CS 5/7320 Artificial Intelligence

Search with Uncertainty

AIMA Chapters 4.3-4.5

Slides by Michael Hahsler with figures from the AIMA textbook



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Types of uncertainty we consider for now*



Nondeterministic Actions:

Outcome of an action in a state is uncertain.



No observations:

Sensorless problem



Partially observable environments: The agent does not know in what state it is.



Exploration:

Unknown environments and Online search

* we will quantify uncertainty with probabilities later.

Consequence of Uncertainty

 Remember: The solution for the known maze was a plan consisting of a fixed sequence of actions from start to goal.

 With uncertainty: Solution is typically not a precomputed sequence, but a

conditional plan (also called strategy or policy)

that depends on percepts.



Nondeterministic Actions

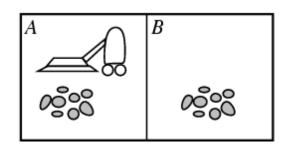
Outcome of actions in the environment is nondeterministic = transition model need to describe uncertainty

Example transition:

$$Results(s_1, a) = \{s_2, s_4, s_5\}$$

i.e., action a in s_1 can lead to one of several states.

Example: Erratic Vacuum World

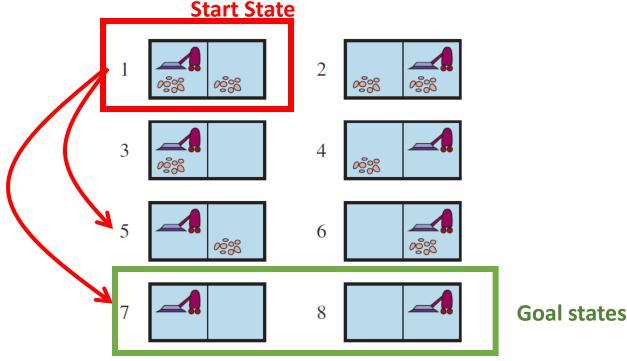


Regular fully-observable vacuum world, but the action 'suck' is more powerful and nondeterministic:

- a) On a dirty square: cleans the square and sometimes cleans dirt on adjacent squares as well.
- **b)** On a clean square: sometimes deposits some dirt on the square.

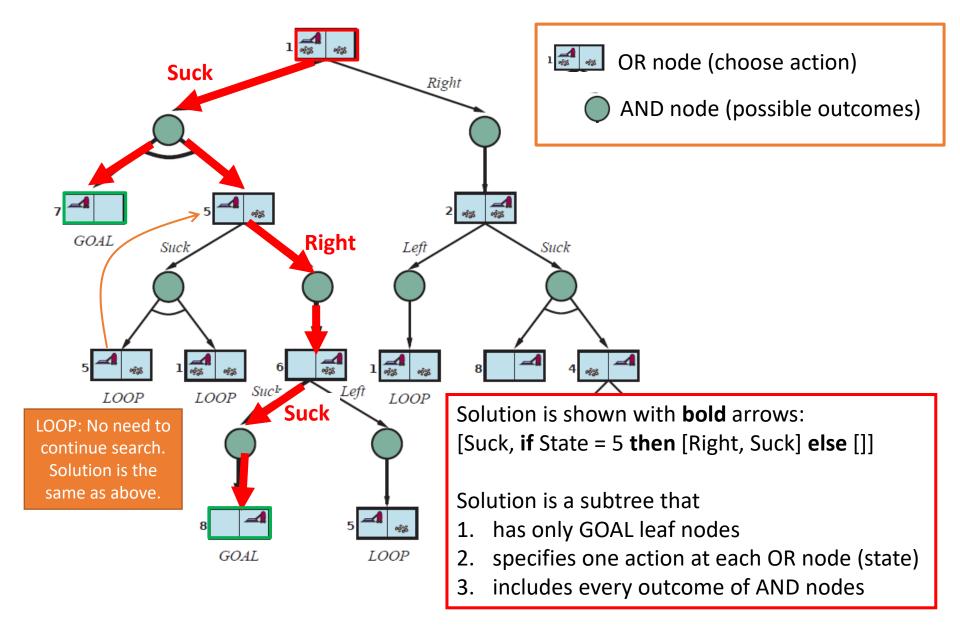
Example: Erratic Vacuum World

 $Results(1, Suck) = \{5, 7\}$

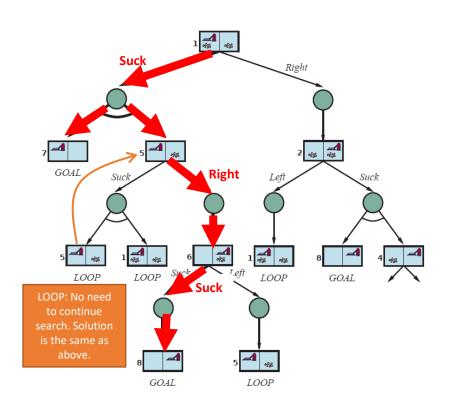


We need a conditional plan
[Suck, if State = 5 then [Right, Suck] else []]

Finding a Cond. Plan: AND-OR Search Tree



AND-OR Tree search: Idea



- Descend the tree by trying an action in each OR node and considering all resulting states of the AND nodes.
- Remove branches (actions) if we cannot find a subtree below that leads to only goal nodes. (see failure in the code on the next slide).
- Stop when we find a subtree that guarantees to only reach goal states.
- Return the conditional plan that represents the subtree.

AND-OR Recursive DFS Algorithm

= nested If-then-else statements

```
function AND-OR-SEARCH(problem) returns a conditional plan, or failure
  return OR-SEARCH(problem, problem.INITIAL, [])
                                                              path is only maintained for cycle checking!
function OR-SEARCH(problem, state, path) returns a conditional plan, or failure
  if problem.IS-GOAL(state) then return the empty plan
  if IS-CYCLE(path) then return failure
                                            // don't follow loops using path.
  for each action in problem. ACTIONS(state) do // try all possible actions
      plan \leftarrow AND\text{-SEARCH}(problem, RESULTS(state, action), [state] + path])
      if plan \neq failure then return [action] + plan
  return failure
                                               // fail means we found no action that leads to
                                               // a goal-only subtree
function AND-SEARCH(problem, states, path) returns a conditional plan, or failure
                                                    // try all possible outcomes, none can fail!
  for each s_i in states do
                                                    // (= belief state)
      plan_i \leftarrow \text{OR-SEARCH}(problem, s_i, path)
      if plan_i = failure then return failure
  return [if s_1 then plan_1 else if s_2 then plan_2 else ... if s_{n-1} then plan_{n-1} else plan_n]
```

Notes:

- The DFS search tree is implicitly created using the call stack (recursive algorithm).
- DFS is **not optimal!** BFS and A* search can be used to find the optimal solution.

Use of Conditional Plans

 The conditional plan can be used in a model-based reflex agent.

Example: After the initial action "suck"



Using Actions to Coerce the World into Known States

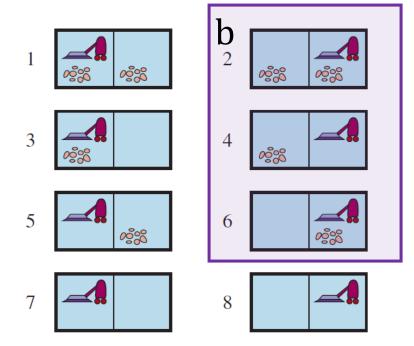
No Observations

 Sensorless problem = unobservable environment also called a conformant problem

- Why is this useful?
- **Example**: Doctor prescribes a broad-band antibiotic instead of performing time-consuming blood work for a more specific antibiotic. This saves time and money.
- Basic idea: Find a solution (a sequence of actions) that works from any state and then just blindly execute it (open loop system).

Belief State

- The agent does not know in which it is exactly in.
- However, it may know that it is in one of a set of possible states.
 This set is called a belief state of the agent.
- Example: $b = \{s_2, s_4, s_6\}$

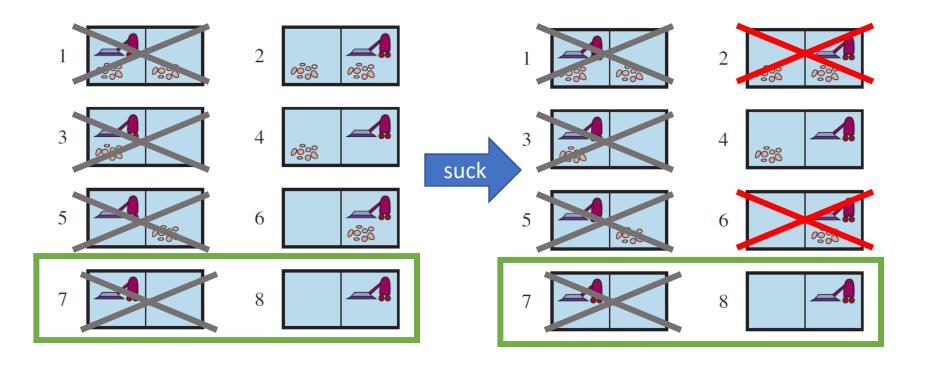


Actions to Coerce the World into States

- Actions can reduce the number of possible states.
- **Example**: Deterministic vacuum world. Agent does not know its position and the dirt distribution.

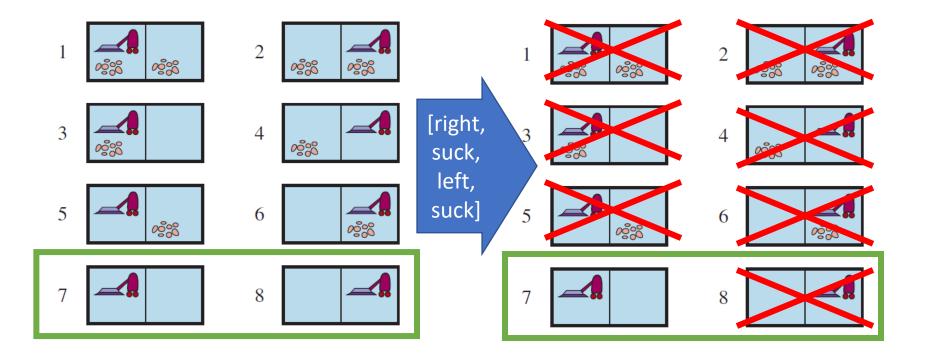
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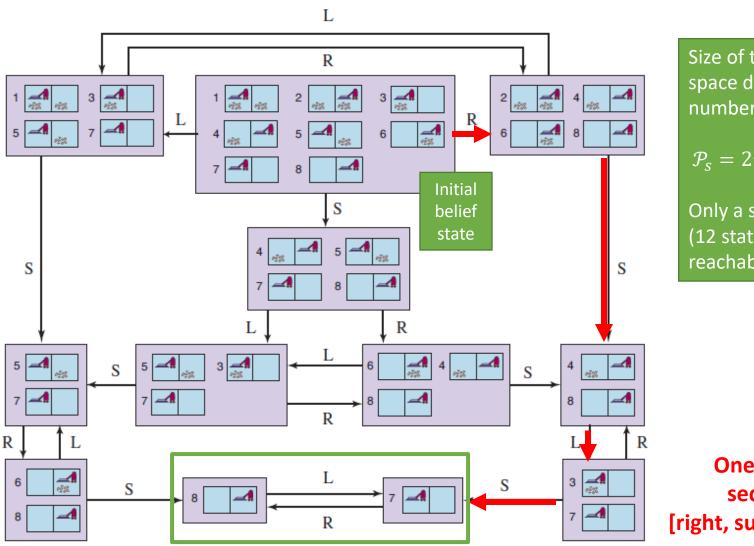


Actions to Coerce the World into States

- The action sequence [right, suck, left, suck] coerces the world into the goal state 7. It works from any initial state!
- There are no observations so there is no need for a conditional plan.



Example: The reachable belief-state space for the deterministic, sensorless vacuum world



Size of the belief state space depends on the number of states *N*:

$$P_s = 2^N = 2^8 = 256$$

Only a small fraction (12 states) are reachable.

One solution sequence: [right, suck, left, suck]

Finding a Solution Sequence

Note: State space size makes this impractical for larger problems!

Formulate as a regular search and solve with DFS, BFS or A*:

- States: All belief states (=powerset \mathcal{P}_{S} of states of size 2^{N} for N states)
- Initial state: Often the belief state consisting of all states.
- Actions: Actions of a belief state are the union of the possible actions for all the states it contains.
- Transition model: $b' = Results(b, a) = \{s' : s' = Result(s, a) \text{ and } s \in b\}$
- Goal test: Are all states in the belief state goal states?
- **Simplifying property:** If a belief state (e.g., $b_1 = \{1,2,3,4,5\}$) is solvable (i.e., there is a sequence of actions that coerce all states to only goal states), then belief states that are subsets (e.g., $b_2 = \{2,5\}$) are also solved using the same action sequence. Used to prune the search tree.

Other approach:

• **Incremental belief-state search**. Generate a solution that works for one state and check if it also works for all other states. This is similar to local search.



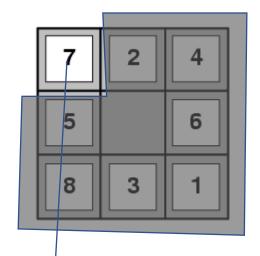
Percepts and Observability

- Many problems cannot be solved efficiently without sensing (e.g., 8-puzzle).
- We need to be able to at least see one square.

Percept function: Percept(s)

s is the state

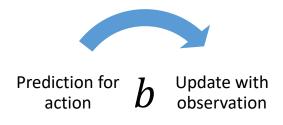
- Fully observable: Percept(s) = s
- Sensorless: Percept(s) = null
- Partially observable: Percept(s) = o

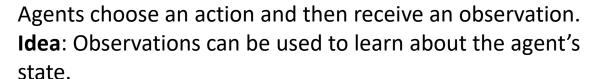


Percept(s) = Tile7

Problem: Many states (different order of the hidden tiles) can produce the same percept!

Use Observations to Learn About the State







Assume we have a current belief state b (i.e., the set of states we could be in).

Prediction for action: Choose an action a and compute a new belief state that results from the action.

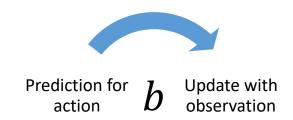
$$\hat{b} = Predict(b, a) = \bigcup_{s \in b} Predict(s, a)$$

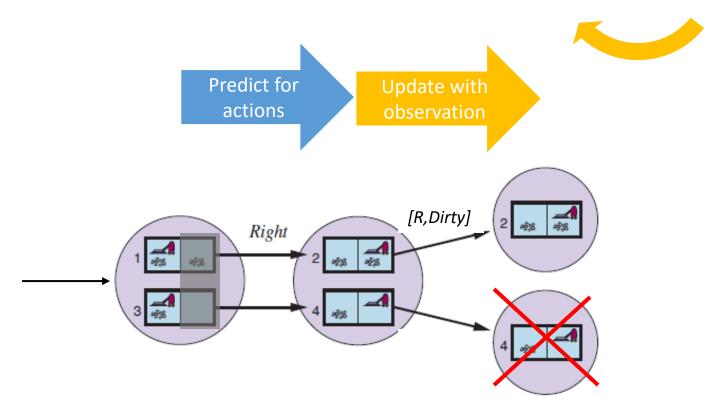
Update with observation: You receive an observation *o* and only keep states that are consistent with the new observation.

$$b_o = Update(\hat{b}, o) = \{s : s \in \hat{b} \land Percept(s) = o\}$$

Both steps in one: $b \leftarrow Update(Predict(b, a), o)$

Example: Deterministic local sensing vacuum world



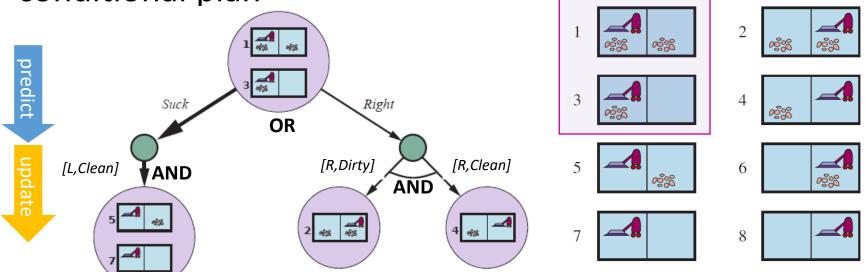


$$b \leftarrow Update(Predict(\ b\ , \ a\), \ o\)$$

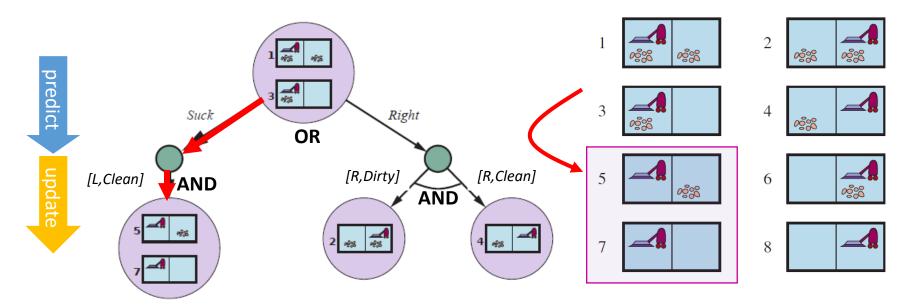
$$Update(Predict(\{1,3\}, Right), [R, Dirty]) = \{2\}$$

Use an AND-OR tree of belief states to create a

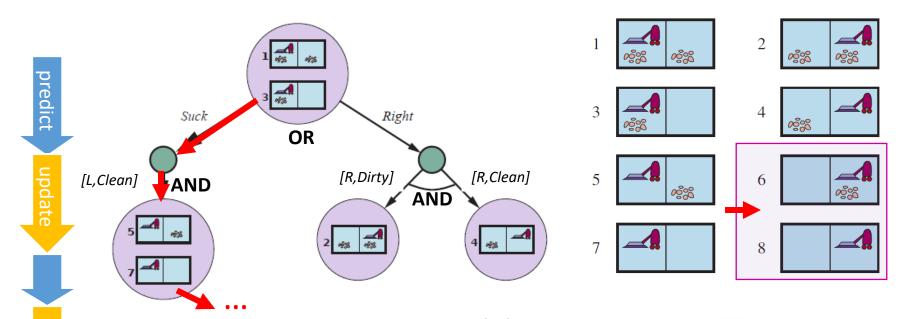
conditional plan



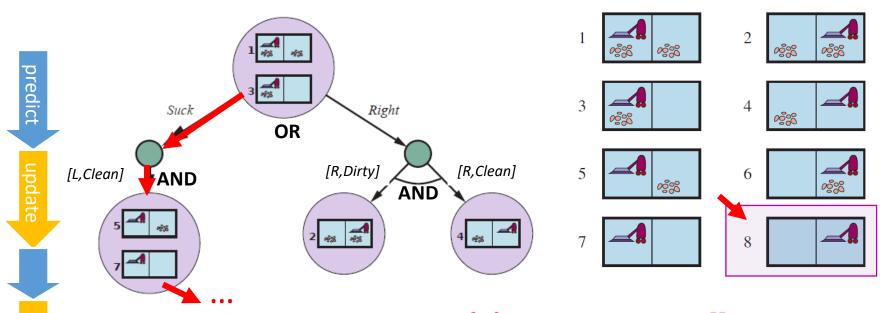
Use an AND-OR tree to create a conditional plan



Use an AND-OR tree to create a conditional plan



Use an AND-OR tree to create a conditional plan

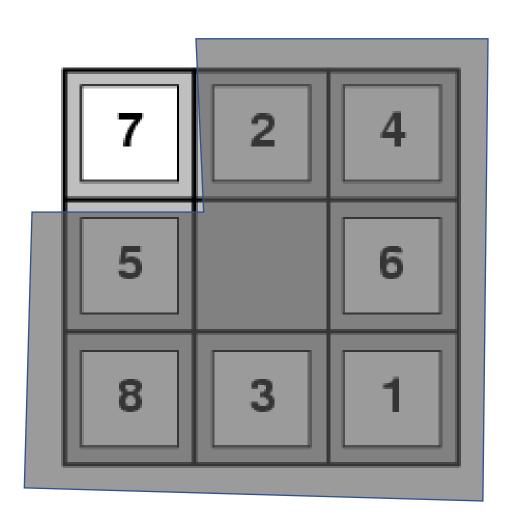


State Estimation and Approximate Belief States

- Agents choose an action and then receive an observation from the environment.
- The agent keep track of its belief state using the following update:

$$b \leftarrow Update(Predict(b, a), o)$$

- This process is often called
 - · monitoring,
 - **filtering**, or
 - state estimation.
- The agent needs to be able to update its belief state following observations in **real time!** For many practical application, there is only time to compute an **approximate belief state!** These approximate methods are outside the scope of this introductory course.

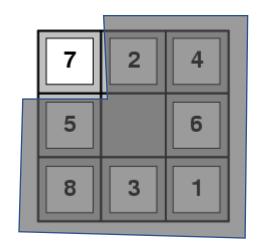


Case Study

Partially Observable 8-Puzzle

Partially Observable 8-Puzzle

How do we solve this problem? What are the main steps?



- Give a problem description for each step.
 - States:
 - Initial state:
 - Actions:
 - Transition model:
 - Goal test:
 - Percept function:

- What type of agent do we use?
- What algorithms can be used?



Online Search

- Recall offline search: Create plan using the state space as a model before taking any action. The plan can be a sequence of actions or a conditional plan to account for uncertainty.
- Online search explores the real world one action at a time. Prediction is replaced by "act" and update by "observe."



- Useful for
 - Real-time problems: When offline computation takes too long and there is a penalty for sitting around and thinking.
 - Nondeterministic domain: Only focus on what actually happens instead of planning for everything!
 - **Unknown environment**: The agent has no complete model of the environment. It needs to explore an unknown state space and/or what actions do. i.e., it needs to learn the transition model $f: S \times A \to S$

Design Considerations for Online Search

- **Knowledge**: What does the agent already know about the outcome of actions? E.g., does go north and then south lead to the same location?
- Safely explorable state space/world: There are no irreversible actions (e.g., traps, cliffs). At least the agent needs to be able to avoid these actions.
- Exploration order: Expanding nodes in local order is more efficient if you have to execute the actions to get observations: Depth-first search with backtracking instead of BFS or A* Search.

Online Search: Agent Program for Unknown Transition model

Environment is deterministic and completely observable (percept(s) = s) but the transition model (function result) and the state space are unknown.

Approach: The algorithm builds the map $result(s, a) \rightarrow s'$ by trying all actions and backtracks when all actions in a state have been explored.

```
Learns results function
function ONLINE-DFS-AGENT(problem, s') returns an action
                                                                                Untried and
               s, a, the previous state and action, initially null
                                                                            unbacktracked are
  persistent: result, a table mapping (s, a) to s', initially empty
               untried, a table mapping s to a list of untried actions
                                                                               the "frontier"
               unbacktracked, a table mapping s to a list of states never backtracked to
  if problem.IS-GOAL(s') then return stop
  if s' is a new state (not in untried) then untried [s'] \leftarrow problem.ACTIONS(s')
  if s is not null then
                                                Record the found transition
      result[s, a] \leftarrow s'
      add s to the front of unbacktracked[s']
  if untried[s'] is empty then
      if unbacktracked[s'] is empty then return stop
      else a \leftarrow an action b such that result[s', b] = POP(unbacktracked[s'])
  else a \leftarrow POP(untried[s'])
  s \leftarrow s'
  return a
```



Important concepts that you should be able to explain and use now...

- Difference between solution types:
 - a fixed actions sequence, and
 - a conditional plan (also called a strategy or policy).
- What are belief states?
- How actions can be used to coerce the world into states.
- How observations can be used to learn about the state: State estimation with repeated predict and update steps.
- The use of AND-OR trees.