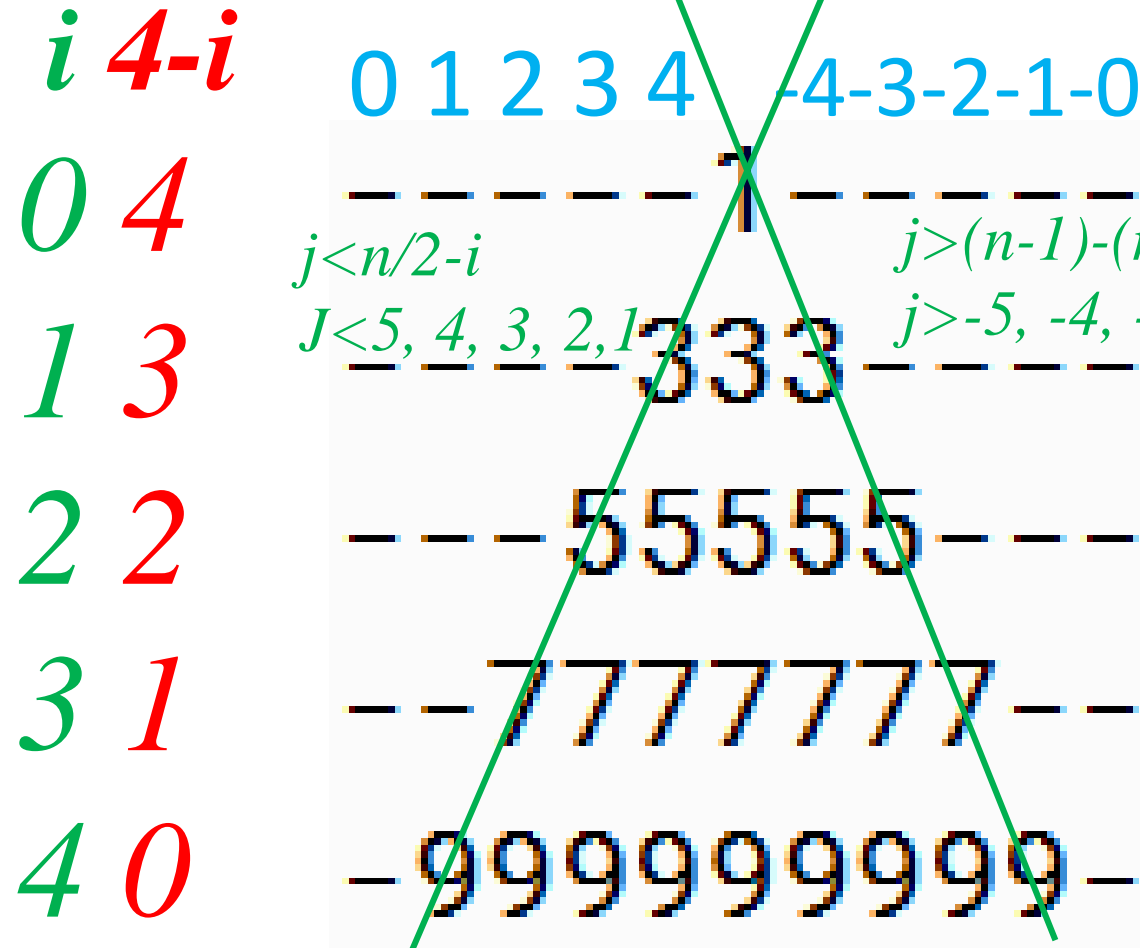
---55555---

--7777777--

-999999999-



$n=11$



$i = 0 \ 1 \ 2 \ 3 \ 4$

$n-i = -5 - 4 - 3 - 2 - 1$

$(n-1)-i = -4 - 3 - 2 - 1 \ 0$

$last-i = -4 - 3 - 2 - 1 \ 0$

```
for (int i=0; i<5; i++)  
    for (int j=0; j<11; j++)  
         $n==11, n/2 == 5$ 
```



ACTIVITY 5

# Divide and Conquer

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# Activity 5:

Many of the patterns we have seen for traversing arrays can also be written recursively. It is not common, but it is a useful exercise.

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1. Write a method called **maxInRange** that takes an array of integers and two indexes, **lowIndex** and **highIndex**, and finds the maximum value in the array, but only considering the elements between **lowIndex** and **highIndex**, including both.
  - This method should be recursive. If the length of the range is 1, that is, if **lowIndex == highIndex**, we know immediately that the sole element in the range must be the maximum. So that's the base case.
  - If there is more than one element in the range, we can break the array into two pieces, find the maximum in each of the pieces, and then find the maximum of the maxima.



## Activity 5: Think Java Exercise 8-8

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1. Methods like **maxInRange** can be awkward to use. To find the largest element in an array, we have to provide the range for the entire array.

```
double max = maxInRange(a, 0, a.length - 1);
```

Write a method called **max** that takes an array and uses **maxInRange** to find and return the largest element.

ACTIVITY 6

# Summary

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# Summary

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Concepts covered in this lab:

1. Positive indexing and negative indexing (Count up and count down)
2. Calculation of array length (high-low+1)
3. Mid-point: low mid-point and high mid-point and their application.

$$\textbf{(low+high)/2, low+N/2}$$

4. Divide the array into half. [low, low+N/2-1], [low+N/2, high]
5. Binary Search ( $\text{mid} = (\text{low} + \text{high}) / 2$ )
6. In range operation (Divide and conquer) for recursive or iterative operation.