

# Crop simulation models evaluation

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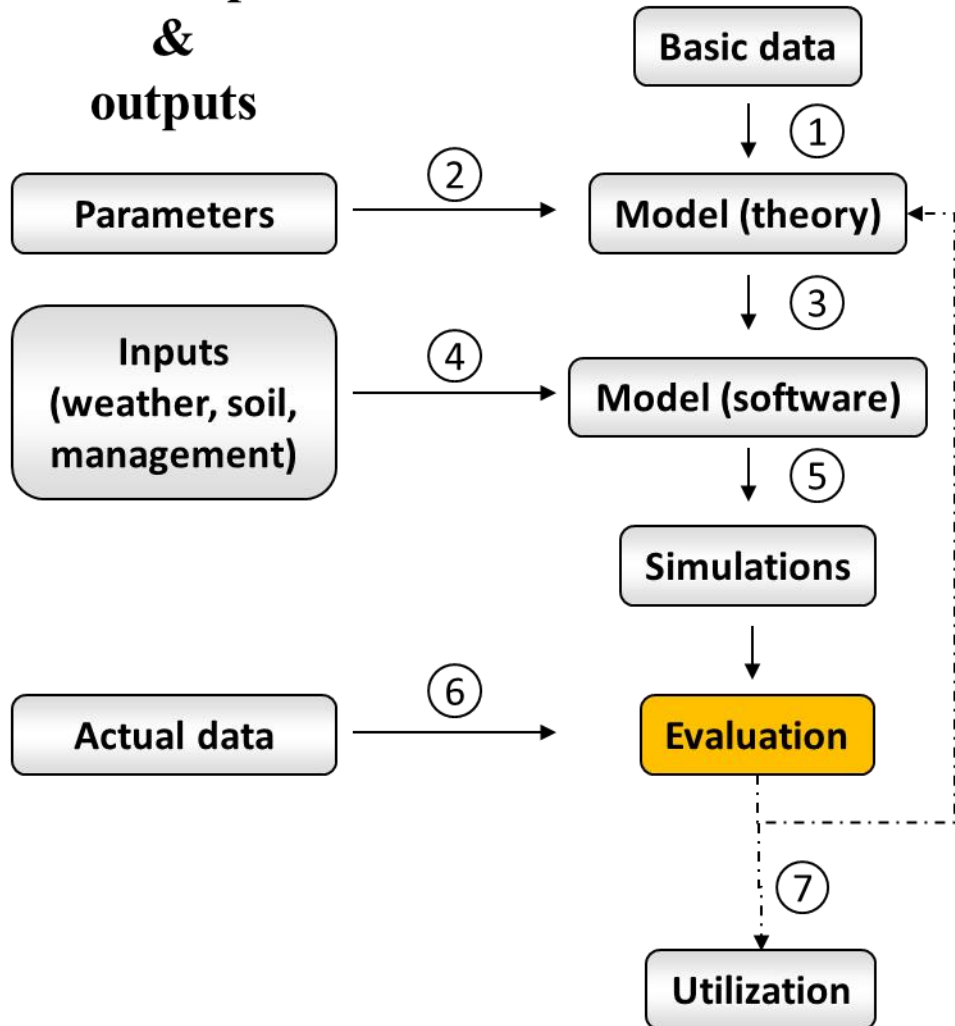
28 April 2015  
Sassari (Italy)

# Agroecological system and modelling process



**Actual system**

## Model inputs & outputs

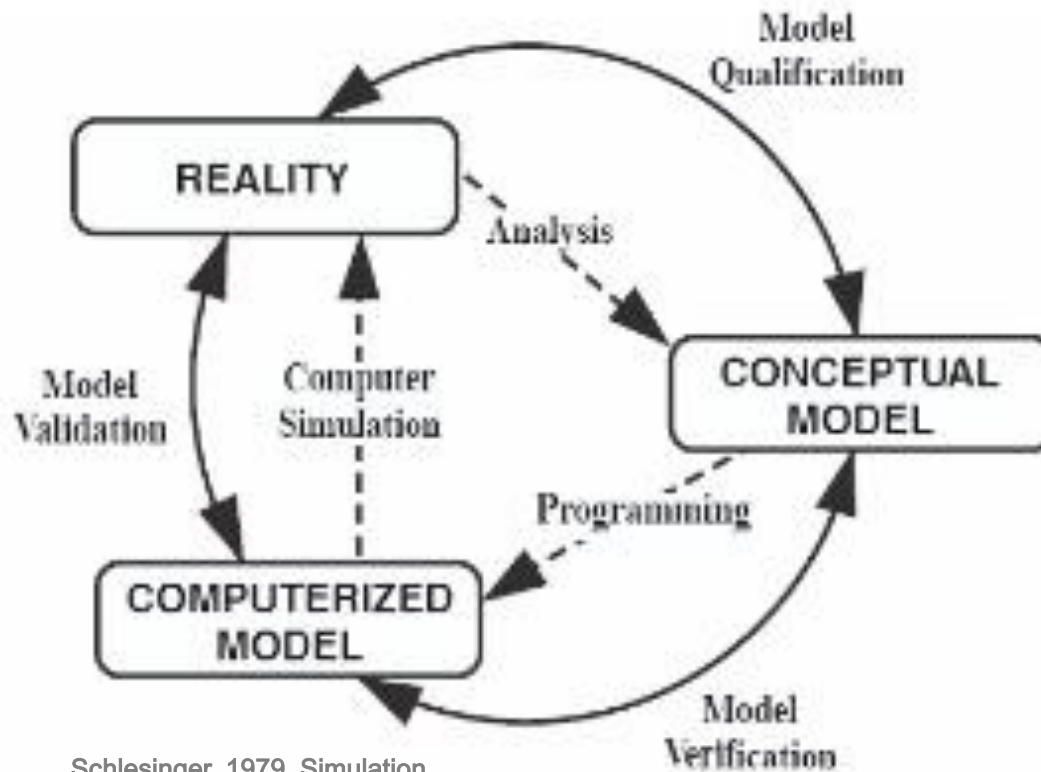


**Modelling flow**

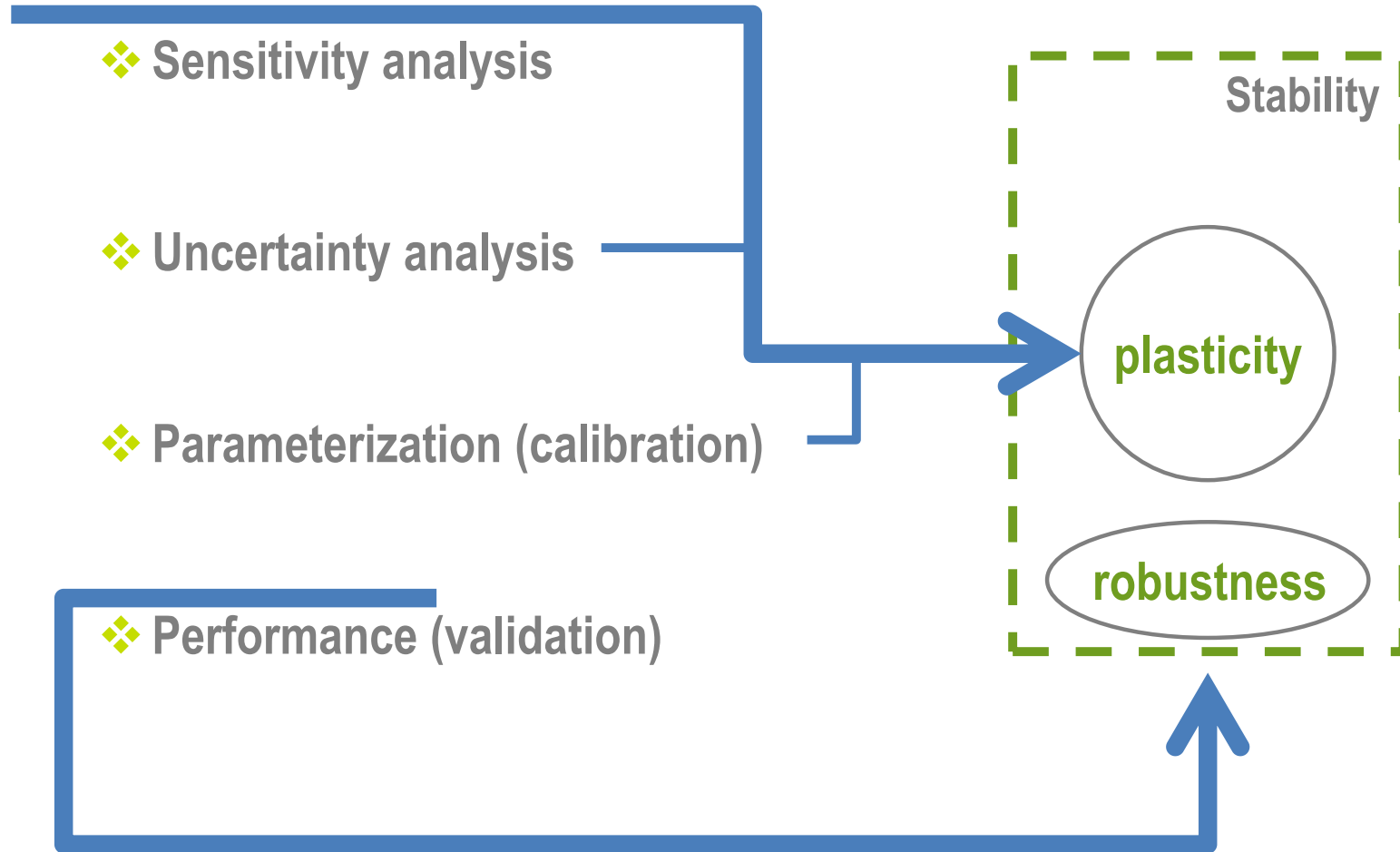
# Model evaluation

Model evaluation (**validation + verification**):

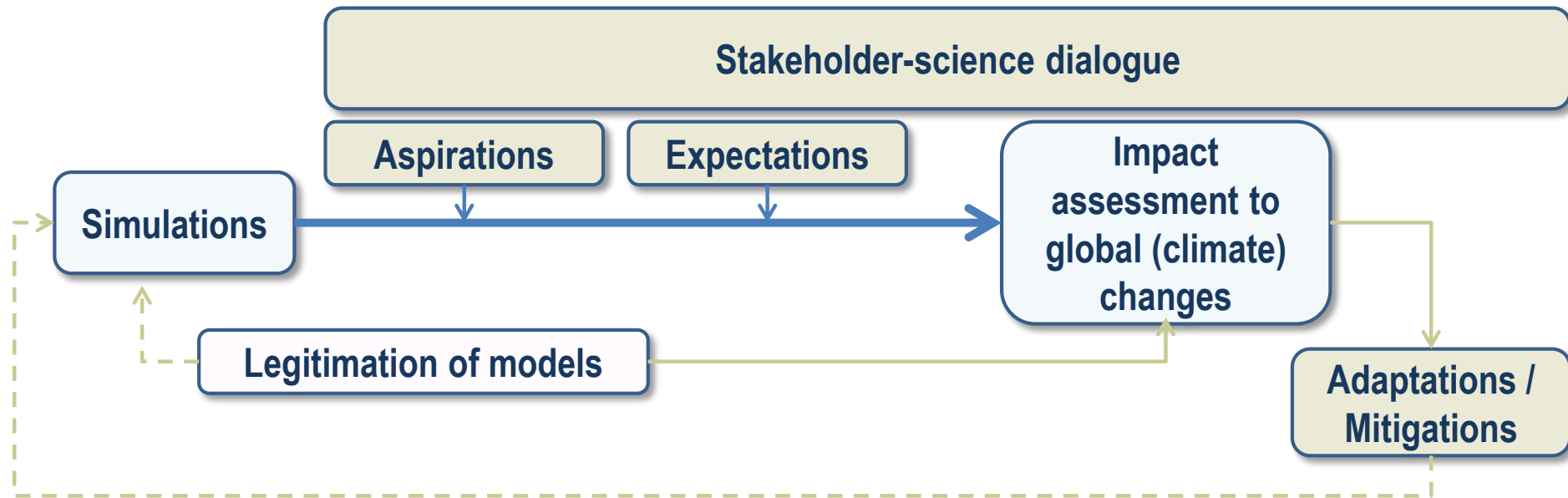
action in which the quality of a mathematical model for specific objectives is established



# Model evaluation components



# Deliberative process in model-based climate change studies



Bellocchi et al. (2006)

Rivington et al. (2007)

Bellocchi et al. (2015)

# A Review of Methodologies to Evaluate Agroecosystem Simulation Models

F. MARTORANA and G. BELLOCCHI

Agron. Sustain. Dev. (2009)  
© INRA, EDP Sciences, 2009  
DOI: 10.1051/agro/2009001

Available online at:  
[www.agronomy-journal.org](http://www.agronomy-journal.org)



Review article

## Validation of biophysical models: issues and methodologies. A review

Gianni BELLOCCHI<sup>1\*,\*\*</sup>, Mike RIVINGTON<sup>2</sup>, Marcello DONATELLI<sup>1\*\*\*</sup>, Ko...



Contents lists available at ScienceDirect

Agricultural Systems

journal homepage: [www.elsevier.com/locate/agr](http://www.elsevier.com/locate/agr)

An evaluation of the statistical methods for testing the performance of crop models with observed data

J.M. Yang<sup>a</sup>, J.Y. Yang<sup>b,\*</sup>, S. Liu<sup>b,c</sup>, G. Hoogenboom<sup>d</sup>

Assessment of the adequacy of

Journal of  
Applied Remote Sensing

Derivation of biophysical variables from  
Earth observation data: validation of  
statistical measures

Katja Richter  
Clement Atzberger  
Tobias B. Hank  
Wolfram Mauser

An Indi



Environmental Modelling & Software 26 (2011) 328–336

Contents lists available at ScienceDirect

Environmental Modelling & Software

journal homepage: [www.elsevier.com/locate/envsoft](http://www.elsevier.com/locate/envsoft)



## Technical assessment and evaluation of environmental models and software: Letter to the Editor

Alexandrov<sup>a,\*</sup>, D. Ames<sup>b</sup>, G. Bellocchi<sup>c</sup>, M. Bruen<sup>d</sup>, N. Crout<sup>e</sup>, M. Erechtkoukova<sup>f</sup>, A. Hildebrandt<sup>g</sup>,  
M. Imma<sup>h</sup>, S. Matsunaga<sup>a</sup>, S.T. Purucker<sup>k</sup>, M. Rivington<sup>l</sup>

Ecological Modelling 220 (2009) 1395–1410

Contents lists available at ScienceDirect

Ecological Modelling

journal homepage: [www.elsevier.com/locate/ecolmodel](http://www.elsevier.com/locate/ecolmodel)



Validation of the models WARM, CropSyst, and WOFOST for rice  
Acutis<sup>b</sup>, Gianni Bellocchi<sup>c</sup>, Marcello Donatelli<sup>d,1</sup>

Ecological Modelling 221 (2010) 960–964

Contents lists available at ScienceDirect

Ecological Modelling

[www.elsevier.com/locate/ecolmodel](http://www.elsevier.com/locate/ecolmodel)



Robustness based on the  
explored conditions

Spanish Journal of Agricultural Research 2009 7(1), 680–686  
ISSN: 1695-071-X

Validation strategies for rice modelling  
M. Boschetti<sup>3</sup> and M. Acutis<sup>4</sup>

Expert System

**Elaboration of new metrics**

**Setting of thresholds**

**Meaning and limitations**

**Intercorrelation**

**Disaggregation**

**Aggregation**

# Some metrics

$$CRM = \frac{\sum_{i=1}^n O_i - \sum_{i=1}^n P_i}{\sum_{i=1}^n O_i}$$

$$MAE = \frac{\sum_{i=1}^n |P_i - O_i|}{n}$$

$$RMSE = \sqrt{\frac{\sum_{i=1}^n (P_i - O_i)^2}{n}}$$

simple

absolute

squared

difference-based  
metrics

non-parametric

$$MdAE = \text{median}_{i=1, \dots, n} |P_i - O_i|$$

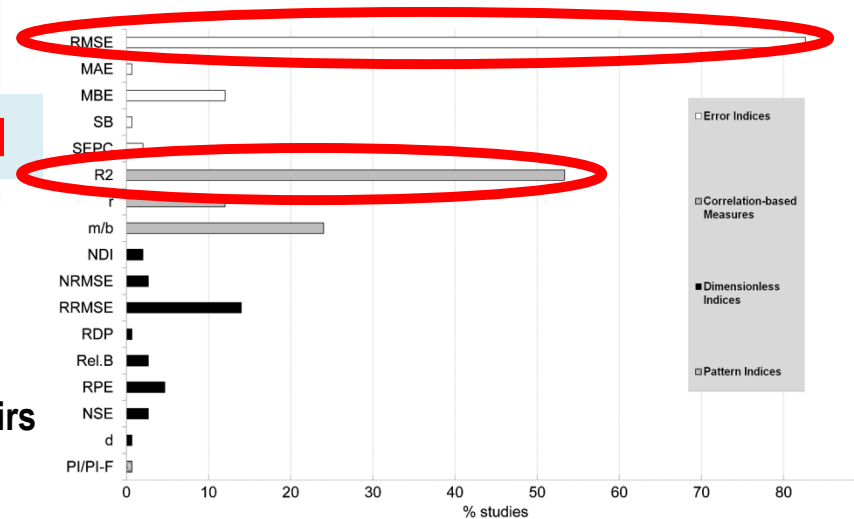
association-based metrics

$$r = \frac{\sum_{i=1}^n (P_i - \bar{P}) \cdot (O_i - \bar{O})}{\sqrt{\sum_{i=1}^n (P_i - \bar{P})^2 \cdot \sum_{i=1}^n (O_i - \bar{O})^2}} \quad r^2, \text{slope, intercept}$$

$$EF = 1 - \frac{\sum_{i=1}^n (P_i - O_i)^2}{\sum_{i=1}^n (O_i - \bar{O})^2}$$

$$d = 1 - \frac{\sum_{i=1}^n (P_i - O_i)^2}{\sum_{i=1}^n (|P_i - \bar{O}| + |O_i - \bar{O}|)^2}$$

combined



Richter et al. (2012)

P = predicted; O = observed; i = i<sup>th</sup> O/P pair; n = number of O/P pairs



# Setting of thresholds

Performance measure	Unit	Value range and purpose	Reliability criteria
Coefficient of determination ( $R^2$ ) of the linear regression estimates versus measurements	dimensionless	0 (absence of fit) to 1 (perfect fit): the closer values are to 1, the better the model	> 0.8
Willmott (1982) index of agreement ( <b>d</b> )	dimensionless	0 (absence of agreement) to 1 (perfect agreement): the closer values are to 1, the better the model	> 0.8
Mean absolute error over the mean of the measured values ( <b>MAE(%)</b> )	%	0 (optimum) to positive infinity: the smaller MAE(%), the better the model performance	< 20

De Jager (1994)



# Key issues and factors

Key validation issues	Major factors to investigate				
	Modelling objective	Model inputs	Model outputs	Model structure	Modelling conditions
Validation purpose	X		X		X
Robustness of results			X		X
Interpretation of phenomena		X	X	X	
Model comparison				X	
Model predictions	X		X		X
Model complexity		X	X	X	
Data accuracy		X	X		
Time histories			X		

# Fuzzy-logic based indicators

**Model Quality Indicator ( $MQI_s$ )**

$MQI_s$

membership function  
 $S[x, a = 0; b = 1]$

membership function  
 $S[x, a = \min(F, U); b = \max(F, U)]$

membership function  
 $S[x, a = \min(F, U); b = \max(F, U)]$

Ratio of relevance parameters ( $R_p$ )  
F Partial U  
 $\geq 0.10 \leftrightarrow \leq 0.50$

A/C relative weight ( $w_k$ )  
F Partial U  
 $\geq 0.70 \leftrightarrow \leq 0.30$

Complexity  
F Partial U  
0  $\leftrightarrow$  1

Agreement  
F Partial U  
0  $\leftrightarrow$  1

**Complexity**

**Agreement**

F	F	0.00
F	U	0.75
U	F	0.25
U	U	1.00

0.00	F	F	F
0.20	F	F	U
0.60	F	U	F
0.80	F	U	U
0.20	U	F	F
0.40	U	F	U
0.80	U	U	F
1.00	U	U	U

# Multi-site, Model Quality Indicator ( $MQI_m$ )

$MQI_m$

membership function  
 $S[x; a = \min(F, U); b = \max(F, U)]$

membership function  
 $S[x; a = 0; b = 1]$

## Agreement

## Complexity

## Robustness

expert weight	Correlation coefficient ( $R$ ) F Partial U $\geq 0.90 \leftrightarrow \leq 0.70$	Index of agreement ( $d$ ) F Partial U $\geq 0.90 \leftrightarrow \leq 0.70$	Probability of equal means ( $P(t)$ ) F Partial U $\geq 0.10 \leftrightarrow \leq 0.05$
0.00	F	F	F
0.20	F	F	U
0.60	F	U	F
0.80	F	U	U
0.20	U	F	F
0.40	U	F	U
0.80	U	U	F
1.00	U	U	U

	Ratio of relevance parameters ( $R_p$ ) F Partial U $\geq 0.10 \leftrightarrow \leq 0.50$	AIC relative weight ( $w_R$ ) F Partial U $\geq 0.70 \leftrightarrow \leq 0.30$
0.00	F	F
0.50	F	U
0.50	U	F
1.00	U	U

	Index of robustness ( $I_R$ ) F Partial U 1 $\leftrightarrow$ 10
0.00	F
1.00	U

	Complexity F Partial U 0 $\leftrightarrow$ 1	Agreement F Partial U 0 $\leftrightarrow$ 1	Robustness F Partial U 0 $\leftrightarrow$ 1
0.00	F	F	F
0.25	F	F	U
0.50	F	U	F
0.75	F	U	U
0.25	U	F	F
0.50	U	F	U
0.75	U	U	F
1.00	U	U	U

membership function  
 $S[x; a = \min(F, U); b = \max(F, U)]$

# Robustness of a model

A **robustness measure** would account for model performance stability over a wide range of conditions (single site versus multiple sites)

How the variability of model performance can be quantified with the variability of conditions?

Index of robustness

$$I_R = \frac{\sigma_{EF}}{\sigma_{SAM}} \quad (0, \text{best}; +\infty, \text{worst})$$

Modelling efficiency

$$EF = 1 - \frac{\sum_{i=1}^n (P_i - O_i)^2}{\sum_{i=1}^n (O_i - \bar{O})^2} \quad (-\infty, \text{worst}; 1, \text{best})$$

Synthetic Agro-Meteorological Indicator

$$SAM = \frac{Rain - ET_0}{Rain + ET_0} \quad (-1, +1)$$

# Synthetic indicators

*Aggregation rules:  
fuzzy-logic based weighing system*

## I. Agreement

- Correlation coefficient
- Index of agreement
- Probability of equal means

## II. Complexity

- Ratio of relevant parameters
- Parameters-agreement criterion

## III. Stability (robustness)

- Index of robustness

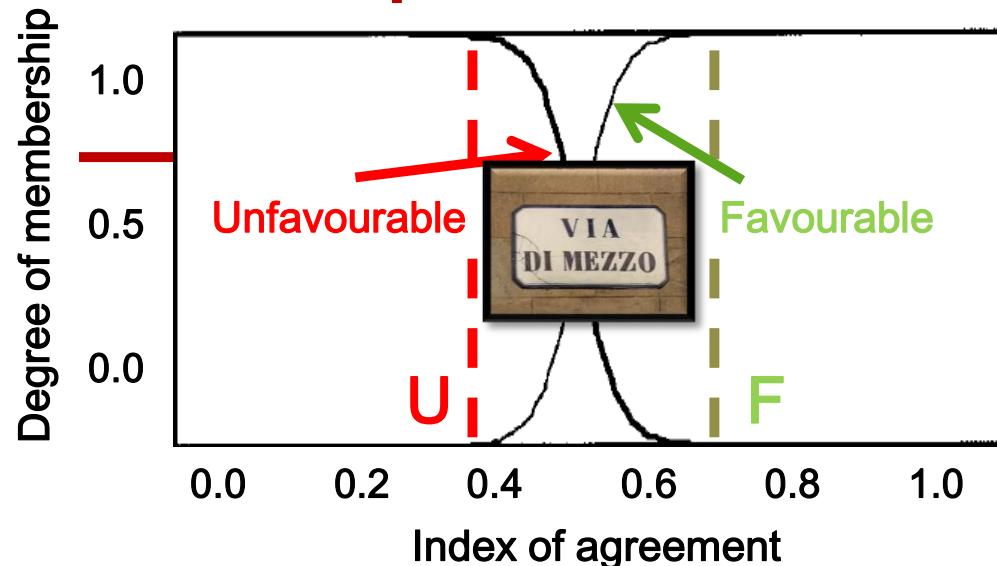
*Hindrances to overcome:  
thresholds and weights*

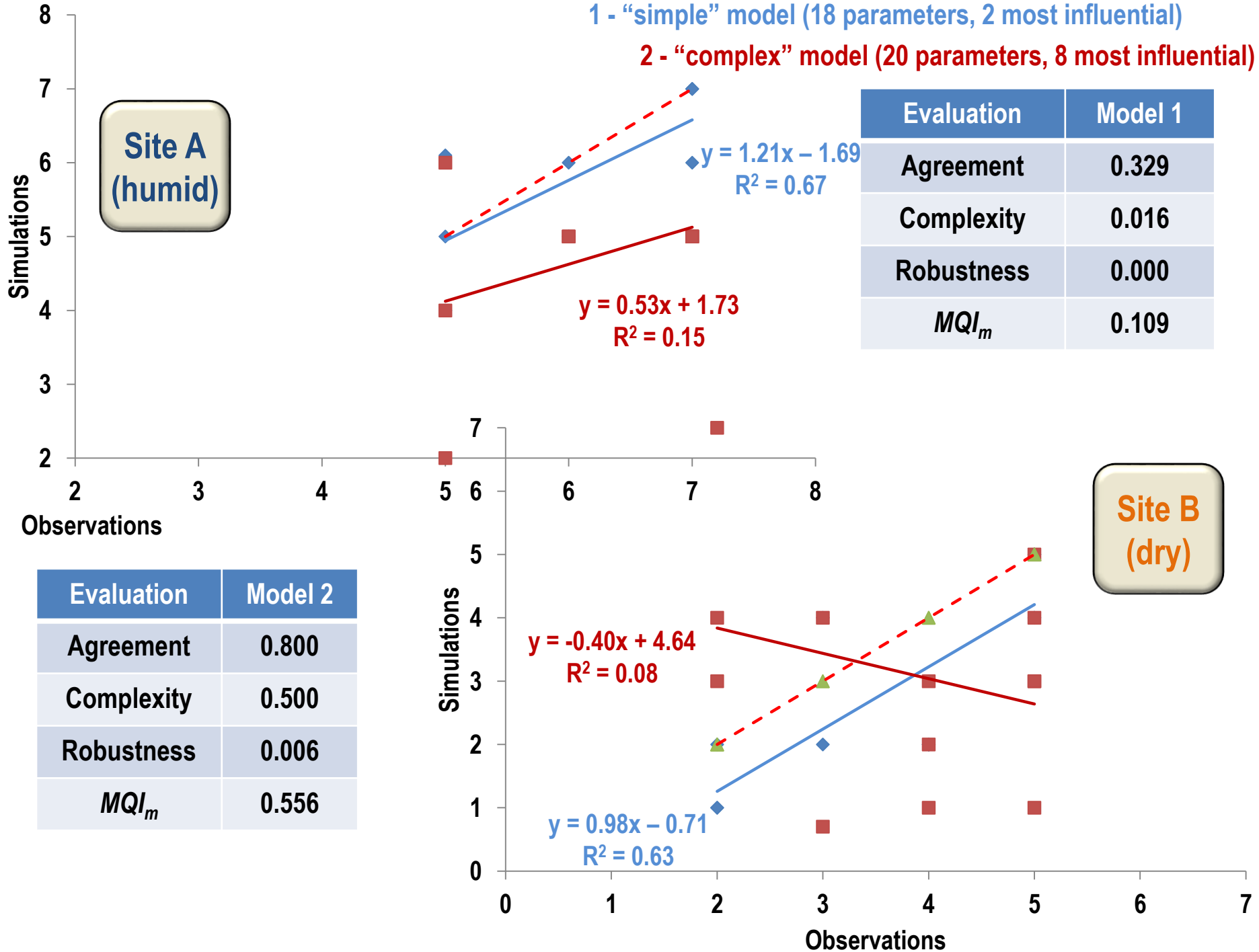
Non-dimensionality

Lower and upper bounding

(best) 0 – 1 (worst)

**Model Quality Indicator**







# Rice simulations: above-ground biomass at maturity

Three models: CropSyst (simple), WARM (intermediate), WOFOST (complex)

$MQI_s$	M1	M2	M3
C. d'Agogna	<b>0.0313</b>	0.1250	0.2174
Vercelli	0.1070	<b>0.0853</b>	0.1372
Mortara	0.2188	<b>0.0000</b>	0.2174
Rosate	<b>0.0313</b>	0.2284	0.2388

$MQI_m$	<b>0.0750</b>	0.1940	0.3356
---------	---------------	--------	--------

$EF$	M1	M2	M3
C. d'Agogna	0.90	0.95	0.93
Vercelli	0.92	0.97	0.96
Mortara	0.96	<b>0.98</b>	<b>0.98</b>
Rosate	0.92	<b>0.62</b>	<b>0.48</b>

$I_R$	<b>0.16</b>	1.24	1.71
-------	-------------	------	------

$MSE$	M1	M2	M3
C. d'Agogna	3.26	<b>1.86</b>	2.42
Vercelli	2.93	<b>1.35</b>	1.57
Mortara	1.66	<b>0.84</b>	0.94
Rosate	<b>0.97</b>	<b>4.96</b>	<b>6.75</b>

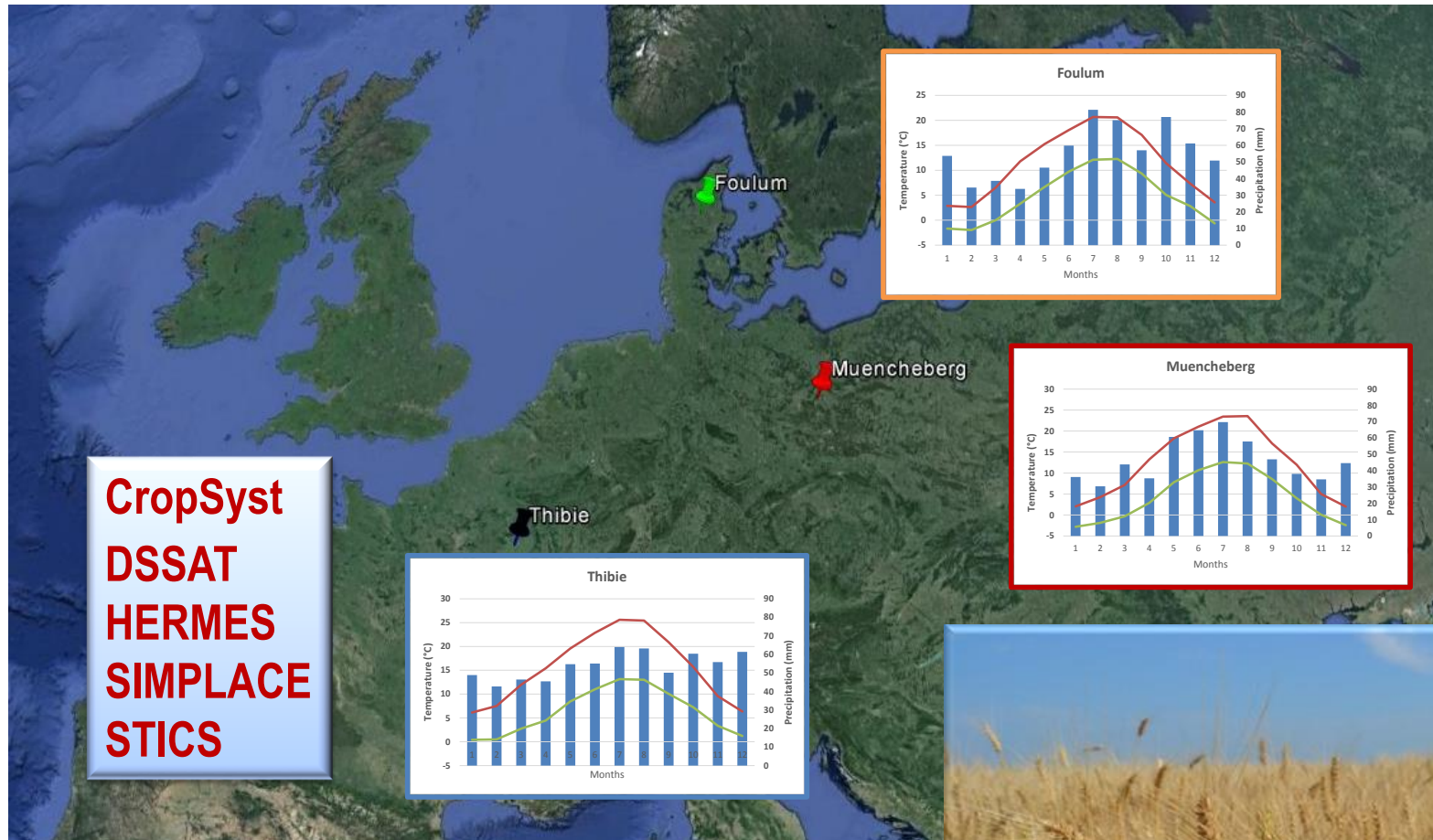
$AIC$	M1	M2	M3
C. d'Agogna	<b>34</b>	37	<b>79</b>
Vercelli	<b>33</b>	34	<b>73</b>
Mortara	<b>26</b>	28	<b>67</b>
Rosate	<b>20</b>	49	<b>91</b>

Complexity

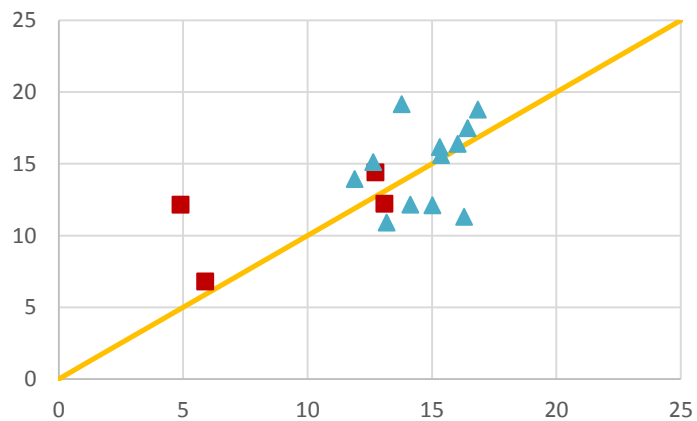
Robustness



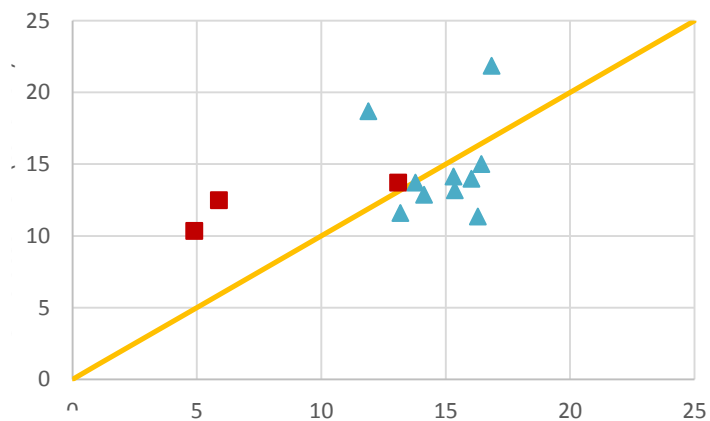
# Wheat simulations: above-ground biomass at maturity



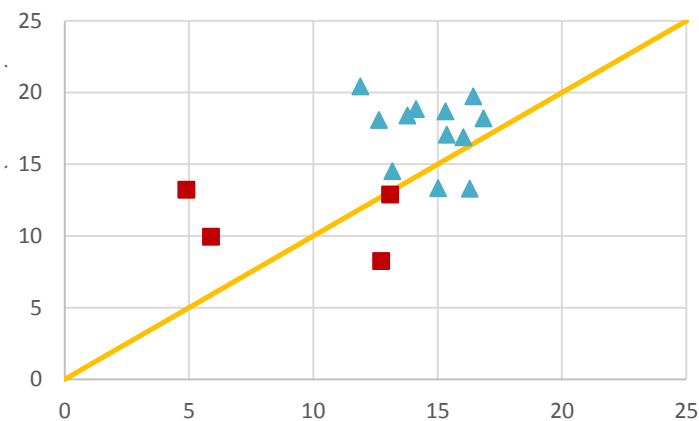
Model M1



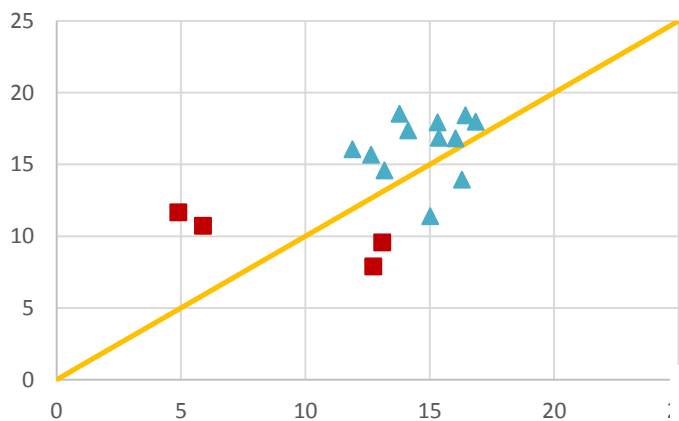
Model M2



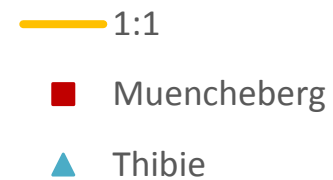
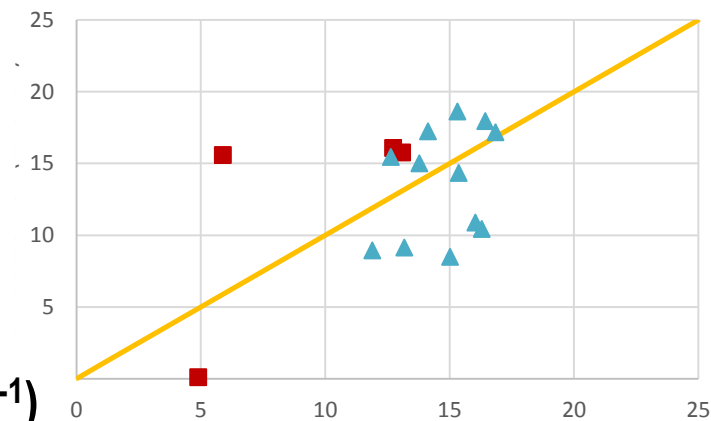
Model M3



Model M4

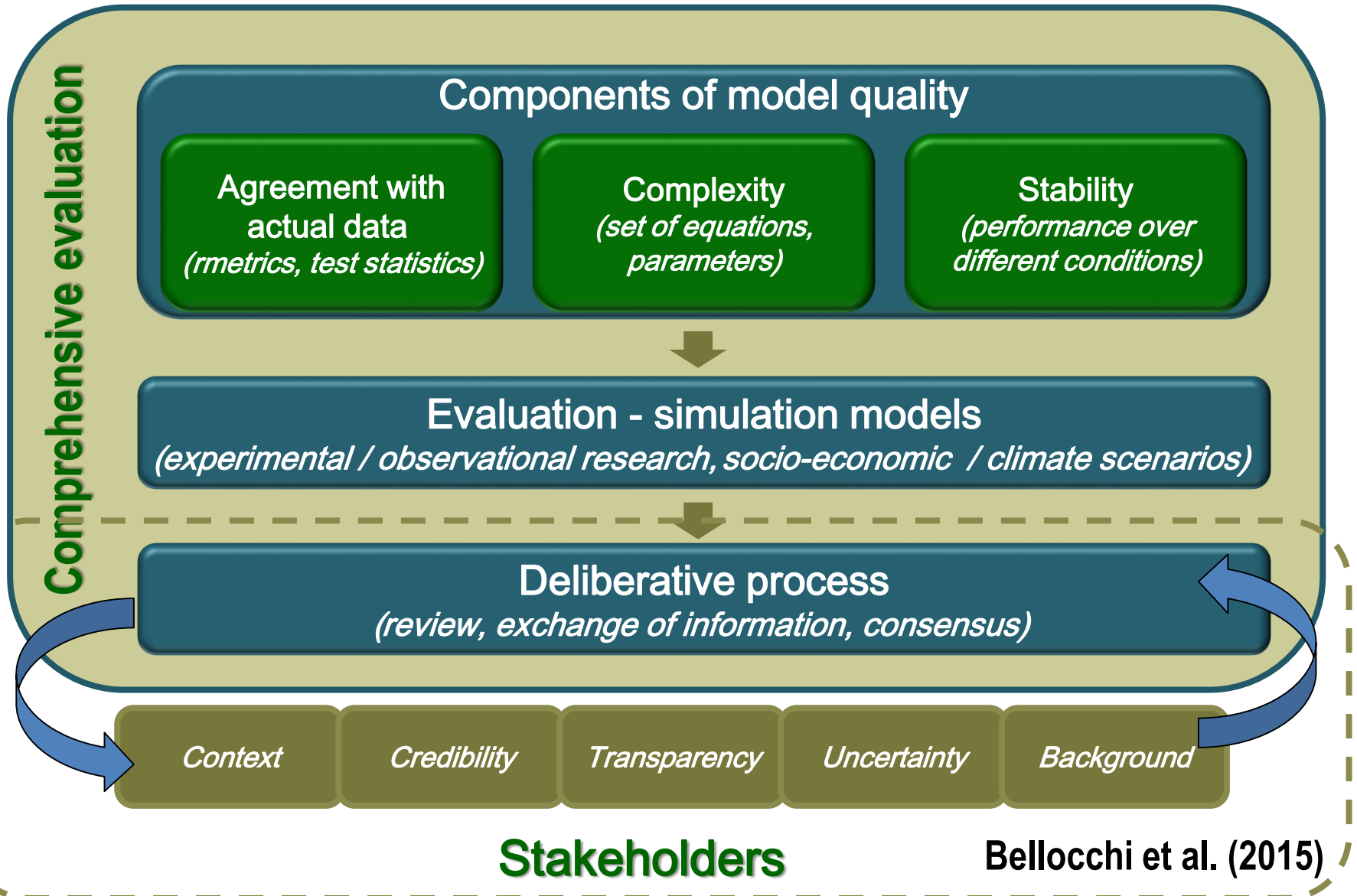


Model M5

Observed AGB (t ha<sup>-1</sup>)Simulated AGB (t ha<sup>-1</sup>)

Model	Aboveground biomass at maturity: performance metrics, modules and indicator					
	$\overline{P(t)}$	$\bar{r}$	$\bar{d}$	$\overline{R_p}$	$\overline{w_k}$	$I_R$
M1	0.23	0.46	0.64	0.32	1.99E-13	65.4
M2	0.20	0.46	0.60	0.28	2.66E-11	6.0
M3	0.01	-0.25	0.70	0.53	0.12	149.5
M4	0.08	-0.36	0.25	0.50	0.88	344.6
M5	0.08	0.49	0.60	0.37	1.34E-08	377.6
	Agreement			Complexity		Robustness
M1		0.8000		0.7975		1.0000
M2		0.8000		0.7975		0.6049
M3		1.0000		1.0000		1.0000
M4		0.8640		0.5000		1.0000
M5		0.8640		0.8944		1.0000
	MQI <sub>m</sub>					
M1	0.8976					
M2	0.7471					
M3	1.0000					
M4	0.8428					
M5	0.9640					

# Model evaluation / deliberative process

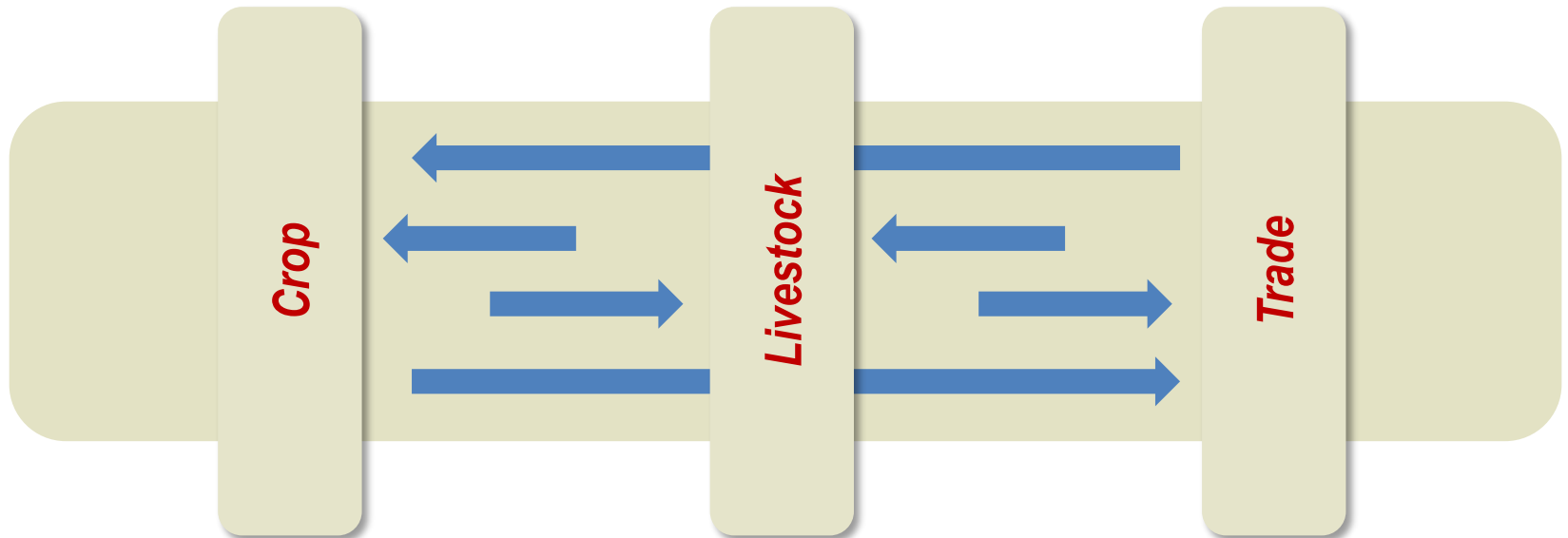


# Towards a consolidated, internationally-agreed protocol to evaluate models: what does go forth?

## ❖ Review of settings

- ❖ Selection of metrics
- ❖ Attribution of thresholds and weights

## ❖ Extension to multiple outputs



# Institutionalising deliberative practices for context-specific model evaluations

Model evaluation(s) are (sometimes) an (important) **orientating landmark** in the skyline of decisions, without replacing them

To evaluate simulation models (in agriculture) is far more urgent as many of the (tactical and strategic) **decisions** (in agriculture) are based on model outcomes

Dealing with (existing) and designing (new) agricultural systems is a priority that deliberations about model evaluation contribute to accomplish in a more efficient (maybe more appropriate) manner, in any case with more **awareness** if (genuine) collective deliberations are possible

The central issue is to think and conceive model evaluation in a (clear) **decisional perspective** about type of model, operability, transparency, etc.

As several models are at hand, **“mod-diversity”** imposes the analysis of case-by-case issues, while also integrating the specific context in a larger-scale perspective (in space and time)

backsliding  
only photo



# Literature sources

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**Schlesinger S., 1979. Terminology for model credibility. Simulation 32, 103-104**



Thank you for your  
attention.

