# **AP** Computer Science A

# Practice Exam #1 and Notes

For the Spring 2020 Exam

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# **Practice Exam**

# Exam Content and Format

The AP Computer Science A Exam is 3 hours long. There are two sections:

- Section I is 1 hour, 30 minutes and consists of 40 multiple-choice questions, accounting for 50 percent of the final score.
- Section II is 1 hour, 30 minutes and consists of 4 free-response questions accounting for 50 percent of the final score.

# Administering the Practice Exam

This section contains instructions for administering the AP Computer Science A Practice Exam. You may wish to use these instructions to create an exam situation that resembles an actual administration. If so, read the indented, boldface directions to the students; all other instructions are for administering the exam and need not be read aloud. Before beginning testing, have all exam materials ready for distribution. These include test booklets and answer sheets. (Reminder: Final instructions for every AP Exam are published in the AP Exam Instructions book.)

# **SECTION I: Multiple Choice**

When you are ready to begin Section I, say:

Section I is the multiple-choice portion of the exam. Mark all of your responses on your answer sheet, one response per question. If you need to erase, do so carefully and completely. Your score on the multiple-choice section will be based solely on the number of questions answered correctly.

You have 1 hour and 30 minutes for this part. Open your Section I booklet and begin.

Note Start Time	Note Stop Time	After 1 hour and
20 minutes, say:		

There are 10 minutes remaining.

After 10 minutes, say:

Stop working. I will now collect your Section I booklet and multiple-choice answer sheet.

There is a 10-minute break between Sections I and II.

#### **SECTION II: Free Response, Questions**

After the break, say:

Section II is the free-response portion of the exam.

You have 1 hour and 30 minutes to complete Section II. You may use any blank space of the page the questions or documents are printed on to organize your answers and for scratch work. You must write your answers in the answer booklet for free-response questions. At the top of each page in your booklet you must fill in the circle that indicates the question number you are answering. Open your Section II booklet and begin.

Note Start Time	Note Stop Time	After 1 hour and
20 minutes, say		

There are 10 minutes remaining.

After 10 minutes, say:

Stop working and close your exam booklet. Put your exam booklet on your desk, face up. Remain in your seat, without talking, while the exam materials are collected.

Collect a Section II booklet from each student and check that each student wrote his or her answers on the pages corresponding to each question. Then say:

The exam is over. You are now dismissed.

Name:	

# AP® Computer Science A Answer Sheet for Multiple-Choice Section

No.	Answer
1	
2	
3	
4	
5	
6	
7	
8	
9	
10	
11	
12	
13	
14	
15	
16	
17	
18	
19	
20	

No.	Answer
21	
22	
23	
24	
25	
26	
27	
28	
29	
30	
31	
32	
33	
34	
35	
36	
37	
38	
39	
40	

# AP® Computer Science A Exam

# **SECTION I: Multiple Choice**

### DO NOT OPEN THIS BOOKLET UNTIL YOU ARE TOLD TO DO SO.

# At a Glance

#### **Total Time**

1 hour and 30 minutes **Number of Questions** 

 $\begin{array}{c} \textbf{Percent of Total Score} \\ 50\% \end{array}$ 

Writing Instrument
Pencil required

Electronic Device
None allowed

#### **Instructions**

The Java Quick Reference is located inside the front cover of this booklet.

Section I of this exam contains 40 multiple-choice questions.

Indicate all of your answers to the multiple-choice questions on the answer sheet. No credit will be given for anything written in this exam booklet, but you may use the booklet for notes or scratch work.

Use your time effectively, working as quickly as you can without losing accuracy. Do not spend too much time on any one question. Go on to other questions and come back to the ones you have not answered if you have time. It is not expected that everyone will know the answers to all of the multiple-choice questions.

Your total score on the multiple-choice section is based only on the number of questions answered correctly. Points are not deducted for incorrect answers or unanswered questions.

# **Java Quick Reference**

Accessible methods from the Java library that may be included in the exam

Class Constructors and Methods	Explanation
	String Class
String(String str)	Constructs a new String object that represents the same sequence of characters as str
int length()	Returns the number of characters in a String object
String substring(int from, int to)	Returns the substring beginning at index from and ending at index to - 1
String substring(int from)	Returns substring(from, length())
int indexOf(String str)	Returns the index of the first occurrence of str; returns -1 if not found
boolean equals(String other)	Returns true if this is equal to other; returns false otherwise
int compareTo(String other)	Returns a value <0 if this is less than other; returns zero if this is equal to other; returns a value >0 if this is greater than other
	Integer Class
Integer(int value)	Constructs a new Integer object that represents the specified int value
Integer.MIN_VALUE	The minimum value represented by an int or Integer
Integer.MAX_VALUE	The maximum value represented by an int or Integer
int intValue()	Returns the value of this Integer as an int
	Double Class
Double(double value)	Constructs a new Double object that represents the specified double value
double doubleValue()	Returns the value of this Double as a double
	Math Class
static int abs(int x)	Returns the absolute value of an int value
static double abs(double x)	Returns the absolute value of a double value
static double pow(double base, double exponent)	Returns the value of the first parameter raised to the power of the second parameter
<pre>static double sqrt(double x)</pre>	Returns the positive square root of a double value
static double random()	Returns a double value greater than or equal to 0.0 and less than 1.0
	ArrayList Class
int size()	Returns the number of elements in the list
boolean add(E obj)	Appends obj to end of list; returns true
<pre>void add(int index, E obj)</pre>	Inserts obj at position index (0 <= index <= size), moving elements at position index and higher to the right (adds 1 to their indices) and adds 1 to size
E get(int index)	Returns the element at position index in the list
E set(int index, E obj)	Replaces the element at position index with obj; returns the element formerly at position index
E remove(int index)	Removes element from position index, moving elements at position index + 1 and higher to the left (subtracts 1 from their indices) and subtracts 1 from size; returns the element formerly at position index
	Object Class
boolean equals(Object other)	
String toString()	

NO TEST MATERIAL ON THIS PAGE

# **COMPUTER SCIENCE A SECTION I**

# Time—1 hour and 30 minutes **40 Questions**

**Directions:** Determine the answer to each of the following questions or incomplete statements, using the available space for any necessary scratch work. Then decide which is the best of the choices given and then enter the letter in the corresponding space on the answer sheet. No credit will be given for anything written in the exam booklet. Do not spend too much time on any one problem.

## Notes:

- Assume that the classes listed in the Java Quick Reference have been imported where appropriate.
- Assume that declarations of variables and methods appear within the context of an enclosing class.
- Assume that method calls that are not prefixed with an object or class name and are not shown within a complete class definition appear within the context of an enclosing class.
- Unless otherwise noted in the question, assume that parameters in method calls are not null and that methods are called only when their preconditions are satisfied.

1. Consider the following code segment.

```
int a = 3 + 2 * 3;
int b = 4 + 3 / 2;
int c = 7 % 4 + 3;
double d = a + b + c;
```

What is the value of d after the code segment is executed?

- (A) 14.0
- (B) 18.0
- (C) 20.0
- (D) 20.5
- (E) 26.0

2. Consider the following code segment. Assume num is a properly declared and initialized int variable.

```
if (num > 0)
{
    if (num % 2 == 0)
    {
        System.out.println("A");
    }
    else
    {
        System.out.println("B");
    }
}
```

Which of the following best describes the result of executing the code segment?

- (A) When num is a negative odd integer, "B" is printed; otherwise, "A" is printed.
- (B) When num is a negative even integer, "B" is printed; otherwise, nothing is printed.
- (C) When num is a positive even integer, "A" is printed; otherwise, "B" is printed.
- (D) When num is a positive even integer, "A" is printed; when num is a positive odd integer, "B" is printed; otherwise, nothing is printed.
- (E) When num is a positive odd integer, "A" is printed; when num is a positive even integer, "B" is printed; otherwise, nothing is printed.

3. Consider the method getHours, which is intended to calculate the number of hours that a vehicle takes to travel between two *mile markers* on a highway if the vehicle travels at a constant speed of 60 miles per hour. A mile marker is a sign showing the number of miles along a road between some fixed location (for example, the beginning of a highway) and the current location.

The following table shows two examples of the intended behavior of getHours, based on the int parameters marker1 and marker2.

marker1	marker2	Return Value
100	220	2.0
100	70	0.5

Consider the following implementation of getHours.

```
public static double getHours(int marker1, int marker2)
   /* missing statement */
   return hours;
```

Which of the following statements can replace /\* missing statement \*/ so getHours works as intended?

```
(A) double hours = (Math.abs(marker1) - Math.abs(marker2)) / 60.0;
```

```
(B) double hours = Math.abs(marker1 - marker2 / 60.0);
```

```
(C) double hours = Math.abs(marker1 - marker2) / 60.0;
```

```
(D) double hours = Math.abs((marker1 - marker2) / 60);
```

```
(E) double hours = (double) (Math.abs(marker1 - marker2) / 60);
```

4. Consider the following method.

```
public static void message(int a, int b, int c)
{
    if (a < 10)
    {
        if (b < 10)
        {
            System.out.print("X");
        }
        System.out.print("Y");
    }
    if (c < 10)
    {
        if (b > 10)
        {
            System.out.print("Y");
        }
        else
        {
            System.out.print("Z");
        }
    }
}
```

What is printed as a result of the call message (5, 15, 5) ?

- (A) XY
- (B) XYZ
- (C) Y
- (D) YY
- (E) Z

5. Consider the following class definition.

```
public class Bird
{
   private String species;
   private String color;
   private boolean canFly;
   public Bird(String str, String col, boolean cf)
      species = str;
      color = col;
      canFly = cf;
   }
}
```

Which of the following constructors, if added to the Bird class, will cause a compilation error?

```
(A) public Bird()
   {
      species = "unknown";
      color = "unknown";
      canFly = false;
   }
(B) public Bird(boolean cf)
      species = "unknown";
      color = "unknown";
      canFly = cf;
(C) public Bird(String col, String str)
       species = str;
      color = col;
      canFly = false;
   }
```

```
(D) public Bird(boolean cf, String str, String col)
{
    species = str;
    color = col;
    canFly = cf;
}

(E) public Bird(String col, String str, boolean cf)
{
    species = str;
    color = col;
    canFly = cf;
}
```

6. Which of the following expressions evaluate to 3.5?

```
I. (double) 2 / 4 + 3II. (double) (2 / 4) + 3III. (double) (2 / 4 + 3)
```

- (A) I only
- (B) III only
- (C) I and II only
- (D) II and III only
- (E) I, II, and III

7. Consider the following code segment.

```
int num = /* initial value not shown */;
boolean b1 = true;
if (num > 0)
   if (num >= 100)
   {
      b1 = false;
}
else
   if (num >= -100)
      b1 = false;
   }
}
```

Which of the following statements assigns the same value to b2 as the code segment assigns to b1 for all values of num?

```
(A) boolean b2 = (num > -100) \&\& (num < 100);
(B) boolean b2 = (num > -100) | (num < 100);
(C) boolean b2 = (num < -100) | (num > 100);
(D) boolean b2 = (num < -100) && (num > 0 | | num < 100);
(E) boolean b2 = (num < -100) \mid | (num > 0 && num < 100);
```

8. Consider the following class definition.

```
public class Points
{
   private double num1;
   private double num2;
                                              // Line 6
   public Points(int n1, int n2)
                                              // Line 8
      num1 = n1;
                                              // Line 9
      num2 = n2;
   public void incrementPoints(int value) // Line 12
                                              // Line 14
      n1 += value;
                                              // Line 15
      n2 += value;
   }
}
```

The class does not compile. Which of the following identifies the error in the class definition?

- (A) In line 6, the Points constructor must have a void return type.
- (B) In lines 8 and 9, int values cannot be assigned to double variables.
- (C) In line 12, the incrementPoints method must have a non-void return type.
- (D) In lines 14 and 15, the variables n1 and n2 are not defined.
- (E) In lines 14 and 15, the variable value is not defined.

9. Consider the following code segment.

```
ArrayList<Integer> numList = new ArrayList<Integer>();
numList.add(3);
numList.add(2);
numList.add(1);
numList.add(1, 0);
numList.set(0, 2);
System.out.print(numList);
```

What is printed by the code segment?

- (A) [1, 3, 0, 1]
- (B) [2, 0, 2, 1]
- (C) [2, 0, 2, 3]
- (D) [2, 3, 2, 1]
- (E) [3, 0, 0, 1]

10. Consider the following method.

```
public static void printSome(int num1, int num2)
   for (int i = 0; i < num1; i++)
      if (i % num2 == 0 && i % 2 == 0)
         System.out.print(i + " ");
      }
   }
}
```

Which of the following method calls will cause "0 10" to be printed?

- (A) printSome(0, 20)
- (B) printSome(5, 10)
- (C) printSome(10, 5)
- (D) printSome(20, 5)
- (E) printSome(25, 5)

GO ON TO THE NEXT PAGE.

```
11. Which of the following code segments produces the output "987654321" ?
   (A) int num = 10;
       while (num > 0)
           System.out.print(num);
           num--;
        }
   (B) int num = 10;
       while (num >= 0)
           System.out.print(num);
           num--;
   (C) int num = 10;
       while (num > 1)
        {
           num--;
           System.out.print(num);
        }
   (D) int num = 10;
       while (num >= 1)
           num--;
           System.out.print(num);
        }
   (E) int num = 0;
       while (num <= 9)
        {
           System.out.print(10 - num);
           num++;
        }
```

12. Consider the following class definitions.

```
public class Person
{
   private String name;
   public String getName()
   { return name; }
}
public class Book
   private String author;
   private String title;
   private Person borrower;
   public Book(String a, String t)
      author = a;
      title = t;
      borrower = null;
   }
   public void printDetails()
   {
      System.out.print("Author: " + author + " Title: " + title);
      if ( /* missing condition */ )
         System.out.println(" Borrower: " + borrower.getName());
      }
   }
   public void setBorrower(Person b)
   { borrower = b; }
}
```

Which of the following can replace /\* missing condition \*/ so that the printDetails method CANNOT cause a run-time error?

- I. !borrower.equals(null)
- II. borrower != null
- III. borrower.getName() != null
- (A) I only
- (B) II only
- (C) III only
- (D) I and II
- (E) II and III

- 13. Assume that a, b, and c are boolean variables that have been properly declared and initialized. Which of the following boolean expressions is equivalent to ! (a && b) | | c?
  - (A) a && b && c
  - (B) a || b || c
  - (C) !a && !b | c
  - (D) !a && !b && c
  - (E) !a || !b || c

- The following categories are used by some researchers to categorize zip codes as urban, suburban, or rural based on population density.
  - An urban zip code is a zip code with more than 3,000 people per square mile.
  - A suburban zip code is a zip code with between 1,000 and 3,000 people, inclusive, per square mile.
  - A rural zip code is a zip code with fewer than 1,000 people per square mile.

Consider the following method, which is intended to categorize a zip code as urban, suburban, or rural based on the population density of the area included in the zip code.

```
public static String getCategory(int density)
   /* missing code */
}
```

Which of the following code segments can replace /\* missing code \*/ so the getCategory method works as intended?

```
String cat;
    if (density > 3000)
        cat = "urban";
    else if (density > 999)
       cat = "suburban";
    else
    {
        cat = "rural";
    return cat;
II.
    String cat;
    if (density > 3000)
        cat = "urban";
    if (density > 999)
        cat = "suburban";
    cat = "rural";
    return cat;
```

- (A) I only
- (B) III only
- (C) I and II only
- (D) I and III only
- (E) I, II, and III

15. Consider the following code segment. Assume that a is greater than zero.

```
int a = /* value not shown */;
int b = a + (int) (Math.random() * a);
```

Which of the following best describes the value assigned to b when the code segment is executed?

- (A) a
- (B) 2 \* a
- (C) A random integer between 0 and a 1, inclusive
- (D) A random integer between a and 2 \* a, inclusive
- (E) A random integer between a and 2 \* a 1, inclusive

16. Consider the following recursive method.

```
public static void stars(int num)
   if (num == 1)
      return;
   stars(num - 1);
   for (int i = 0; i < num; i++)
      System.out.print("*");
   System.out.println();
}
```

What is printed as a result of the method call stars (5) ?

- (A) \*\*\*\*
- (B) \*\* \* \* \*

  - \*\*\*\*
- (C) \*
  - - \*\*\*\*
- (E) \*\*\*\*

  - \*\*\*
  - \* \*

17. Consider the following class definitions.

```
public class Hero
{
   private String name;
   private int power;
   public Hero(String n, int p)
      name = n;
      power = p;
   public void powerUp(int p)
      power += p;
   public int showPower()
     return power; }
}
public class SuperHero extends Hero
   public SuperHero(String n, int p)
   {
      super(n, p);
   }
   public void powerUp(int p)
      super.powerUp(p * 2);
   }
}
```

The following code segment appears in a class other than Hero and SuperHero.

```
Hero j = new SuperHero("JavaHero", 50);
j.powerUp(10);
System.out.println(j.showPower());
```

What is printed as a result of executing the code segment?

- (A) 10
- (B) 20
- (C) 60
- (D) 70
- (E) 100

18. Consider the following method, which is intended to return the number of *local maximum* values in an array. Local maximum values are array elements that are greater than both adjacent array elements. The first and last elements of an array have only a single adjacent element, so neither the first nor the last array element is counted by this method. For example, an array containing the values {3, 9, 7, 4, 10, 12, 3, 8} has two local maximum values: 9 and 12.

```
public static int countPeaks(int[] data)
{
   int numPeaks = 0;
   for ( /* missing loop header */ )
      if (data[p - 1] < data[p] && data[p] > data[p + 1])
         numPeaks++;
      }
   }
   return numPeaks;
}
```

Which of the following can replace /\* missing loop header \*/ so the method countPeaks works as intended?

```
(A) int p = data.length - 1; p > 0; p--
(B) int p = 0; p < data.length; p++
(C) int p = 0; p < data.length - 1; p++
(D) int p = 1; p < data.length; p++
(E) int p = 1; p < data.length - 1; p++
```

19. Consider the following code segment.

```
int[][] values = {{1, 2, 3}, {4, 5, 6}};
int x = 0;

for (int j = 0; j < values.length; j++)
{
    for (int k = 0; k < values[0].length; k++)
    {
        if (k == 0)
        {
            values[j][k] *= 2;
        }
        x += values[j][k];
    }
}</pre>
```

What is the value of x after the code segment is executed?

- (A) 7
- (B) 17
- (C) 21
- (D) 26
- (E) 27

20. Consider the following class definition.

```
public class Book
   private int pages;
   public int getPages()
       return pages;
   // There may be instance variables, constructors, and methods not shown.
}
```

The following code segment is intended to store in maxPages the greatest number of pages found in any Book object in the array bookArr.

```
Book[] bookArr = { /* initial values not shown */ };
int maxPages = bookArr[0].getPages();
for (Book b : bookArr)
   /* missing code */
```

Which of the following can replace /\* missing code \*/ so the code segment works as intended?

```
(A) if (b.pages > maxPages)
   {
      maxPages = b.pages;
   }
(B) if (b.getPages() > maxPages)
      maxPages = b.getPages();
   }
(C) if (Book[b].pages > maxPages)
   {
      maxPages = Book[b].pages;
   }
(D) if (bookArr[b].pages > maxPages)
   {
      maxPages = bookArr[b].pages;
(E) if (bookArr[b].getPages() > maxPages)
      maxPages = bookArr[b].getPages();
   }
```

### Questions 21 - 22 refer to the information below.

Consider the following method.

```
public static String[] strArrMethod(String[] arr)
   String[] result = new String[arr.length];
   for (int j = 0; j < arr.length; <math>j++)
      String sm = arr[j];
      for (int k = j + 1; k < arr.length; k++)
         if (arr[k].length() < sm.length())</pre>
         {
            sm = arr[k]; // Line 12
      }
      result[j] = sm;
   return result;
}
```

21. Consider the following code segment.

```
String[] testOne = {"first", "day", "of", "spring"};
String[] resultOne = strArrMethod(testOne);
```

What are the contents of resultOne when the code segment has been executed?

```
(A) {"day", "first", "of", "spring"}
(B) { "of ", "day ", "first ", "spring "}
(C) {"of", "day", "of", "spring"}
(D) { "of", "of", "of", "spring"}
(E) {"spring", "first", "day", "of"}
```

22. Consider the following code segment.

```
String[] testTwo = {"last", "day", "of", "the", "school", "year"};
String[] resultTwo = strArrMethod(testTwo);
```

How many times is the line labeled  $\//$  Line 12 in the strArrMethod executed as a result of executing the code segment?

- (A) 4 times
- (B) 5 times
- (C) 6 times
- (D) 15 times
- (E) 30 times

23. Consider the following method, which is intended to print the values in its two-dimensional integer array parameter in row-major order.

```
public static void rowMajor(int[][] arr)
   /* missing code */
}
```

As an example, consider the following code segment.

```
int[][] theArray = {{1, 2}, {3, 4}, {5, 6}, {7, 8}};
rowMajor(theArray);
```

When executed, the code segment should produce the following output.

```
1 2 3 4 5 6 7 8
```

Which of the following code segments can replace /\* missing code \*/ so that the rowMajor method works as intended?

```
(A) for (int j : arr)
      for (int k : j)
          System.out.print(j + " ");
(B) for (int j : arr)
      for (int k : j)
         System.out.print(k + " ");
   }
(C) for (int[] j : arr)
      for (int k : j)
          System.out.print(j + " ");
   }
(D) for (int[] j : arr)
      for (int k : j)
          System.out.print(k + " ");
       }
(E) for (int[] j : arr)
      for (int k : j)
          System.out.print(arr[k] + " ");
   }
```

24. Consider the following class definition.

```
public class SomeClass
{
   private int x = 0;
   private static int y = 0;
   public SomeClass(int pX)
     x = pX;
     y++;
   public void incrementY()
   { y++; }
   public void incrementY(int inc)
   { y += inc; }
  public int getY()
   { return y; }
}
```

The following code segment appears in a class other than SomeClass.

```
SomeClass first = new SomeClass(10);
SomeClass second = new SomeClass(20);
SomeClass third = new SomeClass(30);
first.incrementY();
second.incrementY(10);
System.out.println(third.getY());
```

What is printed as a result of executing the code segment if the code segment is the first use of a SomeClass object?

- (A) 0
- (B) 1
- (C) 11
- (D) 14
- (E) 30

25. Consider the following method.

```
public static String rearrange(String str)
{
   String temp = "";

   for (int i = str.length() - 1; i > 0; i--)
   {
     temp += str.substring(i - 1, i);
   }

   return temp;
}
```

What, if anything, is returned by the method call rearrange ("apple") ?

- (A) "app1"
- (B) "apple"
- (C) "elppa"
- (D) "lppa"
- (E) Nothing is returned due to a run-time error.

26. Consider the following two code segments. Assume that the int variables m and n have been properly declared and initialized and are both greater than 0.

```
I. for (int i = 0; i < m * n; i++)
      System.out.print("A");
II. for (int j = 1; j <= m; j++)
      for (int k = 1; k < n; k++)
         System.out.print("B");
      }
   }
```

Assume that the initial values of m and n are the same in code segment I as they are in code segment II. Which of the following correctly compares the number of times that "A" and "B" are printed when each code segment is executed?

- (A) "A" is printed m fewer times than "B".
- (B) "A" is printed n fewer times than "B".
- (C) "A" is printed m more times than "B".
- (D) "A" is printed n more times than "B".
- (E) "A" and "B" are printed the same number of times.

27. Consider the following statement. Assume that a and b are properly declared and initialized boolean variables.

```
boolean c = (a \&\& b) | | (!a \&\& b);
```

Under which of the following conditions will c be assigned the value false?

- (A) Always
- (B) Never
- (C) When a and b have the same value
- (D) When a has the value false
- (E) When b has the value false

28. Consider the following method.

```
public static String abMethod(String a, String b)
{
  int x = a.indexOf(b);

  while (x >= 0)
  {
    a = a.substring(0, x) + a.substring(x + b.length());
    x = a.indexOf(b);
  }

  return a;
}
```

What, if anything, is returned by the method call abMethod("sing the song", "ng")?

- (A) "si"
- (B) "si the so"
- (C) "si the song"
- (D) "sig the sog"
- $(E) \quad Nothing \ is \ returned \ because \ a \quad \texttt{StringIndexOutOfBoundsException} \ \ is \ thrown.$

## GO ON TO THE NEXT PAGE.

29. Consider the following method.

```
public static int calcMethod(int num)
   if (num == 0)
      return 10;
   return num + calcMethod(num / 2);
}
```

What value is returned by the method call calcMethod(16)?

- (A) 10
- (B) 26
- (C) 31
- (D) 38
- (E) 41

30. Consider the following class definitions.

```
public class Rectangle
{
   private int height;
   private int width;
   public Rectangle()
      height = 1;
      width = 1;
   }
   public Rectangle(int x)
      height = x;
      width = x;
   public Rectangle(int h, int w)
      height = h;
      width = w;
   }
   // There may be methods that are not shown.
}
public class Square extends Rectangle
   public Square(int x)
      /* missing code */
   }
```

Which of the following code segments can replace /\* missing code \*/ so that the Square class constructor initializes the Rectangle class instance variables height and width to x?

```
(A) super();
```

- (B) super(x);
- (C) Rectangle(x);
- (D) Square(x, x);
- (E) height = x;
  width = x;

31. Consider an integer array nums, which has been properly declared and initialized with one or more values. Which of the following code segments counts the number of negative values found in nums and stores the count in counter ?

```
int counter = 0;
     int i = -1;
    while (i <= nums.length - 2)</pre>
        i++;
        if (nums[i] < 0)
           counter++;
        }
     }
    int counter = 0;
     for (int i = 1; i < nums.length; i++)</pre>
        if (nums[i] < 0)
           counter++;
     }
III.
    int counter = 0;
     for (int i : nums)
        if (nums[i] < 0)
           counter++;
     }
```

- (A) I only
- (B) II only
- (C) I and II only
- (D) I and III only
- (E) I, II, and III

32. Consider the following class definitions.

```
public class ClassA
{
    public String getValue()
    {
        return "A";
    }

    public void showValue()
    {
        System.out.print(getValue());
    }
}

public class ClassB extends ClassA
{
    public String getValue()
    {
        return "B";
    }
}
```

The following code segment appears in a class other than ClassA or ClassB.

```
ClassA obj = new ClassB();
obj.showValue();
```

What, if anything, is printed when the code segment is executed?

- (A) A
- (B) B
- (C) AB
- (D) BA
- (E) Nothing is printed because the code does not compile.

33. Consider the following code segment.

```
String[][] letters = {{"A", "B", "C", "D"},
                       {"E", "F", "G", "H"},
                       {"I", "J", "K", "L"}};
for (int col = 1; col < letters[0].length; col++)</pre>
   for (int row = 1; row < letters.length; row++)</pre>
      System.out.print(letters[row][col] + " ");
   System.out.println();
}
```

What is printed as a result of executing this code segment?

- (A) A E I
  - FJ
  - K
- (B) B F J
  - CGK
  - D H L
- (C) E I
  - FЈ
  - GK
  - H L
- (D) F G H
  - J K L
- (E) F J
  - G K
  - H L

34. The following method is intended to remove all elements of an ArrayList of integers that are divisible by key and add the removed elements to a new ArrayList, which the method returns.

```
public static ArrayList<Integer> match(ArrayList<Integer> numList, int key)
{
    ArrayList<Integer> returnList = new ArrayList<Integer>();

    int i = 0;
    while (i < numList.size())
    {
        int num = numList.get(i);
        if (num % key == 0)
        {
            numList.remove(i);
            returnList.add(num);
        }
        i++;
    }
    return returnList;
}</pre>
```

As an example, if the method is called with an ArrayList containing the values [5, 2, 10, 20, 16] and the parameter key has the value 5, then numList should contain [2, 16] at the end of the method and an ArrayList containing [5, 10, 20] should be returned.

Which of the following best explains why the method does not always work as intended?

- (A) The method attempts to add an element to returnList after that element has already been removed from numList.
- (B) The method causes a NullPointerException to be thrown when no matches are found.
- (C) The method causes an IndexOutOfBoundsException to be thrown.
- (D) The method fails to correctly determine whether an element of numList is divisible by key.
- (E) The method skips some elements of numList during the traversal.

35. Consider the mode method, which is intended to return the most frequently occurring value (mode) in its int[] parameter arr. For example, if the parameter of the mode method has the contents {6, 5, 1, 5, 2, 6, 5}, then the method is intended to return 5.

```
/** Precondition: arr.length >= 1 */
public static int mode(int[] arr)
   int modeCount = 1;
   int mode = arr[0];
   for (int j = 0; j < arr.length; j++)
      int valCount = 0;
      for (int k = 0; k < arr.length; k++)
          if ( /* missing condition 1 */ )
             valCount++;
          }
      if ( /* missing condition 2 */ )
         modeCount = valCount;
         mode = arr[j];
      }
   return mode;
}
```

Which of the following can replace /\* missing condition 1 \*/ and /\* missing condition 2 \*/ so the code segment works as intended?

```
/* missing condition 1 */
                            /* missing condition 2 */
(A) arr[j] == arr[k]
                             valCount > modeCount
(B) arr[j] == arr[k]
                            modeCount > valCount
(C) arr[j] != arr[k]
                            valCount > modeCount
(D) arr[j] != arr[k]
                            modeCount > valCount
(E) arr[j] != arr[k]
                            modeCount != valCount
```

36. Consider the following methods.

```
/** Precondition: a > 0 and b > 0 */
public static int methodOne(int a, int b)
   int loopCount = 0;
   for (int i = 0; i < a / b; i++)
      loopCount++;
   return loopCount;
}
/** Precondition: a > 0 and b > 0 */
public static int methodTwo(int a, int b)
   int loopCount = 0;
   int i = 0;
   while (i < a)
      loopCount++;
      i += b;
   return loopCount;
}
```

Which of the following best describes the conditions under which methodOne and methodTwo return the same value?

- (A) When a and b are both even
- (B) When a and b are both odd
- (C) When a is even and b is odd
- (D) When a % b is equal to zero
- (E) When a % b is equal to one

37. Consider the following code segment. Assume that num3 > num2 > 0.

```
int num1 = 0;
int num2 = /* initial value not shown */;
int num3 = /* initial value not shown */;
while (num2 < num3)</pre>
   num1 += num2;
   num2++;
}
```

Which of the following best describes the contents of num1 as a result of executing the code segment?

- (A) The product of num2 and num3
- (B) The product of num2 and num3 1
- (C) The sum of num2 and num3
- (D) The sum of all integers from num2 to num3, inclusive
- (E) The sum of all integers from num2 to num3 1, inclusive

38. Consider the following class definition.

```
public class Value
{
   private int num;

public int getNum()
   {
     return num;
   }

   // There may be instance variables, constructors, and methods not shown.
}
```

The following method appears in a class other than Value. It is intended to sum all the num instance variables of the Value objects in its ArrayList parameter.

```
/** Precondition: valueList is not null */
public static int getTotal(ArrayList<Value> valueList)
{
   int total = 0;
   /* missing code */
   return total;
}
```

Which of the following code segments can replace /\* missing code \*/ so the getTotal method works as intended?

```
I. for (int x = 0; x < valueList.size(); x++)
{
    total += valueList.get(x).getNum();
}

II. for (Value v : valueList)
{
    total += v.getNum();
}

III. for (Value v : valueList)
{
    total += getNum(v);
}</pre>
```

- (A) I only
- (B) II only
- (C) III only
- (D) I and II
- (E) I and III

39. Consider the following recursive method.

```
public static boolean recurMethod(String str)
   if (str.length() <= 1)</pre>
      return true;
   else if (str.substring(0, 1).compareTo(str.substring(1, 2)) > 0)
      return recurMethod(str.substring(1));
   else
      return false;
   }
}
```

Which of the following method calls will return true ?

- (A) recurMethod("abcba")
- (B) recurMethod("abcde")
- (C) recurMethod("bcdab")
- (D) recurMethod("edcba")
- (E) recurMethod("edcde")

40. Consider the following class definitions.

```
public class A
{
    public String message(int i)
    {
       return "A" + i;
    }
}

public class B extends A
{
    public String message(int i)
    {
       return "B" + i;
    }
}
```

The following code segment appears in a class other than A or B.

Which of the following best explains the difference, if any, in the behavior of the code segment that will result from removing the message method from class A?

- (A) The statement in line 3 will cause a compiler error because the message method for obj1 cannot be found.
- (B) The statement in line 4 will cause a compiler error because the message method for obj2 cannot be found.
- (C) As a result of the method call in line 3, the message method in class B will be executed instead of the message method in class A.
- (D) As a result of the method call in line 4, the message method in class B will be executed instead of the message method in class A.
- (E) The behavior of the code segment will remain unchanged.

## **END OF SECTION I**

## IF YOU FINISH BEFORE TIME IS CALLED, YOU MAY CHECK YOUR WORK ON THIS SECTION.

DO NOT GO ON TO SECTION II UNTIL YOU ARE TOLD TO DO SO.

MAKE SURE YOU HAVE DONE THE FOLLOWING:

- PLACED YOUR AP ID LABEL ON YOUR ANSWER SHEET
- WRITTEN AND GRIDDED YOUR AP ID CORRECTLY ON YOUR **ANSWER SHEET**
- TAKEN THE AP EXAM LABEL FROM THE FRONT OF THIS BOOKLET AND PLACED IT ON YOUR ANSWER SHEET

# AP<sup>®</sup> Computer Science A Exam

## **SECTION II: Free Response, Questions**

### DO NOT OPEN THIS BOOKLET UNTIL YOU ARE TOLD TO DO SO.

## At a Glance

#### **Total Time**

1 hour and 30 minutes **Number of Questions** 

**Percent of Total Score** 

**Writing Instrument** 

Pencil **Electronic Device** 

None allowed

Weight

The questions are weighted equally.

#### Instructions

The questions for Section II are printed in this booklet. You may use the pages in this booklet to organize your answers and for scratch work, but you must write your answers in the blank space provided for each question.

The Java Quick Reference is located inside the front cover of this booklet.

Write your answer to each question in the blank space provided. Begin your response to each question at the top of a new page and completely fill in the circle at the top of each page that corresponds to the question you are answering.

All program segments must be written in Java. Show all your work. Credit for partial solutions will be given. Write clearly and legibly. Erased or crossed-out work will not be

Manage your time carefully. Do not spend too much time on any one question. You may proceed freely from one question to the next. You may review your responses if you finish before the end of the exam is announced.

## **Java Quick Reference**

Accessible methods from the Java library that may be included in the exam

Class Constructors and Methods	Explanation
	String Class
String(String str)	Constructs a new String object that represents the same sequence of characters as str
<pre>int length()</pre>	Returns the number of characters in a String object
String substring(int from, int to)	Returns the substring beginning at index from and ending at index to - 1
String substring(int from)	Returns substring(from, length())
int indexOf(String str)	Returns the index of the first occurrence of str; returns -1 if not found
boolean equals(String other)	Returns true if this is equal to other; returns false otherwise
int compareTo(String other)	Returns a value <0 if this is less than other; returns zero if this is equal to other; returns a value >0 if this is greater than other
	Integer Class
Integer(int value)	Constructs a new Integer object that represents the specified int value
Integer.MIN_VALUE	The minimum value represented by an int or Integer
Integer.MAX_VALUE	The maximum value represented by an int or Integer
<pre>int intValue()</pre>	Returns the value of this Integer as an int
	Double Class
Double(double value)	Constructs a new Double object that represents the specified double value
double doubleValue()	Returns the value of this Double as a double
	Math Class
static int abs(int x)	Returns the absolute value of an int value
static double abs(double x)	Returns the absolute value of a double value
static double pow(double base, double exponent)	Returns the value of the first parameter raised to the power of the second parameter
static double sqrt(double x)	Returns the positive square root of a double value
static double random()	Returns a double value greater than or equal to 0.0 and less than 1.0
	ArrayList Class
int size()	Returns the number of elements in the list
boolean add(E obj)	Appends obj to end of list; returns true
<pre>void add(int index, E obj)</pre>	Inserts obj at position index (0 <= index <= size), moving elements at position index and higher to the right (adds 1 to their indices) and adds 1 to size
E get(int index)	Returns the element at position index in the list
E set(int index, E obj)	Replaces the element at position index with obj; returns the element formerly at position index
E remove(int index)	Removes element from position index, moving elements at position index + 1 and higher to the left (subtracts 1 from their indices) and subtracts 1 from size; returns the element formerly at position index
	Object Class
boolean equals(Object other)	
String toString()	

## COMPUTER SCIENCE A

## **SECTION II**

Time—1 hour and 30 minutes

4 Questions

**Directions: SHOW ALL YOUR WORK. REMEMBER THAT PROGRAM SEGMENTS ARE TO BE WRITTEN IN JAVA.** You may plan your answers in this Questions booklet, but no credit will be given for anything written in this booklet. You will only earn credit for what you write in the Free Response booklet.

## Notes:

- Assume that the classes listed in the Java Quick Reference have been imported where appropriate.
- Unless otherwise noted in the question, assume that parameters in method calls are not null and that methods are called only when their preconditions are satisfied.
- In writing solutions for each question, you may use any of the accessible methods that are listed in classes defined in that question. Writing significant amounts of code that can be replaced by a call to one of these methods will not receive full credit.

- 1. A mathematical sequence is an ordered list of numbers. This question involves a sequence called a hailstone sequence. If n is the value of a term in the sequence, then the following rules are used to find the next term, if one exists.
  - If *n* is 1, the sequence terminates.
  - If *n* is even, then the next term is  $\frac{n}{2}$ .
  - If *n* is odd, then the next term is 3n + 1.

For this question, assume that when the rules are applied, the sequence will eventually terminate with the term n=1.

The following are examples of hailstone sequences.

## Example 1: 5, 16, 8, 4, 2, 1

- The first term is 5, so the second term is 5 \* 3 + 1 = 16.
- The second term is 16, so the third term is  $\frac{16}{2} = 8$ .
- The third term is 8, so the fourth term is  $\frac{8}{2} = 4$ .
- The fourth term is 4, so the fifth term is  $\frac{4}{2} = 2$ .
- The fifth term is 2, so the sixth term is  $\frac{2}{2} = 1$ .
- Since the sixth term is 1, the sequence terminates.

## Example 2: 8, 4, 2, 1

- The first term is 8, so the second term is  $\frac{8}{2} = 4$ .
- The second term is 4, so the third term is  $\frac{4}{2} = 2$ .
- The third term is 2, so the fourth term is  $\frac{2}{2} = 1$ .
- Since the fourth term is 1, the sequence terminates.

The Hailstone class, shown below, is used to represent a hailstone sequence. You will write three methods in the Hailstone class.

```
public class Hailstone
{
    /** Returns the length of a hailstone sequence that starts with n,
        as described in part (a).
     * Precondition: n > 0
   public static int hailstoneLength(int n)
    { /* to be implemented in part (a) */ }
    /** Returns true if the hailstone sequence that starts with n is considered long
        and false otherwise, as described in part (b).
        Precondition: n > 0
     * /
   public static boolean isLongSeq(int n)
    { /* to be implemented in part (b) */ }
    /** Returns the proportion of the first n hailstone sequences that are considered long,
        as described in part (c).
     * Precondition: n > 0
     * /
   public static double propLong(int n)
    { /* to be implemented in part (c) */ }
    // There may be instance variables, constructors, and methods not shown.
}
```

(a) The length of a hailstone sequence is the number of terms it contains. For example, the hailstone sequence in example 1 (5, 16, 8, 4, 2, 1) has a length of 6 and the hailstone sequence in example 2 (8, 4, 2, 1) has a length of 4.

Write the method hailstoneLength(int n), which returns the length of the hailstone sequence that starts with n.

```
/** Returns the length of a hailstone sequence that starts with n, as described in part (a).
 * Precondition: n > 0
 * /
public static int hailstoneLength(int n)
```

Begin your response at the top of a new page in the Free Response booklet and fill in the appropriate circle indicating the question number. If there are multiple parts to this question, write the part letter with your response.

```
Class information for this question
public class Hailstone
public static int hailstoneLength(int n)
public static boolean isLongSeq(int n)
public static double propLong(int n)
```

(b) A hailstone sequence is considered long if its length is greater than its starting value. For example, the hailstone sequence in example 1 (5, 16, 8, 4, 2, 1) is considered long because its length (6) is greater than its starting value (5). The hailstone sequence in example 2 (8, 4, 2, 1) is not considered long because its length (4) is less than or equal to its starting value (8).

Write the method isLongSeq(int n), which returns true if the hailstone sequence starting with n is considered long and returns false otherwise. Assume that hailstoneLength works as intended, regardless of what you wrote in part (a). You must use hailstoneLength appropriately to receive full credit.

```
/** Returns true if the hailstone sequence that starts with n is considered long
* and false otherwise, as described in part (b).
* Precondition: n > 0
*/
public static boolean isLongSeq(int n)
```

Begin your response at the top of a new page in the Free Response booklet and fill in the appropriate circle indicating the question number. If there are multiple parts to this question, write the part letter with your response.

(c) The method propLong(int n) returns the proportion of long hailstone sequences with starting values between 1 and n, inclusive.

Consider the following table, which provides data about the hailstone sequences with starting values between 1 and 10, inclusive.

Starting Value	Terms in the Sequence	Length of the Sequence	Long?
1	1	1	No
2	2, 1	2	No
3	3, 10, 5, 16, 8, 4, 2, 1	8	Yes
4	4, 2, 1	3	No
5	5, 16, 8, 4, 2, 1	6	Yes
6	6, 3, 10, 5, 16, 8, 4, 2, 1	9	Yes
7	7, 22, 11, 34, 17, 52, 26, 13, 40, 20, 10, 5, 16, 8, 4, 2, 1	17	Yes
8	8, 4, 2, 1	4	No
9	9, 28, 14, 7, 22, 11, 34, 17, 52, 26, 13, 40, 20, 10, 5, 16, 8, 4, 2, 1	20	Yes
10	10, 5, 16, 8, 4, 2, 1	7	No

The method call Hailstone.propLong(10) returns 0.5, since 5 of the 10 hailstone sequences shown in the table are considered long.

Write the propLong method. Assume that hailstoneLength and isLongSeq work as intended, regardless of what you wrote in parts (a) and (b). You must use isLongSeq appropriately to receive full credit.

- /\*\* Returns the proportion of the first n hailstone sequences that are considered long,
  - as described in part (c).
  - **Precondition:** n > 0
  - \* /

public static double propLong(int n)

Begin your response at the top of a new page in the Free Response booklet and fill in the appropriate circle indicating the question number. If there are multiple parts to this question, write the part letter with your response.

```
Class information for this question
public class Hailstone
public static int hailstoneLength(int n)
public static boolean isLongSeq(int n)
public static double propLong(int n)
```

GO ON TO THE NEXT PAGE.

NO TEST MATERIAL ON THIS PAGE

GO ON TO THE NEXT PAGE.

- 2. This question involves the creation and use of a spinner to generate random numbers in a game. A GameSpinner object represents a spinner with a given number of sectors, all equal in size. The GameSpinner class supports the following behaviors.
  - Creating a new spinner with a specified number of sectors
  - Spinning a spinner and reporting the result
  - Reporting the length of the *current run*, the number of consecutive spins that are the same as the most recent spin

The following table contains a sample code execution sequence and the corresponding results.

Statements	Value Returned (blank if no value returned)	Comment	
GameSpinner g = new		Creates a new spinner with four sectors	
<pre>GameSpinner(4);</pre>			
g.currentRun();	0	Returns the length of the current run. The length of the current run is initially 0 because no spins have occurred.	
g.spin();	3	Returns a random integer between 1 and 4, inclusive. In this case, 3 is returned.	
g.currentRun();	1	The length of the current run is 1 because there has been one spin of 3 so far.	
g.spin();	3	Returns a random integer between 1 and 4, inclusive. In this case, 3 is returned.	
g.currentRun();	2	The length of the current run is 2 because there have been two 3s in a row.	
g.spin();	4	Returns a random integer between 1 and 4, inclusive. In this case, 4 is returned.	
g.currentRun();	1	The length of the current run is 1 because the spin of 4 is different from the value of the spin in the previous run of two 3s.	
g.spin();	3	Returns a random integer between 1 and 4, inclusive. In this case, 3 is returned.	
g.currentRun();	1	The length of the current run is 1 because the spin of 3 is different from the value of the spin in the previous run of one 4.	
g.spin();	1	Returns a random integer between 1 and 4, inclusive. In this case, 1 is returned.	
g.spin();	1	Returns a random integer between 1 and 4, inclusive. In this case, 1 is returned.	
g.spin();	1	Returns a random integer between 1 and 4, inclusive. In this case, 1 is returned.	
g.currentRun();	3	The length of the current run is 3 because there have been three consecutive 1s since the previous run of one 3.	

Write the complete the example.	GameSpinner	class. Your impl	ementation must n	neet all specifications and	l conform to
aı	nd fill in the appr	opriate circle inc	page in the Free I dicating the questi write the part lette		
			G	O ON TO THE NEX	T PAGE.

3. A student plans to analyze product reviews found on a Web site by looking for keywords in posted reviews. The ProductReview class, shown below, is used to represent a single review. A product review consists of a product name and a review of that product.

public class ProductReview

```
private String name;
       private String review;
       /** Constructs a ProductReview object and initializes the instance variables. */
       public ProductReview(String pName, String pReview)
          name = pName;
          review = pReview;
       }
       /** Returns the name of the product. */
       public String getName()
       { return name; }
       /** Returns the review of the product. */
       public String getReview()
       { return review; }
   }
The ReviewCollector class, shown below, is used to represent a collection of reviews to be analyzed.
   public class ReviewCollector
   {
       private ArrayList<ProductReview> reviewList;
       private ArrayList<String> productList;
       /** Constructs a ReviewCollector object and initializes the instance variables. */
       public ReviewCollector()
          reviewList = new ArrayList<ProductReview>();
          productList = new ArrayList<String>();
       /** Adds a new review to the collection of reviews, as described in part (a). */
       public void addReview(ProductReview prodReview)
       { /* to be implemented in part (a) */ }
       /** Returns the number of good reviews for a given product name, as described in part (b). */
       public int getNumGoodReviews(String prodName)
       \{ /* \text{ to be implemented in part (b) } */ \}
       // There may be instance variables, constructors, and methods not shown.
   }
```

- (a) Write the addReview method, which adds a single product review, represented by a ProductReview object, to the ReviewCollector object. The addReview method does the following when it adds a product review.
  - The ProductReview object is added to the reviewList instance variable.
  - The product name from the ProductReview object is added to the productList instance variable if the product name is not already found in productList.

Elements may be added to reviewList and productList in any order.

Complete method addReview.

/\*\* Adds a new review to the collection of reviews, as described in part (a). \*/
public void addReview(ProductReview prodReview)

Begin your response at the top of a new page in the Free Response booklet and fill in the appropriate circle indicating the question number. If there are multiple parts to this question, write the part letter with your response.

(b) Write the getNumGoodReviews method, which returns the number of good reviews for a given product name. A review is considered good if it contains the string "best" (all lowercase). If there are no reviews with a matching product name, the method returns 0. Note that a review that contains "BEST" or "Best" is not considered a good review (since not all the letters of "best" are lowercase), but a review that contains "asbestos" is considered a good review (since all the letters of "best" are lowercase).

Complete method getNumGoodReviews.

/\*\* Returns the number of good reviews for a given product name, as described in part (b). \*/ public int getNumGoodReviews(String prodName)

Begin your response at the top of a new page in the Free Response booklet and fill in the appropriate circle indicating the question number. If there are multiple parts to this question, write the part letter with your response.

```
Class information for this question
public class ProductReview
private String name
private String review
public ProductReview(String pName, String pReview)
public String getName()
public String getReview()
public class ReviewCollector
private ArrayList<ProductReview> reviewList
private ArrayList<String> productList
public ReviewCollector()
public void addReview(ProductReview prodReview)
public int getNumGoodReviews(String prodName)
```

NO TEST MATERIAL ON THIS PAGE

GO ON TO THE NEXT PAGE.

4. A theater contains rows of seats with the same number of seats in each row. Some rows contain tier 1 seats, and the remaining rows contain tier 2 seats. Tier 1 seats are closer to the stage and are more desirable. All seats in a row share the same tier.

The Seat class, shown below, represents seats in the theater. The boolean instance variable available is false if a ticket for the seat has been sold (the seat is no longer available). The int instance variable tier indicates whether the seat is a tier 1 or tier 2 seat.

```
public class Seat
   private boolean available;
   private int tier;
   public Seat(boolean isAvail, int tierNum)
      available = isAvail;
      tier = tierNum;
   }
   public boolean isAvailable()
   { return available; }
   public int getTier()
   { return tier; }
   public void setAvailability(boolean isAvail)
   { available = isAvail; }
}
```

The Theater class represents a theater of seats. The number of seats per row and the number of tier 1 and tier 2 rows are determined by the parameters of the Theater constructor. Row 0 of the theaterSeats array represents the row closest to the stage.

```
public class Theater
{
   private Seat[][] theaterSeats;
   /** Constructs a Theater object, as described in part (a).
    * Precondition: seatsPerRow > 0; tier1Rows > 0; tier2Rows >= 0
   public Theater(int seatsPerRow, int tier1Rows, int tier2Rows)
   { /* to be implemented in part (a) */ }
   /** Returns true if a seat holder was reassigned from the seat at fromRow, fromCol
       to the seat at toRow, toCol; otherwise it returns false, as described in part (b).
       Precondition: fromRow, fromCol, toRow, and toCol represent valid row and
                    column positions in the theater.
                    The seat at fromRow, fromCol is not available.
    * /
   public boolean reassignSeat(int fromRow, int fromCol,
                                    int toRow, int toCol)
   { /* to be implemented in part (b) */ }
}
```

(a) Write the constructor for the Theater class. The constructor takes three int parameters, representing the number of seats per row, the number of tier 1 rows, and the number of tier 2 rows, respectively. The constructor initializes the theaterSeats instance variable so that it has the given number of seats per row and the given number of tier 1 and tier 2 rows and all seats are available and have the appropriate tier designation.

Row 0 of the theaterSeats array represents the row closest to the stage. All tier 1 seats are closer to the stage than tier 2 seats.

Complete the Theater constructor.

```
/** Constructs a Theater object, as described in part (a).
 * Precondition: seatsPerRow > 0; tier1Rows > 0; tier2Rows >= 0
public Theater(int seatsPerRow, int tier1Rows, int tier2Rows)
```

Begin your response at the top of a new page in the Free Response booklet and fill in the appropriate circle indicating the question number. If there are multiple parts to this question, write the part letter with your response.

```
Class information for this question
public class Seat
private boolean available
private int tier
public Seat(boolean isAvail, int tierNum)
public boolean isAvailable()
public int getTier()
public void setAvailability(boolean isAvail)
public class Theater
private Seat[][] theaterSeats
public Theater(int seatsPerRow, int tier1Rows, int tier2Rows)
public boolean reassignSeat(int fromRow, int fromCol,
                             int toRow, int toCol)
```

(b) Write the reassignSeat method, which attempts to move a person from a source seat to a destination seat. The reassignment can be made if the destination seat is available and has the same or greater tier than the source seat (that is, it is equally or less desirable). For example, a person in a tier 1 seat can be moved to a different tier 1 seat or to a tier 2 seat, but a person in a tier 2 seat can only be moved to a different tier 2 seat.

The reassignSeat method has four int parameters representing the row and column indexes of the source ("from") and destination ("to") seats. If the reassignment is possible, the source seat becomes available, the destination seat becomes unavailable, and the method returns true. If the seat reassignment is not possible, no changes are made to either seat and the method returns false. Assume that the source seat is occupied when the method is called.

Complete method reassignSeat.

Begin your response at the top of a new page in the Free Response booklet and fill in the appropriate circle indicating the question number. If there are multiple parts to this question, write the part letter with your response.

**STOP** 

**END OF EXAM** 

Important: Completely fill in the circle	Question 1	Question 2	Question 3	Question 4
that corresponds to the question you are answering on this page.	$\bigcirc$	$\bigcirc$	$\bigcirc$	$\bigcirc$
Begin your response to	each question at the	ne top of a new p	age.	
	Page 2			

Question 1

Use a pencil only. Do NOT write your name. Do NOT write outside the box.

Important: Completely fill in the circle	Question 1	Question 2	Question 3	Question 4
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	Page 6			

Important: Completely fill in the circle	Question 1	Question 2	Question 3	Question 4
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Begin your response to e	each question at the	ne top of a new p	page.	
	Page 7			

that corresponds to the question you are answering on this page.  Begin your response to each question at the top of a new page.
Begin your response to each question at the top of a new page.
Page 8

Important: Completely fill in the circle	Question 1	Question 2	Question 3	Question 4
that corresponds to the question you are answering on this page.	$\bigcirc$	$\bigcirc$	$\bigcirc$	$\bigcirc$
Begin your response to e	each question at the	ne top of a new p	page.	
	Page 9			

Important: Completely fill in the circle	Question 1	Question 2	Question 3	Question 4
that corresponds to the question you are answering on this page.	$\bigcirc$	$\bigcirc$	$\bigcirc$	$\circ$
Begin your response to e	each question at th	ne top of a new p	age.	
	Page 10			

Important: Completely fill in the circle	Question 1	Question 2	Question 3	Question 4
that corresponds to the question you are answering on this page.	$\bigcirc$	$\bigcirc$	$\bigcirc$	$\bigcirc$
Begin your response to e	each question at th	ne top of a new p	page.	
	Page 11			

Important: Completely fill in the circle	Question 1	Question 2	Question 3	Question 4
that corresponds to the question you are answering on this page.	$\circ$	$\circ$	$\circ$	$\circ$
Begin your response to ea	ich question at th	ne top of a new p	age.	
	Page 12			

Question 2 Question 3

**Question 4** 

# Notes on the AP Computer Science A **Practice Exam**

## **Multiple-Choice Section**

Course Framework Alignment and Rationales

Skill		<b>Learning Objective</b>	Topic			
2.B: Determine the result or output based on statement execution order in a code segment without method calls (other than output).  CON-1.A: Evaluate arithmetic expressions in program code.  Statements						
(A)						
(B)	Incorrect. This would be the result if the addition operation in the second assignment statement was evaluated before the integer division operation, as in int $b = (4 + 3) / 2$ .					
(C)	Correct. In the first assignment statement, the multiplication operation is evaluated before the addition operation and a is assigned the value 9. In the second assignment statement, the integer division is evaluated first and produces a result of 1, which is added to 4 so that the variable b is assigned the value 5. In the third assignment statement, the remainder operation is evaluated before the addition operation and c is assigned the value 6. The variable d is assigned the value 20.0.					
(D)	Incorrect. This would be the result if the division operator in the second assignment statement performed floating point division instead of integer division, as in int $b = 4 + 3.0 / 2$ .					
(E)	first assignment staten	nent was evaluated before the	instead of integer division, as in int $b = 4 + 3.0 / 2$ .  Incorrect. This would be the result if the addition operation in the first assignment statement was evaluated before the multiplication operation, as in int $a = (3 + 2) * 3$ .			

Skill		Learning Objective	Topic			
5.A: Describe the behavior of CON-2.B: Represent			Compound			
a given s	egment of program	branching logical processes	Boolean			
code.		by using nested conditional	Expressions			
		statements.	if-else Statements			
		CON-2.A: Represent				
		branching logical processes				
		by using conditional				
		statements.				
(A)	Incorrect. When num	is zero or a negative integer,	whether even or			
	odd, the body of the outer if statement is not executed and nothing					
	is printed. When num is a positive integer, either "A" or "B" is					
(D)	printed.					
(B)		is zero or a negative integer,				
	odd, the body of the outer if statement is not executed and nothing					
	is printed. When num is a positive integer, either "A" or "B" is printed.					
(C)	Incorrect. "B" is only printed in the case of a positive odd integer.					
	Nothing is printed if num is not positive.					
(D)	Correct. When num is positive and even, "A" is printed. When					
	num is positive and not even (odd), "B" is printed. When num is					
	not positive, nothing is printed.					
(E)	Incorrect. This would be	be the result if the condition in	n the second if			
	statement was num %	s 2 != 0.				

Skill		Learning Objective	Topic		
1.C: Det	ermine code that	CON-1.D: Evaluate	Using the Math		
would be	e used to interact with ed code.	expressions that use the Math class methods.	Class Expressions and		
		CON-1.A: Evaluate arithmetic expressions in program code. CON-1.C: Evaluate arithmetic expressions that use casting.	Assignment Statements Casting and Ranges of Variables		
(A)	Incorrect. Since marker1 and marker2 are always positive, taking the absolute value of each one has no effect. In this statement, if marker2 is greater than marker1, hours is assigned a negative value.				
(B)	Incorrect. In this statement, parentheses are incorrectly placed, so only marker2 is divided by 60.0, not the absolute value of the difference between marker1 and marker2.				
(C)	Correct. The code segment takes the absolute value of the difference between marker1 and marker2, always producing a positive distance, and then divides the result by the vehicle's speed.				
(D)	Incorrect. Since marker1 and marker2 are both of type int, the expression (marker1 - marker2) / 60 performs integer division. For example, when marker1 has the value 100 and marker2 has the value 70, the expression evaluates to 0 instead of the intended 0.5.				
(E)	Incorrect. Since marker1 and marker2 are both of type int, the expression (marker1 - marker2) / 60 performs integer division. The casting of the result of the division to a double occurs too late.				

Skill		Learning Objective	Topic
2.B: Determine the result or		CON-2.B: Represent	Compound
output b	ased on statement	branching logical processes	Boolean
executio	n order in a code	by using nested conditional	Expressions
segment	without method calls	statements.	if Statements and
(other th	an output).	CON-2.A: Represent	Control Flow
		branching logical processes	if-else Statements
		by using conditional	
		statements.	
(A)	Incorrect. This result w	vould be printed as a result of	the call
	message(5, 5, 1	5).	
(B)	Incorrect. This result w	would be printed as a result of	the call
	message(5, 5, 5	).	
(C)	Incorrect. This result w	would be printed as a result of	the call
	message(15, 15,	5).	
(D)	<b>Correct.</b> Since a <	10 evaluates to true, the l	oody of the if
	statement is executed.	Since b < 10 evaluates to	false, "X"
	is not printed; "Y" is printed. Since c < 10 evaluates to true,		
	the body of the if statement is executed, and since b > 10		
	evaluates to true, "Y" is printed.		
(E)	Incorrect. This result would be printed as a result of the call		
	message(15, 5,	5).	

Skill		Learning Objective	Topic
1.C: Det	ermine code that	MOD-1.C: Identify, using	Creating and
would b	e used to interact with	its signature, the correct	Storing Objects
complete	ed code.	constructor being called.	(Instantiation)
(A)	A) Incorrect. This constructor's signature differs from the signature of t existing constructor, so the new constructor can safely be added to t class definition.		
(B)	Incorrect. This constructor's signature differs from the signature of the existing constructor, so the new constructor can safely be added to the class definition.		
(C)	Incorrect. This constructor's signature differs from the signature of the existing constructor, so the new constructor can safely be added to the class definition.		
(D)	Incorrect. This constructor's signature differs from the signature of the existing constructor, so the new constructor can safely be added to the class definition.		
(E)	Correct. This constructor has the same signature as the existing constructor (String, String, boolean). A compiler error will occur.		

Skill		Learning Objective	Topic
2.A: App	bly the meaning of	CON-1.A: Evaluate	Expressions and
specific o	operators.	arithmetic expressions in program code. CON-1.C: Evaluate	Assignment Statements Casting and
		arithmetic expressions that use casting.	Ranges of Variables
(A)	Correct. In option I, the cast applies to the value 2, so floating-poin division is performed and the expression evaluates to 0.5 + 3, or 3.5. In option II, the cast applies to the result of the integer division 2 / 4, so the expression evaluates to 0.0 + 3, or 3.0. In option III, the cast applies to the sum of 3 and the result of the integer division 2 / 4, so the expression evaluates to (double)		o 0.5 + 3, or e integer division or 3.0. In result of the
	(0 + 3),  or  3.0.		
(B)	Incorrect. In option I, the cast applies to the value $2$ , so floating-point division is performed and the expression evaluates to $0.5 + 3$ , or $3.5$ . In option III, the cast applies to the sum of $3$ and the result of the integer division $2 / 4$ , so the expression evaluates to (double) $(0 + 3)$ , or $3.0$ .		
(C)	Incorrect. In option II, the cast applies to the result of the integer division 2 / 4, so the expression evaluates to 0.0 + 3, or 3.0.		
(D)	Incorrect. In option I, the cast applies to the value $2$ , so floating-point division is performed and the expression evaluates to $0.5 + 3$ , or $3.5$ . In option II, the cast applies to the result of the integer division $2 / 4$ , so the expression evaluates to $0.0 + 3$ , or $3.0$ . In option III, the cast applies to the sum of $3$ and the result of the integer division $2 / 4$ , so the expression evaluates to $(double) (0 + 3)$ , or $3.0$ .		o the result of uates to to the sum of
(E)	Incorrect. In option II, the cast applies to the result of the integer division 2 / 4, so the expression evaluates to 0.0 + 3, or 3.0. In option III, the cast applies to the sum of 3 and the result of the integer division 2 / 4, so the expression evaluates to (double) (0 + 3), or 3.0.		

Skill		<b>Learning Objective</b>	Topic
4.C: Determine if two or more		CON-2.B: Represent	Compound
code segments yield equivalent		branching logical processes	Boolean
results.		by using nested conditional	Expressions
		statements.	if-else Statements
		CON-2.A: Represent	
		branching logical processes	
		by using conditional	
		statements.	
		CON-1.F: Evaluate	
		compound Boolean	
		expressions in program	
		code.	
(A)	Incorrect. The stateme	nt assigns a different value to	b2 than
	the code segment assig	gns to b1 when num is bet	ween -100,
	exclusive, and 0, inclusive, or when num is less than -100.		
(B)	Incorrect. The stateme	nt assigns true to b2 for	all values of
	num.		
(C)	Incorrect. The stateme	nt assigns a different value to	b2 than the
	_	to b1 when num is betwee	n 0 and 100,
	exclusive, or when nu	im is greater than 100.	
(D)		nt assigns a different value to	
	code segment assigns to b1 when num is between 0 and 100,		
	exclusive.		
(E)	· ·	of the first if clause in the c	U
		e if num is between 0 and	
	•	se clause, b1 retains the v	
		00. The statement assigns tr	
	num is less than -10	00 or between 0 and 100,	exclusive.

Skill		Learning Objective	Topic
4.B: Ider	ntify errors in program	VAR-1.G: Explain where	Scope and Access
code.		variables can be used in the	Creating and
		program code.	Storing Objects
		MOD-1.C: Identify, using	(Instantiation)
		its signature, the correct	
		constructor being called.	
(A)	Incorrect. A constructe	or signature consists of the con	nstructor name
	and the parameter list.	A correct constructor header	does not include
	a return type.		
(B)	Incorrect. Assigning	int values to double var	iables is allowed,
		ouble values to int varia	bles is not
	allowed.		
(C)	Incorrect. The void return type of the incrementPoints		
	method is correct beca	use the method does not retu	rn a value.
(D)	<b>Correct.</b> The variables n1 and n2 are not instance variables of the		
	Points class, nor are they defined in the incrementPoints		
	method. The instance variables num1 and num2 should have been		
	used instead of n1 and n2.		
(E)	Incorrect. The variable value is the parameter passed to the		
	incrementPoints	method.	

	Question 5			
Skill		Learning Objective	Topic	
2.C: Det	ermine the result or	VAR-2.D: Represent	ArrayList	
output b	ased on the statement	collections of related	Methods	
executio	n order in a code	object reference data using		
segment	containing method	ArrayList objects.		
calls.				
(A)	Incorrect. This output	would be printed if the two-pa	arameter add	
	method call were num	nList.add(0, 1) and th	e set method	
	call were numList.	set(2, 0).		
(B)	<b>Correct.</b> The three sing	gle-parameter add method	calls create an	
	ArrayList with the	e contents [3, 2, 1]. Th	e two-parameter	
	add method call inse	rts an element with the value	0 at position	
	1, so the ArrayLis	st contains [3, 0, 2, 1	]. The set	
	method call sets the value of the element at position 0 to 2, and			
	the ArrayList contains [2, 0, 2, 1] at the end of the			
	code segment.			
(C)	Incorrect. This output	would be printed if the one-pa	arameter add	
	method calls were numList.add(0, 3), numList.add(0,			
	2), and numList.add(0, 1).			
(D)	Incorrect. This output would be printed if the two-parameter add			
	method call were numList.add(0, 1).			
(E)	Incorrect. This output	would be printed if the two-pa	arameter set	
	method call were num			
	1	<u> </u>		

Skill		Learning Objective	Topic
4.A: Use	test-cases to find	CON-2.E: Represent	for Loops
errors or	validate results.	iterative processes using a	Expressions and
		for loop.	Assignment
		CON-1.A: Evaluate	Statements
		arithmetic expressions in	
		program code.	
(A)	Incorrect. The loop bo	dy is never executed as a resul	t of this method
	call and nothing is prin	nted.	
(B)	Incorrect. This method call results in the output "0".		
(C)	Incorrect. This method call results in the output "0".		
(D)	<b>Correct.</b> The for loop iterates from $i = 0$ to $i = 19$ . The		
	expression i % num	2 == 0 evaluates to true	when i is
	divisible by 5 and the expression i % 2 == 0 evaluates to true		
	when i is even. The only values in the range 0 to 19, inclusive,		
	that are both divisible by 5 and even are 0 and 10, so the		
	statement prints "0 10 ".		
(E)	Incorrect. This method	l call results in the output "0	10 20 ".

Skill		Learning Objective	Topic
1.B: Determine code that would		CON-2.C: Represent	while Loops
be used t	o complete code	iterative processes using a	Compound
segment	S.	while loop.	Assignment
		CON-1.B: Evaluate what	Operators
		is stored in a variable as a	
		result of an expression with	
		an assignment statement.	
(A)	Incorrect. This code se	gment prints "109876543	21".
(B)	Incorrect. This code segment prints "109876543210".		
(C)	<b>Correct.</b> During the fir	rst iteration of the while lo	oop, num is
	decremented and "9"	' is printed. During the secon	nd iteration,
	num is decremented a	and "8" is printed. This con	tinues until the
	last iteration of the loo	p, when num is decremented	dand "1" is
	printed. At this point, the Boolean expression in the while loop		
	evaluates to false and the loop terminates. The code segment		
	prints "987654321".		
(D)	Incorrect. This code segment prints "9876543210".		
(E)	Incorrect. This code se	gment prints "109876543	21".

Skill		Learning Objective Topic	
1.C: De	termine code that	CON-1.H: Compare object	Comparing
would b	be used to interact with	references using Boolean	Objects
comple	ted code.	expressions in program	if Statements and
		code.	Control Flow
		CON-2.A: Represent	
		branching logical processes	
		by using conditional	
		statements.	
(A)		is incorrect. If no Person	object has been
	assigned to borrowe		
	borrower.equals		
		ption. Condition II is corre	
	l l	er contains a reference to ar	object when it is
		method call that follows.	
(B)		s incorrect. If no Person o	bject has been
	assigned to borrowe		
	borrower.equals		
		ption. Condition II is corre	
		borrower contains a refer in the println method ca	
	'	ect. If no Person object ha	
		nod call borrower.getNa	•
	NullPointerExce		me () throws a
(C)	+	I is correct. This condition ens	ures that
		a reference to an object when	
		ll that follows. Condition III i	
	-		
	Person object has been assigned to borrower, the method call borrower.getName() throws a NullPointerException.		
(D)		is incorrect. If no Person	
		porrower, the method call	,
	borrower.equals		
	NullPointerExce		
(E)	+	- II is incorrect. If no Person	
	object has been assigned	ed to borrower, the method	od call
	,	e() throws a NullPoint	

Skill		Learning Objective	Topic
4.C: Det	ermine if two or more	CON-1.G: Compare and	Equivalent
code seg	ments yield equivalent	contrast equivalent Boolean	Boolean
results.		expressions.	Expressions
(A)	Incorrect. The expressi	ons are not equivalent when	a has the value
	false, b has the va	lue true, and c has the v	alue true.
(B)	Incorrect. The expressi	ons are not equivalent when	a has the value
	false, b has the value false, and c has the value false.		
(C)	Incorrect. The expressions are not equivalent when a has the value		
	true, b has the value false, and c has the value false.		
(D)	Incorrect. The expressions are not equivalent when a has the value		
	true, b has the value false, and c has the value false.		
(E)	Correct. By De Morgan's laws, ! (a && b) is equivalent to !a		
	!b and the entire exp	ression is equivalent to !a	!b    c.

Skill		Learning Objective	Topic
1.B: Dete	ermine code that would	CON-2.A: Represent	if Statements and
be used	to complete code	branching logical processes	Control Flow
segment	S.	by using conditional	else if Statements
		statements.	
(A)	Incorrect. Code segme	nt III returns the correct cates	gory through the
	use of an immediate	return within each of the o	ne-way selection
	statements.		
(B)	Incorrect. Code segme	nt I uses multi-way selection	to assign and
	return the correct cates	gory.	
(C)	Incorrect. Code segme	nt II returns "rural" for	all values of
	density because it	uses a series of one-way select	ion statements
	instead of multi-way se	election. Code segment III ret	urns the correct
	category through the use of an immediate return within each of		
	the one-way selection statements.		
(D)	Correct. Code segment I uses multi-way selection to assign and		
	return the correct cates	gory. Code segment II returns	"rural" for
	all values of density	y because it uses a series of o	ne-way selection
		nulti-way selection. Code segi	
	the correct category through the use of an immediate return		
	within each of the one-way selection statements.		
(E)	Incorrect. Code segment II returns "rural" for all values of		
	_	uses a series of one-way select	ion statements
	instead of multi-way se	election.	

Skill		Learning Objective	Topic	
5.A: Des	cribe the behavior of	CON-1.D: Evaluate	Using the Math	
a given s	egment of program	expressions that use the	Class	
code.		Math class methods.		
(A)	Incorrect. This would o	describe the value assigned to	b if the value	
	returned by random	was cast to an int before	being multiplied	
	by a, as in int b	= a + ((int) Math.ra	ndom()) * a.	
(B)	Incorrect. This would o	describe the value assigned to	b if the value	
	returned by random	was rounded up to 1 befor	e being multiplied	
	by a, as in int b	= a + (int) (Math.ra	andom() + 1)	
	* a.			
(C)	Incorrect. This would describe the value assigned to b if the second			
	assignment statement was int b = (int) (Math.random()			
	* a).			
(D)	Incorrect. This would describe the value assigned to b if random			
	returned values between 0.0 and 1.0, inclusive. Instead,			
	random returns values between 0.0, inclusive, and 1.0,			
	exclusive.			
(E)	Correct. The random method returns a value between 0.0,			
	inclusive, and 1.0, exclusive. Multiplying that value by a and			
	casting to an int produces a result between 0 and a - 1,			
		a and a value between 0 ar		
	inclusive, is a value bet	ween a and $2 * a - 1$ ,	inclusive.	

Skill		<b>Learning Objective</b>	Topic	
2.C: Det	ermine the result or	CON-2.O: Determine the	Recursion	
output b	ased on the statement	result of executing recursive	for Loops	
executio	n order in a code	methods.		
segment	containing method	CON-2.E: Represent		
calls.		iterative processes using a		
		for loop.		
(A)	Incorrect. This output	would be printed if the recurs	ive call	
	stars(num - 1)	were missing.		
(B)	<b>Correct.</b> The recursive	call of the stars method	occurs before	
	any output is printed, s	so the method call stars (5	) results in	
	a recursive call to sta	ars(4), then to stars(3)	), then to	
		lly to $stars(1)$ . The call to		
	returns immediately without printing any output, so the first call that			
	1	ears (2), which prints a row		
		rints a row of three stars, sta		
		inally stars(5) printsar		
(C)	_	would be printed if the base ca	ase was num ==	
	0 instead of num == 1.			
(D)	Incorrect. This output would be printed if the recursive call			
	stars (num - 1) was the last line of the method instead of			
	occurring before the statements that produce output.			
(E)	Incorrect. This output would be printed if the recursive call			
		was the last line of the method		
		atements that produce output	and if the base	
	case was num == 0	instead of $num == 1$ .		

Skill		Learning Objective	Topic
2.C: Det	ermine the result or	MOD-3.B: Create an	Overriding
output b	ased on the statement	inheritance relationship	Methods
executio	n order in a code	from a subclass to the	super Keyword
segment	containing method	superclass.	Polymorphism
calls.		MOD-3.D: Call methods in	
		an inheritance relationship.	
(A)	Incorrect. This value w	rould be printed if j was ins	tantiated as
	a Hero object instea	d of as a SuperHero object	ct, and if the
	powerUp method in	the Hero class assigned the	e value p to the
	instance variable power rather than incrementing power by p.		
(B)	Incorrect. This value w	rould be printed if the power	cUp method
	in the Hero class assigned the value p to the instance variable		
	power rather than incrementing power by p.		
(C)	Incorrect. This value would be printed if j was instantiated as a		
	Hero object instead of as a SuperHero object.		
(D)	Correct. Since j is instantiated as a SuperHero object, the		
	j.powerUp(10) method call accesses the subclass method. The		
	subclass method uses t	the super keyword to access	ss the superclass
	method with the parameter 20. As a result, the instance variable		
	power is incremented by 20.		
(E)	Incorrect. This value would be printed if the powerUp method in		
	the Hero class doubled the value of the instance variable power		
	rather than incrementi	ng power by p.	

Skill		Learning Objective	Topic
1.B: Dete	ermine code that would	VAR-2.B: Traverse the	Traversing Arrays
be used t	to complete code	elements in a 1D array.	for Loops
segment	S.	CON-2.E: Represent	
		iterative processes using a	
		for loop.	
(A)	Incorrect. The reference	e data[p + 1] in the Bo	olean condition
	in the if statement	causes an	
	ArrayIndexOutOf	BoundsException to be	thrown when p
	has the value data.	length - 1.	
(B)	Incorrect. The reference	e data[p - 1] in the Bo	olean condition
	in the if statement of	causes an	
	ArrayIndexOutOf	BoundsException to be	thrown when p
	has the value 0.		
(C)	Incorrect. The reference	e data[p - 1] in the Bo	olean condition
	in the if statement	causes an	
	_	BoundsException to be	thrown when p
	has the value 0.		
(D)	Incorrect. The reference	e data[p + 1] in the Bo	olean condition
	in the if statement	causes an	
	ArrayIndexOutOf	BoundsException to be	thrown when p
	has the value data.length - 1.		
(E)	<b>Correct.</b> By definition, the first candidate for a local maximum is the		
	element at index 1 (t	he second element in the arra	y), and the last
	candidate is the element	nt at index data.length	- 2 (the next to
	last element in the arra	y).	

Skill		Learning Objective	Topic
2.B: Dete	ermine the result or	VAR-2.G: For 2D array	Traversing 2D
output b	ased on statement	objects— a. Traverse using	Arrays
executio	n order in a code	nested for loops. b. Traverse	2D Arrays
segment	without method calls	using nested enhanced for	
(other th	nan output).	loops.	
		VAR-2.F: Represent	
		collections of related	
		primitive or object reference	
		data using two-dimensional	
		(2D) array objects.	
(A)	Incorrect. This would be	oe the result if the Boolean exp	pression in the
	outer for loop was j < values.length - 1.		
(B)	Incorrect. This would be	oe the result if the Boolean exp	pression in the
	<pre>inner for loop was k &lt; values[0].length - 1.</pre>		
(C)	Incorrect. This would be	oe the result of adding the orig	ginal elements of
	the values array, w	vithout doubling the first elem	ent of every row.
(D)	<b>Correct.</b> The nested f	for loops traverse the two-di	imensional array
	values. The first ele	ment of each row is doubled a	and then the sum
	of all elements is computed as 2+2+3+8+5+6=26.		
(E)	Incorrect. This would be the result if the condition in the if		
	statement was j ==	0 instead of $k == 0$ . This	s would have the
	effect of doubling the e	elements in the first row of va	alues instead of
	those in the first colum	nn.	

Skill		Learning Objective	Topic	
1.C: Det	ermine code that	VAR-2.C: Traverse the	Enhanced for	
would be	e used to interact with	elements in a 1D array	Loop for Arrays	
complete	ed code.	object using an enhanced	Developing	
		for loop.	Algorithms	
		CON-2.I: For algorithms in	Using Arrays	
		the context of a particular		
		specification that requires		
		the use of array traversals—		
		a. Identify standard		
		algorithms. b. Modify		
		standard algorithms. c.		
(4)		Develop an algorithm.	1	
(A)		e variable pages is declared	-	
	using the accessor met	must be accessed from outsid	e the Book class	
(B)		d for loop traverses book	7 mm and the	
( <b>B</b> )		*		
	loop control variable b is assigned Book objects. The instance variable pages is declared private in the Book class,			
	so it must be accessed from outside the Book class using the			
	accessor method getPages. The if statement compares the			
	value returned by the call b.getPages() to the current value			
	of maxPages. If the returned value is greater than maxPages,			
	maxPages is updated with the new maximum value.			
(C)	Incorrect. In the enhanced for loop, b is a Book object and			
	cannot be used as an ir	ndex. In addition, Book is a	class name,	
	not a variable, and can	not be indexed. Finally, the in	stance variable	
	pages is declared private in the Book class, so it must be			
	accessed from outside the Book class using the accessor method			
	getPages.			
(D)	Incorrect. In the enhanced for loop, b is a Book object and			
	cannot be used as an index. The instance variable pages is declared			
		ok class, so it must be access		
(E)	the Book class using the accessor method getPages.			
(E)		nced for loop, b is a Boo	ok object and	
	cannot be used as an in	ndex.		

Skill		Learning Objective	Topic	
2.C: Det	ermine the result or	CON-2.I: For algorithms in	Developing	
output b	ased on the statement	the context of a particular	Algorithms	
executio	n order in a code	specification that requires	Using Arrays	
segment	containing method	the use of array traversals—	String Methods	
calls.		a. Identify standard		
		algorithms. b. Modify		
		standard algorithms. c.		
		Develop an algorithm.		
		VAR-1.E: For String class—		
		a. Create String objects. b.		
		Call String methods.		
(A)	Incorrect. This would i	represent the contents of res	sultOne if the	
	method assigned value	es to elements of resultOne	e in ascending,	
	alphabetical order.			
(B)	Incorrect. This would i	represent the contents of res	sultOne if the	
	method assigned value	es to elements of resultOne	e in increasing	
	order of string length.			
(C)	Incorrect. This would i	represent the contents of res	sultOne if the	
	inner for loop initialization were $k = j + 2$ instead of $k = j$			
	j + 1.			
(D)	<b>Correct.</b> The method assigns the shortest string that occurs in any			
	element of arr between arr[n] and arr[arr.length -			
		ult[n]. The shortest string		
		B] is "of", so result[	•	
		shortest string found between		
		", so result[1] is also a	_	
		ue for the part of the array tha	•	
	2 and ends at index 3, so result[2] is also assigned the value "of". In the last iteration of the outer for loop, there are no			
		r arr[3], so result[3]	is assigned the	
	value "spring".			
(E)		represent the contents of res		
	_	es to elements of resultOne	e in decreasing	
	order of string length.			

Skill		Learning Objective	Topic	
2.D: Det	ermine the number	CON-2.I: For algorithms in	Developing	
of times	a code segment will	the context of a particular	Algorithms	
execute.		specification that requires	Using Arrays	
		the use of array traversals—	String Methods	
		a. Identify standard		
		algorithms. b. Modify		
		standard algorithms. c.		
		Develop an algorithm.		
		VAR-1.E: For String class—		
		a. Create String objects. b.		
		Call String methods.		
(A)	<b>Correct.</b> Line 12 is exe	ecuted each time the variable	sm is updated	
		t value is found. When 🗦 has	· ·	
	is updated for "day" and "of". When j has the value 1, sm			
	is updated for "of". When j has the value 4, sm is updated for			
	"year". When j has any of the values 2, 3, or 5, sm is not			
	updated. Line 12 is executed four times.			
(B)		be the result if sm was updat		
		arr[j] was found instead o	f once each time a	
	new smallest value was	s identified.		
(C)	Incorrect. This would be the result if line 12 were executed once for			
	each element of arr.			
(D)	Incorrect. This would be the result if the method had no if			
	statement and sm was updated once for each pair arr[j] and			
	arr[k] encountered in the nested for loops.			
(E)	Incorrect. This would be the result if the method had no if			
	statement and the initi	alization in the inner for lo	oop was k = 1	
	instead of $k = j +$	1.		

Skill		Learning Objective	Topic
1.B: Dete	ermine code that would	VAR-2.G: For 2D array	Traversing 2D
be used t	to complete code	objects— a. Traverse using	Arrays
segment	s.	nested for loops. b. Traverse	
		using nested enhanced for	
		loops.	
(A)	Incorrect. The outer f	or loop in this code segment	t declares j,
	a row of arr, as an	<pre>int rather than an int[]</pre>	. This code
	segment also attempts	to print j, a row of arr, i	nstead of k, an
	element of j.		
(B)	Incorrect. The outer for loop in this code segment declares j, a		
	row of arr, as an int rather than an int[].		
(C)	Incorrect. This code segment attempts to print j, a row of arr,		
	instead of k, an element of j.		
(D)	<b>Correct.</b> The outer for loop stores each row of the two-dimensional		
	array in j, a one-dimensional array. The inner for loop stores		
	each element of j in k and prints k.		
(E)	Incorrect. This code segment uses k, an element of the two-		
	dimensional array, as a	n index in a one-dimensional	array.

Skill		Learning Objective	Topic
2.C: Determine the result or output based on the statement execution order in a code segment containing method calls.		MOD-2.H: Define the static variables that belong to the class.	Static Variables and Methods
(A)	Incorrect. This would be the result if y was not declared as a static variable and the SomeClass constructor did not increment y.		
(B)	Incorrect. This would be the result if y was not declared as a static variable.		
(C)	Incorrect. This would be the result if the SomeClass constructor did not increment y.		
(D)	Correct. Since y is declared as a static variable, it is associated with the class and all objects of the class share the single variable y. Each time a new SomeClass object is instantiated, the value of y is incremented by 1. After the third object is instantiated, the value of y is 3. The call to incrementy with no parameter increments the value of y by 1, and the call to incrementy with a parameter value of 10 adds 10 to the value of y, resulting in 14.		
(E)	Incorrect. This would be instead of y.	pe the result if the getY me	thod returned x

Skill		<b>Learning Objective</b>	Topic
2.C: Det	ermine the result or	CON-2.F: For algorithms in	Developing
output based on the statement		the context of a particular	Algorithms
executio	n order in a code	specification that involves	Using Strings
segment	containing method	String objects— a. Identify	String Methods
calls.		standard algorithms.	for Loops
		b. Modify standard	
		algorithms. c. Develop an	
		algorithm.	
		VAR-1.E: For String class—	
		a. Create String objects.	
		b. Call String methods.	
		CON-2.E: Represent	
		iterative processes using a	
		for loop.	
(A)	Incorrect. This would l	be the result if the statement a	ssigning a value to
	temp were temp =	str.substring(i - 1	L, i) + temp.
(B)	Incorrect. This would l	be the result if the statement a	ssigning a value to
	temp were temp =	str.substring(i - 1	L, i) + temp
	and if the loop control	variable in the for loop we	ere initialized to
	str.length() ins	tead of str.length() -	1.
(C)	Incorrect. This would l	be the result if the loop contro	l variable in the
	for loop were initial	ized to str.length() in	stead of str.
	length() - 1.		
(D)	Correct. When i ha	s the value 4, temp is assig	gned the value
		ne value 3, "p" is appende	_
	resulting in "lp". When i has the value 2, "p" is appended to		
		g in "lpp". In the last iterat	
	_	1 and "a" is appended to	temp, resulting
	in "lppa".		
(E)	Incorrect. This would l	be the result if the condition in	n the for loop
	were i >= 0 instea	$d \circ f i > 0.$	

Skill		Learning Objective	Topic
2.D: Det	termine the number	CON-2.H: Compute	Informal Code
of times	a code segment will	statement execution counts	Analysis
execute.		and informal run-time	for Loops
		comparison of iterative	Nested Iteration
		statements.	
		CON-2.E: Represent	
		iterative processes using a	
		for loop.	
		CON-2.G: Represent nested	
		iterative processes.	
(A)	Incorrect. This would be	oe the correct comparison if the	ne initialization
	and Boolean condition	in the inner for loop of co	ode segment II
	were $k = 0$ and $k \le n$ , respectively.		
(B)		be the correct comparison if the	
	in the outer and inner	for loops of code segment	II were $j = 0$
	and $k = 0$ , respectively.		
(C)	<b>Correct.</b> There are m	* n iterations of the for	loop in code
		ment II, the outer loop execut	
		s n - 1 times for each itera	
	loop. There are m * n - m iterations of the inner loop in code		
	segment II, so "A" is printed m more times than "B" is printed.		
(D)	Incorrect. This would be the correct comparison if the Boolean		
		and inner for loops of coo	de segment II were
	j < m and k <= r		
(E)		be the correct comparison if the	
	condition in the inner	for loop of code segment I	I were $k \le n$ .

Skill		Learning Objective	Topic
5.D: Des	cribe the initial	CON-1.G: Compare and	Equivalent
conditio	ns that must be met for	contrast equivalent Boolean	Boolean
a progra	m segment to work as	expressions.	Expressions
intended	l or described.		
(A)	Incorrect. The variable	c will be assigned the value	true when
	a and b both have t	he value true or when a	has the value
	false and b hasth	ne value true.	
(B)	Incorrect. The variable	c will be assigned the value	false when
	b has the value fals	se, regardless of the value of	a.
(C)	Incorrect. If a and b are both true, then (a && b) is		
	true, (!a && b) is false, and the entire expression true		
	false evaluates to true.		
(D)	Incorrect. If a has the value false and b has the value true,		
	then (a && b) is false, (!a && b) is true, and the		
	entire expression fal	se    true evaluates to	true.
(E)	Correct. When b has	s the value false, both of	the expressions
	(a && b) and (!a	a && b) evaluate to fals	e, regardless
	of the value of a. The	e entire expression evaluates to	false
	false, or false. When b has the value true, one of the		
	expressions (a && b) or (!a && b) evaluates to true.		
	The entire expression, in this case, is either true    false		
	or false    true, or true. A truth table can be used to		n be used to
	summarize these result	ts.	

Skill		<b>Learning Objective</b>	Topic
2.C: Determine the result or		CON-2.F: For algorithms in	Developing
output based on the statement		the context of a particular	Algorithms Using
executio	n order in a code	specification that involves	Strings
segment	containing method	String objects— a. Identify	String Methods
calls.		standard algorithms.	while Loops
		b. Modify standard	
		algorithms. c. Develop an	
		algorithm.	
		VAR-1.E: For String class—	
		a. Create String objects.	
		b. Call String methods.	
		CON-2.C: Represent	
		iterative processes using a	
		while loop.	
(A)	Incorrect. This value would be returned if the first statement in the		
	while loop was $a = a.substring(0, x)$ .		
(B)	Correct. The method abMethod (String a, String b)		
	removes all non-overlapping occurrences of string b from string		
	a and returns the resulting String. It does this by repeatedly		
	setting x to the index of an occurrence of b in a, then assigning		
	a the result of the concatenation of the parts of a before and after		
	the occurrence of b. The method call abMethod ("sing the		
	song", "ng") removes all occurrences of "ng" from "sing		
(0)	the song", returning "si the so".		
(C)	Incorrect. This value would be returned if the statements inside the		
(- )	while loop were executed only one time.		
(D)	Incorrect. This value would be returned if the first statement		
	in the while loop was $a = a.substring(0, x) +$		
(-)	a.substring(x + b.length() - 1).		
(E)			
begins at an index less than 0 or ends at an index greater th			greater than
	length - 1.		

Skill		Learning Objective	Topic
2.C: Determine the result or		CON-2.O: Determine the	Recursion
output based on the statement		result of executing recursive	
execution order in a code		methods.	
segment containing method			
calls.			
(A)	Incorrect. This would be the result if the value returned in cases other		
	than the base case was calcMethod(num / 2).		
(B)	Incorrect. This would be the result if the value returned in cases other		
	than the base case was num + calcMethod(num % 2).		
(C)	Incorrect. This would be the result if the value returned in the base		
	case was 0 instead of 10.		
(D)	Incorrect. This would be the result if the base case was num == 2		
	instead of num == 0.		
(E)	<b>Correct.</b> The result of the method call calcMethod (16)		
	is 16 + calcMethod(8). The result of the method call		
	calcMethod(8) is 8 + calcMethod(4). The recursive		
	calls continue until the call calcMethod(0), which returns the		
	value 10. The result of the method call calcMethod (16) can		
	be calculated as 16+8+4+2+1+10=41.		

Skill		<b>Learning Objective</b>	Topic
1.C: Determine code that		MOD-3.B: Create an	Writing
would be used to interact with		inheritance relationship	Constructors for
completed program code.		from a subclass to the superclass.	Subclasses
(A)	Incorrect. Calling the no-argument superclass constructor would		
	initialize both height and width to 1, which is not		
	necessarily the intended behavior.		
(B)	<b>Correct.</b> A call to the one-argument superclass constructor with the		
	single parameter x will set both the height and the width		
	instance variables to x.		
(C)	Incorrect. This statement would result in a compiler error.		
	Constructors cannot be called by name from other constructors. The		
	super keyword is used to call the constructor of the superclass.		
(D)	Incorrect. This statement would result in a compiler error.		
	Constructors cannot be called by name from other constructors. In		
	addition, the Square class does not define a constructor with a		
	matching signature.		
(E)	Incorrect. This code segment would result in a compiler error. The		
	instance variables height and width are defined as private		
	in the superclass and cannot be accessed directly from the subclass.		

Skill		Learning Objective	Topic	
1.B: Determine code that would		VAR-2.B: Traverse the	Traversing Arrays	
be used to complete code		elements in a 1D array.	Enhanced for	
segmen	nts.	VAR-2.C: Traverse the	Loop for Arrays	
		elements in a 1D array	Developing	
		object using an enhanced	Algorithms	
		for loop.	Using Arrays	
		CON-2.I: For algorithms in		
		the context of a particular		
		specification that requires		
		the use of array traversals—		
		a. Identify standard		
		algorithms. b. Modify		
		standard algorithms.		
		c. Develop an algorithm.		
(A)	Correct. In code segment I, i takes on the values -1 through			
nums.length - 2, inclusive, in the while loop. Since incremented before the if statement, the array elements in				
	through nums [nums.length - 1] are compared to (code segment II, array element nums [0] is excluded since			
	iteration of the for loop accesses nums [1]. In code segment			
	III, the variable i represents an element of the array rather than an index.			
(B)				
(D)	Incorrect. In code segment I, i takes on the values -1 through nums.length - 2, inclusive, in the while loop. Since i is			
	incremented before the if statement, the array elements nums [0] through nums [nums.length - 1] are compared to 0. In code segment II, array element nums [0] is excluded since the first			
		loop accesses nums[1].		
(C)	Incorrect. In code segment II, array element nums [0] is excluded			
	since the first iteration of the for loop accesses nums[1].			
(D)	Incorrect. In code segment III, the variable i represents an element			
	of the array rather than an index.			
(E)	Incorrect. In code segr	Incorrect. In code segment II, array element nums [0] is excluded		
	_	of the for loop accesses n		
	code segment III, the variable i represents an element of the array			
	rather than an index.	-	•	

Skill		Learning Objective	Topic	
2.C: Determine the result or		MOD-3.D: Call methods in	Polymorphism	
output based on the statement		an inheritance relationship.	Constructors	
execution order in a code		MOD-2.B: Define instance	Creating	
segment	containing method	variables for the attributes	Superclasses and	
calls.		to be initialized through the	Subclasses	
		constructors of a class.		
		MOD-3.B: Create an		
		inheritance relationship		
		from a subclass to the		
		superclass.		
(A)	Incorrect. This output would be printed if obj was instantiated			
	by calling the ClassA constructor instead of the ClassB			
	constructor.			
(B)	Correct. Since obj is instantiated as a ClassB object but the			
	showValue method is not defined in ClassB, the showValue			
	method call accesses the showValue method in the superclass,			
	ClassA. Since the getValue method is defined in ClassB,			
	the getValue method call accesses the getValue method in			
	the subclass, ClassB, and "B" is printed.			
(C)	Incorrect. This output would be printed if the getValue method			
		<pre>super.getValue() +</pre>		
	"B". The value returned by the getValue method of ClassA			
	("A") would be concatenated with "B" and the String "A			
<i>i</i> >	would be printed by the showValue method.			
(D)	Incorrect. This output would be printed if the getValue method			
	in ClassB returned "B" + super.getValue() instead			
	of "B". The String "B" would be concatenated with the value			
	returned by the getValue method of ClassA and the String "BA" would be printed by the showValue method.			
(D)		· · · · · · · · · · · · · · · · · · ·		
(E)		mpiles without error since of	_	
	an object of type ClassA and the showValue method is			
	in ClassA.			

Skill		Learning Objective	Topic
2.B: Determine the result or		VAR-2.G: For 2D array	Traversing 2D
output based on statement		objects— a. Traverse using	Arrays
execution order in a code		nested for loops. b. Traverse	
segment without method calls		using nested enhanced for	
(other th	an output).	loops.	
(A)	Incorrect. This output would be generated if col and row were		
	initialized to 0 and col, respectively, in the for loops.		
(B)	Incorrect. This output would be generated if col and row were		
	initialized to 1 and 0, respectively, in the for loops.		
(C)	Incorrect. This output would be generated if col and row were		
	initialized to 0 and 1, respectively, in the for loops.		
(D)	Incorrect. This output would be generated if the positions of the two		
	for loop headers were reversed, with row as the loop control		
	variable in the outer for loop and col as the loop control		
	variable in the inner f	for loop.	
(E)	<b>Correct.</b> The code segment performs a column-major traversal of the		
	array, beginning with the second column and the second row. For each		
	column, all values in that column after the value in the first row are		
	printed on a single line. The println method call causes data from		
	subsequent columns to appear on new lines in the output.		

Skill		Learning Objective	Торіс			
5.B: Exp	lain why a code	VAR-2.E: For ArrayList	Traversing			
segment	will not compile or	objects— a. Traverse using	ArrayLists			
work as	intended.	a for or while loop. B.				
		Traverse using an enhanced				
		for loop.				
(A)	Incorrect. The order of	addition and removal does no	ot matter, since			
	the value to be added t	o returnList is stored in	n a separate			
	variable num prior to	its removal from numList				
(B)	Incorrect. When there	are no matches, the method r	eturns an empty			
	ArrayList.					
(C)	Incorrect. The get and remove methods are always called with a					
	valid index, since the b	ody of the while loop is exe	ecuted for values of			
	i between 0 and the current value of numList.size() - 1.					
(D)	Incorrect. The expression num % key == 0 is correctly used to					
	identify values of num that are divisible by key.					
(E)	<b>Correct.</b> When the element at position i is removed from					
	numList, subsequer	nt elements are shifted left. Aft	er the removal,			
	the element that used t	to be at position $i + 1$ is n	ow at position i.			
		crements i regardless of wh				
	at position i was removed, the method does not always work as					
	_	, if two adjacent elements are l				
		t element is removed. The met				
	1	ting i only when the elemen	_			
	is not removed or by d	ecrementing i when an eler	nent is removed.			

Skill		<b>Learning Objective</b>	Topic				
1.B: Dete	ermine code that would	CON-2.I: For algorithms in	Developing				
be used	to complete code	the context of a particular	Algorithms				
segment	S.	specification that requires	Using Arrays				
		the use of array traversals—					
		a. Identify standard					
		algorithms. b. Modify					
		standard algorithms.					
		c. Develop an algorithm.					
(A)	Correct. For each elem	nent arr[j], the inner fo	or loop counts				
	the number of times th	at arr[j] appearsin ar:	r and stores				
	the result in valCou	nt. It does this by evaluating	the condition				
	arr[j] == arr[k	] and incrementing valCc	ount when the				
	condition evaluates to	true. After the inner loop	completes, the				
	method evaluates the o	condition valCount > mo	deCount. If				
	the condition evaluates	s to true, a new mode has	been found and				
	mode and modeCou	ant are updated.					
(B)	Incorrect. The replacer	ment for /* missing condition	n 2 */ is				
	incorrect. It would upo	late the mode value to be retu	rned only if it was				
	less common than values considered previously.						
(C)	Incorrect. The replacement for /* missing condition 1 */ is						
	incorrect. Instead of co	ounting the number of times ti	hat arr[j]				
	appears in arr, it wo	ould count the number of time	es that values				
	different than arr[j] appear in arr.						
(D)	Incorrect. The replacer	ments for /* missing conditi	on 1 */ and				
	/* missing condition 2 */ are incorrect. Because of the incorrect						
	replacement for /* r	nissing condition $1 */$ , the n	nethod would				
	count the number of ti	mes that values different than	arr[j]				
	appear in arr instead of the number of times that arr[j]						
	appears in arr. Beca	ause of the incorrect replacem	ent for /*				
	missing condition 2 */	, the method would update	the mode value				
	to be returned only if i	t was less common than value	s considered				
	previously.						
(E)	_	ments for /* missing conditi					
	_	2 */ are incorrect. Because					
		nissing condition $1 */$ , the n					
		mes that values different than	_				
		d of the number of times that					
		nuse of the incorrect replacem	•				
		nethod would update the mod					
	•	irred either more or less frequ	ently than values				
	considered previously.						

Skill		Learning Objective	Topic			
5.D: Des	cribe the initial	CON-2.E: Represent	for Loops			
conditio	ns that must be met for	iterative processes using a	while Loops			
a progra	m segment to work as	for loop.	Expressions and			
intended	l or described.	CON-2.C: Represent	Assignment			
		iterative processes using a	Statements			
		while loop.				
		CON-1.A: Evaluate				
		arithmetic expressions in				
		program code.				
(A)	Incorrect. When a h	as the value 6 and b has th	ne value 4,			
		1 and methodTwo retur	•			
	_	alto 0, methodOne return	ns a / b and			
	methodTwo returns					
(B)		as the value 21 and b has				
		4 and methodTwo retur	· ·			
	_	ulto 0, methodOne return	is a / b and			
( = )	methodTwo returns a / b + 1.					
(C)		as the value 10 and b has				
		3 and methodTwo return	•			
	if a % b is not equal to 0, methodOne returns a / b and					
(D)	methodTwo returns a / b + 1.  Correct. The body of the for loop in methodOne is executed					
(D)	1	dy of the while loop in m				
		imes only when a % b is ea				
		equal to 0, the body of the	*			
		recuted an additional time. Fo	_			
	a has the value 11 and b has the value 5, a / b evaluates to					
		is executed two times but the				
	executed three times.		-			
(E)	Incorrect. When a h	as the value 7 and b has th	ne value 3,			
	methodOne returns	2 and methodTwo retur	ns 3. In general,			
	if a % b is not equa	nlto 0, methodOne return	ns a / b and			
	methodTwo returns	a / b + 1.				

Skill		Learning Objective	Topic				
5.A: Des	scribe the behavior of	CON-2.C: Represent	while Loops				
a given s	segment of program	iterative processes using a					
code.		while loop.					
		CON-2.D: For algorithms					
		in the context of a particular					
		specification that does					
		not require the use of					
		traversals— a. Identify					
		standard algorithms.					
		b. Modify standard					
		algorithms. c. Develop an					
	T	algorithm.					
(A)	1	Incorrect. The product of num2 and num3 could be computed by					
	an algorithm that adds num2 to num1 a total of num3 times.						
(B)		of num2 and num3 - 1					
	computed by an algorithm that adds num2 to num1 a total of						
	num3 - 1 times.						
(C)		num2 and num3 could be					
	algorithm that adds 1 to num2 a total of num3 times.						
(D)	Incorrect. This would correctly describe the behavior of the code						
	segment if the Boolean condition in the while loop was num2						
	<= num3.						
(E)		n of the while loop adds r					
		num2. The last value assigned					
		um3 – 1. Since each value					
		code segment computes the su	ım of the integers				
	from num2 to num3	3 - 1.					

Skill		Learning Objective	Topic			
1.C: Determine code that would be used to interact with completed program code.		VAR-2.D: Represent collections of related object reference data using ArrayList objects.  VAR-2.E: For ArrayList	ArrayList Methods Traversing ArrayLists			
		objects— a. Traverse using a for or while loop. b. Traverse using an enhanced for loop.				
(A)	for loop to traverse t	correct. The code segment use the valueList array. The Num method to access the r	statement inside			
(B)	to traverse the value calls the get method	correct. The code segment use EList array. The statement in the access a Value object access the num instance variations.	nside the loop and then calls the			
(C)	Incorrect. Option I is correct. The code segment uses a for loop to traverse the valueList array. The statement inside the loop calls the get method to access a Value object and then calls the getNum method to access the num instance variable. Option II is correct. The code segment uses an enhanced for loop to traverse the valueList array. The statement inside the loop calls the getNum method to access the num instance variable. Option III is incorrect. The code segment causes a compilation error because the getNum method must be called using the dot operator, not by passing the object reference as an argument.					
(D)	Correct. Option I is correct. The code segment uses a for loop to traverse the valueList array. The statement inside the loop calls the get method to access a Value object and then calls the getNum method to access the num instance variable. Option II is correct. The code segment uses an enhanced for loop to traverse the valueList array. The statement inside the loop calls the getNum method to access the num instance variable. Option III is incorrect. The code segment causes a compilation error because the getNum method must be called using the dot operator, not by passing the object reference as an argument.					
(E)	for loop to traverse to inside the loop calls the instance variable. Option compilation error because the compilation of the co	correct. The code segment use the valueList array. The e getNum method to access on III is incorrect. The code so suse the getNum method m y passing the object reference	statement s the num egment causes a oust be called using			

Skill		Learning Objective	Topic				
	test-cases to find r validate results.	CON-2.O: Determine the result of executing recursive methods.	Recursion				
(A)		l call returns false becaus hically less than the second ch					
(B)		Incorrect. This method call returns false because the first character is lexicographically less than the second character of the string.					
(C)	Incorrect. This method call returns false because the first character is lexicographically less than the second character of the string.						
(D)	Correct. If the first character of str is lexicographically greater than the second character of str, the method returns the result of the recursive call with a parameter that contains all but the first character of str. If the first character of str is lexicographically less than or equal to the second character of str, the method returns false. If no such character pair (where the first character of str is lexicographically less than or equal to the second character of str is lexicographically less than or equal to the second character of str) is found, the base case is reached and the value true is returned.						
(E)		l call returns false becaus hically less than the fourth cha					

Skill Learning Objective Topic						
5.C: Exp	lain how the result of	MOD-3.D: Call methods in	Polymorphism			
	code changes, given a o the initial code.	an inheritance relationship.				
(A)	<b>Correct.</b> At compile time, methods in or inherited by the declared					
(A)	type determine the correctness of a non-static method call. In line 1, obj1 is declared as an object of type A. Therefore, at compile time, there must be a message method in class A or its superclass. If the message method in class A is removed, the statement in line 3 will no longer compile.					
(B)	Incorrect. At compile time, methods in or inherited by the declared type determine the correctness of a non-static method call. In line 2, obj2 is declared as an object of type B. Therefore, at compile time, there must be a message method in class B or its superclass. Since the message method in class B has not been removed, this statement will not cause a compiler error.					
(C)	Incorrect. The message method in class A is not executed in the original code segment. At run-time, the method in the actual object type is executed for a non-static method call. In line 1, obj1 is instantiated as an object of type B. Therefore, in line 3 at run-time, the message method of class B rather than the message method of class A is executed.					
(D)	Incorrect. The message method in class A is not executed in the original code segment. At run-time, the method in the actual object type is executed for a non-static method call. In line 2, obj2 is instantiated as an object of type B. Therefore, in line 4 at run-time, the message method of class B rather than the message method of class A is executed.					
(E)	type determine the corobj1 is declared as a there must be a mess	ime, methods in or inherited rectness of a non-static methon object of type A. Therefore age method in class A or inhod in class A is removed, the	od call. In line 1, e, at compile time, its superclass.			

# Answer Key and Question Alignment to Course Framework

Multiple-Choice Question	Answer	Skill	Learning Objective	Торіс
1	С	2.B	CON-1.A	Expressions and Assignment Statements
2	D	5.A	CON-2.B	Compound Boolean Expressions
			CON-2.A	if-else Statements
3	C	1.C	CON-1.D	Using the Math Class
			CON-1.A	Expressions and Assignment Statements
			CON-1.C	Casting and Ranges of Variables
4	D	2.B	CON-2.B	Compound Boolean Expressions
			CON-2.A	if Statements and Control Flow if-else Statements
5	Е	1.C	MOD-1.C	Creating and Storing Objects (Instantiation)
6	A	2.A	CON-1.A	Expressions and Assignment Statements
			CON-1.C	Casting and Ranges of Variables
7	Е	4.C	CON-2.B	Compound Boolean Expressions
			CON-2.A CON-1.F	if-else Statements Compound Boolean Expressions
8	D	4.B	VAR-1.G MOD-1.C	Scope and Access Creating and Storing Objects (Instantiation)
9	В	2.C	VAR-2.D	ArrayList Methods
10	• • • • • • • • • • • • • • • • • • • •	• • • • • • • • • • • • • • • • • • • •	CON-2.E	. *
10	D	4.A	CON-2.E CON-1.A	for Loops Expressions and Assignment Statements
11	С	1.B	CON-2.C CON-1.B	while Loops Compound Assignment Operators
12	В	1.C	CON-1.H CON-2.A	Comparing Objects if Statements and Control Flow
13	E	4.C	CON-1.G	Equivalent Boolean Expressions
14	D	1.B	CON-2.A	if Statements and Control Flow else if Statements
15	E	5.A	CON-1.D	Using the Math Class
16	В	2.C	CON-2.O CON-2.E	Recursion for Loops

Multiple-Choice Question	Answer	Skill	Learning Objective	Topic
17	D	2.C	MOD-3.B	Overriding Methods
				super Keyword
			MOD-3.D	Polymorphism
18	Е	1.B	VAR-2.B	Traversing Arrays
			CON-2.E	for Loops
19	D	2.B	VAR-2.G	Traversing 2D Arrays
			VAR-2.F	2D Arrays
20	В	1.C	VAR-2.C	Enhanced for Loop for Arrays
			CON-2.I	Developing Algorithms Using
	• • • • • • • • • • • • • • • • • • • •	• • • • • • • • • • • • • • • • • • • •	•••••	Arrays
21	D	2.C	CON-2.I	Developing Algorithms Using
			374 D 1 F	Arrays
			VAR-1.E	String Methods
22	A	2.D	CON-2.I	Developing Algorithms Using
			VAR-1.E	Arrays String Methods
23	D	1.B	VAR-2.G	Traversing 2D Arrays
24	D	• · · · · · · · · · · · · · ·	• • • • • • • • • • • • • • • • • • • •	Static Variables and Methods
•••••	• • • • • • • • • • • • • • • • • • • •	2.C	MOD-2.H	••••••
25	D	2.C	CON-2.F	Developing Algorithms Using Strings
			VAR-1.E	String Methods
			CON-2.E	for Loops
26	C	2.D	CON-2.H	Informal Code Analysis
			CON-2.E	for Loops
			CON-2.G	Nested Iteration
27	Е	5.D	CON-1.G	Equivalent Boolean Expressions
28	В	2.C	CON-2.F	Developing Algorithms Using
				Strings
			VAR-1.E	String Methods
	• • • • • • • • • • • • • • • • • • • •	• • • • • • • • • • • • • • • • • • • •	CON-2.C	while Loops
29	Е	2.C	CON-2.O	Recursion
30	В	1.C	MOD-3.B	Writing Constructors for
			•	Subclasses
31	A	1.B	VAR-2.B	Traversing Arrays
			VAR-2.C	Enhanced for Loop for Arrays
			CON-2.I	Developing Algorithms Using
			1105.25	Arrays
32	В	2.C	MOD-3.D	Polymorphism
			MOD-2.B	Constructors Creating Superclasses and
			MOD-3.B	Creating Superclasses and Subclasses
33	Е	2.B	VAR-2.G	Traversing 2D Arrays
	ப்	۷,ں	v/11\C-2.\U	mavershing 210 milays

Multiple-Choice Question	Answer	Skill	Learning Objective	Торіс
34	Е	5.B	VAR-2.E	Traversing ArrayLists
35	A	1.B	CON-2.I	Developing Algorithms Using Arrays
36	D	5.D	CON-2.E CON-2.C CON-1.A	for Loops while Loops Expressions and Assignment Statements
37	Е	5.A	CON-2.C CON-2.D	while Loops
38	D	1.C	VAR-2.D VAR-2.E	ArrayList Methods Traversing ArrayLists
39	D	4.A	CON-2.O	Recursion
40	A	5.C	MOD-3.D	Polymorphism

## **Free-Response Section**

Scoring Guidelines

## **Applying the Scoring Criteria**

Apply the question scoring criteria first, which always takes precedence. Penalty points can only be deducted in a part of the question that has earned credit via the question rubric. No part of a question (a, b, c) may have a negative point total. A given penalty can be assessed only once for a question, even if it occurs multiple times or in multiple parts of that question. A maximum of 3 penalty points may be assessed per question.

## 1-Point Penalty

- v) Array/collection access confusion ([] get)
- w) Extraneous code that causes side-effect (e.g., printing to output, incorrect precondition check)
- x) Local variables used but none declared
- y) Destruction of persistent data (e.g., changing value referenced by parameter)
- z) Void method or constructor that returns a value

### **No Penalty**

- Extraneous code with no side-effect (e.g., valid precondition check, no-op)
- Spelling/case discrepancies where there is no ambiguity\*
- Local variable not declared provided other variables are declared in some part
- private or public qualifier on a local variable
- Missing public qualifier on class or constructor header
- Keyword used as an identifier
- Common mathematical symbols used for operators  $(\times \bullet \div \leq \geq <> \neq)$
- [] vs. () vs. <>
- = instead of == and vice versa
- length/size confusion for array, String, List, or ArrayList; with or without
   ( )
- Extraneous [] when referencing entire array
- [i, j] instead of [i][j]
- Extraneous size in array declaration, e.g., int[size] nums = new int[size];
- Missing ; where structure clearly conveys intent
- Missing { } where indentation clearly conveys intent
- Missing ( ) on parameter-less method or constructor invocations
- Missing ( ) around if or while conditions

<sup>\*</sup>Spelling and case discrepancies for identifiers fall under the "No Penalty" category only if the correction can be **unambiguously** inferred from context, for example, "ArayList" instead of "ArrayList". As a counterexample, note that if the code declares "int G=99, g=0;", then uses "while (G<10)" instead of "while (g<10)", the context does **not** allow for the reader to assume the use of the lower case variable.

Learning Objectives: con-1.a con-1.c con-1.e con-2.a con-2.c con-2.e mod-1.g mod-2.f

#### **Canonical solution**

```
(a)
                                                               3 points
    public static int hailstoneLength(int n)
       int count = 1;
       while (n > 1)
          if (n % 2 == 0)
             n = n / 2;
          else
             n = 3 * n + 1;
          count++;
       return count;
    public static boolean isLongSeq(int n)
(b)
                                                               2 points
       return hailstoneLength(n) > n;
    public static double propLong(int n)
(c)
                                                               4 points
       int count = 0;
       for (int i = 1; i <= n; i++)
          if (isLongSeq(i))
              count++;
       return (double) count / n;
    }
```

(a)	hailstoneLength
-----	-----------------

(/	<u> </u>		
	Scoring Criteria	Decision Rules	
1	Loops from given starting value n until the sequence terminates, using updated values for the current term	<ul><li>Responses still earn the point even if they</li><li>update n incorrectly.</li></ul>	1 point 3.C CON-2.C
2	Computes the next value	<ul> <li>Responses still earn the point even if they</li> <li>use a correct formula in an incorrect case.</li> </ul>	1 point 3.C CON-1.A
3	Uses correct formula for next value depending on even/odd	Total for part (a)	1 point 3.c CON-2.A 3 points
		iotal for part (a)	3 points
(b)	isLongSeq		
	Scoring Criteria	Decision Rules	
4	Calls hailstoneLength		1 point 3.A MOD-1.G
5	Correctly compares length and starting value to determine return value	Responses still earn the point even if they  • call hailstoneLength incorrectly.	1 point 3.C CON-1.E
		Total for part (b)	2 points
(c)	propLong		
	Scoring Criteria	Decision Rules	
6	Calls isLongSeq in the context of a loop		1 point 3.A MOD-1.G
7	Loops 1 to n (no bounds errors)		1 point 3.C CON-2.E
8	Calculates double proportion	<ul> <li>Responses still earn the point even if they</li> <li>use incorrect values for the count of long sequences or n.</li> </ul>	1 point 3.C CON-1.C
9	Returns correctly calculated value		1 point 3.B MOD-2.F
		Total for part (c)	4 points
	Question-specific penalties		
	None		
		Total for question 1	9 points

9 points

Learning Objectives: MOD-2.B MOD-2.D CON-1.B CON-1.D CON-2.A

#### **Canonical solution**

```
public class GameSpinner
  private int sectors;
  private int previousSpin = 0;
  private int currentLength = 0;
  public GameSpinner(int s)
      sectors = s;
   }
  public int spin()
      int newSpin = (int) (Math.random() * sectors) + 1;
      if (newSpin == previousSpin)
         currentLength++;
      else
         previousSpin = newSpin;
         currentLength = 1;
      return newSpin;
  public int currentRun()
      return currentLength;
}
```

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GameSpinner

	Scoring Criteria	Decision Rules	
1	Declares all appropriate private instance variables		1 poin
2	Declares method headers:  public int spin() and  public int currentRun()		1 poin
3	Declares header:  GameSpinner(int)  (must not be private)		1 poin 3.1 MOD-2.
4	Constructor initializes instance variable for number of sectors using parameter. Instance variables for previous spin and length of current run initialized correctly when declared or in constructor with default values.	Responses still earn the point even if they  • declare instance variables incorrectly.	1 poin
5	Computes random integer [1, number of sectors]		1 poin 3.7 CON-1.1
6	Compares new spin and last spin to determine required updates to state	<ul> <li>Responses still earn the point even if they</li> <li>use an incorrectly computed random integer for new spin; or</li> <li>incorrectly declare the instance variable intended to store last spin.</li> </ul>	1 poin 3.0 CON-2
7	Updates instance variable that represents length of current run appropriately if new spin and previous spin are the same	<ul> <li>Responses still earn the point even if they</li> <li>incorrectly compare new spin and last spin.</li> </ul>	1 poin  MOD-2.
8	Updates previous spin and length of current run appropriately when new spin differs from the previous spin	<ul> <li>Responses still earn the point even if they</li> <li>incorrectly compare new spin and last spin.</li> </ul>	1 poin
9	currentRun returns updated instance variable value	<ul> <li>Responses still earn the point even if they</li> <li>incorrectly update instance variables in the spin method.</li> </ul>	1 poir  MOD-2.
	Question-specific penalties		
	, r		

Total for question 2

9 points

Learning Objectives: VAR-1.E.b VAR-2.D VAR-2.E.a MOD-1.G CON-2.F.a CON-2.J.a CON-2.K

#### **Canonical solution**

```
(a)
                                                         6 points
    public void addReview(ProductReview prodReview)
       reviewList.add(prodReview);
       String prodName = prodReview.getName();
       boolean found = false;
       for (String n : productList)
          if (n.equals(prodName))
              found = true;
       if (!found)
          productList.add(prodName);
    }
(b)
                                                        3 points
    public int getNumGoodReviews(String prodName)
       int numGoodReviews = 0;
       for (ProductReview prodReview: reviewList)
          if (prodName.equals(prodReview.getName()))
              String review = prodReview.getReview();
              if (review.indexOf("best") >= 0)
                 numGoodReviews++;
           }
       return numGoodReviews;
```

# (a) addReview

	Scoring Criteria	<b>Decision Rules</b>	
1	Adds a ProductReview object to reviewList	Responses still earn the point even if they  • add a ProductReview object other than the one referenced by the parameter prodReview.	1 point 3.D VAR-2.D
2	Gets product name of review to be added		1 point 3.A MOD-1.G
3	Traverses productList (no bounds errors)	<ul><li>Responses still earn the point even if they</li><li>use a for, an enhanced for, or a while loop.</li></ul>	1 point 3.D VAR-2.E.a
4	Compares name in productList with name from review to be added	<ul> <li>Responses still earn the point even if they</li> <li>use an incorrectly accessed value for either name.</li> </ul>	1 point 3.C VAR-1.E.b
5	Adds new product name to productList	<ul> <li>Responses still earn the point even if they</li> <li>add the new product name under the wrong conditions; or</li> <li>add an incorrectly accessed value for the new product name</li> </ul>	1 point 3.D VAR-2.D
6	Correctly adds product name to productList if and only if the product name is not already in productList		1 point 3.D CON-2.K
		Total for part (a)	6 points

## (b) getNumGoodReviews

	Scoring Criteria	<b>Decision Rules</b>	
7	Traverses reviewList (no bounds errors)	<ul><li>Responses still earn the point even if they</li><li>use a for, an enhanced for, or a while loop.</li></ul>	1 point 3.D VAR-2.E.a
8	Selects all and only reviews with matching product names that contain "best"		1 point 3.C CON-2.F.a
9	Returns correct count of good reviews		1 point 3.D CON-2.J.a
		Total for part (b)	3 points
	Question-specific penalties		
	None		
		Total for question 3	9 points

Learning Objectives: MOD-1.D.b MOD-1.G CON-1.H CON-2.A CON-2.N.c VAR-2.F VAR-2.G.a

#### **Canonical solution**

```
(a)
                                                                  5 points
      public Theater (int seatsPerRow, int tier1Rows,
                      int tier2Rows)
         theaterSeats =
            new Seat[tier1Rows + tier2Rows][seatsPerRow];
         for (int r = 0; r < tier1Rows + tier2Rows; r++)</pre>
            for (int c = 0; c < seatsPerRow; c++)</pre>
               if (r < tier1Rows)
                  theaterSeats[r][c] = new Seat(true, 1);
               else
                  theaterSeats[r][c] = new Seat(true, 2);
            }
      }
      public boolean reassignSeat(int fromRow, int fromCol,
(b)
                                                                  4 points
                                    int toRow, int toCol)
         Seat toS = theaterSeats[toRow][toCol];
         if (!toS.isAvailable())
            return false;
         Seat fromS = theaterSeats[fromRow][fromCol];
         if (toS.getTier() < fromS.getTier())</pre>
            return false;
         toS.setAvailability(false);
         fromS.setAvailability(true);
         return true;
```

# (a) Theater

	Scoring Criteria	Decision Rules	
1	Instantiates a new Seat[][] with the correct number of rows and columns, based on parameters		1 point 3.E VAR-2.F
2	Traverses the theaterSeats array (no bounds errors)		1 point 3.E VAR-2.G.a
3	Instantiates a new Seat object with a tier and availability status	<ul> <li>Responses still earn the point even if they</li> <li>incorrectly assign the new object to a theaterSeats element.</li> </ul>	1 point 3.A  MOD-1.D.b
4	Accesses a theaterSeats element and assigns it a new Seat object	<ul> <li>Responses still earn the point even if they</li> <li>incorrectly instantiate the new Seat object; or</li> <li>assign the new Seat object to an incorrect theaterSeats element.</li> </ul>	1 point 3.E VAR-2.F
5	Correct tiers assigned to all array elements		1 point 3.C CON-2.A
		Total for part (a)	5 points

# (b) reassignSeat

	Scoring Criteria	Decision Rules	
6	Accesses from and to Seat		1 point
	objects		3.E
			VAR-2.F
7	Calls isAvailable and	Responses still earn the point even if they	1 point
	getTier on Seat objects	<ul> <li>correctly call methods on</li> </ul>	3.A
		theaterSeats elements other	MOD-1.G
		than the to and from seats.	
8	Checks if move can be made based		1 point
	on both tiers and the availability		3.C
	status of to Seat object		CON-1.H
9	Correctly updates availability of		1 point
	both seats and returns true if		3.E
	the move can be made; otherwise,		CON-2.N.c
	returns false		
		Total for part (b)	4 points
	Question-specific penalties		
	None		
		Total for question 4	9 points

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