# Working with lists

# Tad Dallas

# Contents

What are lists?								
usefusolve be u a sin	ul whe ed this seful i ngle sin	en dealing with s before by con in my research mulation, or wh	multiple data.: sidering a singl when I'm simu	frames that each le data.frame valating ecologic functions to re	ch correspond to with a column of al dynamics, we turn data that	to a different us corresponding where each list is t is not really s	name type). The nit of study (not to country). List item can be the tructured as a dects.	te that we ts tend to results of
lst	<- 1:	ist(runif(100	), data.fram	ne(x=runif(10	00), y=runif	(100)), lette	ers[1:10], 'a	')
<pre># index single list elements lst[[1]]</pre>								
## ## ## ## ## ## ## ## ## ##	[7] [13] [19] [25] [31] [37] [43] [49] [55] [61] [67] [73] [79] [85] [91]	0.126463111 0.602484902 0.923601537 0.995989168 0.173852696 0.115741640 0.080241389 0.806415981 0.800384199 0.428420319 0.034133181 0.996726355 0.772098457 0.323888728 0.389481444	0.345887301 0.640952523 0.812405247 0.015106945 0.743967811 0.506830390 0.570753892 0.858652729 0.581949470 0.872079416 0.953042187 0.349469113 0.191934285 0.340390051 0.605172041 0.618297326 0.443346858	0.801419775 0.552596993 0.745050451 0.220956105 0.614981351 0.315901366 0.210387068 0.912762206 0.026579988 0.905021955 0.802252213 0.059203505 0.617618100 0.894832945 0.734688197	0.703852942 0.435955625 0.073284685 0.663049563 0.33218715 0.367685139 0.499990614 0.656683683 0.528983004 0.585571432 0.363345457 0.467623840 0.077781499 0.591233902 0.896326262	0.692316750 0.534386890 0.113772524 0.898064294 0.970304654 0.573164525 0.745983964 0.221398124 0.477748008 0.338094982 0.013893382 0.828425161 0.351816075 0.443998539	0.661239739 0.944155622 0.449166791 0.068160296 0.991651755 0.357366330 0.127897062 0.001243219 0.930355262 0.582047309 0.417913733 0.591229726 0.481981283 0.365908439	
lst	[[2]]							

```
##
                  Х
       0.5929958255 0.17029630
## 1
## 2
       0.2273250618 0.53290314
## 3
       0.9836112957 0.86924316
       0.6195508826\ 0.12927133
## 5
       0.5355325681 0.67682812
```

```
## 6
       0.4026766657 0.43604307
       0.6762322055 0.40647950
## 8
       0.3963014511 0.65137982
## 9
       0.6644938316 0.40649973
## 10
       0.7806688529 0.11119371
## 11
      0.7036440966 0.08355948
       0.2227644119 0.09273169
## 12
## 13
       0.9076592533 0.56791180
  14
       0.0635249263 0.92151644
##
  15
       0.3846838397 0.88746459
  16
       0.0828204176 0.34702496
       0.0089157571 0.92305583
##
   17
##
   18
       0.2628677031 0.55358793
##
   19
       0.2834337901 0.55690307
## 20
       0.4602273584 0.22505792
##
  21
       0.7177088670 0.89639362
##
       0.6354470754 0.54169483
   22
##
       0.8354455414 0.28061722
##
       0.9358799148 0.10206755
  24
##
   25
       0.5355347167 0.71250764
##
  26
       0.8747624087 0.06888842
   27
       0.2216022352 0.93237516
## 28
      0.5067166621 0.27075326
       0.0707920054 0.75904288
##
   29
##
   30
       0.4882760381 0.27788979
   31
       0.3969312292 0.97731666
##
   32
       0.5253981669 0.40926696
##
   33
       0.5058445535 0.35889997
##
   34
       0.7965803898 0.31126656
##
   35
       0.0596600999 0.25050042
##
  36
       0.7038921718 0.76961634
##
   37
       0.1191473629 0.64044271
##
   38
       0.9839006439 0.94068814
##
       0.4704159640 0.30293546
   39
##
       0.2987238981 0.19892445
##
       0.8741614837 0.42501121
  41
       0.7907014692 0.31980800
## 43
       0.9785891976 0.59483399
##
  44
       0.5011787198 0.41937950
       0.9215252022 0.51594234
##
       0.6987903509 0.95576815
## 47
       0.4357083272 0.29526233
##
   48
       0.4117776004 0.38421484
##
   49
       0.4168347928 0.10734488
       0.9232791164 0.75880276
## 50
## 51
       0.9032334939 0.24470358
##
   52
       0.3211764796 0.65926991
## 53
       0.2621534232 0.89903603
##
  54
       0.3911324134 0.85420419
## 55
       0.5994308286 0.56347249
##
  56
       0.1905797804 0.45521579
## 57
       0.0301213486 0.23576408
## 58
      0.8193471823 0.88387164
## 59 0.3885250064 0.13804423
```

```
## 60 0.9287083931 0.30271911
      0.2830678045 0.13248990
     0.1789407472 0.01514116
## 63 0.3676212989 0.44306144
       0.7971775078 0.41296414
      0.6569309647 0.31814069
##
   65
     0.2762217510 0.44418724
   66
     0.4994225851 0.41114025
## 67
## 68
       0.1897352901 0.78714515
## 69 0.4413122577 0.04854814
  70
      0.9033120016 0.85028695
      0.4265394043 0.72077410
  71
##
      0.3448200265 0.80585701
   72
  73 0.2047726877 0.60327130
##
## 74
     0.2204449545 0.89111093
## 75
       0.6505701537 0.48149126
##
      0.1425985745 0.80020751
  76
##
      0.0936325965 0.98537957
##
      0.7073836210 0.69407463
  78
##
  79
       0.5972432334 0.67179105
##
  80
      0.4497663204 0.09625875
## 81
     0.3366073773 0.53599529
## 82 0.0005900322 0.85409393
## 83
       0.0109457942 0.24297398
     0.2126020296 0.43961311
## 84
## 85
     0.8253891452 0.38094641
      0.3196911684 0.13826310
## 86
       0.2563249010 0.49484376
  87
      0.0729169154 0.11026593
## 88
## 89
      0.1348894653 0.39964117
## 90
     0.9543932071 0.99344686
##
  91
      0.7279738130 0.76181286
## 92
     0.2284339434 0.11774609
      0.0653524157 0.11063333
## 93
## 94
       0.0506504318 0.88935758
## 95
      0.6178512189 0.75469403
## 96
      0.0067869988 0.79478008
## 97
      0.6904353665 0.64182053
       0.2003440587 0.79347836
## 99 0.6667320076 0.92626494
## 100 0.4037483367 0.04517744
lst[[3]]
## [1] "a" "b" "c" "d" "e" "f" "g" "h" "i" "j"
lst[[4]]
## [1] "a"
# index multiple list elements
lst[1:2]
## [[1]]
     [1] 0.042178699 0.345887301 0.139452587 0.206275186 0.452084869 0.717351019
##
     [7] 0.126463111 0.640952523 0.801419775 0.703852942 0.692316750 0.661239739
   [13] 0.602484902 0.812405247 0.552596993 0.435955625 0.534386890 0.944155622
```

```
[19] 0.923601537 0.015106945 0.745050451 0.073284685 0.113772524 0.449166791
    [25] 0.995989168 0.743967811 0.220956105 0.663049563 0.898064294 0.068160296
##
    [31] 0.173852696 0.506830390 0.614981351 0.033218715 0.970304654 0.991651755
    [37] 0.115741640 0.570753892 0.315901366 0.367685139 0.573164525 0.357366330
##
    [43] 0.080241389 0.858652729 0.210387068 0.499990614 0.745983964 0.127897062
    [49] 0.806415981 0.581949470 0.912762206 0.656683683 0.221398124 0.001243219
##
    [55] 0.800384199 0.872079416 0.026579988 0.528983004 0.477748008 0.930355262
    [61] 0.428420319 0.953042187 0.905021955 0.585571432 0.338094982 0.582047309
##
    [67] 0.034133181 0.349469113 0.802252213 0.363345457 0.013893382 0.417913733
    [73] \quad 0.996726355 \quad 0.191934285 \quad 0.059203505 \quad 0.467623840 \quad 0.828425161 \quad 0.591229726
##
    [79] 0.772098457 0.340390051 0.617618100 0.077781499 0.351816075 0.481981283
    [85] 0.323888728 0.605172041 0.894832945 0.591233902 0.443998539 0.365908439
##
    [91] 0.389481444 0.618297326 0.734688197 0.896326262 0.097087294 0.725656056
    [97] 0.600022382 0.443346858 0.393072930 0.642777560
##
##
## [[2]]
##
                  Х
##
       0.5929958255 0.17029630
  1
## 2
       0.2273250618 0.53290314
## 3
       0.9836112957 0.86924316
## 4
       0.6195508826 0.12927133
       0.5355325681 0.67682812
## 5
       0.4026766657 0.43604307
## 6
## 7
       0.6762322055 0.40647950
## 8
       0.3963014511 0.65137982
## 9
       0.6644938316 0.40649973
## 10
      0.7806688529 0.11119371
## 11
       0.7036440966 0.08355948
## 12
       0.2227644119 0.09273169
## 13
       0.9076592533 0.56791180
## 14
       0.0635249263 0.92151644
##
  15
       0.3846838397 0.88746459
##
  16
       0.0828204176 0.34702496
       0.0089157571 0.92305583
  17
##
       0.2628677031 0.55358793
##
       0.2834337901 0.55690307
##
  19
       0.4602273584 0.22505792
## 21
       0.7177088670 0.89639362
       0.6354470754 0.54169483
## 22
       0.8354455414 0.28061722
## 23
       0.9358799148 0.10206755
       0.5355347167 0.71250764
## 25
##
  26
       0.8747624087 0.06888842
##
       0.2216022352 0.93237516
  27
## 28
       0.5067166621 0.27075326
## 29
       0.0707920054 0.75904288
##
  30
       0.4882760381 0.27788979
##
  31
       0.3969312292 0.97731666
##
  32
       0.5253981669 0.40926696
##
  33
       0.5058445535 0.35889997
##
  34
       0.7965803898 0.31126656
## 35
       0.0596600999 0.25050042
## 36
      0.7038921718 0.76961634
## 37 0.1191473629 0.64044271
```

```
0.9839006439 0.94068814
## 39
       0.4704159640 0.30293546
       0.2987238981 0.19892445
##
      0.8741614837 0.42501121
  41
##
       0.7907014692 0.31980800
       0.9785891976 0.59483399
##
   43
       0.5011787198 0.41937950
## 45
       0.9215252022 0.51594234
##
   46
       0.6987903509 0.95576815
##
       0.4357083272 0.29526233
   48
       0.4117776004 0.38421484
##
       0.4168347928 0.10734488
   49
##
   50
       0.9232791164 0.75880276
##
  51
       0.9032334939 0.24470358
## 52
       0.3211764796 0.65926991
## 53
       0.2621534232 0.89903603
##
       0.3911324134 0.85420419
  54
##
       0.5994308286 0.56347249
##
       0.1905797804 0.45521579
  56
##
   57
       0.0301213486 0.23576408
##
   58
       0.8193471823 0.88387164
       0.3885250064 0.13804423
       0.9287083931 0.30271911
## 60
       0.2830678045 0.13248990
   61
  62
##
      0.1789407472 0.01514116
   63
       0.3676212989 0.44306144
##
   64
       0.7971775078 0.41296414
##
   65
       0.6569309647 0.31814069
##
       0.2762217510 0.44418724
   66
##
   67
       0.4994225851 0.41114025
## 68
       0.1897352901 0.78714515
##
   69
       0.4413122577 0.04854814
##
   70
       0.9033120016 0.85028695
       0.4265394043 0.72077410
##
  71
##
       0.3448200265 0.80585701
##
       0.2047726877 0.60327130
  73
  74
       0.2204449545 0.89111093
##
  75
       0.6505701537 0.48149126
##
   76
       0.1425985745 0.80020751
       0.0936325965 0.98537957
##
  77
       0.7073836210 0.69407463
##
  79
       0.5972432334 0.67179105
##
   80
       0.4497663204 0.09625875
##
   81
       0.3366073773 0.53599529
       0.0005900322 0.85409393
  82
## 83
       0.0109457942 0.24297398
##
   84
       0.2126020296 0.43961311
##
  85
       0.8253891452 0.38094641
##
   86
       0.3196911684 0.13826310
##
  87
       0.2563249010 0.49484376
       0.0729169154 0.11026593
##
   88
  89
       0.1348894653 0.39964117
## 90
      0.9543932071 0.99344686
## 91 0.7279738130 0.76181286
```

```
## 92  0.2284339434  0.11774609

## 93  0.0653524157  0.11063333

## 94  0.0506504318  0.88935758

## 95  0.6178512189  0.75469403

## 96  0.0067869988  0.79478008

## 97  0.6904353665  0.64182053

## 98  0.2003440587  0.79347836

## 99  0.6667320076  0.92626494

## 100  0.4037483367  0.04517744
```

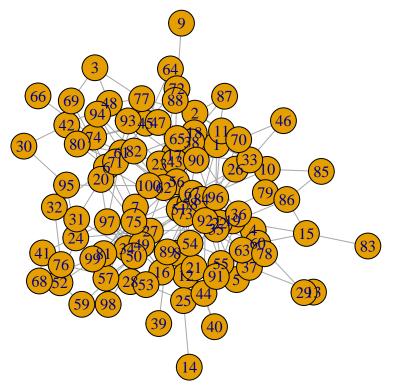
Let's think about how we might use lists. For one, many functions in R output data in list format. For instance, working with network data in R through igraph, most things are lists. Let's explore this, both as a way to introduce lists and to talk about how to analyze network data in R.

```
#install.packages('igraph')
library(igraph)
##
## Attaching package: 'igraph'
## The following objects are masked from 'package:dplyr':
##
##
       as_data_frame, groups, union
## The following objects are masked from 'package:stats':
##
##
       decompose, spectrum
## The following object is masked from 'package:base':
##
##
       union
g <- igraph::sample_gnm(100, 200)
str(g)
## Class 'igraph'
                  hidden list of 10
    $ : num 100
##
##
    $ : logi FALSE
   $ : num [1:200] 10 11 18 22 24 26 27 27 30 32 ...
   $ : num [1:200] 1 4 14 6 13 23 11 20 19 0 ...
##
    $ : NULL
##
  $ : NULL
##
  $ : NULL
   $ : NULL
##
##
    $ :List of 4
##
     ..$: num [1:3] 1 0 1
##
     ..$ :List of 4
##
     .... $ name : chr "Erdos-Renyi (gnm) graph"
     .. .. $ type : chr "gnm"
##
##
     .. ..$ loops: logi FALSE
##
     .. ..$ m
                 : num 200
     ..$ : list()
##
##
     ..$ : list()
```

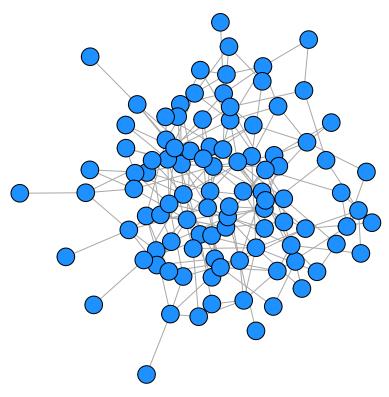
Recall when we introduced the plot function, and I said that packages build in functionality such that some base functions will work with more complex objects (the igraph object above is a list). Try it here.

\$ :<environment: 0x5561b6205c60>

# plot(g)



Nice. That's neat. We can also write a wrapper function (we will not go over function writing now, but will save that for the coming weeks), which can be useful across multiple projects. This is a function I routinely use for visualizing networks in a prettier way.



But let's get back to lists. We've seen that igraph graph objects are lists, but also many of the outputs of functions within igraph are lists (or even lists of lists!). I will not defend nested lists as being all that useful, but we will see them in a couple of weeks when we talk about APIs and spatial data.

So one of the functions built into igraph is the sir function. This is a function which runs a model on the network known as the Susceptible-Infected-Recovered model (or SIR for short), which aims to capture how diseases spread through populations.

$$\frac{dS}{dt} = -\beta SI \tag{1}$$

$$\frac{dS}{dt} = -\beta SI \tag{1}$$

$$\frac{dI}{dt} = \beta SI - \gamma I \tag{2}$$

$$\frac{dR}{dt} = \gamma I \tag{3}$$

The default behavior of the function (?sir) will run 100 simulations of the SIR model on a graph object that you provide to the function, and store the output as a list.

```
sims <- igraph::sir(g, beta=0.5, gamma=0.5, no.sim=100)</pre>
typeof(sims)
## [1] "list"
class(sims)
## [1] "sir"
# explore the structure of each list element
sims[[1]]
## $times
```

 $\begin{bmatrix} 1 \end{bmatrix} \quad 0.0000000 \quad 0.1921186 \quad 0.2149632 \quad 0.3312428 \quad 0.4021254 \quad 0.4726701$ 

```
[7] 0.5800408 0.6413701 0.7161071 0.9886130 1.0304971 1.0696435
##
   Г137
        1.2313899
                   1.2872173 1.3119527
                                       1.4449528 1.5140874 1.5755478
                                                 1.9688433
##
   [19]
        1.6062055
                   1.6473703 1.7077337
                                       1.7928525
   [25]
                   2.0607897
                             2.0807966
                                       2.1513068
##
        1.9960763
                                                  2.1532876
                                                            2.1898241
##
   [31]
        2.2713481
                   2.2867670
                             2.3019247
                                       2.3509631
                                                  2.3918212
                                                            2.3918680
                                       2.6385709
##
   [37]
        2.3922000
                   2.5481631
                            2.6262734
                                                 2.6628643
                                                            2.7045432
##
   Γ431
        2.7519082 2.8219201
                             2.8325705
                                       2.8426960
                                                  2.8435007
                                                            2.8454576
##
   [49]
         2.8605168
                   2.8910748
                             2.9486736
                                       2.9881167
                                                  3.0211511
                                                            3.0342535
##
   [55]
         3.0757526
                   3.1321501
                             3.1367684
                                       3.1473258
                                                  3.1487937
                                                            3.1893742
##
   [61]
         3.2898005
                   3.3066820
                             3.3401556
                                       3.3510520
                                                  3.3605245
                                                            3.3749615
   [67]
        3.4082842
                   3.4146831
                             3.4194386
                                       3.6133908
                                                 3.6428218
                                                            3.7000315
   [73]
##
         3.7061213
                   3.7338666
                             3.7768862
                                       3.8196489
                                                  3.8396501
                                                            3.8509928
                                                           4.2723094
##
   [79]
        3.9119508
                   4.0545137
                             4.0881923
                                       4.1628582
                                                 4.2105582
                                                            4.3844769
##
   [85]
        4.3056992
                   4.3125000
                             4.3502725
                                       4.3504797
                                                 4.3601547
                   4.6101286
                             4.6386225
                                       4.7206608
                                                 4.7344202
##
   [91]
        4.4808210
                                                           4.7887437
##
   [97]
        4.7908863
                   4.8782672
                             4.8945931
                                       4.9015184
                                                  4.9495701
                                                            4.9640523
## [103]
        4.9918006
                  4.9954934
                             5.0405440
                                       5.1994470 5.2130955
                                                            5.2472855
  [109] 5.2483268
                   5.2484064
                             5.2954193 5.3686232 5.3748980
                                                            5.4029873
## [115] 5.4160585
                   5.4601942 5.5156173 5.5354701 5.7068908
                                                           5.7766615
## [121]
        5.7785157
                   5.9292836
                             6.1361620
                                       6.1435300
                                                  6.1463360
                                                            6.2195805
## [127]
        6.2809526
                   6.3276955
                             6.3846034 6.4233745 6.4539118
                                                            6.4757150
                   6.5796885
                             6.6043169
                                       6.6366575
## [133] 6.5328834
                                                 6.6476493
                                                            6.6690822
                                       7.0031820
## [139]
        6.8082685
                   6.8798711
                             6.9199198
                                                  7.0939676
                                                            7.1745020
## [145]
        7.2261478
                   7.2590301
                             7.6945963
                                       7.7038922
                                                  7.8408254
                                                            8.0291370
## [151] 8.1667851 8.8027106 8.8190854 8.8299496 9.0961298 9.1867725
## [157] 9.2331006 9.4058848 9.4305037 9.9327765 10.7029140 10.8638923
  [163] 11.1481500 11.4511554 12.5097873 14.1424459
##
## $NS
##
    [1] 99 98 97 96 96 96 95 94 93 92 91 90 89 89 88 87 86 86 85 84 83 82 82 81
##
    [26] 81 80 80 79 79 78 78 77 76 75 74 73 72 72 71 70 69 69 68 67 66 65 64 64 63
   [51] 62 62 62 61 60 59 59 59 58 57 56 55 54 53 52 52 51 51 51 51 50 49 48 48 48
   [76] 48 47 47 47 47 47 46 46 45 45 44 44 43 43 43 42 41 40 39 38 38 37 37 37 36
  [101] 35 35 35 35 34 33 33 32 31 30 30 30 29 28 28 28 27 27 26 25 24 23 22 22
  ##
##
## $NI
    [1] 1 2 3 4 3 2 3 4 5 6 7 8 9 8 7 8 9 10 9 10 11 12 13 12 13
##
   [26] 12 13 12 13 12 13 12 13 14 15 16 17 18 17 18 19 20 19 20 21 22 23 24 23 24
##
   [51] 25 24 23 24 25 26 25 24 25 26 27 28 29 30 31 30 31 30 29 28 29 30 31 30 29
   [76] 28 29 28 27 26 25 26 25 26 25 26 25 26 25 24 25 26 27 28 29 28 29 28 27 28
## [101] 29 28 27 26 27 28 27 28 29 30 29 28 29 30 29 28 29 28 29 30 31 32 33 32 31
  [126] 30 31 30 29 30 29 30 29 28 29 28 27 26 25 24 23 22 21 20 19 18 17 16 15 14
## [151] 13 14 13 12 11 10 9 8 7 6 5 4 3 2 1 0
##
## $NR
##
    [1]
        [26] 7 7 8 8 9 9 10 10 10 10 10 10 10 11 11 11 11 12 12 12 12 12 12 13 13
   [51] 13 14 15 15 15 15 16 17 17 17 17 17 17 17 17 18 18 19 20 21 21 21 21 22 23
   [76] 24 24 25 26 27 28 28 29 29 30 30 31 31 32 33 33 33 33 33 33 34 34 35 36 36
## [101] 36 37 38 39 39 39 40 40 40 40 41 42 42 42 43 44 44 45 45 45 45 45 45 46 47
## [126] 48 48 49 50 50 51 51 52 53 53 54 55 56 57 58 59 60 61 62 63 64 65 66 67 68
## [151] 69 69 70 71 72 73 74 75 76 77 78 79 80 81 82 83
```

# # each list element is another list sims[[1]][[1]]

```
##
     [1]
          0.0000000
                      0.1921186
                                0.2149632 0.3312428
                                                        0.4021254
                                                                    0.4726701
##
     [7]
          0.5800408
                      0.6413701
                                 0.7161071
                                             0.9886130
                                                        1.0304971
                                                                    1.0696435
##
    Γ137
          1.2313899
                      1.2872173
                                 1.3119527
                                             1.4449528
                                                        1.5140874
                                                                    1.5755478
                      1.6473703
##
    [19]
          1.6062055
                                 1.7077337
                                             1.7928525
                                                        1.9688433
                                                                    1.9776394
##
    [25]
          1.9960763
                      2.0607897
                                 2.0807966
                                             2.1513068
                                                        2.1532876
                                                                    2.1898241
##
    [31]
          2.2713481
                      2.2867670
                                 2.3019247
                                             2.3509631
                                                        2.3918212
                                                                    2.3918680
    [37]
          2.3922000
                      2.5481631
                                 2.6262734
                                             2.6385709
                                                        2.6628643
##
                                                                    2.7045432
    [43]
##
          2.7519082
                      2.8219201
                                 2.8325705
                                             2.8426960
                                                        2.8435007
                                                                    2.8454576
    [49]
          2.8605168
                      2.8910748
                                 2.9486736
                                             2.9881167
                                                        3.0211511
##
                                                                    3.0342535
                      3.1321501
                                                        3.1487937
##
    [55]
          3.0757526
                                 3.1367684
                                             3.1473258
                                                                    3.1893742
##
    [61]
          3.2898005
                      3.3066820
                                 3.3401556
                                             3.3510520
                                                        3.3605245
                                                                    3.3749615
##
    [67]
          3.4082842
                      3.4146831
                                 3.4194386
                                             3.6133908
                                                        3.6428218
                                                                    3.7000315
                      3.7338666
##
    [73]
          3.7061213
                                 3.7768862
                                             3.8196489
                                                        3.8396501
                                                                    3.8509928
    [79]
          3.9119508
                      4.0545137
                                             4.1628582
##
                                 4.0881923
                                                        4.2105582
                                                                    4.2723094
##
    [85]
          4.3056992
                      4.3125000
                                 4.3502725
                                             4.3504797
                                                        4.3601547
                                                                    4.3844769
                                             4.7206608
##
    [91]
          4.4808210
                      4.6101286
                                 4.6386225
                                                        4.7344202
                                                                    4.7887437
##
    [97]
          4.7908863
                      4.8782672
                                 4.8945931
                                             4.9015184
                                                        4.9495701
                                                                    4.9640523
                      4.9954934
                                             5.1994470
##
   [103]
          4.9918006
                                 5.0405440
                                                        5.2130955
                                                                    5.2472855
  [109]
          5.2483268
                      5.2484064
                                 5.2954193
                                             5.3686232
                                                        5.3748980
##
                                                                    5.4029873
## [115]
          5.4160585
                      5.4601942
                                 5.5156173
                                             5.5354701
                                                        5.7068908
                                                                    5.7766615
                                                        6.1463360
   Γ121]
                      5.9292836
                                             6.1435300
##
          5.7785157
                                 6.1361620
                                                                    6.2195805
   [127]
          6.2809526
                      6.3276955
                                 6.3846034
                                             6.4233745
                                                        6.4539118
                                                                    6.4757150
   [133]
          6.5328834
                      6.5796885
                                 6.6043169
                                             6.6366575
                                                        6.6476493
                                                                    6.6690822
   [139]
          6.8082685
                      6.8798711
                                 6.9199198
                                             7.0031820
                                                        7.0939676
##
                                                                    7.1745020
                      7.2590301
                                             7.7038922
## [145]
          7.2261478
                                 7.6945963
                                                        7.8408254
                                                                    8.0291370
          8.1667851
                      8.8027106
                                 8.8190854
                                             8.8299496
                                                        9.0961298
  [151]
                                                                    9.1867725
## [157]
          9.2331006
                      9.4058848
                                 9.4305037
                                             9.9327765 10.7029140 10.8638923
## [163] 11.1481500 11.4511554 12.5097873 14.1424459
```

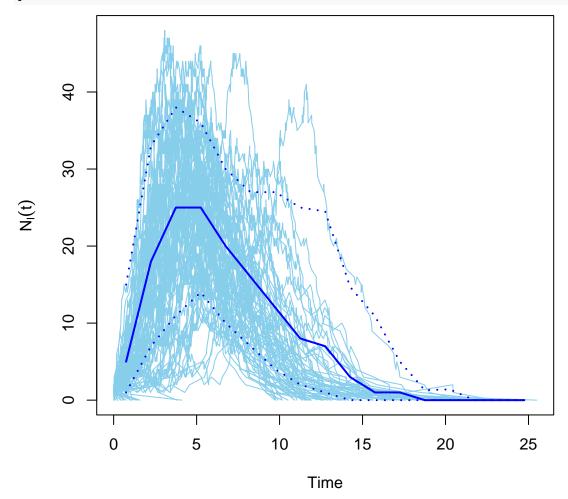
#### sims[[1]]\$times

```
[1] 0.0000000
                      0.1921186
                                0.2149632
                                            0.3312428
                                                        0.4021254
##
                                                                    0.4726701
##
     [7]
          0.5800408
                      0.6413701
                                 0.7161071
                                             0.9886130
                                                         1.0304971
                                                                    1.0696435
                      1.2872173
                                             1.4449528
##
    [13]
          1.2313899
                                 1.3119527
                                                        1.5140874
                                                                    1.5755478
##
    [19]
          1.6062055
                      1.6473703
                                 1.7077337
                                             1.7928525
                                                         1.9688433
                                                                    1.9776394
##
    [25]
          1.9960763
                      2.0607897
                                 2.0807966
                                             2.1513068
                                                        2.1532876
                                                                    2.1898241
    [31]
          2.2713481
                      2.2867670
                                 2.3019247
                                             2.3509631
                                                         2.3918212
                                                                    2.3918680
##
                      2.5481631
##
    [37]
          2.3922000
                                 2.6262734
                                             2.6385709
                                                         2.6628643
                                                                    2.7045432
    [43]
                      2.8219201
                                             2.8426960
                                                         2.8435007
##
          2.7519082
                                 2.8325705
                                                                    2.8454576
                      2.8910748
##
    [49]
          2.8605168
                                 2.9486736
                                             2.9881167
                                                         3.0211511
                                                                    3.0342535
                      3.1321501
                                 3.1367684
                                             3.1473258
                                                        3.1487937
##
    [55]
          3.0757526
                                                                    3.1893742
##
    [61]
          3.2898005
                      3.3066820
                                 3.3401556
                                             3.3510520
                                                         3.3605245
                                                                    3.3749615
                      3.4146831
                                             3.6133908
##
    Γ67]
          3.4082842
                                 3.4194386
                                                         3.6428218
                                                                    3.7000315
                                                                    3.8509928
##
    [73]
          3.7061213
                      3.7338666
                                 3.7768862
                                             3.8196489
                                                         3.8396501
##
    [79]
          3.9119508
                      4.0545137
                                 4.0881923
                                             4.1628582
                                                        4.2105582
                                                                    4.2723094
    [85]
                      4.3125000
                                             4.3504797
##
          4.3056992
                                 4.3502725
                                                         4.3601547
                                                                    4.3844769
##
    [91]
          4.4808210
                      4.6101286
                                 4.6386225
                                             4.7206608
                                                        4.7344202
                                                                    4.7887437
##
    [97]
          4.7908863
                      4.8782672
                                 4.8945931
                                             4.9015184
                                                        4.9495701
                                                                    4.9640523
   [103]
                      4.9954934
##
          4.9918006
                                 5.0405440
                                             5.1994470
                                                        5.2130955
                                                                    5.2472855
   [109]
          5.2483268
                      5.2484064
                                 5.2954193
                                             5.3686232
                                                        5.3748980
                                                                    5.4029873
                      5.4601942
                                             5.5354701
##
   [115]
          5.4160585
                                 5.5156173
                                                        5.7068908
                                                                    5.7766615
  [121]
          5.7785157
                      5.9292836 6.1361620
                                             6.1435300 6.1463360
                                                                    6.2195805
```

```
## [127]
          6.2809526
                     6.3276955
                                 6.3846034
                                            6.4233745
                                                       6.4539118
                                                                   6.4757150
          6.5328834
                     6.5796885
                                 6.6043169
                                            6.6366575
                                                       6.6476493
                                                                   6.6690822
   Γ1337
          6.8082685
                     6.8798711
                                 6.9199198
                                            7.0031820
                                                       7.0939676
                                                                   7.1745020
                     7.2590301
                                 7.6945963
                                            7.7038922
                                                       7.8408254
                                                                   8.0291370
   [145]
          7.2261478
##
   [151]
          8.1667851
                     8.8027106
                                 8.8190854
                                            8.8299496
                                                       9.0961298
                                                                   9.1867725
          9.2331006
                     9.4058848
                                 9.4305037
                                            9.9327765 10.7029140 10.8638923
  [157]
  [163] 11.1481500 11.4511554 12.5097873 14.1424459
```

And just to go back to plotting for a quick second, igraph has written functionality into the sir class to work well with the base R plot function.

#### plot(sims)



Neat, right?

But back to lists. Let's work through the rest of working with lists through some exercises. Given the simulations above (sims list) ...

Calculate the mean number of infected individuals for each simulation

Find the time associated with the maximum number of infected nodes

Calculate the fraction of all simulations in which fewer than 5 nodes are infected

### apply statements

How did we approach the above questions? You almost certaintly used a for loop, right? This is perfectly fine, but there is another way. apply statements allow you to take a function and run it over all elements of a vector, columns/rows of a matrix, or a list.

apply statements typically have a prefix which gives information about what type of data it works well with. For instance, working with lists, we will use lapply. The base apply function is to work with matrices, where we want to apply a function to every row or column of a matrix (e.g., apply(matrix, 2, sum) is the same as colSums(matrix)). We will go over more examples of apply statements at some point, but for now we will focus on lapply and our problem of working with lists.

And here we hit an issue. lapply statements take a function argument, where the function needs to take the list object as an argument and then does something with it. So we'll have to learn a bare minimum of function writing now. Let's use a problem above as a motivating example, where we try to calculate the mean number of infected individuals for each simulation.

```
meanInfections <- function(x){
    # if we consider the mean infecteds as the mean of the infected vector
    return(mean(x$NI))
    # if we consider the mean infecteds as the mean number of nodes infected
    # return((x$NS[1]+1)-tail(x$NS,1))
}

meanInfs <- lapply(sims, meanInfections)
str(meanInfs)</pre>
```

```
## List of 100
   $: num 20.6
   $: num 18.4
##
   $ : num 0.5
##
   $: num 24.7
##
   $: num 26.4
   $: num 24.2
##
##
   $: num 25.1
##
   $: num 21.4
##
   $: num 15.1
##
   $: num 20.9
##
   $: num 18.6
   $ : num 1.5
##
   $: num 15.8
##
   $: num 18.2
##
   $: num 13.4
##
   $: num 18.1
   $: num 21.7
##
   $ : num 0.5
##
   $ : num 1
##
   $: num 27.5
##
   $: num 23.6
   $ : num 20.2
##
##
   $: num 19
##
   $ : num 0.5
   $: num 15.2
##
##
   $: num 1
   $: num 23.5
```

```
##
   $: num 15.4
   $: num 19.6
##
##
   $ : num 21.3
##
    $ : num 14.5
##
   $: num 25.8
    $: num 14.2
##
    $ : num 0.5
##
    $ : num 21.1
##
   $ : num 0.5
    $ : num 17.5
    $ : num 0.5
##
##
    $ : num 21
##
   $ : num 1
##
    $ : num 19.7
##
    $ : num 9.22
##
    $ : num 16.8
##
   $: num 26.3
##
    $: num 24.9
##
    $: num 12.5
##
   $ : num 12.2
##
   $ : num 1
    $ : num 0.5
##
##
    $ : num 0.5
##
   $: num 23.3
    $: num 21.8
##
    $ : num 21.4
##
    $ : num 17.3
##
   $ : num 13.4
##
    $: num 23.6
##
    $: num 8.04
   $ : num 1
##
##
    $ : num 18.8
##
    $ : num 13.3
    $: num 25.4
##
##
    $: num 18.8
##
   $: num 27.7
##
    $ : num 21.3
##
    $: num 21.7
##
   $ : num 0.5
##
   $ : num 0.5
##
    $ : num 1
##
    $: num 20.1
##
   $ : num 15.6
   $ : num 18.9
##
    $ : num 13.3
##
    $ : num 1
##
    $: num 17.4
   $ : num 24
##
##
    $ : num 12.5
##
    $ : num 16
##
   $ : num 19.4
##
   $ : num 16.9
## $ : num 21.5
```

## \$ : num 12.9

```
$: num 16.9
##
##
    $: num 26.7
##
    $: num 24.1
        num 20.8
##
##
        num 25.6
##
    $ : num 0.5
##
        num 0.5
        num 22.7
##
    $
##
    $
      : num 11.3
##
    $: num 18.5
##
    $: num 14.5
##
    $
        num 1.17
##
    $: num 17.3
    $: num 20.3
##
    $ : num 0.5
##
##
    $: num 15.5
    $ : num 0.5
##
##
    $: num 17.6
##
     [list output truncated]
```

lapply is nice in that if we give it a list object, it gives us a list object back. This makes analytical pipelines that deal with lists pretty straightforward, but if the output is a single value, we may want this to be a vector instead of a list.

```
unlist(meanInfs)
     [1] 20.596386 18.431507 0.500000 24.664835 26.352273 24.231707 25.077778
##
     [8] 21.387640 15.104938 20.873626 18.586957
                                                  1.500000 15.757143 18.223684
##
    [15] 13.414286 18.092105 21.664179 0.500000
                                                  1.000000 27.466667 23.596386
    [22] 20.235632 19.000000 0.500000 15.220000
                                                  1.000000 23.535294 12.892857
##
    [29] 15.402778 19.585366 21.290123 14.486842 25.782353 14.234177
##
    [36] 21.125000
                    0.500000 17.525000 0.500000 20.971264
                                                             1.000000 19.662162
##
         9.224638 16.808642 26.316092 24.900000 12.511905 12.166667
                    0.500000 23.253086 21.783784 21.371795 17.285714 13.426471
##
          0.500000
##
    [57] 23.650000
                   8.037037
                             1.000000 18.770270 13.342857 25.379121 18.842857
                                        0.500000
##
    [64] 27.675824 21.347059 21.660920
                                                  0.500000 1.000000 20.084416
##
    [71] 15.589744 18.909091 13.253247
                                        1.000000 17.371795 24.000000 12.455224
    [78] 16.013158 19.357143 16.948276 21.512195 16.897260 26.683908 24.117284
##
##
    [85] 20.833333 25.566667 0.500000
                                        0.500000 22.660920 11.340000 18.486842
    [92] 14.525316 1.166667 17.253247 20.290698 0.500000 15.545977 0.500000
##
    [99] 17.608434 28.467391
##
#or
meanInfs2 <- sapply(sims, meanInfections)</pre>
```

sapply statements are essentially just lapply statements that simplify the result to a vector. This is useful when the output of the function is a single value, and not so useful when function returns multiple values.

A side note: some people will criticize for loops in R, and say "just use apply, it's faster". It's not, really. Write however you feel comfortable. For awhile, apply statements were super confusing to me, so I tended to use for loops instead. After more work in, I shifted and tend to use apply statements when it fits, as they are less code and are more intuitive to me for many situations.

### Let's practice a bit.

Calculate the maximum number of infected inviduals at any time in the sims list using the apply approach.

What is the mean duration (the total time the epidemic took before it stopped) across all the epidemics in sims?

# plyr apply functionality tweaks

XYply statements as nice wrappers to more classic apply statements. Here, X and Y can take values of 'a', 'l', or 'd', depending on the input or output data structure desired. For instance, if we have a list that we would like to apply over and return a data frame, we would use ldply, where the 1 is claiming that the input is a list object, and the d is claiming that the output should be formatted as a data frame. Other examples of this syntax would be adply, ddply, laply, aaply, etc. etc.

Below, I provide an example of the aXply syntax (e.g., adply, alply, aaply).

```
arr <- array(1:27, c(3,3,3))
rownames(arr) = c("Curly", "Larry", "Moe")
colnames(arr) = c("Groucho", "Harpo", "Zeppo")
dimnames(arr)[[3]] = c("Bart", "Lisa", "Maggie")
arr</pre>
### Bart
```

```
##
   , , Bart
##
##
          Groucho Harpo Zeppo
                               7
## Curly
                 1
                        4
                 2
                               8
## Larry
                        5
## Moe
                 3
                        6
                               9
##
##
   , , Lisa
##
##
          Groucho Harpo Zeppo
## Curly
                10
                       13
                              16
                       14
                              17
## Larry
                11
                12
##
  Moe
                       15
                              18
##
##
   , , Maggie
##
##
          Groucho Harpo Zeppo
                19
                       22
                              25
## Curly
                       23
                              26
## Larry
                20
## Moe
                21
                       24
                              27
```

Arrays are something that we did not introduce when we talked about R basics, and that is because they really are not used *too* often. Think of matrix. It has two dimensions (x and y), so it can be viewed as a rectangle of data. Arrays simply add more dimensions. In the example above, there is another dimension, forming a data cube (in the rectangle analogy).

We can use plyr functionality to operate on this array and return different forms. For instance, aaply takes an array and returns a simplified array (here a vector).

```
plyr::aaply(arr, 1, sum)

## Curly Larry Moe

## 117 126 135
```

We can change one letter and now return a data frame containing two columns. This is also a good time to point out the flexibility of the XYply statements to different margins. Margins (denoted as .margins argument in R, asks along which axis you would like to operate on the array. If we set .margins=1, this corresponds to a row-wise operation, so we calculate the sum across the array for Curly, Larry, and Moe. If

we change this to .margins=2, we operate on columns, and will return sums for Groucho, Harpo, and Zeppo. And if we use .margins=3, we will return sums for Bart, Lisa, and Maggie.

```
plyr::adply(.data=arr, .margins=1, .fun=sum)
##
        X1 V1
## 1 Curly 117
## 2 Larry 126
## 3
       Moe 135
plyr::adply(.data=arr, .margins=2, .fun=sum)
##
          X1 V1
## 1 Groucho
## 2
       Harpo 126
## 3
       Zeppo 153
plyr::adply(.data=arr, .margins=3, .fun=sum)
##
         Х1
             V1
## 1
       Bart
            45
## 2
      Lisa 126
## 3 Maggie 207
```

Finally, we can return a list object. In this use case, this is not super helpful, but in other use cases the list output is pretty helpful.

```
plyr::alply(.data=arr, .margins=1, .fun=sum)
## $`1`
## [1] 117
##
## $\2\
## [1] 126
##
## $`3`
## [1] 135
##
## attr(,"split_type")
## [1] "array"
## attr(,"split_labels")
##
## 1 Curly
## 2 Larry
## 3
```

A pitch for plyr::ldply. I really like this function, as I often find myself with lists of similar structures that I want to operate on and get a single clean object back. I will not go into an example, but this is a pretty useful function (though all the utility is basically contained in vapply).

Finally, you may wonder why am I pushing apply statements so hard. It has nothing to do with speed, and only a bit to do with code clarity. The main advantage is understanding the programmatic nature of apply statements (which will be similar but less chronological than a for loop), and many parallel computing packages have their own little versions of apply statements ready to go (e.g., parallel::mclapply, parallel::parLapply, parallel::clusterApplyLB).

Let's do one practice problem to showcase the utility of ldply specifically.

Calculate the correlation between number of infections and time for each simulation, reporting the estimate,

p-value, and confidence intervals around the estimate. (you will use cor.test to do this, whose output is a list object as well)

#### A note about do.call and Reduce

While a bit opaque, these functions are pretty useful in a variety of situations. Speaking of data manipulation functions that are useful but a bit conceptually difficult, do.call and Reduce are solid base R functions.

do.call is a way of calling the same function recursively on multiple objects, and may have similar output to Reduce, which is also a way to recursively apply a function.

```
lst <- list(1:10, 1:10, 1:10, 1:10, 1:10)</pre>
lst
## [[1]]
   [1] 1 2 3
                  4 5 6 7 8 9 10
##
##
## [[2]]
         1 2 3
##
   [1]
                  4
                     5
                        6
                           7
                              8
##
## [[3]]
##
   [1]
         1
            2
               3
                     5
##
## [[4]]
   [1]
         1
            2
               3
                  4
                     5
                           7
##
## [[5]]
  [1]
        1 2 3 4 5 6 7 8 9 10
#this makes a single rbind call with each element of the list as an argument
str(do.call(rbind, lst))
    int [1:5, 1:10] 1 1 1 1 1 2 2 2 2 2 2 ...
#this does it iteratively (so makes n-1 rbind calls)
Reduce(rbind, 1st)
        [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10]
##
                2
                                5
                                     6
                                          7
                                                8
                                                     9
                                                          10
## init
           1
                     3
                           4
##
           1
                2
                     3
                           4
                                5
                                     6
                                                8
                                                          10
                2
                     3
                           4
                                5
                                     6
                                          7
                                                     9
                                                          10
##
           1
                                                8
##
           1
                2
                     3
                           4
                                5
                                     6
                                          7
                                                8
                                                     9
                                                          10
                     3
                                     6
                                                8
##
           1
                                                          10
sessionInfo
```

```
## R version 4.3.1 (2023-06-16)
## Platform: x86_64-pc-linux-gnu (64-bit)
## Running under: Ubuntu 22.04.2 LTS
##
## Matrix products: default
## BLAS: /usr/lib/x86_64-linux-gnu/blas/libblas.so.3.10.0
## LAPACK: /usr/lib/x86_64-linux-gnu/lapack/liblapack.so.3.10.0
##
## locale:
```

```
[1] LC CTYPE=en US.UTF-8
                                   LC NUMERIC=C
##
   [3] LC_TIME=en_US.UTF-8
                                   LC_COLLATE=en_US.UTF-8
   [5] LC MONETARY=en US.UTF-8
                                   LC MESSAGES=en US.UTF-8
   [7] LC_PAPER=en_US.UTF-8
                                   LC_NAME=C
##
   [9] LC ADDRESS=C
                                   LC TELEPHONE=C
## [11] LC MEASUREMENT=en US.UTF-8 LC IDENTIFICATION=C
## time zone: America/New York
## tzcode source: system (glibc)
##
## attached base packages:
## [1] stats
                 graphics grDevices utils
                                               datasets methods
                                                                    base
## other attached packages:
## [1] igraph_1.5.0.1 dplyr_1.1.2
                                     plyr_1.8.8
                                                     DBI_1.1.3
                                                                    rgbif_3.7.7
## [6] jsonlite_1.8.7 httr_1.4.6
                                     rmarkdown_2.23
##
## loaded via a namespace (and not attached):
  [1] utf8_1.2.3
                          generics_0.1.3
                                                               RSQLite_2.3.1
                                            xm12_1.3.5
                          httpcode 0.3.0
   [5] stringi 1.7.12
                                             digest_0.6.33
                                                               magrittr 2.0.3
## [9] evaluate_0.21
                          grid_4.3.1
                                             fastmap_1.1.1
                                                               blob_1.2.4
## [13] maps_3.4.1
                          whisker_0.4.1
                                             crul 1.4.0
                                                               tinytex 0.45
                          purrr_1.0.1
                                             fansi_1.0.4
                                                               scales_1.2.1
## [17] urltools_1.7.3
## [21] oai 0.4.0
                          lazyeval 0.2.2
                                             cli 3.6.1
                                                               rlang 1.1.1
## [25] dbplyr_2.3.2
                          triebeard 0.4.1
                                             bit64_4.0.5
                                                               munsell_0.5.0
## [29] withr 2.5.0
                          cachem 1.0.8
                                             yaml_2.3.7
                                                               tools 4.3.1
## [33] memoise_2.0.1
                          colorspace_2.1-0
                                            ggplot2_3.4.2
                                                               curl_5.0.1
## [37] vctrs_0.6.3
                          R6_2.5.1
                                             lifecycle_1.0.3
                                                               stringr_1.5.0
## [41] bit_4.0.5
                                                               gtable_0.3.3
                          pkgconfig_2.0.3
                                             pillar_1.9.0
                                                               xfun_0.39
## [45] data.table_1.14.8 glue_1.6.2
                                             Rcpp_1.0.11
## [49] tibble_3.2.1
                          tidyselect_1.2.0
                                            highr_0.10
                                                               knitr_1.43
## [53] htmltools_0.5.5
                          compiler_4.3.1
```