SPARTACUS-Surface User Guide

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1 Introduction

SPARTACUS-Surface is a Fortran-2003 software library for computing the 3D interaction of solar (or *shortwave*) and thermal-infrared (or *longwave*) radiation with complex surface canopies, especially forests and urban areas. It uses a multi-layer description of the canopy but with a statistical description of the horizontal distribution of trees and buildings. This greatly reduces the variables needed to describe the canopy, and makes the scheme fast enough to use in weather and climate models.

The detailed theoretical basis of the library is provided in two papers: Hogan et al. (2018) developed the short-wave forest solver, and Hogan (2019b) extended this to include buildings and longwave radiative transfer (these works developed two prototype codes in Matlab: *SPARTACUS-Vegetation* and *SPARTACUS-Urban*, both available from the SPARTACUS web site). The resulting algorithm combines three key ideas from earlier papers in the atmospheric radiative transfer literature:

- To represent horizontal variations in vegetation leaf density (or equivalently, extinction coefficient), each layer in a vegetation canopy is divided horizontally into three regions: clear-air (unvegetated) and two vegetated regions of equal fractional cover but different extinction coefficient. This approach was proposed by Shonk and Hogan (2008), who showed (in the context of cloudy radiative transfer) that the radiative effect of the full distribution of extinction coefficient could be approximated well given an appropriate choice for the extinction coefficients of the two regions.
- Three-dimensional radiative effects are treated rigorously by using the *Speedy Algorithm for Radiative Transfer through Cloud Sides* (SPARTACUS) of Hogan et al. (2016), but replacing clouds with trees and buildings. Since it is reasonable to treat trees and buildings as randomly distributed in the horizontal plane (see also Hogan, 2019a), the rate of exchange of radiation between the clear and vegetated parts of a layer may be assumed to be proportional to the length of the interface between them, and likewise for the rate of interception of radiation by building walls.
- The *Discrete Ordinate Method* is used to approximate the zenithal distribution of diffuse radiation, with the coupled ordinary differential equations solved by Eigen decomposition similarly to Stamnes et al. (1988). This is more robust than the matrix-exponential method used by Hogan et al. (2016), and more accurate since *SPARTACUS-Surface* allows the diffuse radiation field to be described by more than just two streams.

Section 2 describes how to compile and use the offline version of *SPARTACUS-Surface*, which is essentially a Unix program that reads a configuration file and a netCDF file containing a description of a number of surfaces, and outputs a netCDF file containing the computed radiation properties. Sections 3–7 describe how to configure and run the offline software, and the contents of the input and output data files. Section 8 outlines how to incorporate *SPARTACUS-Surface* into a larger Fortran program, such as an atmospheric model.

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2 Compiling the package

The offline version of *SPARTACUS-Surface* is designed to be used on a Unix-like platform. You will need a Fortran compiler that supports the 2003 standard, such as gfortran. As a prerequisite, you will need to install the netCDF library, including the Fortran interface (packages to install on a Linux system are typically called libnetcdff-dev or libnetcdff-devel). If you have a recent netCDF version then the command

```
nc-config --fc
```

should return the Fortran compiler for which the netCDF library was compiled. To run some of the tests, you will also need to install the NCO utilities for manipulating netCDF Files.

First unpack the package and enter the subdirectory as follows:

```
tar xvfz spartacus_surface-0.8.tar.gz cd spartacus_surface-0.8
```

On a non-GNU platform you may need to untar and unzip the package using the tar and gunzip commands separately. The README file contains concise instructions on compilation and testing, while the COPYING file provides the license conditions. The subdirectories are as follows:

radsurf The SPARTACUS-Surface souce code for canopy radiative transfer

radtool Mathematical support routines for radiative transfer

utilities Source code for useful utilities, such as reading netCDF files

driver The source code for the offline driver program spartacus_surface

mod Where Fortran module files are written

lib Where the static libraries are written

bin Where the executable spartacus_surface is written

test Test cases including Matlab code to plot the outputs

doc The source for this document

Compilation on different platforms using different compilers is facilitated by the various Makefile_include.<prof> files in the top-level directory: if you type

```
make
```

or

```
make PROFILE=gfortran
```

the code will be compiled using the gfortran compiler via the Makefile variables set in the Makefile_include.gfortran file. Using instead PROFILE=pgi will use the Makefile_include.pgi file to attempt to compile with the PGI compiler, while PROFILE=intel selects the Intel compiler. If everything goes to plan this should create the executable bin/spartacus_surface and various static libraries in the lib directory.

One common reason the code doesn't compile out of the box is that it can't find the netCDF library files. The SPARTACUS-Surface Makefile uses the nf-config script that comes with recent versions of the netCDF library to create the Makefile variables NETCDF_INCLUDE and NETCDF_LIB. If nf-config is not available on your system, or it fails to correctly locate the netCDF library files, then the cleanest way to fix this is to create a Makefile_include.local file (starting from one of the existing Makefile_include.* files) that defines NETCDF_INCLUDE and NETCDF_LIB explicity to contain arguments for the compile and link operations, respectively. Suppose you installed netCDF in /path/to/netcdf and you use the gfortran compiler then your file might contain:

```
include Makefile_include.gfortran
NETCDF = /path/to/netcdf
NETCDF_INCLUDE = -I$(NETCDF)/include
NETCDF_LIB = -L$(NETCDF)/lib -lnetcdff -lnetcdf -Wl,-rpath,$(NETCDF)/lib
```

You should then be able to build the code with

```
make PROFILE=local
```

To compile with debugging options turned on (no optimization, bounds checking and initializing real numbers with not-a-number), type

```
make PROFILE=gfortran DEBUG=1
```

Finer tuning may be achieved by overriding the optimization and debugging flags used in Makefile explicitly, for example

```
make PROFILE=gfortran OPTFLAGS="-01" DEBUGFLAGS="-g1 -pg"
```

Remember that if you change the compile settings you will probably want to recompile everything, in which case you first need to remove all compiled files with

```
make clean
```

3 Running the offline scheme

To test the code, type

```
make test
```

which runs make in each of the subdirectories of the test directory. The README files in these directories provide more information on what they are doing, and some Matlab scripts are provided to visualize the outputs.

You will see in the output of the tests the command line in each invocation of *SPARTACUS-Surface*, which is of the form

```
spartacus_surface config.nam input.nc output.nc
```

where spartacus_surface needs to be the full path to the SPARTACUS-Surface executable, config.nam is a Fortran namelist file configuring the code, input.nc contains the input atmospheric profiles and output.nc contains the output irradiance (flux) profiles. The namelist file contains a radsurf namelist that configures the SPARTACUS-Surface scheme itself; the parameters available are described in section 4. The file also contains a radsurf_config namelist that configures aspects of the offline package, described in section 5. Only the radsurf namelist is used when SPARTACUS-Surface is incorporated into an atmospheric model.

The input netCDF file contains numerous floating-point variables listed in Table 1. The dimensions are shown in the order that they are listed by the ncdump utility, with the first dimension varying slowest in the file (opposite to the Fortran convention). Most variables are stored as a function of column and layer (dimensions named col and layer in Table 1, although the actual dimension names are ignored by *SPARTACUS-Surface*). The layer_int dimension corresponds to interfaces between layers, plus the top-of-canopy and surface, and so must be one more than layer. Note that both layer and layer_int should increase upwards from the surface.

The optional sw and lw dimensions allow for shortwave and longwave optical properties of leaves and facets to be specified in user-defined spectral intervals. If these dimensions are omitted for these variables then constant optical properties will be assumed across the longwave and shortwave spectra.

Some variables can be omitted in which case default values will be used or these fields will be constructed according to radsurf_config namelist parameters (section 5).

Table 1: Main variables contained in the input netCDF file to *SPARTACUS-Surface*. All are floating-point numbers except for surface_type, which contains integers.

Variable	Dimensions	Description
cos_solar_zenith_angle	col	Cosine of solar zenith angle
surface_type	col	Surface type: (0) flat, (1) forest, (2) urban, (3) vegetated urban,
		(4) simple urban, and (5) infinite street
height	col, layer_in	t Height of layer interfaces (m)
veg_fraction	col, layer	Vegetation fraction
veg_scale	col, layer	Vegetation horizontal scale (m)
veg_extinction	col, layer	Wavelength-independent vegetation extinction coefficient (m^{-1})
veg_fsd	col, layer	Fractional standard deviation of vegetation extinction
veg_contact_fraction	col, layer	Fraction of building walls in contact with vegetation; note that
		in version 0.7.2 and earlier this was instead defined as the
		fraction of vegetation edge in contact with buildings
building_fraction	col, layer	Building fraction
building_scale	col, layer	Building horizontal scale (m)
clear_air_temperature	col, layer	Temperature of clear (unvegetated) part of layer (K)
veg_temperature	col, layer	Temperature of leaves (K)
veg_air_temperature	col, layer	Temperature of air in vegetated part of layer (K)
air_temperature	col, layer	Alternative way to specify clear_air_temperature and
		${\tt veg_air_temperature}$ if the same (K)
ground_temperature	col	Ground temperature (K)
roof_temperature	col, layer	Temperature of the roofs at the top of the layer (K)
wall_temperature	col, layer	Wall temperature (K)
ground_sw_albedo	col, sw	Shortwave albedo of ground
ground_sw_albedo_direct	col, sw	Shortwave albedo of ground to direct beam (if different)
ground_lw_emissivity	col, lw	Longwave emissivity of ground
veg_sw_ssa	col, layer, s	
veg_lw_ssa	col, layer, l	
roof_sw_albedo	col, layer, s	
roof_sw_albedo_direct	col, layer, s	
roof_lw_emissivity	col, layer, l	· ·
wall_sw_albedo	col, layer, s	
wall_sw_specular_fraction	col, layer, s	•
wall_lw_emissivity	col, layer, l	·
sky_temperature	col	Equivalent emitting temperature of sky (K)
top_flux_dn_sw	col, sw	Top-of-canopy downwelling shortwave flux (W m ⁻²)
top_flux_dn_direct_sw	col, sw	Top-of-canopy downwelling direct shortwave flux (W m ⁻²)

Input fields should be provided in order of increasing height, and the output data use the same convention. The surface_type variable selects how the column is to be treated, as depicted in Fig. 1. Types 1–3 use the SPARTACUS method as described by Hogan (2019b) but differ according to whether trees, buildings or both are represented. Types 4 and 5 use a simplified description of unvegetated urban areas in which all buildings are assumed to have the same height, and the Harman et al. (2004) method is used to represent multiple scattering within the urban canopy by solving a 2×2 matrix problem. Type 4 makes the same assumption about the horizontal distribution of buildings as SPARTACUS, which is that the wall-to-wall separation distances follow an exponential distribution (Hogan, 2019a). Type 5 makes the 'infinite street' assumption: streets are assumed to be of equal width and infinite in length. While the latter assumption is commonly used in urban exchange models, it was found by Hogan (2019a) to be a poorer fit to the building distributions in real cities.

The output netCDF file contains the typical set of broadband fluxes and absorption rates listed in Table 2. If you need them spectrally resolved (using the input spectral discretization) then set the radsurf_config namelist variable do_spectral to true and the same variables will be output but with the prefix spectral_.

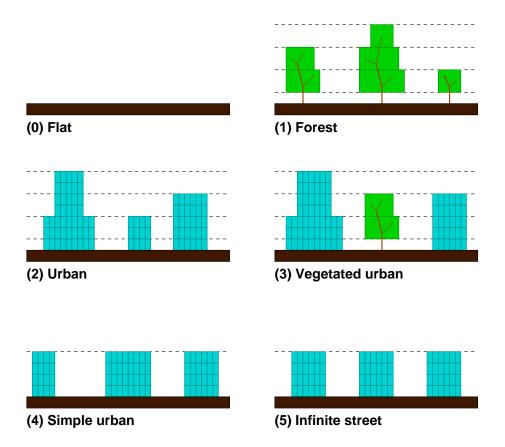


Figure 1: Schematic of the six surface types represented by the surface_type variable provided in the SPARTACUS-Surface input file (see Table 1).

Table 2: Variables contained in the output netCDF file from *SPARTACUS-Surface*. All fluxes (or irradiances) and absorption rates have units of W m⁻², but note that this is power per unit area of the *entire domain*, not per unit area of a specific facet type. 'Net' fluxes are defined as the flux into a facet type (or downward) minus the flux out of a facet type (or upward).

Variable	Dimensions	Description
height	col, layer_int	Height of layer interfaces above ground (m)
ground_flux_dn_sw	col	Downwelling shortwave flux into the ground
ground_flux_dn_direct_sw	col	Direct downwelling shortwave flux into the ground
ground_flux_net_sw	col	Net shortwave flux into the ground
ground_flux_dn_direct_sw	col	Direct downwelling shortwave flux into the ground
ground_flux_vertical_diffuse_sw	col	Diffuse shortwave flux into a vertical surface at ground
		level
top_flux_dn_sw	col	Top-of-canopy downwelling shortwave flux
top_flux_net_sw	col	Top-of-canopy net shortwave flux
top_flux_dn_direct_sw	col	Top-of-canopy direct downwelling shortwave flux
roof_flux_in_sw	col, layer	Shortwave flux into roofs
roof_flux_in_direct_sw	col, layer	Direct shortwave flux into roofs
roof_flux_net_sw	col, layer	Net shortwave flux into roofs
wall_flux_in_sw	col, layer	Shortwave flux into walls
wall_flux_in_direct_sw	col, layer	Direct shortwave flux into walls
wall_flux_net_sw	col, layer	Net shortwave flux into walls
clear_air_absorption_sw	col, layer	Shortwave absorption rate in clear-air part of layer
veg_absorption_sw	col, layer	Shortwave absorption rate by leaves
veg_absorption_direct_sw	col, layer	Direct shortwave absorption rate by leaves

veg_air_absorption_sw	col, layer	Shortwave absorption rate by air in vegetated part of layer
ground_flux_dn_lw	col	Downwelling longwave flux into the ground
ground_flux_net_lw	col	Net longwave flux into the ground
ground_flux_vertical_lw	col	Longwave flux into a vertical surface at ground level
top_flux_dn_lw	col	Top-of-canopy donwelling longwave flux
top_flux_net_lw	col	Top-of-canopy net longwave flux
roof_flux_in_lw	col, layer	Longwave flux into roofs
roof_flux_net_lw	col, layer	Net longwave flux into roofs
wall_flux_in_lw	col, layer	Longwave flux into walls
wall_flux_net_lw	col, layer	Net flux into walls
clear_air_absorption_lw	col, layer	Net longwave absorption rate in clear-air part of layer
veg_absorption_lw	col, layer	Net longwave absorption rate by leaves
veg_air_absorption_lw	col, layer	Net longwave absorption rate by air in vegetated part of layer
ground_sunlit_fraction	col	Fraction of the ground area in direct sunlight
roof_sunlit_fraction	col, layer	Fraction of the roof area in direct sunlight
wall_sunlit_fraction	col, layer	Fraction of the wall area in direct sunlight
veg_sunlit_fraction	col, layer	Fraction of the one-sided leaf area that is in direct
		sunlight

The ground_flux_vertical_* variables are diffuse fluxes into a vertical plane at ground level, and are useful for computing thermal comfort indices and mean radiant temperature. If you want them at other heights in the urban canopy then they may be estimated from the wall incoming fluxes wall_flux_in_*. For example, the diffuse flux into a vertical plane averaged over layer i in the urban canopy may be computed from

$$V_i = \frac{2}{\pi} \frac{W_i}{L_i \Delta z_i},\tag{1}$$

where W_i is the reported diffuse flux into walls in layer i (i.e. wall_flux_in_lw in the longwave and wall_flux_in_sw - wall_flux_in_direct_sw in the shortwave), L_i is the normalized wall perimeter length and Δz_i is the thickness of layer i. The factor of $2/\pi$ converts from fluxes into a wall that may be oriented in any azimuthal direction to fluxes into a vertical plane oriented in one direction.

Some urban models predict temperatures separately for sunlit and shaded roofs, walls and streets. Similarly, to compute photosynthesis rates more accurately, some vegetation models need to know the fraction of leaf area that is sunlit. To support such applications, Table 2 lists four *_sunlit_fraction variables quantifying the fraction of these surfaces that are in direct sunlight. Note that because walls are assumed to be vertical surfaces, the maximum wall fraction that can be sunlit is 1/2. In the case of vegetation, the sunlit fraction refers to the fraction of one-sided leaf area, so can approach 1 in thin layers at the top of a vegetation canopy. These variables are accompanied by direct fluxes ground_dn_direct_sw, roof_in_direct_sw, wall_in_direct_sw and veg_absorption_direct_sw. Therefore sufficient information is provided to treat sunlit and shaded surfaces separately, assuming that diffuse radiation evenly illuminates all surfaces in a layer.

If you set namelist parameter do_save_flux_profile to true, then the flux-profile variables listed in Table 3 will also be output, which are averaged over both the clear and vegetated regions. Note that these variables are output at the top and base of each layer. In forests, the fluxes at the top of one layer will be equal to the fluxes at the base of the layer above, whereas in urban areas, since the fluxes are per unit horizontal area of the entire domain, these fluxes will not match when the building fraction decreases with height.

Table 3: Additional variables contained in the output netCDF file from *SPARTACUS-Surface* if the namelist parameter do_save_flux_profile is set to true. All fluxes have units of W m⁻², but note that this is power per unit area of the *entire domain*, not per unit area of the clear/vegetated part of the layer.

flux_dn_layer_top_sw	col, layer	Downwelling shortwave flux in the clear/vegetated regions at the top of each layer
flux_dn_direct_layer_top_sw	col, layer	Direct downwelling shortwave flux in the clear/vegetated regions at the top of each layer
flux_up_layer_top_sw	col, layer	Upwelling shortwave flux in the clear/vegetated regions at the top of each layer
flux_dn_layer_base_sw	col, layer	Downwelling shortwave flux in the clear/vegetated regions at the base of each layer
flux_dn_direct_layer_base_sw	col, layer	Direct downwelling shortwave flux in the clear/vegetated regions at the base of each layer
flux_up_layer_base_sw	col, layer	Upwelling shortwave flux in the clear/vegetated regions at the base of each layer
flux_dn_layer_top_lw	col, layer	Downwelling longwave flux in the clear/vegetated regions at the top of each layer
flux_up_layer_top_lw	col, layer	Upwelling longwave flux in the clear/vegetated regions at the top of each layer
flux_dn_layer_base_lw	col, layer	Downwelling longwave flux in the clear/vegetated regions at the base of each layer
flux_up_layer_base_lw	col, layer	Upwelling longwave flux in the clear/vegetated regions at the base of each layer

4 Configuring the SPARTACUS-Surface algorithm

The detailed settings of *SPARTACUS-Surface* are configured using the radsurf namelist in the namelist file provided as the first command-line argument to the spartacus_surface executable. The available namelist parameters are listed in Table 4.

Table 4: Options for the radsurf namelist that configures SPARTACUS-Surface algorithm. The type of each parameter can be inferred from its name: logicals begin with do_ or use_, integers start with i_ or n_, strings end with _name, and all other parameters are real numbers.

Parameter	Default , other values	Description
General		
do_sw	true	Compute shortwave fluxes?
do_lw	true	Compute longwave fluxes?
do_vegetation	true	Will vegetation be represented?
do_urban	true	Will urban areas be represented?
use_sw_direct_albedo	false	Specify ground and roof albedos separately for direct solar radiation?
min_vegetation_fraction	10 ⁻⁶	Minimum area fraction below which a region is removed completely
do_save_flux_profile	false	Save the flux profile variables listed in Table 3
Options specific to forest tiles		
n_vegetation_region_forest	1 , 2	Number of regions used to describe vegetation (2 needed for heterogeneity)
n_stream_sw_forest	4	Streams per hemisphere to describe diffuse shortwave radiation
n_stream_sw_forest	4	Streams per hemisphere to describe longwave radiation

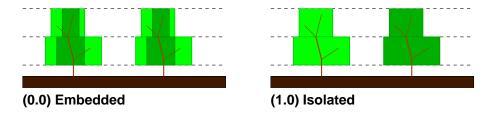


Figure 2: Schematic illustrating how the vegetation_isolation_factor_* parameters in Table 4 describe the contact between the clear-air region and the two vegetated regions in each layer.

use_symmetric_vegetation_scale_forest	true	Compute vegetation perimeter length using Eq. 20 of Hogan et al. (2018)? Otherwise Eq. 19
<pre>vegetation_isolation_factor_forest</pre>	0.0,0.0-1.0	In forests dense vegetation region is (0.0) embedded within sparse region or (1.0) in physically isolated regions, or in between
vegetation_isolation_factor_urban	0.0,0.0-1.0	In urban areas dense vegetation region is (0.0) embedded within sparse region or (1.0) in physically isolated regions, or in between
Options specific to urban tiles		
min_building_fraction	10 ⁻⁶	Minimum building area fraction below which a building is ignored
n_vegetation_region_urban	1 , 2	Number of regions used to describe vegetation (2 needed for heterogeneity)
n_stream_sw_urban	4	Streams per hemisphere to describe diffuse shortwave radiation
n_stream_sw_urban	4	Streams per hemisphere to describe longwave radiation
use_symmetric_vegetation_scale_urban	true	Compute vegetation perimeter length using Eq. 20 of Hogan et al. (2018)? Otherwise Eq. 19
vegetation_isolation_factor_urban	0.0,0.0-1.0	Dense vegetation region is (0.0) embedded within sparse region or (1.0) in physically isolated regions

The number of streams can be any positive integer, but note that this is the number of quadrature points that the radiation field is divided into *per hemisphere*, so a value of 4 corresponds to an '8-stream scheme' in the convention that all possible directions are considered. Larger values give more accuracy at greater computational cost, but as shown by Hogan (2019b), there is little change in the results above a value of 4.

The other parameters in Table 4 allow the treatment of vegetation to be fine tuned. If the number of vegetation regions is 1 then the trees are represented as in Fig. 1, with a single vegetation extinction coefficient per layer. In order to represent horizontal heterogeneity within tree crowns, a value of 2 should be selected, resulting in the representation in Fig. 2. The vegetation_isolation_factor_* parameters describe the contact between the clear region and the two vegetated regions in each layer, with the extremes being 0.0 in which the denser vegetation region is completely embedded in the sparser region (the assumption used by Hogan et al., 2018), and 1.0 in which the dense and sparse regions form unconnected tree crowns.

5 Configuring the offline package

In addition to the namelist parameters described in section 4 an additional set of parameters are available in the radsurf_config namelist that are specific to the offline version of SPARTACUS-Surface and are listed in Table

5. In general if these parameters are present in the namelist then they will override the corresponding variable provided in the input file.

Table 5: Options for the radsurf_config namelist that configures additional aspects of the offline radiation scheme. All entries must be scalars. If an override parameter is present then usually it need not be included in the input file.

Parameter	Description
Execution control	
nrepeat	Number of times to repeat, for benchmarking
istartcol	Start at specified input column (1 based)
iendcol	End at specified input column (1 based)
iverbose	Verbosity in offline setup (default 2)
do_parallel	Use OpenMP parallelism? (default true)
nblocksize	Number of columns per block when using OpenMP
do_conservation_check	Check final energy balance for each column
Override input variables	
cos_solar_zenith_angle	Override cosine of solar zenith angle
isurfacetype	Override value of surface type (0–5)
ground_sw_albedo	Override shortwave albedo of ground
roof_sw_albedo	Override shortwave albedo of roofs
wall_sw_albedo	Override shortwave albedo of walls
ground_lw_emissivity	Override longwave emissivity of ground
roof_lw_emissivity	Override longwave emissivity of roofs
wall_lw_emissivity	Override longwave emissivity of walls
vegetation_fraction	Override vegetation fraction
vegetation_extinction	Override vegetation extinction coefficient (m ⁻¹)
vegetation_fsd	Override vegetation fractional standard deviation of extinction
vegetation_sw_ssa	Override vegetation shortwave single scattering albedo
vegetation_lw_ssa	Override vegetation longwave single scattering albedo
top_flux_dn_sw	Override top-of-canopy downwelling shortwave flux (W m ⁻²)
top_flux_dn_direct_sw	Override top-of-canopy downwelling direct shortwave flux (W m ⁻²)
top_flux_dn_lw	Override top-of-canopy downwelling longwave flux (W m ⁻²)

6 Interpretation of geometry input variables

6.1 Forests

SPARTACUS-Surface assumes that the rate of lateral exchange of radiation between the clear-air and vegetated regions is proportional to the normalized length of the perimeter separating the vegetation and clear regions, L_{av} , i.e. the perimeter length divided by the horizontal area of the domain. This variable has units of m^{-1} and in practice is a strong function of vegetation fraction, so it is more convenient for models to parameterize the horizontal size of typical tree crowns, as expressed by the vegetation_scale input variable in Table 1. The use_symmetric_vegetation_scale_* parameters determine how this scale is used to compute L_{av} in the 'forest' and 'vegetated urban' surface types (shown in Fig. 1). If a symmetric vegetation scale is selected then Eq. 20 of Hogan et al. (2018) is used:

$$L_{av} = \frac{4av}{S_v},\tag{2}$$

where a is the clear-air fraction, v is the vegetation fraction and S_v is the vegetation scale. In the case of a forest, there are no other regions so a = 1 - v and as the vegetation fraction approaches one, the normalized perimeter approaches zero, indicating that the tree crowns effectively merge. If use_symmetric_vegetation_scale_* is false then Eq. 19 of Hogan et al. (2018) is used:

$$L_{av} = \frac{4v}{D_v},\tag{3}$$

where this time vegetation_scale is interpreted as the effective crown diameter, D_{ν} . This has the property that $L_{a\nu}$ approaches a constant value as the vegetation fraction approaches one, which could be thought of as the property of *crown shyness* exhibited by some forest canopies.

If you have two vegetated regions (n_vegetation_region_* in Table 4 is 2) then the normalized perimeter length between vegetation and clear-air, L_{av} , will be partitioned between the two vegetated regions in proportion to the relevant vegetation_isolation_factor_* parameter f:

$$L_{a1} = L_{av}(1 - f/2);$$
 (4)

$$L_{a2} = L_{av} f/2, \tag{5}$$

where L_{a1} and L_{a2} are the normalized perimeter lengths between clear-air and each of the two vegetation regions. Figure 2 illustrates the limits of f=0 and f=1. This still leaves the length of the interface between the two vegetated regions, L_{12} , to be determined, which is used internally to compute the rate of lateral radiation exchange between these two regions. It is computed in *SPARTACUS-Surface* as follows. If the symmetric vegetation scale is selected then the horizontal scale of the vegetation inhomogeneities is assumed to be the same as the scale of the tree crowns themselves. Therefore, to compute the length of the interface between the two vegetated regions we use (2) but replace the vegetation fraction v with the fraction of just one of the two vegetation regions, v/2, such that

$$L_{12} = (1 - f) \frac{4(\nu/2)(1 - \nu/2)}{S_{\nu}} = (1 - f) \frac{\nu(2 - \nu)}{S_{\nu}}.$$
 (6)

If the non-symmetric vegetation scale, D_v , is to be used then the following formula is applied instead

$$L_{12} = (1 - f) \frac{4v}{2^{1/2} D_{v}}. (7)$$

The factor of $2^{1/2}$ on the denominator was used by Hogan et al. (2018) and is consistent with a tree model depicted in their Fig. 1 in which crowns are quasi-circular in horizontal cross-section and the optically thicker of the two region lies within a quasi-circular core surrounded by the optically thinner region.

If you are trying to simulate a 3D forest scene for which you know the exact location and sizes of the trees (e.g. from one of the RAMI intercomparisons) then you should analyze the scene to compute the vertical profile of L_{av} , then invert either (2) or (3) to obtain the profile of vegetation scale to use as input to the algorithm. The two formulas for L_{12} above do not allow for both L_{av} and L_{12} to be specified independently, even if you are analysing a 3D scene for which information on L_{12} might be known, but it should be noted that L_{av} has a much larger impact on radiative fluxes in the canopy than L_{12} .

6.2 Urban areas

The building_scale input variable in Table 1 is always interpreted as an effective building diameter, i.e. the code uses the equivalent of (3) to convert to the normalized building perimeter length in each layer, L_b , given the building fraction b:

$$L_b = \frac{4b}{D_b}. (8)$$

If there is no vegetation then all the building perimeter length is in contact with clear air, so $L_{ab} = L_b$. If vegetation is present then the building perimeter L_b is divided between clear-air and vegetation according to the veg_contact_fraction variable, c:

$$L_{ab} = (1 - c)L_b; (9)$$

$$L_{vh} = cL_h. (10)$$

In the offline version of *SPARTACUS-Surface*, if veg_contact_fraction is not provided in the input file then it is assumed that trees are randomly located in the space between buildings, and therefore that the probability of a building wall being in contact with vegetation is equal to the fraction of this space containing vegetation, i.e.:

$$c = v/(a+v). (11)$$

Note that the building, clear-air and vegetation fractions sum to one: b + a + v = 1. If SPARTACUS-Surface is embedded in a larger model then veg_contact_fraction must be provided explicitly, in which case it is recommended that (11) is used. Please note that in SPARTACUS-Surface version 0.7.2 and earlier, veg_contact_fraction was defined as the fraction of vegetation perimeter in contact with the walls, rather than the current definition which is the fraction of building perimeter in contact with vegetation.

The length of the interface between vegetation and clear-air is treated slightly differently for vegetated urban areas than forests, due to the fact that the building fraction b is removed from consideration. If a symmetric vegetation scale is selected then we apply (2) to the non-building part of the domain only (with fraction a + v):

$$\frac{L_{av}}{a+v} = \frac{4}{S_v} \frac{a}{a+v} \frac{v}{a+v},$$
 (12)

leading to

$$L_{av} = \frac{4}{S_v} \frac{av}{a+v}.$$
 (13)

If a non-symmetric vegetation scale is selected then (3) is applied as before. If there are two vegetation regions in an urban area then the normalized perimeter length between clear-air and each of the two vegetation regions uses (4) and (5), as before. If the symmetric vegetation scale is selected then we take a similar approach and (6) becomes

$$L_{12} = (1 - f) \frac{4(\nu/2)(1 - \nu/2 - b)}{(a + b)S_{\nu}},$$
(14)

while for a non-symmetric vegetation scale, (7) is applied as before.

7 Checking the configuration

When spartacus_surface is run, it outputs to the screen a summary of the configuration options, with the level of detail controlled by the radsurf_config namelist parameter iverbose. This can be used to check that SPARTACUS-Surface has been configured as intended. The following is an example from the default test in the test/simple directory, in the case of iverbose=2:

```
----- OFFLINE SPARTACUS-SURFACE RADIATION SCHEME ------
Copyright (C) 2019-2020 European Centre for Medium-Range Weather Forecasts
Contact: Robin Hogan (r.j.hogan@ecmwf.int)
Floating-point precision: double
General settings:
  Represent vegetation ON
                                          (do_vegetation=T)
  Represent urban areas ON
                                          (do_urban=T)
 Do shortwave (SW) calculations ON
                                          (do_sw=T)
 Do longwave (LW) calculations ON
                                          (do_sw=T)
 Number of SW spectral intervals = 1
                                          (nsw)
 Number of LW spectral intervals = 1
                                          (nlw)
 Minimum vegetation fraction = .100E-05 (min_vegetation_fraction)
Settings for forests:
 Number of vegetation regions = 2
                                          (n_vegetation_region_forest)
 Use symmetric vegetation scale ON
                                          (use_symmetric_vegetation_scale_forest=T)
                                          (vegetation_isolation_factor_forest)
 Vegetation isolation factor = 0.00
                                        (n_stream_sw_forest)
 SW diffuse streams per hemisphere = 2
 LW streams per hemisphere = 2
                                          (n_stream_lw_forest)
Settings for urban areas:
 Number of vegetation regions = 2
                                          (n_vegetation_region_urban)
 Use symmetric vegetation scale ON
                                          (use_symmetric_vegetation_scale_urban=T)
 Vegetation isolation factor = 0.00
                                          (vegetation_isolation_factor_urban)
 SW diffuse streams per hemisphere = 2
                                          (n_stream_sw_urban)
 LW streams per hemisphere = 2
                                          (n_stream_lw_urban)
Reading NetCDF file test_surfaces_in.nc
 Overriding cosine of the solar zenith angle with 0.500
 Overriding vegetation extinction with 0.250
 Setting temperature of clear-air and air in vegetation to air_temperature
  Setting vegetation temperature equal to air temperature
```

```
Assuming roof albedo to direct albedo is the same as to diffuse
 Assuming wall reflection is Lambertian (no specular component)
   1: Flat
   2: Forest,
                       2 layers, 2 diffuse streams per hemisphere, 3 regions
   3: Unvegetated urban, 2 layers, 2 diffuse streams per hemisphere, 1 region
   4: Vegetated urban, 2 layers, 2 diffuse streams per hemisphere, 3 regions
Direct shortwave budget
      Ground Air
                        Wall
                                Roof
Laver
                                        Vea Air-vea
                                                              Residual
                                                          goT
                                      0.000
      320.000
               0.000
                       0.000
                               0.000
                                              0.000 320.000 0.000E+00
   1
      87.441
               0.000
                      0.000
                              0.000 293.893
                                               0.000
                                                      381.334 0.568E-13
              0.000 185.652 119.081 0.000
0.000 163.389 119.057 51.620
      51.015
                                               0.000
                                                      355.748 -0.568E-13
      25.686
                                               0.000 359.752
                                                              0.000E+00
Diffuse shortwave budget
Layer
      Ground Air
                        Wall
                                Roof
                                         Veg Air-veg
                                                          Top
                                                               Residual
                                      0.000
                      0.000
                                              0.000
       80.000
               0.000
                               0.000
                                                       80.000 0.000E+00
   1
              0.000
                      0.000
                              0.000 67.146
                                                      94.710 0.000E+00
   2
      27.565
                                               0.000
              0.000 37.465 30.846
                                      0.000
                                               0.000 88.514 0.000E+00
      20.203
              0.000 33.583
                              30.840 12.105
                                              0.000 89.726 -0.142E-13
   4
      13.199
Internal longwave budget
Laver Ground Air
                        Wall
                               Roof
                                        Veg Air-veg
                                                          Top
                                                               Residual
                      0.000
                                     0.000
                                              0.000 -328.035 0.000E+00
   1 -328.035
              0.000
                              0.000
   2 -327.647 0.031 0.000 0.000 216.819
                                               0.011 -110.785 0.847E-05
   3 -80.093 -0.158 -138.486 -125.417 0.000
                                              0.000 -344.211 0.569E-01
   4 -55.546 -0.151 -130.312 -125.423 -32.158 -0.002 -343.627 0.351E-01
Incoming longwave budget
Layer Ground Air
                        Wall
                               Roof
                                        Vea Air-vea
                                                              Residual
                                                          goT
   1 263.855 0.000 0.000 0.000 0.000
                                              0.000 263.855 0.000E+00
   2 89.108 0.029 0.000 0.000 198.716
                                              0.010 287.868 -0.416E-02
   3 64.432 0.157 111.365 100.876 0.000 0.000 276.877 -0.462E-01
   4 41.886 0.146 101.133 100.871 34.728 0.002 278.796 -0.287E-01
Writing NetCDF file test_surfaces_out.nc
```

8 Incorporating SPARTACUS-Surface into another program

SPARTACUS-Surface is primarily a software library that is designed to be called from within a larger program such as an atmospheric model. The library is written entirely using Fortran modules, and you will need all the Fortran source files in the utilities, radtool and radsurf directories. The utilities/radiation_io.F90 file provides the nulout unit for logging messages and the radiation_abort routine for exiting if an error occurs. This file will likely need to be rewritten for your model, for example to ensure appropriate clean-up after an anomalous abort.

SPARTACUS-Surface adopts a strict policy of no global variables and no variables in modules (which are really a type of global variable). Therefore, information is passed to and from routines only via the arguments to those routines. This includes configuration information, which is stored in a <code>config_type</code> object from the <code>radsurf_config</code> module. As part of the initialization stage of the atmospheric model, such an object should be created, and will later be passed to the routine that performs the radiative transfer. A configuration object is created as follows:

```
use radsurf_config, only : config_type ! Read module defining configuration type
type(config_type) :: config ! Create a configuration object
! ...optionally set some default values - see radsurf/radsurf_config.F90...
call config%read(namelist_file_name) ! Read configuration information from a namelist file
call config%consolidate() ! Perform any additional configuration steps needed
```

Performing radiative transfer on a set of ncol surface canopy profiles is carried out in two parts. In the first part, the geometric and spectral properties of the canopies are used to compute (1) the top-of-canopy properties presented to the atmosphere above such as spectral albedo and upward longwave emission, and (2) fluxes within the canopy that are normalized with respect to downwelling shortwave and longwave fluxes at the top-of-canopy. It is envisaged that after this step, the top-of-canopy properties presented to the atmosphere are used as boundary

conditions for a full atmospheric radiative transfer calculation. One of the outputs of such a calculation is the downwelling spectral shortwave and longwave fluxes at top-of-canopy. The second (much simpler) part of the interface to *SPARTACUS-Surface* involves scaling the normalized fluxes computed in the first step to obtain the absolute fluxes within the canopy, including net fluxes into ground, roofs, walls and vegetation. These fluxes and heating rates can then be used by a canopy energy balance model.

The first part involves calling the radsurf routine, which takes as arguments a number of objects. The input description of the canopy is in the form of three Fortran derived types: the canopy_properties_type describes the wavelength-independent properties of the canopy, and the sw_spectral_properties_type and lw_spectral_properties_type describe the shortwave and longwave spectral properties. Each object describes ncol surface 'columns' to be treated independently; each column could correspond to an atmospheric model column, or alternatively may represent multiply 'tiles' underlying one or more atmospheric columns.

The arrays in the <code>canopy_properties_type</code> could have been dimensioned <code>nmaxlay*ncol</code>, where <code>nmaxlay</code> is the maximum number of layers in any of the individual columns. However, it is recognised that in a global model many or even most of the columns would be treated as 'flat' (type 0 in Fig. 1) and many layers would be unused. Therefore the arrays in these objects use a 'packed' representation, explained by considering some of the elements of <code>canopy_properties_type</code>:

```
! Integers

ncol ! Number of columns

ntotlay ! Total number of layers

! Allocatable integer vectors of length "ncol"

nlay ! Number of layers in column (can be 0)

istartlay ! Index to first layer of the column

i_representation ! Surface type (0-5)

! Allocatable real vectors of length "ncol"

cos_sza, ground_temperature

! Allocatable real vectors of length "ntotlay"

roof_temperature, wall_temperature, building_fraction, veg_fraction...
```

It can be seen that the variables describing properties as a function of height (e.g. wall temperature) are vectors of dimension ntotlay, expressing the total number of layers in this block of columns. The integer vectors nlay and istartlay enable the range of elements corresponding to the layers of a particular column to be identified. The sw_spectral_properties_type and lw_spectral_properties_type are packed similarly, except that each array has an additional nspec dimension expressing the number of shortwave or longwave spectral intervals.

Preparation of these three objects can be done as follows:

```
! Read modules defining the three derived types
                               only : canopy_properties_type
use radsurf_canopy_properties,
use radsurf_sw_spectral_properties, only : sw_spectral_properties_type
use radsurf_lw_spectral_properties, only : lw_spectral_properties_type
! Declare instances of these types
type (canopy_properties_type) :: canopy_props
type(sw_spectral_properties_type) :: sw_spectral_props
type(lw_spectral_properties_type) :: lw_spectral_props
! Allocate canopy properties given existing configuration object "config", number of columns
! "ncol", total number of layers "ntotlay" and number of shortwave and longwave spectral
! intervals "nsw" and "nlw":
call
       canopy_props%allocate(config, ncol, ntotlay)
call sw_spectral_props%allocate(config, ncol, ntotlay, nsw)
call lw_spectral_props%allocate(config, ncol, ntotlay, nlw)
```

Subsequent code would then populate the arrays within these three objects using data from the host model (consult the files radsurf_canopy_properties.F90, radsurf_sw_spectral_properties.F90 and radsurf_lw_spectral_properties.F90 for precise contents of these arrays). Note that the offline driver pro-

gram driver/spartacus_surface_driver.F90 does not use these allocate type-bound procedures, but rather populates the arrays within the objects directly using the contents of the input netCDF file.

We also need to prepare objects to hold the output from the radsurf routine:

```
! Read modules defining the relevant derived types
use radsurf_canopy_flux,
                                 only : canopy_flux_type
! Declare an object holding the top-of-canopy boundary conditions presented to the atmosphere
! above
type (boundary_conds_out_type) :: bc_out
! Declare canopy flux components: the first three contain the fluxes and net absorption rates
! within the canopy normalized by the shortwave-diffuse, shortwave-direct and longwave
! downwelling flux at top-of-canopy. The fourth contains the same but purely due to internal
! longwave emission within the canopy
type(canopy_flux_type)
                        :: sw_norm_diff, sw_norm_dir, lw_norm, lw_internal
! Allocate these objects, noting that the shortwave objects use internal arrays to also store
! direct fluxes, not needed in the longwave
call
        bc_out%allocate(ncol, nsw, nlw)
call sw_norm_diff%allocate(config, ncol, ntotlay, nsw, use_direct=.true.)
call sw_norm_dir%allocate(config, ncol, ntotlay, nsw, use_direct=.true.)
call lw_internal%allocate(config, ncol, ntotlay, nlw, use_direct=.false.)
call
         lw_norm%allocate(config, ncol, ntotlay, nlw, use_direct=.false.)
! Optionally set all fluxes to zero
call sw_norm_dir%zero_all()
call sw_norm_diff%zero_all()
call lw_internal%zero_all()
call lw_norm%zero_all()
```

We are now in a position to call the radsurf routine:

Optionally, a call to radsurf may specify the range of columns to process via istartcol and iendcol. This is useful for OpenMP parallelization: if the objects contain a large number of columns then radsurf can be called simultaneously by multiple threads, each thread being instructed to work on a different range of columns. This is done by the offline SPARTACUS-Surface driver. The final four canopy flux objects are marked as 'optional' because the config object may have specified to only perform shortwave or longwave radiative transfer, in which case only two such output objects would be needed.

The boundary_conds_out_type is fairly small, containing four arrays. The arrays sw_albedo and sw_albedo_dir are the shortwave spectral albedo at top-of-canopy presented to incoming diffuse and direct solar radiation, and are dimensioned $nsw \times ncol$. The arrays $lw_emissivity$ and $lw_emission$ are the top-of-canopy longwave spectral emissivity and upward emission (in W m⁻²), dimensioned $nlw \times ncol$.

After the atmospheric radiative transfer calculation has completed using these arrays as boundary conditions, we need to use the downwelling fluxes at top-of-canopy to scale the normalized canopy fluxes.

```
! Declare objects to contain total (unnormalized) canopy fluxes
type(canopy_flux_type) :: lw_flux, sw_flux

! Allocate these objects
call sw_flux%allocate(config, ncol, ntotlay, nsw, use_direct=.true.)
call lw_flux%allocate(config, ncol, ntotlay, nlw, use_direct=.false.)
```

```
! Suppose the atmospheric radiative transfer scheme has provided three arrays of spectral
! downwelling radiation at top of canopy, top_flux_dn_diffuse_sw(nsw,ncol),
! top_flux_dn_direct_sw(nsw,ncol) and top_flux_dn_lw(nlw,ncol), we can use them to scale
! the normalized shortwave and longwave canopy fluxes, also taking as input the number of
! layers stored in each column, canopy_props%nlay
call sw_norm_diff%scale(canopy_props%nlay, top_flux_dn_diffuse_sw)
call sw_norm_dir%scale(canopy_props%nlay, top_flux_dn_direct_sw)
call lw_norm%scale(canopy_props%nlay, top_flux_dn_lw)

! Finally, sum the two contributions in each spectral region to obtain total (unnormalized)
! canopy fluxes
call sw_flux%sum(sw_norm_dir, sw_norm_diff)
call lw_flux%sum(lw_internal, lw_norm)
```

The contents of sw_flux and lw_flux are then available to use in a canopy energy balance scheme. See radsurf_radsurf_canopy_flux.F90 for the precise contents of these objects. Note that at this stage they are still in the same spectral intervals as used by the *SPARTACUS-Surface* calculation. In the shortwave this is useful as it enables the photosynthetically active part of the spectral absorption by vegetation to be computed.

Further development is still needed on the spectral aspect of SPARTACUS-Surface. It is expected that in the shortwave, the radiation calculations will all be performed in the user-specified spectral intervals, and atmospheric extinction will either be ignored or it will be left to the user to provide atmospheric extinction coefficients, especially due to aerosols. It ought to be reasonable to neglect gas absorption and Rayleigh scattering since the Rayleigh optical depth is small through the limited depth of a surface canopy, and in the parts of the near-infrared spectrum where the gaseous absorption is large, little solar radiation is likely to penetrate down through the atmosphere to the top of the canopy.

In the longwave, there will need to be a mechanism to treat gaseous absorption given its importance (Hogan, 2019b). This could be implemented by mapping the user-specified longwave spectral intervals on to a larger number of intervals suitable for longwave radiative transfer and running SPARTACUS-Surface at this spectral resolution. The larger number of intervals could then be passed to the atmospheric longwave radiative transfer. For the canopy energy balance model, only the broadband longwave fluxes are likely to be of interest, which could be computed by simply summing the fluxes along the nlw dimension.

9 License and copyright

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