

Evaluation of a Bin Packing Approach for Distributed Global Rescheduling

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Abstract—Morbi luctus, wisi viverra faucibus pretium, nibh est placerat odio, nec commodo wisi enim eget quam. Quisque libero justo, consectetur a, feugiat vitae, porttitor eu, libero. Suspendisse sed mauris vitae elit sollicitudin malesuada. Maecenas ultricies eros sit amet ante. Ut venenatis velit. Maecenas sed mi eget dui varius euismod. Phasellus aliquet volutpat odio. Vestibulum ante ipsum primis in faucibus orci luctus et ultrices posuere cubilia Curae; Pellentesque sit amet pede ac sem eleifend consectetur. Nullam elementum, urna vel imperdiet sodales, elit ipsum pharetra ligula, ac pretium ante justo a nulla. Curabitur tristique arcu eu metus. Vestibulum lectus. Proin mauris. Proin eu nunc eu urna hendrerit faucibus. Aliquam auctor, pede consequat laoreet varius, eros tellus scelerisque quam, pellentesque hendrerit ipsum dolor sed augue. Nulla nec lacus.

I. INTRODUCTION

With the arrival of Petascale and highly parallel computing platforms, scientific simulations, such as molecular dynamics, have been able to achieve great advance in their respective fields [1], [2]. However, load imbalance is a recurrent problem in scientific applications, specially in those with an intrinsic dynamic nature [3]. Global rescheduling strategies try to solve this issue, redistributing work amongst Processing Elements (PEs), seeking a more homogeneous state of the system load.

The cost of dynamically rescheduling an application is bound to two main steps: i) a decision step, in which the scheduler remaps tasks to PEs; ii) a migration step, in which the data associated to the tasks is migrated [4]. In a small scale system, the higher cost is associated with migration costs, since communication is limited (less PEs to communicate). As systems scale, the communication costs associated with the decision step may considerably grow. Thus, applications may present significant performance losses when rescheduling strategies do not take into account the communication costs [5].

Centralized global rescheduling strategies are very efficient when aggregating data and dealing with it does not create unexpectedly high migration or decision time overheads. However, as researchers want to execute scientific applications to solve larger problems in highly parallel machines, the overhead of centralized rescheduling may be higher than the effects of load imbalance. This creates a need for scalable schedulers,

able to present close to homogeneous distribution of load with a low overhead.

Distributed rescheduling strategies use the local information available on PEs to redistribute work without global information. This way PEs take decisions based on a best local scenario, making most of these algorithms *Greedy*. This is advantageous, since scheduling work amongst PEs perfectly is an NP-Hard problem [6].

As Exascale approaches, computing platforms become able of higher levels of scalability. Schedulers have to work with ever increasing amounts of information in these platforms, which demands higher performance and efficiency on load balancing. Even though few distributed strategies exist [5], [7], it is still a field to be explored since each platform and application may benefit from different strategies.

In this paper, we propose and present an evaluation of a *Bin Packing* approach for refinement-based distributed global rescheduling called *Task Packing*. Our novel strategy is based on previous distributed approaches and attempts to minimize the communication during the remapping process. Migrating groups of work-units instead one-by-one exchanges should mitigate most network-related issues, such as network congestion and jitter.

Our results show that ...

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II. RELATED WORK

Global rescheduling is a well studied theme in high performance computing [3], [5], [8], [9], [10], [7], [11]. In the centralized domain, strategies implement a variety of heuristics in order to achieve an homogeneous distribution of load. Although centralized algorithms are used the most, they lack scalability and new approaches must be pursued as systems grow.

Refinement based solutions in centralized load balancing are very effective in dealing with low imbalance or high migration costs [12]. Since these strategies use a limited migration heuristic, they are able to efficiently balance load with a low overhead. However, since refine strategies limit a total number of migrations, they cannot deal with very unbalanced systems.

Different approaches have been used to scale scheduling strategies. Hierarchical algorithms will work differently in different levels, exploring parallelism and delivering better performance [8], [9], [13]. Strategies in this domain have been able to ensure scalability so far, but are still limited by a centralized beginning and data dependency.

Also in the hierarchical domain, multilevel graph partitioning has been used to efficiently reschedule tasks [10]. The hypergraph abstraction accurately represents communication, which provides more precision for load balance [14], [15]. However, the cost of this representation is very high for a first task mapping process, being more recommended for repartitioning.

Work stealing is one of the most broadly used techniques for balancing load in parallel systems [16], [17]. The completely distributed essence of this techniques make them very effective scheduling solutions for parallel and distributed irregular applications.

Diffusive load balancing is a completely distributed solution that may benefit iterative applications [7]. These schedulers irradiate work from overloaded PEs to their neighbors, in an effort to achieve load balance in an iterative fashion. Very unbalanced systems suffer with this kind of approach, since the scheduler may take too long to reach a solution.

Grapevine is a completely distributed refinement-based scheduling solution. It uses probabilistic transfer of load and epidemic communication protocols to achieve scalability [5]. We intend to use what was created in *Grapevine* and reduce its communication, using the *Task Packing* approach.

Add related work on BinLPT

III. THE TASK PACKING APPROACH

Global rescheduling algorithms must be effective in order to improve scheduling, but should also have low overhead in order to avoid reducing its benefits. To ensure a quick and informed remapping of tasks, we present the *Task Packing Approach*. Sharing global information (e.g. processor affinity, estimated computational load, expected communication patterns, etc) allows a PE to create groups of the best tasks to leave a given processor and take the migration decision with one message, instead of several.

In this work we present the *PackDrop* strategy, a distributed refinement-based technique implementing our new approach. We expect that: i) reducing unnecessary communication; ii) exploring locality of tasks mapped to the same PE, since migrations are done in groups; thus iii) resulting in an accelerated decision making process, which should bring a better overall runtime for applications.

First we will explain the *Pack Creation* (Algorithm 1) and the *Pack Sending* (Algorithm 2) processes of this strategy. Then the complete strategy will be presented in Algorithm 3, *PackDrop*.

For simplicity, in all algorithms presented here: i) the symbol: “ \rightarrow ” will represent a remote procedure call; ii) and the symbol: “ \Rightarrow ” will represent the start of a reduction process.

A. Pack Creation

The *Pack Creation* process for the *PackDrop* strategy is presented in Algorithm 1. It uses an estimated pack size (ps), a set of local tasks (T), the current PE *load* and a threshold for PE loads ($thrs$), to create a set of *Packs*. The threshold is used to calculate an upper bound (ub) of the average system load (\overline{load}), using Equation 1.

$$ceil(l, v) = (1 + v) \times l \quad (1)$$

$$load(B) = \sum_{t \in B} t \quad | \quad B \text{ is a bag of tasks} \quad (2)$$

With this information, each PE will take the task with the lower load within its pool, and pack it (lines 3 – 6). Then, if the sum of all tasks in the pack is greater then the expected pack size (ps), the pack is closed and the strategy start filling another one (lines 7 – 10). The process is repeated while ub is greater than $load$ (line 2).

Algorithm 1: Pack Creation

Input: ps ; T ; $load$; $thrs$
Output: *Packs*

```

1  $P \leftarrow \emptyset$ ,  $Packs \leftarrow \emptyset$ ,  $ub \leftarrow ceil(\overline{load}, thrs)$ 
2 while  $load > ub$  do
3    $t \leftarrow a \in T \mid a \text{ is the lower bound of } T$ 
4    $T \leftarrow T \setminus \{t\}$ 
5    $P \leftarrow P \cup \{t\}$ 
6    $load \leftarrow load - t$ 
7   if  $load(P) > ps$  then
8      $Packs \leftarrow Packs \cup P$ 
9      $P \leftarrow \emptyset$ 
10  end
11 end
12  $Packs \leftarrow Packs \cup P$ 
```

B. Pack Sending

The *Pack Sending* process is presented in Algorithm 2. The algorithm will use the set of *Packs*, produced by *Pack Creation*, and the set of *Targets*, produced by an information propagation step (*Gossip* [18]), in order to schedule packs on remote PEs. This will produce a set with expected *Pack/Target* pairs, which should be confirmed by the remote target.

Basically, while the local PE still has available *Packs* to send (line 2), it will choose a random *Target* for it (line 4) and invoke a remote *Send* procedure on its *target* (line 5). The selected *pack* will be removed from the *Packs* set (line 6) and paired up with its *target* on the R set (line 7), waiting for confirmation. This process is repeated until all elements in *Packs* have attempted a *Send*.

C. The PackDrop Algorithm

The *PackDrop* strategy is presented in Algorithm 3. It will run individually on each PE, in a distributed fashion. Using a current local mapping of tasks to PEs (M), local load (l) and

Algorithm 2: Pack Sending

Input: *Packs*, *Targets***Output:** *R*

```

1  $R \leftarrow \emptyset$ 
2 while  $Packs \neq \emptyset$  do
3    $pack \leftarrow p \mid p \in Packs$ 
4    $target \leftarrow rand(Targets)$ 
5    $Send(pack) \rightarrow target$ 
6    $Packs \leftarrow Packs \setminus \{pack\}$ 
7    $R \leftarrow R \cup \{(pack, target)\}$ 
8 end

```

knowing all PEs in the system (P), to produce a new mapping (M'). The mapping of tasks is defined by Equation 3 as a set of pairs (task, PE), describing the location of tasks. A local map of tasks contains only tasks that are assigned to the current PE.

$$M : T \rightarrow P \quad (3)$$

In this implementation we used two constants: 1.05, in order to limit the imbalance at 5% (on line 5), and 2, in order to regulate the size of packs (on line 6).

The first part of the algorithm (lines 1 – 6) is the information sharing and setup process. This process is done through 2 global reductions of average PE load (line 2) and global number of tasks (line 3).

Then (line 7) PEs are divided between two different workflows. At this time, *overloaded* PEs will start the Pack Creation process (line 8), further explained in Algorithm 1. Meanwhile, *underloaded* PEs will start a *Gossip Protocol* [18] in order to inform other elements they are willing to receive work (line 11). *Gossip* is a well known epidemic algorithm used to spread information on a system, providing fast convergence and almost-global awareness of what was shared.

Then, each PE must synchronize to start the remap (line 13). At this point, the remapping process will begin. PEs will send their packs using Algorithm 2, *Pack Send*, asynchronously (line 14). After a pack is sent, a PE will accept or reject it based on their current load, this is done via *three-way handshake*, so both parts confirm the migration.

If one or more packs were not successfully exchanged, an *overloaded* PE must attempt a new *Pack Send*, in order to achieve load balance. Once the PEs know their new mappings, tasks are migrated and the strategy is finished (line 15).

PackDrop intends to remap tasks to PEs in a distributed, workload-aware fashion. This approach is the basis for new bin packing distributed strategies that may take other factors into account.

IV. ANALYSIS OF THE ALGORITHM

This section presents an analysis of the Parallel Algorithm 3 (*PackDrop*). The complexity of the information propagation (*Gossip*) has been evaluated as $O(\log_f n)$ [5], where f is the fanout for the algorithm and n is the number of PEs

Algorithm 3: PackDrop

Input: M , l , P **Output:** M'

```

1  $M' \leftarrow \emptyset$ 
2  $al \leftarrow (AveragePeLoadReduction(l) \Rightarrow P)$ 
3  $tc \leftarrow (TotalTaskCountReduction(|M|) \Rightarrow P)$ 
4 //Average task size //5% precision on balance
   $ats \leftarrow \frac{al}{tc}$        $thrs \leftarrow 0.05$ 
5  $ub \leftarrow ceil(al, thrs)$  //Upper migration threshold
6  $ps \leftarrow ats \times (2 - \frac{|P|}{tc})$  //Pack load
7 if  $l > ub$  then
8    $packs \leftarrow PackCreation(ps, T(M), l, thrs)$ 
9 else
10   $packs \leftarrow \emptyset$ 
11   $T \leftarrow (Gossip \rightarrow P)$  //Targets for migration
12 end
13  $---SynchronizationBarrier---$ 
14 //Requests are processed as they are received back
   $R \leftarrow PackSend(packs, T)$ 
15  $TaskMap(R, M, MyId)$ 

```

in the system. Here we use $f = 2$, in order to avoid network congestion.

For the sake of simplicity, in the remainder of this analysis, the number of tasks in the system will be referred to as m , and the costs for computation and communication will be represented as p_c and c_c , respectively. We also assume $c_c > p_c$ for all concurrent scenarios, since communication costs are several orders of magnitude higher than computational costs. $T(f)$ is referred here as the total cost for a given function f . Unmentioned lines are assumed to have non-varying cost, and thus will not interfere in the asymptotic analysis.

Lines 2 and 3 are global reductions, which have a well known cost of $O(\log n)$. Lines 8 and 11 are concurrent, so their cost will be the max among both:

$$\max(T(PackCreation), T(Gossip)) \quad (4)$$

We also know that the worst case for *PackCreation* (Algorithm 1) is rather unrealistic, since it would assume that a single PE contains m tasks and a single task may have a load greater than the average system load, being $O(m - 1)$, assuming 1 would not be migrated, asymptotically, $O(m)$.

This takes lines 8 and 11 cost to:

$$\max(O(p_c m), O(c_c \log_f n)) \quad (5)$$

and since c_c is several orders of magnitude bigger than p_c , we could assume $T(PackCreation) \in T(Gossip)$, which makes the complexity of these lines to $O(\log_f n)$.

Finally, line 14 will have a complexity equal to the largest number of packs migrated by an overloaded PE. Let ps be the mean number of tasks inside of a pack, and m_l the maximum number of tasks in a given overloaded PE. At this step, a solution without Task Packing would have a cost of $c_c \times m_l$, while our approach will divide this complexity by ps . Great

gains come with optimizations of this step, since it is the most expensive in Algorithm 3. Our final asymptotic complexity will be:

$$T(\text{PackDrop}) = O(m_l/ps) + O(\log n) \quad (6)$$

This shows that determining a good ps value is crucial to achieve the best performance with this algorithm. Higher values of ps will lower communication complexity, but may lead to an imprecise scheduling. In our Implementation, we chose a moderate value of ps , of around 2 average tasks, varying to smaller values according to system load. This guarantees a precise scheduling, but still gives margin to have several small tasks migrating at once, saving communication costs.

V. IMPLEMENTATION

PackDrop was implemented as a load balancing strategy in Charm++¹. Charm++ is a parallel programming model that provides a *load balancing framework* based on migration of its parallel, message-driven objects, the *chares* [19]. *Chares* are mapped as *tasks* onto PEs and the Charm++ runtime system (RTS) provides the load information needed for the *PackDrop* strategy.

The Charm++ RTS allows for the desired asynchronous behavior of *PackDrop*, creates a need for synchronization mechanisms, in order to guarantee workability. This is handled the same way that was in *Grapevine*, giving processes such as resending packs and the *Gossip Protocol* a limited number of rounds, or a *time to live* [5]. The RTS manages application synchronization before load balancing and its restart.

Charm++ provides application-independent load balancing, which means that any application (that implements a PUP framework [20]), may use load balancers implemented for this RTS. With this in mind, a suite of previously implemented benchmarks and applications to test our novel strategy. This also makes the comparison to existing strategies easier, since they are already implemented in this RTS.

A. Benchmarks

We experimented our strategy with 2 benchmarks that are publicly available for Charm++. The first is a synthetic benchmark called **LB Test**. It simulates work with a variety of communication topologies, such as ring, meshes and randomized patterns. *LB Test* is known to have a low migration cost, with light *tasks*, and most of its load bound to computation, instead of communication.

The second is a molecular dynamics (MD) mini-app called **LeanMD**². This mini-app simulates the behavior of atoms and it mimics the force computation done in the state-of-the-art MD application NAMD, winner of the Golden Bell Award [5]. LeanMD uses geometric decomposition in a three-dimensional (3D) simulation space. However, since the number of simulated atoms in each region affects the number of exchanged

messages, it has an irregular and dynamic communication pattern, even though it respects the geometric distribution.

B. Other schedulers

PackDrop was compared strategies available on the Charm++ benchmark suite. More specifically, strategies that may be selected by Charm++’s workload-aware *Meta-balancer* [12]. Their behavior is briefly presented ahead.

- **Refine** is a refinement-based strategy that tries to minimize the number of migrated *tasks*, exchanging load among PEs. This strategy is specially efficient if the imbalance isn’t too high.
- **Greedy** creates two heaps, one for *tasks* (max-min) and one for PEs (min-max). Then, it assigns tasks to PEs, putting the most work-heavy tasks on the least loaded PEs. This strategy provides a good load balance, but may incur in high migration overhead.
- **Distributed**, also known as *Grapevine*, is a distributed strategy based on epidemic communication and probabilistic transfer of work. This strategy has good scalability, but does not performs as well as centralized ones in smaller scenarios.

VI. PERFORMANCE EVALUATION

Two platforms were for performance evaluation of our novel *PackDrop* scheduler: i) A tightly coupled *Supercomputer* with 24 (in 2 separate NUMA nodes) PEs per node, using an Infiniband interconnection supported by Intel’s Parallel Studio XE implementation of MPI (v2017.4). ii) A smaller *Cluster* with 4 PEs per node, using a Gigabit Ethernet interconnection. Details of both platforms are available on Table I.

Node Info.	Supercomputer	Cluster
CPUs	2 × 12	4
Intel Xeon	E5-2695v2	X3440
CPU Freq.	2.4GHz	2.53GHz
RAM	64GB	16GB
Network	Infiniband FDR	Gigabit Ethernet
OS	RedHat Linux 6.4	Ubuntu 14.04
GCC	5.3.1	5.4.0
Charm++	6.8.1	6.8.1
MPI	3.1.0	-
GCC Flags	-std=c++11 -O3	-std=c++11 -O3

TABLE I
PLATFORM INFORMATION OF EACH NODE FROM SUPERCOMPUTER AND CLUSTER EVALUATIONS.

Ahead we’ll present the metrics used to compare our new global rescheduling strategy with *Greedy*, *Refine* and *Distributed*. Then, we’ll discuss results obtained in both platforms described in Table I and the scalability of our proposed solution. All raw data of our results, as well as parsing scripts for analysis are publicly available³.

Metrics: Application time is one of the most relevant metrics to evaluate load balancers in Charm++. Since migrations may induce high overhead and impact communication costs, a bad algorithm may finish fast, but increase imbalance, and thus, application time.

¹Available at: <https://github.com/OMMITED-FOR-BLIND-REVIEW>

²Available at: <http://charmplusplus.org/miniApps>

³Available at: <https://github.com/OMMITED-FOR-BLIND-REVIEW>.

Iteration times are fractions of the total application time, and as such can describe how well a scheduling strategy balances the system. The increasing of iteration times after scheduling is an indicator that the algorithm is not supporting the application well.

Load balancer decision time, although not the most relevant for the application itself, the decision time is an indicator of its scalability. Some centralized schedulers, such as *Greedy*, work very well on local machines, with a reasonable data input. However, when executing on distributed memory environments, the scalability of these strategies is limited.

A. Evaluation on Supercomputer

Evaluation with Synthetic Load: LB Test experiments had a total of 35990 tasks, executed over 150 iterations, performing load balance every 40 iterations. Task loads vary from 20ms to 6000ms. The chosen communication topology was a two-dimensional (2D) mesh.

Evaluation with Molecular Dynamics: LeanMD experiments generated a $10 \times 15 \times 10$ space, with a total of 171K tasks. Each execution ran 100 iterations, with a first rescheduling step at the 9th iteration. Load balancing was performed every 30 iterations and each configuration of LeanMD was executed 10 times, making a total of 1000 steps per configuration.

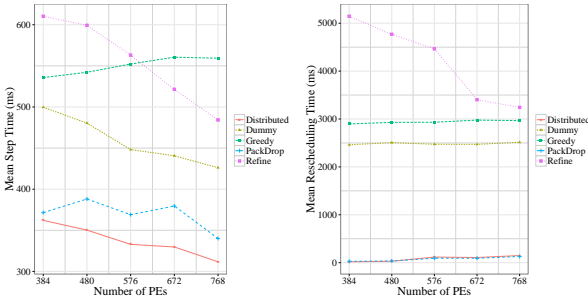


Fig. 1. LeanMD supercomputer execution results.

Check sched time results, almost sure PackDrop and Distributed should be around 500.

B. Evaluation on Cluster

All experiments ran on cluster were compiled with Charm++ using the `--with-production` option, combined with the specifications detailed on Table I. 32 equal compute nodes were used, with a total of 128 PEs. In addition to previously mentioned schedulers, *Dummy* was added as the representative of a situation with no remap of tasks.

Evaluation with Synthetic Load: LB Test experiments had a total of 18990 tasks, executed over 150 iterations, performing load balance every 40 iterations. Task loads vary from 30ms to 9000ms, which provides reasonable imbalance of load, causing global rescheduling to be useful in this case. Ring, 2D mesh and 3D mesh communication topologies were used to provide different levels of migration impact and communication cost.

Scheduler	Time (Ring)	Time (2D)	Time (3D)
Distributed	47.49298s	48.64839s	49.05481s
Greedy	46.54101s	49.56052s	51.06850s
Dummy	52.43016s	53.17254s	53.94068s
PackDrop	46.81598s	47.37120s	47.97426s
Refine	45.49095s	46.29277s	47.21924s

TABLE II

LB TEST MEAN APPLICATION TIME ON THE CLUSTER EXECUTION.

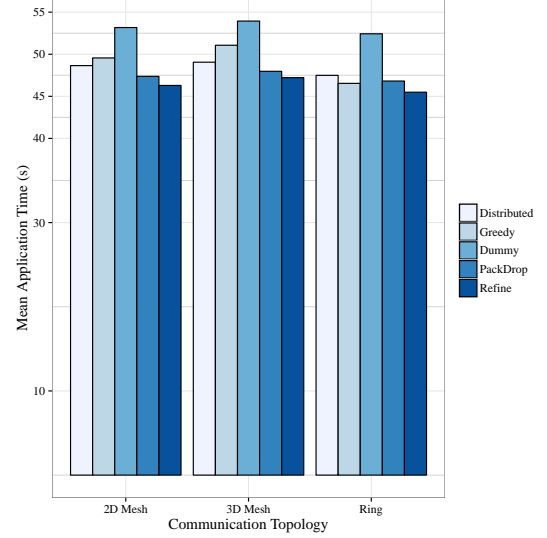


Fig. 2. LB Test cluster execution results.

Each configuration of the benchmark was executed 15 times, with results depicted on Figure 2 and Table II. Results for *Greedy* show how different communication topologies affect the scheduling performance. Since *Greedy* migrates many tasks, the more they communicate, the more migrations impact the application time.

The increased in communication cost can be verified among all scheduling strategies, but in none as much as in *Greedy*. Our novel approach, *PackDrop* has outperformed the closest approach, *Distributed* in the *LB Test* case of this scale. However, since the platform is not large enough to present the potential gains of decentralized strategies, *Refine*, with a reduced migration count approach, still outperforms any other scheduler in this benchmark.

Evaluation with Molecular Dynamics: LeanMD experiments generated a $9 \times 9 \times 9$ space, with a total of 27702 tasks. Each execution ran 500 iterations, with a first rescheduling step at the 10th iteration. Load balancing periods of every 30 and every 60 iterations were used, providing different impacts of rescheduling on the application.

Each configuration of LeanMD was executed 10 times, making a total of 5000 steps per configuration.

Correct X label on LMD images in cluster subsection

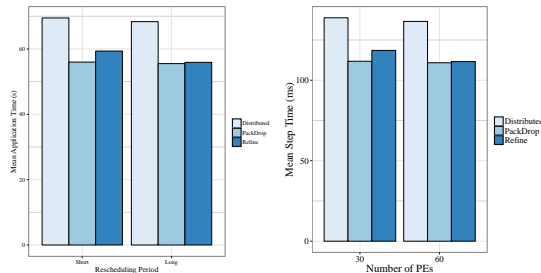


Fig. 3. LeanMD cluster execution results.

C. Scalability

VII. CONCLUSION

A. Future Work

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@Laércio, adicionar agradecimentos no contexto do projeto de pesquisa ao CNPq?

Adicionar agradecimentos para ambas as bolsas de mestrado

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