

A User's Guide for HARK: Heterogeneous Agents Resources and toolKit

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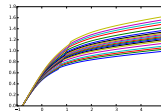
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0.1 Introduction

If you are willing to risk some mild psychological trauma, conjure to mind your first experience of hand-coding a structural economic model. Your clunky effort probably built on legacy code provided by an adviser or colleague – which itself came from who-knows-what apocryphal sources. Efforts to combine elements from one model with those from another were likely frustrated by the “Tower of Babel” problem: Code from one source could not “speak” to code from another without your own intermediation as a translator, possibly between two unfamiliar languages and aided only by oracular comments that, at best, made sense only in the context of other (now missing) code.

After months of effort, you may have had the character-improving experience of proudly explaining to your adviser that not only had you grafted two ideas together, you also found a trick that speeded the solution by an order of magnitude, only to be told that your breathtaking insight had been understood for many years, as reflected in an appendix to a 2008 paper; or, worse, your discovery was something that “everybody knows” but did not exist at all in published form!

Learning by doing has value, but only within limits. We do not require young drivers to design an internal combustion engine before driving a car, nor must graduate students write their own matrix inversion algorithms before running an OLS regression.

In recent years, considerable progress has been made in addressing these kinds of problems in many areas of economic modeling. Macroeconomists using representative agent models can send Dynare model files to each other; reduced form econometricians can choose from a host of econometric packages. But modelers whose questions require explicit structural modeling involving nontrivial kinds of heterogeneity (that is, heterogeneity that cannot simply be aggregated away) are mostly still stuck in the bad old days.

The ultimate goal of the HARK project is to fix these problems. Specifically, our aim is to produce an open source repository of highly modular, easily interoperable code for solving, simulating, and estimating dynamic

economic models with heterogeneous agents.¹ Further, we seek to establish (with input from the community) standards for the description and specification of objects like discrete approximations to continuous distributions and interpolated function approximations, so that numeric methods can be quickly swapped without ugly “patching.”

We hope that HARK will make it much easier and faster for researchers to develop solution and estimation methods for new models. The open source nature of HARK will make it easier for other researchers to audit and verify new models and methods, and to collaborate on correcting deficiencies when found. As HARK expands to include more canonical models and more tools and utilities, we can all spend less time managing numerical minutiae and more time fretting about identification arguments and data accuracy.

0.1.1 Getting Started

If you want to get started using HARK right away, this section provides a very easy quickstart guide for getting HARK up and running on your computer in just a few minutes. More information can be found in the `README.md` file in the HARK repository (step 4), but here is a quick version for those who want to jump right in:

1. **Download Anaconda:** Go to <https://www.anaconda.com/download/> and download Anaconda for your operating system; be sure to get the version for Python 2.7.
2. **Install Anaconda:** Follow the easy instructions on that page to install Anaconda.
3. **Add extra packages:** (optional) If you want to use HARK’s multi-threading feature, you need to add two packages that aren’t part of the default Anaconda distribution. Simply open a command prompt and do `conda install joblib` and `conda install dill`, accepting defaults to install.

¹By “heterogeneous,” we mean that agents might differ before anything in the model has “happened” (*ex-ante* heterogeneity); and agents might experience different stochastic events during the model (*ex-post* heterogeneity).

4. **Download HARK:** Go to <https://github.com/econ-ark/HARK>, the home of the HARK repository. Click on the lime green button labeled “Clone or download” toward the upper right of the main panel, and select “Download ZIP”.²
5. **Unzip HARK:** Unpack the `HARK.zip` file using any archive utility, like `Peazip`. Put the files anywhere you’d like, maintaining the internal directory structure.
6. **Run Spyder:** Open a command prompt and do `spyder`. Spyder is an interactive development environment (IDE) for iPython, a slightly prettier, more interactive flavor of Python.
7. **Open a HARK module:** Go to the directory where you put HARK and open any file with the `.py` extension; we recommend `/Demos/ConsumptionSaving/ConsIndShockModel.py`.
8. **Run the module:** Click on the green arrow “play” button toward the right side of the toolbar of icons at the top of the Spyder window (accept defaults if a dialogue box pops up). Congratulations! HARK is now up and running on your computer.

If you followed our recommendation to try `/Demos/ConsumptionSaving/ConsIndShockModel.py` you should see graphical representations of the solution to a few consumption-saving models with idiosyncratic shocks to permanent and transitory income (see `/Documentation/ConsumptionSavingModels.pdf` for details of these models). If you chose a different module, you might get some examples of some other model, results of a structural estimation, a polite notification that this particular module doesn’t do much on its own, or no output at all. See the `README.md` for a full list of modules from which you can expect non-trivial output.

²This is the fastest way to get HARK running on a computer. Later, if you want to make your own contributions to HARK by adding code (or fixing ours!), you’ll need to clone the repository on your computer. See section 0.5.2 for more.

0.1.2 Structure of HARK

HARK is written in Python, an object-oriented programming (OOP) language that has experienced increasing popularity in the scientific community in the past several years. A significant reason for the adoption of Python is the `numpy` and `scipy` packages, which offer a wide array of mathematical and statistical functions and tools; HARK makes liberal use of these libraries. Python’s object-oriented nature allows models in HARK to be easily extended: more complex models can inherit functions and methods from more fundamental “parent” models, eliminating the need to reproduce or repurpose code.

As implied in the previous section, we strongly encourage HARK users to use the Anaconda distribution of Python, which includes all commonly used mathematical and scientific packages, an interactive development environment for iPython (Spyder), and a package manager that allows users to quickly install or update packages not included in the default distribution (conda).

For users unfamiliar with OOP, we strongly encourage you to review the background material on OOP provided by the good people at [QuantEcon](#) (for more on them, see below) at this link: [Object Oriented Programming](#). Unlike non-OOP languages, OOP bundles together data and functions into *objects*. These can be accessed via: `object_name.data` and `object_name.method_name()`, respectively. For organizational purposes, definitions of multiple objects are stored in *modules*, which are simply files with a `.py` extension. Modules can be accessed in Python via:

```
import module_name as import_name
```

This imports the module and gives it a local name of `import_name`. We can access a function within this module by simply typing: `import_name.function_name()`. The following example will illustrate the usage of these commands. `CRRAutility` is the function object for calculating CRRA utility supplied by `HARK.utilities` module. `CRRAutility` is called *attributes* of the module `HARK.utilities`. In order to calculate CRRA utility with a consumption of 1 and a coefficient of risk

aversion of 2 we run:

```
import HARK.utilities as Hutil
Hutil.CRRAUtility(1,2)
```

Python modules in HARK can generally be categorized into three types: tools, models, and applications. **Tool modules** contain functions and classes with general purpose tools that have no inherent “economic content”, but that can be used in many economic models as building blocks or utilities; they could plausibly be useful in non-economic settings. Tools might include functions for data analysis (e.g. calculating Lorenz shares from data, or constructing a non-parametric kernel regression), functions to create and manipulate discrete approximations to continuous distributions, or classes for constructing interpolated approximations to non-parametric functions. Tool modules generally reside in HARK’s root directory and have names like `HARK.simulation` and `HARK.interpolation`; they do not necessarily do anything when run.

Model modules specify particular economic models, including classes to represent agents in the model (and the “market structure” in which they interact) and functions for solving the “one period problem” of those models. For example, `ConsIndShockModel.py` concerns consumption-saving models in which agents have CRRA utility over consumption and face idiosyncratic shocks to permanent and transitory income. The module includes classes for representing “types” of consumers, along with functions for solving (several flavors of) the one period consumption-saving problem. When run, model modules might demonstrate example specifications of their models, filling in the model parameters with arbitrary values. When `ConsIndShockModel.py` is run, it specifies an infinite horizon consumer with a particular discount factor, permanent income growth rate, coefficient of relative risk aversion (etc), who faces lognormal shocks to permanent and transitory income each period with a particular standard deviation; it then solves this consumer’s

problem and graphically displays the results.³ Model modules generally have `Model` in their name.

Application modules use tool and model modules to solve, simulate, and/or estimate economic models *for a particular purpose*. While tool modules have no particular economic content and model modules describe entire classes of economic models, applications are uses of a model for some research purpose. For example, `/Demos/SolvingMicroDSOPs/StructEstimation.py` uses a consumption-saving model from `ConsIndShockModel.py`, calibrating it with age-dependent sequences of permanent income growth, survival probabilities, and the standard deviation of income shocks (etc); it then estimates the coefficient of relative risk aversion and shifter for an age-varying sequence of discount factors that best fits simulated wealth profiles to empirical data from the Survey of Consumer Finance. A particular application might have multiple modules associated with it, all of which generally reside in one directory.

0.1.3 Other Resources

In the incredibly unlikely scenario in which this document does not fill all of the gaps in your knowledge and answer any questions you might have while reading it, here is a collection of potentially helpful other resources.

- [Online documentation](#) for HARK tool and model modules, produced using Sphinx.
- [A tutorial on Python 2.7](#), straight from the source.
- [Wikipedia article on object-oriented programming](#), not the subject of an edit war.
- [QuantEcon](#), a collection of lectures on quantitative economic modeling from a couple of economists, which definitely in no way influenced HARK whatsoever.

³Running `ConsIndShockModel.py` also demonstrates other variations of the consumption-saving problem, but their description is omitted here for brevity.

- A [tutorial on git](#), the repository management and tracking system used by the HARK project, created by Linus Torvalds.
- A [tutorial on GitHub](#), a website that provides a useful framework for git that makes it significantly more user-friendly, despised by Linus Torvalds.
- [Wikipedia article on Linus Torvalds](#), just in case.
- The [homepage for NumPy](#), a numerical package extensively used by HARK.
- The [homepage for Sphinx](#), a tool for producing HTML documentation.
- A [collection of lecture notes](#) by Chris Carroll, to catch you up on the basics of consumption-saving models.
- A [particular set of lecture notes](#) by Chris Carroll, explaining many of the numeric techniques used in HARK and offering an example of a simple structural model that, in a stunning coincidence, is implemented in HARK as an example.
- A [deep dive](#) into the theoretical foundations of buffer stock saving. Warning: dense.

0.2 General Purpose Tools

This section has been integrated into the [econ-ark documentation](#).

0.3 Microeconomics: the AgentType Class

This section has been integrated into the [econ-ark documentation](#).

0.3.1 Sample Model: Perfect Foresight Consumption-Saving

To provide a concrete example of how the `AgentType` class works, consider the very simple case of a perfect foresight consumption-saving model. The agent has time-separable, additive CRRA preferences over consumption, discounting future utility at a constant rate; he receives a particular stream of labor income each period, and knows the interest rate on assets that he holds from one period to the next. His decision about how much to consume in a particular period can be expressed in Bellman form as:

$$\begin{aligned} V_t(M_t) &= \max_{C_t} u(C_t) + \beta \mathcal{D}_t \mathbb{E}[V_{t+1}(M_{t+1})], \\ A_t &= M_t - C_t, \\ M_{t+1} &= R A_t + Y_{t+1}, \\ Y_{t+1} &= \Gamma_{t+1} Y_t, \\ u(C) &= \frac{C^{1-\rho}}{1-\rho}. \end{aligned}$$

An agent's problem is thus characterized by values of ρ , R , and β plus sequences of survival probabilities \mathcal{D}_t and income growth factors Γ_t for $t = 0, \dots, T$. This problem has an analytical solution for both the value function and the consumption function.

The `ConsIndShockModel` module defines the class `PerfForesightConsumerType` as a subclass of `AgentType` and provides solver functions for several variations of a consumption-saving model, including the perfect foresight problem.⁴ A HARK user could specify and solve a ten period perfect foresight model with the following commands:

```
MyConsumer = PerfForesightConsumerType(time_flow=True, cycles=1,
    CRRA = 2.7, Rfree = 1.03, DiscFac = 0.98,
    LivPrb = [0.99,0.98,0.97,0.96,0.95,0.94,0.93,0.92,0.91,0.90],
    PermGroFac = [1.01,1.01,1.01,1.01,1.01,1.02,1.02,1.02,1.02,1.02],
    Nagents=1000)
MyConsumer.solve()
```

⁴As the name implies, the module is mostly concerned with models with idiosyncratic shocks to income.

The first line makes a new instance of `ConsumerType`, specifying that time is currently “flowing” forward⁵ and that the sequence of periods happens exactly once; the next three lines (all part of the same command) set the time invariant (`CRRA`, `Rfree`, `DiscFac`) and time varying parameters (`LivPrb`, `PermGroFac`). Note that `dir(MyConsumer)` shows all the attributes of `MyConsumer`. After running the `solve` method, `MyConsumer` will have an attribute called `solution`, which will be a list with eleven `ConsumerSolution` objects, representing the period-by-period solution to the model.⁶ Each `ConsumerSolution` has several attributes:

- **cFunc**: Optimal consumption function for this period as a function of (normalized) market resources $m_t = M_t/Y_t$. Can be called like any other function: `MyConsumer.solution[0].cFunc(5)` returns consumption at $m_t = 5$.
- **vFunc**: Value function (over market resources m_t); can be evaluated like `cFunc`.
- **mNrmMin**: Minimum value of normalized market resources m_t such that `cFunc` and `vFunc` are defined.
- **hNrm**: Normalized human wealth– the PDV of future income (ignoring mortality) divided by current period income Y_t .
- **MPC**: The constant marginal propensity to consume (linear consumption function).

The following command generates the plot for the perfect foresight consumption function:

```
mMin = MyConsumer.solution[0].mNrmMin
plotFuncs(MyConsumer.solution[0].cFunc, mMin, mMin+10)
```

To solve a version of this problem in which the sequence of ten periods happens three times (yielding a `solution` attribute with thirty-one elements), the user can do:

⁵This is relevant for the interpretation of the time-varying inputs `LivPrb` and `PermGroFac`.

⁶The last element of `solution` represents the terminal period solution, where the agent consumes all available resources because there is no future.

```
MyConsumer(cycles = 3)
MyConsumer.solve()
```

To solve an infinite horizon problem in which the agent experiences the same one period problem indefinitely, the user can do:

```
OtherConsumer = PerfForesightConsumerType(cycles=0, CRRA=3.5,
Rfree=1.02,
DiscFac=0.95, LivPrb = [0.99], PermGroFac = [1.01], Nagents=1000)
OtherConsumer.solve()
```

This instance is specified as being infinite horizon by setting `cycles=0`. Note that the time-varying inputs are still specified as (one element) lists, even though they take on the same value in every period; this is because an infinite horizon model might consist of a multi-period sequence repeated indefinitely, rather than just one repeated period. The `solution` attribute of `OtherConsumer` will be a list containing one instance of `ConsumerSolution`, representing the solution to every period of the model.

0.4 Macroeconomics: the Market Class

This section has been integrated into the [econ-ark documentation](#).

0.4.1 Sample Model: FashionVictim

To illustrate the `Market` class, consider a simple example in the emerging economic subfield of aesthemetrics, the `FashionVictimModel`.⁷⁸ This module defines a subclass of `AgentType` called `FashionVictimType`. Each period, fashion victims make a binary choice of style *s*: to dress as a jock (0) or punk (1). They receive utility directly from the outfit they wear and as a function of the proportion of the population who *just wore* the same style;

⁷This model is inspired by the paper “The hipster effect: When anticonformists all look the same” by Jonathan Touboul.

⁸For a more traditional macroeconomic model, the `ConsAggShocksModel` module includes a consumption-saving model with both idiosyncratic and aggregate shocks, in which individual asset holdings are aggregated into total productive capital, endogenizing the (dynamic) interest and wage rate.

they also pay switching costs (c_{pj}, c_{jp}) if they change styles rather than keep the same as the previous period. Moreover, they receive an idiosyncratic type 1 extreme value (T1EV) preference shock to each style in each period. Defining the population punk proportion as p and the conformity utility function as $f : [0, 1] \rightarrow \mathbb{R}$, the current period utility function is thus:

$$u(s_t; s_{t-1}, p_t) = s_t f(p_t) + (1-s_t) f(1-p_t) + s_t U_p + (1-s_t) U_j - c_{pj} s_{t-1} (1-s_t) - c_{jp} (1-s_{t-1}) s_t.$$

Fashion victims are forward looking and discount future utility at a constant rate of β per period. To simplify the analysis, we assume they believe that the population punk proportion in the next period is a linear function of the punk proportion in the current period, subject to a uniformly distributed shock. No restrictions are put on the function f ; fashion victims might be conformists who like to dress the same as others ($f'(p) > 0$) or hipsters who like to style themselves in the minority ($f'(p) < 0$).⁹ A fashion victim’s problem can be written in Bellman form as:

$$V(s_{t-1}, p_t) = \mathbb{E} \left[\max_{s_t \in \{0,1\}} u(s_t; s_{t-1}, p_t) + \eta_{s_t} + \beta \mathbb{E} [V(s_t, p_{t+1})] \right],$$

$$p_{t+1} = ap_t + b + \pi_{t+1}, \quad \pi_{t+1} \sim U[-w, w], \quad \eta_0, \eta_1 \sim T1EV.$$

An instance of `FashionVictimType` is thus characterized by values of U_p , U_j , c_{pj} , c_{jp} and a function f , as well as beliefs about p_{t+1} as a function of p_t (summarized by slope a , intercept b , and uniform shock width w). Given this information, a `FashionVictimType`’s infinite horizon microeconomic model can be solved by backward induction in a few lines; the “one period solver” is given by `solveFashion`. However, while individual agents treat the dynamics of p_t as exogenous, they are in fact endogenously determined by the actions of all the fashion victims in the market.¹⁰ A dynamic general equilibrium of the “macroeconomic fashion model” is thus characterized by a triple of (a, b, w) such that when fashion victims believe in this “punk evolution rule” and act optimally, their collective fashion choices exhibit this same rule when the model is simulated.

⁹In practice, f is parameterized as the beta distribution for convenience.

¹⁰The market might consist of agents all of the same type, or might have several types with *ex-ante* heterogeneity.

The search for a dynamic general equilibrium is implemented in HARK's `Market` class with the following definitions:

```
sow_vars = ['pNow'] (macroeconomic outcome is  $p_t$ )
reap_vars = ['sNow'] (microeconomic outcomes are  $s_t$  for many agents)
track_vars = ['pNow'] (must track history of  $p_t$ )
dyn_vars = ['pNextSlope', 'pNextIntercept', 'pNextWidth']
(dynamic rule  $(a, b, w)$ )
millRule = calcPunkProp (aggregate process: average the style choices of
all agents)
calcDynamics = calcFashionEvoFunc (calculate new  $(a, b, w)$  with au-
toregression of  $p_t$ )
act_T = 1000 (simulate 1000 periods of the fashion market)
tolerance = 0.01 (terminate solution when  $(a, b, w)$  changes by less than
0.01)
```

The `agents` attribute has a list of 22 `FashionVictimTypes`, which vary in their values of U_p and U_j , and their f functions. The `marketAction` method of `FashionVictimType` simulates one period of the microeconomic model: each agent receives style preference shocks η_0 and η_1 , sees the current proportion of punks p_t (sown to them as `pNow`), and chooses which style to wear, storing it in the binary array `sNow`, an attribute of `self`.

The `millRule` for this market is extremely simple: it flattens the list of binary arrays of individual style choices (gathered in the `reap` step) and averages them into a new value of p_t , to be tracked as a history and `sown` back to the `agents` to begin the cycle again. Once a history of 1000 values of p_t has been generated with the `makeHistory` method, we can calculate a new dynamic fashion rule with `calcFashionEvoFunc` by regressing p_t on p_{t-1} , approximating w as twice the standard deviation of prediction errors.¹¹ The new fashion rule is an instance of the simple `FashionEvoFunc` class, whose only methods are inherited from `HARKObject`.

When the `solve` method is run, the solver successively solves each agent's microeconomic problem, runs the `makeHistory` method to generate a 1000 period history of p_t , and calculates a new punk evolution rule based on this

¹¹This is an arbitrary way to calculate w , but accuracy is not important in a silly example.

history; the solver terminates when consecutive rules differ by less than 0.01 in any dimension.

0.5 Contributing to HARK

This section provides an overview of how users can contribute new code to HARK, what sort of contributions are most desired, and style conventions for the toolKit. Before attempting to extend HARK, we strongly recommend that you familiarize yourself with its features and models by looking at the source code.

0.5.1 What Does HARK Want?

The easiest and most straightforward way to contribute to HARK is by writing new general purpose tools for inclusion in one of the top-level modules. This might be a commonly known data analysis technique (e.g. a kernel density estimator) for `HARK.utilities`, an optimization method (local or global) for `HARK.estimate`, an interpolation method for `HARK.interpolate`, etc. If you've found a technique useful in your own research and believe it could be of use to others on entirely different projects, then it probably belongs in HARK. Likewise, if you read through a HARK module expecting to find a certain tool or function (because of similar functions that are present, or merely because *it's very useful*) but don't, this is a good sign that HARK has a hole that you can fill.¹²

Secondly, the development team wants to expand HARK to include more canonical models. Most of the models available in the toolKit at the time of its public beta release concern agents with (geometrically discounted) CRRA utility over a unitary consumption good, who receive permanent and transitory shocks to income and have access to a single risk free asset. This is an important class of models, but that description has an awful lot of qualifiers. In short, there are many more common features of dynamic

¹²Case in point: As of this moment, `HARK.utilities` has no function for making a discrete approximation to the normal distribution, even though there are several well known methods for doing so and it is an obviously useful function.

household models that are not yet in HARK, but would be very valuable for the toolKit. New model contributions should “play nicely” with existing models and tools, following HARK style guidelines (see sections 5.4 and 5.5) to the greatest extent possible. For ideas of potential model extensions for HARK, see section 0.6.2.¹³

Finally, contributions to HARK are not restricted to entirely new functionality. While we have done our best to provide flexible frameworks and useful tools, we have almost certainly overlooked an unexpected case that would not be (properly) handled by the toolKit as is. Moreover, there might even be flaws in our solution or simulation methods. If you find a mistake or error, we strongly encourage you to contribute a fix for the problem, or at least to flag it as an Issue on GitHub so that someone else might. The “mistake” you find might not even be in the code itself, but a deficiency in the documentation: a misnamed (or incorrectly typed) parameter or return variable in the docstring, an incorrect (or missing) comment, even a grammatical or spelling error. No matter how niggling, we want your fix.

For those who want to contribute to the HARK project without programming a new model or digging through the code for errors and omissions, consider reading through the Issues page on GitHub to see what other users have flagged for development. You might find several pieces of “low hanging fruit” for you to quickly fix.

0.5.2 Git and GitHub

Git is a distributed version control system that has gained increasing popularity in the decade since its creation; it is designed to enable collaboration and “non-linear workflow” among a (potentially disperse) programming team. As HARK is to be developed by volunteer researchers all around the world, git is an excellent fit for the toolKit. Originally designed by Linus Torvalds as a command line tool, others have since extended git with further functionality and a user interface more friendly to those more familiar with GUIs. Foremost among these tools is GitHub.com, where the HARK project

¹³Although that list is limited to extensions and variations on consumption-saving models, HARK has no such restrictions. If there is an entirely different sort of dynamic model that fits in the HARK framework, it can be contributed.

is hosted. This section provides a brief overview of how to use GitHub to interact with (and potentially contribute to) HARK.

To prepare to contribute to HARK, follow these simple steps:

1. **Make a GitHub account:** Go to github.com; the homepage should prompt you to choose a username and password. Signing up is quick, easy, and free.¹⁴
2. **Install GitHub Desktop:** Go to desktop.github.com and download the Desktop application for your operating system, then install it. After opening Desktop for the first time, enter your GitHub login to connect it to your account.
3. **Fork the HARK repository:** Go to the [HARK repository page](#), click on the Fork button in the upper right, and choose to fork HARK to your own GitHub account. This creates a new repository identical to the one hosted by Econ-Ark at the moment you fork it, but hosted on your account instead.
4. **Add the repository to Desktop:** Open GitHub Desktop, click on the + icon in the upper left, and select clone. Find the repository named `yourusername/HARK`, click the Clone button at the bottom of the dialogue window, and choose a directory on your local machine.

You now control a “fork” of the main HARK repository, hosted by GitHub, and have a clone of this fork on your local machine. You are free to edit your fork of HARK in any way you’d like; other GitHub users can view your fork (and fork it themselves), but they cannot make changes to your fork unless you give them permission by adding them as a contributor. Changes made to the local copy of your fork do not get automatically sent to the remote copy on GitHub for public viewing. To make changes to your fork on GitHub, follow these steps:

1. **Make local changes:** Edit your local copy of the repository in any way you’d like: add or delete lines from existing files; add, delete, or rename entire files or directories.

¹⁴There are non-free ways to sign up for GitHub, but you don’t need to worry about them.

2. **Commit local changes:** Open the repository in GitHub Desktop and click on the Changes tab. In the lower left, provide a short description of the changes made in the Summary field, and (optionally) longer comments about these changes in the Description field. Click the check-mark Commit button.
3. **Push the commit:** Click on the Sync button near the upper right to “push” your local commits to the remote server; this will also pull down remote commits from other contributors to your fork that were made since the last time you synced.

The left hand panel of the Changes tab has a summary of the files that have been changed, added, or removed since your last commit; the right hand panel shows the specific changes made to each changed file. After step 2, a record of your changes has been stored locally by the git system, but is not yet reflected in the public remote copy on GitHub.¹⁵ The “timeline” summary of the repository at the top of the Desktop window shows the history of commits for the repository: each dot represents a commit that was pushed to the remote server, and each open ring represents a local commit that has not been pushed to the remote server; the large broken ring on the far right represents changes that have not been locally committed.¹⁶ The History tab lists all previous commits, including the timestamp, contributor, and a record of changes made.

Suppose you have mucked about in your fork for a while and have made changes to HARK that you think should be included in the main repository hosted by Econ-Ark. To make your dream a reality, follow these steps:

1. **Isolate the changes:** If you mucked around for quite a while, making various changes here and there, and then later made some contribution that you want to include in the main repository, you should *isolate the desired changes in a new branch of your fork*. Make a new branch by clicking the button toward the upper left of GitHub Desktop, revert that branch to the commit just before you forked from the main

¹⁵You can make several local commits without syncing with the remote server. This is useful for working without an internet connection. Say, on an intercontinental flight.

¹⁶Clicking on a dot or ring will display the changes made in that commit (or uncommitted changes).

repository,¹⁷ then edit this branch to include *only the changes you want to push to the main repository*.

2. **Issue a pull request:** Go to **HARK's GitHub page** and click the “New pull request” button. Click the text that says “compare across forks”, and select **econ-ark/HARK** as the base fork, **master** as the base, your fork as the head fork, and the branch to be merged as the “compare”. In the boxes below, give a name to your pull request and provide sufficient comments about your contribution so that a development team member can understand what you’ve done. Click the “Create pull request” button.
3. **Be patient:** Someone from the development team will look at your contribution and either merge it into the main repository or return it with comments. See section 0.5.3 for procedures followed by the HARK team when evaluating outside contributions.

0.5.3 Submission Approval Process

Before submitting to HARK, the development team would like you to make sure that your intended contribution is listed as an Issue on the GitHub page. If you are going to fix or address an Issue that is already posted, reply to that post with a note indicating that you are about to work on it and an estimate of when you will make a pull request for it. If you want to do something that no one has mentioned yet as an Issue, make a new Issue on GitHub (briefly) describing what you intend to do.¹⁸ This will both help prevent two people from working on the same thing (and one of them potentially wasting time on it), and lets the development team know what’s coming. Moreover, if you propose a contribution that is (a) already in HARK, (b) not in the spirit of HARK, or (c) a fix for something that’s not actually broken, this gives the team a chance to let you know not to spend effort on it.

¹⁷Or since your last update from the main repository hosted by Econ-Ark.

¹⁸If your contribution is a tiny adjustment or to fix/add some documentation or comments, you shouldn’t make an Issue.

After creating a pull request to submit your contribution, it will be evaluated by one or more members of the HARK team. Criteria that the HARK team will consider when choosing whether to accept a submission include:

1. **Does the contribution break previous code?** If you change or expand an existing function, you should make sure that this does not cause some models or applications to work incorrectly. In the near future, HARK will have a core set of tests to run to check for full compatibility.
2. **Is the code well documented?** Code submissions should have properly formatted docstrings for each new function, class, method, and module (see section 0.5.5) and enough comments for a reader to follow the algorithm.
3. **Is the contribution relevant?** The development team intends for HARK to be diverse, but not everything goes in HARK. If your submission concerns a representative agent model or a method for estimating a reduced form model, then it probably doesn't belong in HARK.
4. **Is the code demonstrated with an example?** If you solve a new model in HARK, you should include a set of example parameters for other users to easily test. If you've contributed a new function, consider providing a snippet of code demonstrating its use.¹⁹
5. **Is the code correct?** Your code should actually do what it claims to do.
6. **Does the code use HARK conventions?** To the best of your ability, contributions to HARK should follow the style guidelines in section 0.5.4. We don't demand perfection, as these are guidelines rather than rules.

¹⁹In the future, HARK will make use of in-line testing.

7. **Is the code well integrated in HARK?** In the beta release of HARK, we have tried to present a “taxonomy” of consumption-saving models that build up from each other. When possible, new models in HARK should try to continue this pattern. A submission that introduces a model in a new module that could have easily been made as an extension of an existing module might be rejected. However, we acknowledge that there is value in providing a solver for a new model, and that a future contributor might make her mark by integrating it into the existing hierarchy.
8. **Is this already in HARK?** If your contribution is already in HARK, then it will almost certainly be rejected. Of course, if you submit a version that dominates the existing implementation (or even one that works better in a well described, non-trivial set of circumstances), it belongs in HARK.

The HARK team intends to release more specific guidelines in the near future, so that contributors are better able to judge their submissions before issuing a pull request. We are in the process of recruiting “czars” to oversee particular aspects of HARK, providing their knowledge and expertise.²⁰ While czars might directly evaluate submissions as a HARK team member, their more important role is to help establish these guidelines for their domain, more specifically nailing down what we mean by “correct” or “well integrated”.

0.5.4 Naming Conventions

Object naming conventions in HARK are fairly different than existing standards, and differ somewhat between tool modules vs model or application modules. The following conventions apply throughout HARK:

- Functions and methods are always in “camel case”: no underscores, first letter is lower case, first letter of each subsequent word is capitalized. E.g. `approxLognormal`.

²⁰If you have knowledge and/or expertise and would like to contribute as a czar, please contact a HARK team member so that we can judge your credentials even though we have way less expertise.

- Function and method names should accurately and concisely describe what the function does; the first word in the name *must be a verb*.²¹
- Variable and class names *should not* have a verb as their first word.
- Class names should use no underscores and capitalize the first letter of each word; moreover, a class name *must include a noun*. E.g. `ConsPerfForesightSolver`.

When naming variables in model modules, the HARK team strongly discourages using single letter names, like `c` for consumption. Instead, we encourage contributors to use longer, more descriptive variable names using additional words and common abbreviations to specify the variable more precisely. In `/Documentation/MARK.pdf`, we list standard single letter variable “bases” and an array of prefixes and suffixes to adjust them. Economic variables in model modules should (usually) not use underscores, instead using camel case to the greatest extent possible.²² The development team prefers this standard so that users can translate between Python code and LaTeX script with minimal work.

Conventions for naming variables in HARK’s tool modules are significantly closer to more commonly used standards. Variable names should be in all lower case, with underscores between words, e.g. `data_to_match`. The functions and classes in these modules are more general and almost surely do not have any inherent “economic content”; they are numerical or algorithmic objects, not variables that might appear in an equation in an article for a (non-computational) economics journal. Variable names in application modules (e.g. the files that execute the `cstwMPC` estimations) are a mix of the conventions for tool and model files, as appropriate for each variable. That is, variables that are directly related to “economic variables” in model modules should follow those conventions, while objects created solely for data manipulation or reporting should use the style of tool modules.

²¹HARK standards have specified several “keyword verbs” that have specific meaning.

²²For “non-economic” variables that are only used temporarily, underscores are permissible.

0.5.5 Documentation Conventions

The HARK team wants the toolKit to be as accessible to users as possible; our greatest fear²³ is that a new user will open up our code, get hopelessly confused trying to read it, and then never look at HARK again. To prevent this tragic outcome, we have tried hard to provide comprehensive, accurate documentation and comments within the code describing our methods.²⁴ Moreover, HARK uses the Sphinx utility to generate a website with [online documentation](#) for all of our tool and model modules, so that users can learn about what's available in HARK without digging through the source code. When making contributions to HARK, the development team asks users to format their inline documentation to work with Sphinx by following a few simple rules.

- The top of every module should begin with a “docstring” providing a clear description of the contents of the module. The first sentence should concisely summarize the file, as it may appear in an index or summary of all modules without the remaining sentences. A docstring at the top of a module should be formatted as:²⁵

```
"""
```

```
Specifies an economic model and provides methods for  
solving it. More specific description of the key features  
of the model and variations of it in this module. Maybe  
some comments about the solution method or limitations of  
the model. Your bank account routing number.
```

```
"""
```

- The line directly below the declaration of a function, method or class should begin a docstring describing that object. As with modules, the first sentence should concisely summarize the function or class,

²³Other than spiders, of course.

²⁴To the extent that documentation and comments are missing, we encourage users to rectify this in their contributions.

²⁵The triple quote to begin and end a docstring can use either the apostrophe ' or quotations marks ".

as it might be included in an index or summary. For functions and methods, the docstring should be formatted as:

```
def functionName(input1,input2):
    """
        Concise description of the function. More details
        about what
            the function does, options or modes available, and
        maybe mathematical
            methods used. Credit to a source if you poached
        their algorithm.

        Parameters
        -----
        input1:  type
            Description of what input1 represents.
        input2:  type
            Description of what input2 represents.

        Returns
        -----
        output_name:  type
            Description of the output(s) of the function.
    Might have
        multiple entries. If no output, this is just
        "None".
    """
```

- Provide ample comments within a function or method so that a relatively intelligent reader can follow along with your algorithm. Short

comments can follow at the end of a line, longer comments (or descriptions of the step or task about to be performed) should precede a block of code on the line(s) above it.

Finally, if you write a new model module, the HARK team asks that you also provide a short mathematical writeup of the model as a PDF. This document does not need to go into great detail about the solution method for the model or the functions and classes included in the module, merely specify the economic model and provide a summary of how it is solved. See [/Documentation/ConsumptionSavingModels.pdf](#) for an example of this.

0.6 Future of HARK

HARK is in a state of perpetual incompleteness, always expanding to include more tools and more models. As an open source project in the hands of many contributors around the world, the HARK team cannot fully predict future features of the toolKit. This section provides an overview of what we would like to see in the near future, as well as potential mechanisms to encourage researchers to contribute their code to the project.

0.6.1 Future Tools

The current frameworks in `HARK.core` concern agents who have “isolated” dynamic problems or interact with each other only through aggregate outcomes to which they contribute atomically. We hope to eventually provide a framework for models in which agents directly interact with each other; this may include a system for specifying the state of networks and how connections are formed and broken. `HARK.core` might also develop a framework more suited to industrial organization models and dynamic games.²⁶

The `HARK.estimation` module in particular is very sparsely populated, with its functions mostly serving as wrappers for “off the shelf” optimization methods from `scipy.optimize`. There are plenty of non-standard or more

²⁶It might already be possible to shoehorn some of these models into the `Market` framework.

complex optimization techniques available, including global and/or stochastic search methods. We believe that additional optimizers are “low hanging fruit” as straightforward contributions to HARK and thus will be added in the near future. Moreover, there are plenty of distributions that have no approximator in `HARK.utilities` (or data generator in `HARK.simulation`), and these functions are among the easiest for new contributors to write. The data analysis tools in `HARK.utilities` only include functions that we happened to use for our current research projects, and we expect that this will be the mode of growth for future tools. There are some obvious holes that we believe will be filled quite quickly; for example, we provide a rudimentary non-parametric kernel regression function, but have not written a kernel density estimator to generate PDFs from data.

The classes currently in `HARK.interpolation` are all variations on linear (or cubic) spline interpolation, and each is specifically written for a fixed number of dimensions. As these methods use full tensor grids, they are highly impractical for representing functions in higher dimensions, suffering greatly from the curse of dimensionality.²⁷ We are quite confident that `HARK.interpolation` will soon include techniques more applicable to high dimensional state spaces, including Smolnyak interpolation, other (adaptive) sparse grid methods, and regression-based interpolation. For lower-dimensional spaces, HARK will also soon provide Delaunay interpolation classes.

The `HARK.parallel` module currently provides a simple interface for handling *ex-ante* heterogeneity among agents. While useful for speeding up moderately-sized problems, the libraries used are only able to access the CPU of the local machine running the code. In the very near future, the HARK team will provide an interface (and example) for using Apache Spark, which bills itself as a “fast and general engine for large-scale data processing”. Specifically, users will be able to easily scale up their computing resources and run HARK code on an Amazon EC2 session or other cluster.

²⁷The HARK team only included interpolators for up to 4 dimensions, and some would argue this is already too many for tensor grid methods.

0.6.2 Future Models

The economics models currently included in HARK mostly concern consumption-saving problems with constant relative risk aversion consumers who experience fully permanent and fully transitory shocks to income. This is obviously a very small subset of all consumption-saving models (which are themselves a small subset of all dynamic models economists might be interested in). Consider some examples of variants, features, and extensions that are not included in HARK, but could be in the future:

- Consumers with other utility functions, such as CARA or expo-power.
- Consumers with time-inconsistent preferences, e.g. hyperbolic discounting.
- Income shocks that are neither fully transitory nor fully permanent.
- Consumers with a bequest motive or terminal utility function.
- Utility from leisure and endogenous labor supply.
- Investment in a durable consumption good such as housing.
- Exogenous shocks to expenses.
- Multiple consumption goods, as with endogenous medical care.
- Portfolio allocation between a risky and riskless asset.
- Job search intensity as a control variable.
- Endogenous health evolution and health investment.

The HARK team is currently developing a module for mixing discrete and continuous choice models, in the style of Jorgensen, Rust, Iskakov, and Schjerning (2015). Among many other models, this framework will enable HARK users to easily develop features like:

- Labor supply on the extensive margin: the timing of retirement.

- Selection of job type or sector (by riskiness, specific human capital, etc).
- Choice of medical insurance contract.
- Decision to rent or own housing.
- Endogenous default on debt (with “macroeconomic” pricing of debt).
- Household formation, dissolution, and reproduction.

Finally, we hope to provide a generic solver for any discrete choice model with T1EV shocks. The scope of HARK is limited only by what users choose to put in it. We hope that within a year of its debut, HARK will include a significant number of canonical models, providing more building blocks for future researchers to create novel combinations and new extensions.

0.6.3 Bounty Hunting

While HARK users are free to write and contribute any tools and models that they believe could be helpful, building the toolKit in a “bottom up” style, the HARK team hopes to provide mechanisms for targeted “top down” development. The team is working to secure grant funding for HARK so as to offer “bounties” for particular models, tools, applications, or frameworks. Suppose the team decides that the model in Important Paper X should be included as part of HARK; we will issue a call for contributions to fill this hole, offering a modest prize of, say, \$20,000 to the programmer who submits the best implementation of the model, as judged by clearly stated criteria.²⁸ The bounty would be announced as an Issue on HARK’s GitHub page, as well as in a potential electronic digest of HARK news.

Bounties might be placed on items as small as a single data analysis tool or as large as a complex estimation of a large general equilibrium model, with prizes scaling accordingly. We hasten to emphasize that we cannot guarantee funding for HARK, so the bounties (like everything else in this section) are purely speculative. As economists, the HARK team understands

²⁸Actual bounties may be significantly smaller than this. But be honest: You’re much more interested in contributing to HARK after reading that sentence.

the incentive compatibility problems associated with asking researchers to contribute significant amounts of their time, effort, and unique skills in service of a tenuous concept like the Greater Good in exchange for even more tenuous Glory. We acknowledge that economic researchers are also optimizing agents with their own preferences over leisure and consumption, and agree that Greed is a valid mechanism to expand HARK.

0.6.4 All Aboard the Ark

As observant readers may have noticed, the HARK repository is hosted by a GitHub account named Econ-Ark, with no explanation as to what this might mean. Looking a few years into the future, the development team believes that HARK might be the first piece of a broader collection of computational economics resources. HARK is open source but somewhat akin to an exclusive club: contributions are required to adhere to standards and norms so as to foster modularity and interoperability among models and tools. Consistent with its namesake ship, the Econ-Ark has a significantly lower bar for admission, with a place on board for everything.

On one level, the Ark might serve as a warehouse for any and all quantitative models and tools, for any economic purpose, in any subfield, and written in any language. Through nearly unanimous feedback, the HARK team understands that many economists are willing to share code that they have already written, but are reluctant to expend the considerable effort to translate and format it for HARK. In the future, we will set up a mechanism for code like this to be hosted on the Ark, with minimal requirements imposed on its authors (and correspondingly minimal warranty for potential users). Relevant projects on the Ark might become bounty targets for HARK, with users incentivized to port the original code into Python and to meet HARK standards; direct access to the original source code will significantly expedite the translation process, and provide a suitable benchmark for testing and verifying the contribution to HARK.

On a different level, the Ark might also include cohesive toolkits like HARK, but geared toward purposes other than heterogeneous agents macroeconomics models. For example, the previously mentioned modules for networks among agents (and other agent-based modeling), industrial

organization and dynamic games, and traditional discrete choice models might become their own toolkits, with some interoperability with HARK. In support of this, some of the tool modules currently in HARK might be “promoted” and become universally shared across all Econ-Ark toolkits.

The dark secret of HARK is that it is named for heterogeneous agents macroeconomics, but designed and written by structural microeconomists. The development team believes these subfields to have considerable overlap in terms of methods and techniques, and that HARK might not be noticed by half of its potential audience due to its name. In a general sense, the Econ-Ark gives us cover to expand the scope of our efforts and/or rebrand the toolKit for an alternative audience.