Assignment Two

Ethan Morton

Ethan.Morton1@Marist.edu

October 14, 2024

1 SETTING UP THE SCENARIO

1.1 READING FROM MAGICITEMS.TXT

The lines in magicitems.txt are loaded into the lines array at runtime. NUM_LINES is defined as 666. main.cpp

```
int main() {
       //{\it Read\ lines\ from\ magicitems.txt}
       std::ifstream file("../magicitems.txt");
       if (!file.is_open()) {
            printf("Unable to open file\n");
            return 1;
       string lines[NUM_LINES];
90
       string line;
       int index = 0;
       while (std::getline(file, line)) {
            lines[index] = line;
            index++;
95
       file.close();
98
       //...
99
   }
```

1.2 Picking 42 random items

The lines array is first shuffled using the Knuth shuffle algorithm.

```
main.cpp
   void knuthShuffle(string* arr, const int size) {
        std::random_device rd;
72
        std::mt19937 gen(rd());
        //count backwards from the array
        for (int i = size - 1; i > 0; i--) {
             //pick a random index in the array and swap the element with the
                 element at i
             std::uniform_int_distribution dist(0, i);
             const int ii = dist(gen);
            swap(arr[i], arr[ii]);
79
        }
   }
   The first 42 items of the shuffled lines array are copied into a new array called rand42. NUM RAND is
   defined as 42.
   main.cpp
    int main() {
        //...
97
        //Get 42 random items
        string rand42[NUM_RAND];
100
        knuthShuffle(lines, NUM_LINES);
101
        for (int i = 0; i < NUM_RAND; i++) {</pre>
102
            rand42[i] = lines[i];
103
104
        mergeSort(lines, NUM_LINES);
105
106
        //...
107
   }
108
   Then the lines array is sorted via the merge sort algorithm.
   main.cpp
    int mergeSortHelper(string* arr, const int left, const int right) {
14
        if (left >= right) {
            return 0;
        }
17
        int comparisons = 0;
18
        const int mid = left + (right - left) / 2;
        //merge sort on left side of array
        comparisons += mergeSortHelper(arr, left, mid);
21
        //merge sort on right side of array
        comparisons += mergeSortHelper(arr, mid + 1, right);
        //divide into left and right temp arrays
24
```

```
const int leftArrLen = mid - left + 1;
25
       const int rightArrLen = right - mid;
       std::vector<string> leftArr = std::vector<string>(leftArrLen);
       std::vector<string> rightArr = std::vector<string>(rightArrLen);
28
       // string leftArr[leftArrLen];//the stack won't be happy about this
29
       // string rightArr[rightArrLen];
       for (int i = 0; i < leftArrLen; i++) {
31
            leftArr[i] = arr[left + i];
32
       }
       for (int i = 0; i < rightArrLen; i++) {</pre>
34
            rightArr[i] = arr[mid + 1 + i];
35
36
        //compare and sort
       int i = 0, ii = 0, iii = left;
38
       while (i < leftArrLen && ii < rightArrLen) {
39
            comparisons++;
            if (leftArr[i] <= rightArr[ii]) {</pre>
                arr[iii] = leftArr[i];
42
                i++;
43
            } else {
                arr[iii] = rightArr[ii];
                ii++;
46
            }
            iii++;
49
       comparisons++;//A comparison is made when the while loop stops
50
       //merge back together
       while (i < leftArrLen) {</pre>
52
            arr[iii] = leftArr[i];
53
            i++;
            iii++;
56
       while (ii < rightArrLen) {</pre>
57
            arr[iii] = rightArr[ii];
            ii++;
59
            iii++;
60
       }
       return comparisons;
62
   }
63
   //Time\ complexity\ O(nlog2(n))
   //Specifically it's slightly better on average
66
   int mergeSort(string* arr, const int size) {
67
       return mergeSortHelper(arr, 0, size - 1);
```

2 Linear Search

A linear search is performed over the lines array to check if each of the 42 random items are in the array. The number of comparisons is tracked and printed for each of the 42 items. Then the average is printed for all 42 items. The linear search goes through the lines array one at a time to check if the item is equal to the target item. Since the 42 items were randomly chosen, we should expect the 42 items to be evenly distributed within the lines array. Therefore we should expect the average number of comparisons to be equal to half of the length of the list, or n/2. 666/2 = 333, which is close to the observed average of 334.2 over 5 samples. It should be half because a linear search can stop when it finds the item. Since it's evenly distributed, the average value of the 42 items should be roughly equal to the average value of all items. Linear search has an asymptotic running time of O(n/2) = O(n).

```
main.cpp
```

```
int main() {
104
        //...
105
106
        //Linear search
107
        int comparisons = 0;
108
        int totalComparisons = 0;
109
        for (const string& rand : rand42) {
110
            for (const string& ln : lines) {
111
                 comparisons++;
112
                 if (rand == ln) {
113
                     break; //It's assumed that the target string will be found
114
                 }
115
             }
116
            if constexpr (PRINT_EACH_ITEM) {
                 printf("Linear search comparisons for %s: %d\n", rand.c_str(),
118
                     comparisons);
            }
119
            totalComparisons += comparisons;
120
             comparisons = 0;
121
122
        printf("Linear search average comparisons: %.2f\n",
123
             static_cast<float>(totalComparisons) /
             static_cast<float>(NUM_RAND));
124
        //...
   }
126
```

3 BINARY SEARCH

A binary search is performed over the same arrays. The comparisons are tracked and printed, same as with linear search. I chose to use iteration instead of recursion for this implementation of binary search. The binary search divides the lines array in half until the item in the middle matches the target. This gives the asymptotic running time of $O(log_2(n))$. Since we are dividing by 2, we expect that in the worst case, the number of comparisons should be $log_2(n)$. $log_2(666) = 9.379...$, which is a little higher than the observed average of 8.14 over 5 samples. The reason it's slightly lower is because that is worst case. The best case is O(1), so we should expect some elements to be found quickly. There is a 1/666 chance at finding the item at depth=0, a 2/332 chance at finding the item at depth=1, and at depth=d, the chance is given by the following equation:

$$\frac{2^d}{\left(\frac{666}{d+1}\right) - d} \tag{3.1}$$

At any given depth, you have to subtract the chances for all the previous depths because the item did not exist at that depth, so we can rewrite the equation:

$$\frac{2^d}{\left(\frac{666}{d+1}\right) - d} - \sum_{n=0}^{d-1} \frac{2^n}{\left(\frac{666}{n+1}\right) - n} \tag{3.2}$$

At approx. d = 7.028, the chance of finding the item is .5 or 50%. Even if d=0, we still have to count the initial comparison, so the number of comparisons = d + 1, which means there should be 8.028 comparisons to find the item 50% of the time. 8.028 is much closer to the observed value of 8.14. Keep in mind only 5 samples were taken. More samples would likely have made the observed average closer to 8.028.

main.cpp

```
int main() {
122
        //...
123
124
        //Binary search
125
         //That's right, I did it without recursion. Stay mad Haskell developers!
126
        totalComparisons = 0;
        int left, right, mid;
128
        for (const string& rand : rand42) {
129
             left = 0;
             right = NUM_LINES - 1;
131
             while (left <= right) {</pre>
132
                  comparisons++;
133
                 mid = (left + right) / 2;
134
                  if (rand == lines[mid]) {
135
                      break; //It's assumed that the target string will be found
136
                  }
137
                  if (rand < lines[mid]) {</pre>
138
                      right = mid - 1;
139
                  } else {
140
                      left = mid + 1;
141
                  }
142
             }
143
```

```
if constexpr (PRINT_EACH_ITEM) {
144
                 printf("Binary search comparisons for %s: %d\n", rand.c_str(),
145

    comparisons);

146
            totalComparisons += comparisons;
147
             comparisons = 0;
148
149
        printf("Binary search average comparisons: %.2f\n",
150
             static_cast<float>(totalComparisons) /
             static_cast<float>(NUM_RAND));
151
        //...
152
   }
153
```

4 Hash Table

4.1 HASH TABLE IMPLEMENTATION

The HashTable struct is implemented with an array of Buckets of size 250, and a static hashing function. This HashTable only works with strings. This implementation uses chaining to handle collisions. It comes with a method to insert a new string, and search for an existing string. The search function returns how many comparisons where made to find the string, or a non-positive number if it doesn't exist.

To insert 666 items into a HashTable with 250 buckets, there must necessarily be collisions. If we assume that all 666 items were evenly distributed in each buckets, then each bucket should have 666/250 = 2.664 items, which is a little bit less than the observed average of 3.21 over 5 samples. The reason for this discrepancy is that 2.664 items per bucket is the best case scenario, where there are no empty buckets. In reality, it is very unlikely for there to be no empty buckets. Some buckets will be empty, and some queues will have more than 2.664 items. When we search for an item that we know is in the hash table, we will never come across a bucket that is empty during the search. If we assume there are fewer than 666 buckets with items in them, there will necessarily be a higher average number of items per bucket than 2.664 among buckets with items, because it has to compensate for the empty buckets. In buckets with multiple items, we would expect the number of comparisons to be half of the number of items in the bucket because it uses a linear search, which would imply that there are around 6.42 items per bucket. We can calculate the efficiency of the hash function with the following equation:

Efficiency =
$$\left(\frac{\text{Ideal Average Items per Bucket}}{\text{Actual Average Items per Non-empty Bucket}}\right) \times 100$$
 (4.1)

With our values:

$$41.5\% = \left(\frac{2.664}{6.42}\right) \times 100\tag{4.2}$$

41.5% efficiency isn't very good for a hashing function, but it could be worse.

hashtable.hpp

37

```
struct HashTable {
   void insert(const string& new_str);
```

```
///Returns how many comparisons were used to check if the string is in
38
            the hash table.
       ///Returns 0 if it doesn't exist.
39
       int search(const string& find_str) const;
40
   private:
42
       static int hash(string value);
43
44
       Bucket arr[HASHTABLE_SIZE]; //hopefully the stack is cool with me dumping
            10,000 bytes on it
   };
46
```

The insert and search functions call the hash function to obtain the index in the Bucket array, then insertion or search logic is delegated to the Bucket's insert or search method.

The hash function converts all characters to upper case, then sums the ASCII value of each character. The index returned is the remainder of the sum divided by the size of the hash table.

hashtable.cpp

4.2 Bucket implementation

The Bucket struct is a tagged union which represents one of three variants: Empty, Str, and Queue. Str means the bucket only has one string, and Queue means the bucket has a linked list of strings.

hashtable.hpp

```
enum class Tag {Empty, Str, Queue};

///Tagged union for either an empty bucket, one string, or a linked list of
strings.

///I was going to use std::variant, but I can't link with it, so now I have
to make my own tagged union.

struct Bucket {

Tag tag;
```

```
union {
17
            string str;
           Queue<string> queue;
19
       };
20
21
       Bucket();
       ~Bucket();
23
24
       ///If the bucket is empty, it will insert the new_str.
       ///If the bucket has a string, it will turn it into a linked list with
        \rightarrow the old string + new_str.
       ///If the bucket has a linked list, it will add new_str to the end.
       void insert(const string& new_str);
29
       ///Returns how many comparisons were used to check if the string is in
30
            the bucket.
       ///Returns <= 0 if not found.
31
       int search(const string& str) const;
32
   };
33
```

In Bucket::insert, it uses the tag to determine how to insert the new string into the bucket. If it's Empty, it sets str to the new string and updates the tag to Str. If it's Str, it creates a queue and adds the existing string and the new string to that queue, and updates the tag to Queue. If it's Queue, it simply enqueues the new string.

hashtable.cpp

```
void Bucket::insert(const string& new_str) {
31
        switch (tag) {
32
            case Tag::Empty:
33
                tag = Tag::Str;
34
                new (&str) string(new_str);
35
                break;
            case Tag::Str: {
                std::string copy = std::move(str);
38
                str.~string();
39
                tag = Tag::Queue;
                new (&queue) Queue<string>();
41
                queue.enqueue(copy);
42
                queue.enqueue(new_str);
                break;
44
            }
45
            case Tag::Queue:
46
                queue.enqueue(new_str);
       }
48
   }
49
```

In Bucket::search, it uses the tag to determine how to search for the target string. If it can't find the target string, a non-positive integer is returned (either 0 or -1). If it's Str, it just returns 1 because 1 comparison was made. If it's Queue, it delegates the search logic to the search method for Queue, and adds 1 for the initial comparison.

hashtable.cpp

```
int Bucket::search(const string& find_str) const {
51
       switch (tag) {
52
            case Tag::Empty:
53
                return -1; //not found
54
            case Tag::Str:
                assert(str == find_str);
                return 1;
57
            case Tag::Queue:
58
                return 1 + queue.search(find_str);
       }
60
       return -1; //unreachable
61
   }
62
```

4.3 Queue implementation

The Queue struct is a stripped-down queue with methods only required by this program. It uses a linked list implementation and uses a template for generic types, but only uses string in this program.

Queue::search uses a linear search to go through each element in the linked list until the item is found. It returns the number of comparisons, or -1 if the item was not found.

queue.hpp

```
///First in, first out data structure with linked-list implementation.
   ///For this project, this queue will be used more like a regular linked
       list.
   ///and has some linked list methods instead of queue methods.
   template<typename T> struct Queue {
   private:
       Node < T > * head;
11
       Node<T>* tail;
12
   public:
       /// Creates an empty queue.
15
       Queue() : head(nullptr), tail(nullptr) {}
16
       /// Deallocates all allocated nodes from the heap.
18
       ~Queue() {
19
           while (head != nullptr) {
                Node<T>* next = head->next;
21
                delete head;
22
                head = next;
23
```

```
}
        /// Adds the item to the tail of the queue.
27
       void enqueue(const T& item) noexcept {
28
            if (head == nullptr) {
                head = tail = new Node<T>(item);
30
                return;
31
            }
            tail->next = new Node<T>(item);
33
            tail = tail->next;
34
       }
35
        ///Returns how many comparisons were used to check if the target is in
37
            the queue.
        ///Returns -1 if it doesn't exist.
        int search(const T& target) const {
39
            int comparisons = 0;
40
            Node<T>* curr = head;
41
            while (curr != nullptr) {
                 comparisons++;
43
                 if (curr->data == target) {
44
                     return comparisons;
                 }
46
                 curr = curr->next;
47
            }
48
            return -1;
       }
50
   };
51
   4.4 Node implementation
   The Node struct is the container for each element in a linked list. It uses a template for generic types, but
   only string is used in this program. It holds some data, and a pointer to the next element in the list.
   node.hpp
   /// Node for linked-list-style data structures.
   /// Data structures are responsible for cleaning up resources used by Nodes.
   template<typename T> struct Node {
       T data;
       Node* next;
        explicit Node(const T& item, Node* next = nullptr) : data(item),
        → next(next) {}
```

}

24

};

11