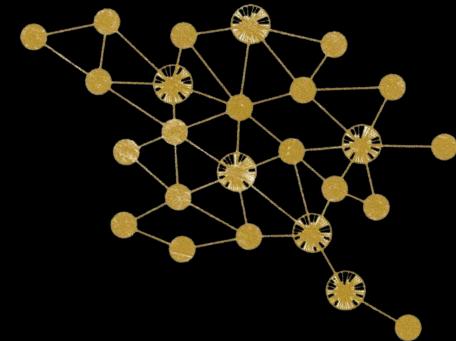


# Multilayer ecological networks

Sonia Kéfi



SANTA FE  
INSTITUTE



Institut des Sciences de l'Evolution-Montpellier

# Black out : ce 28 septembre 2003, l'Italie plonge dans l'obscurité

Le pays ayant abandonné le nucléaire en 1987 est alors jugé trop dépendant de ses importations électriques.  
Depuis, il a misé sur les énergies renouvelables

Temps de lecture estimé : 1 minute

Publié le 12 décembre 2016 à 17:48 - Maj 24 octobre 2021 à 20:49



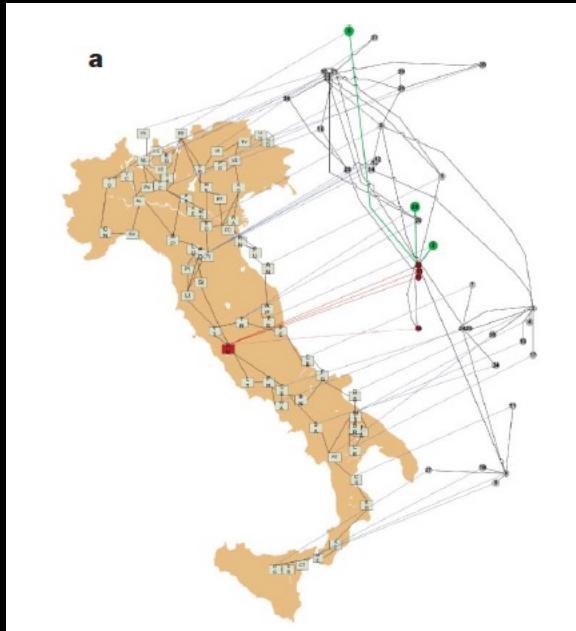
Buldyrev et al. 2010, Nature



Blackout en Italie en 2003 - Sipa Press

# Interdependent networks

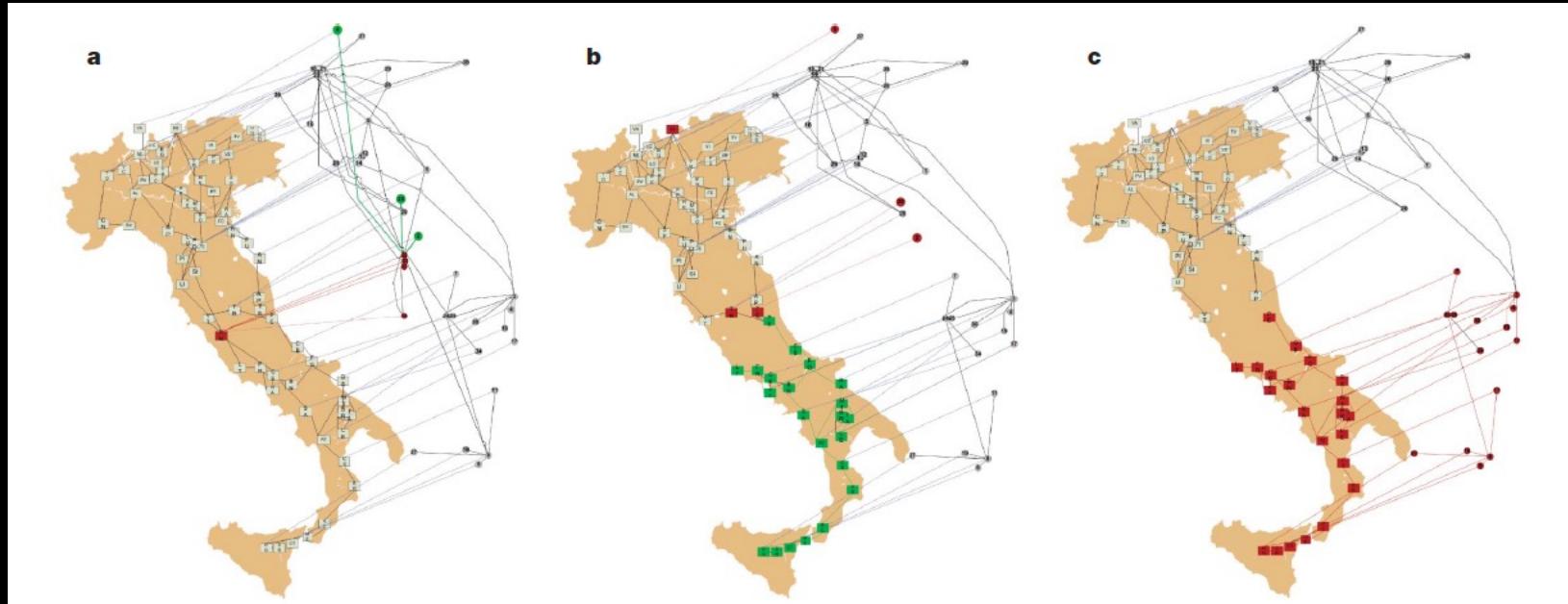
power network



Internet network

One power station removed (**red**)  
→ nodes removed from internet network  
(**red**)  
→ Isolated power station removed next  
(**green**)

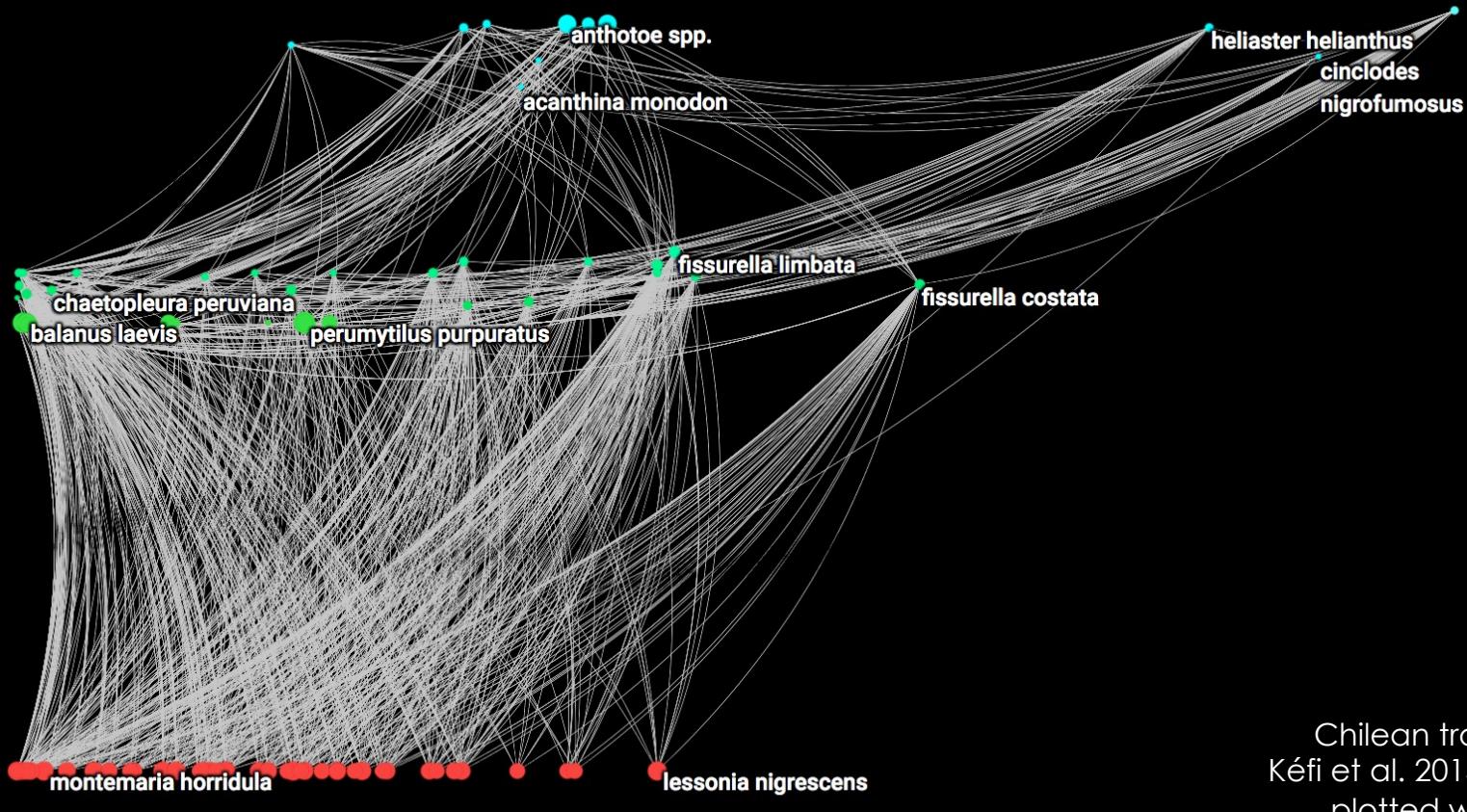
power network



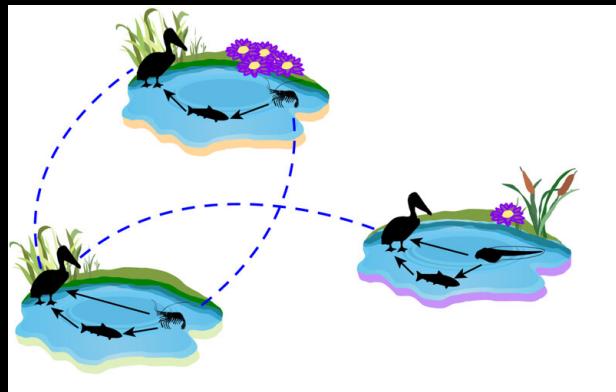
Internet network

Modern systems are interdependent networks  
→ Cascades of failures possible

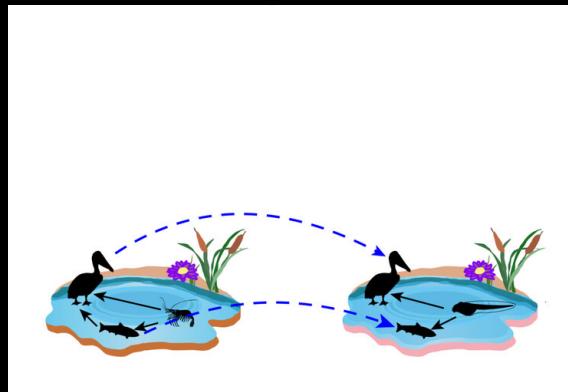
What about ecological networks?



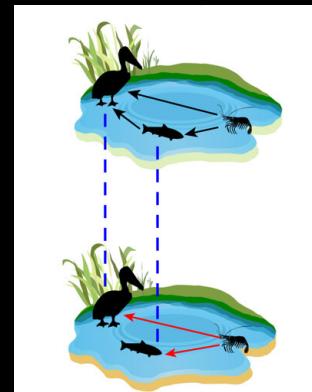
Spatial



Temporal



Multi-interactions



# multilayer ecological networks

## Mathematical Formulation of Multilayer Networks

Manlio De Domenico,<sup>1</sup> Albert Solé-Ribalta,<sup>1</sup> Emanuele Cozzo,<sup>2</sup> Mikko Kivelä,<sup>3</sup> Yamir Moreno,<sup>2,4,5</sup>  
Mason A. Porter,<sup>6</sup> Sergio Gómez,<sup>1</sup> and Alex Arenas<sup>1</sup>

*Journal of Complex Networks* (2014) 2, 203–271

doi:10.1093/comnet/cnu016

Advance Access publication on 14 July 2014

### Multilayer networks

MIKKO KIVELÄ

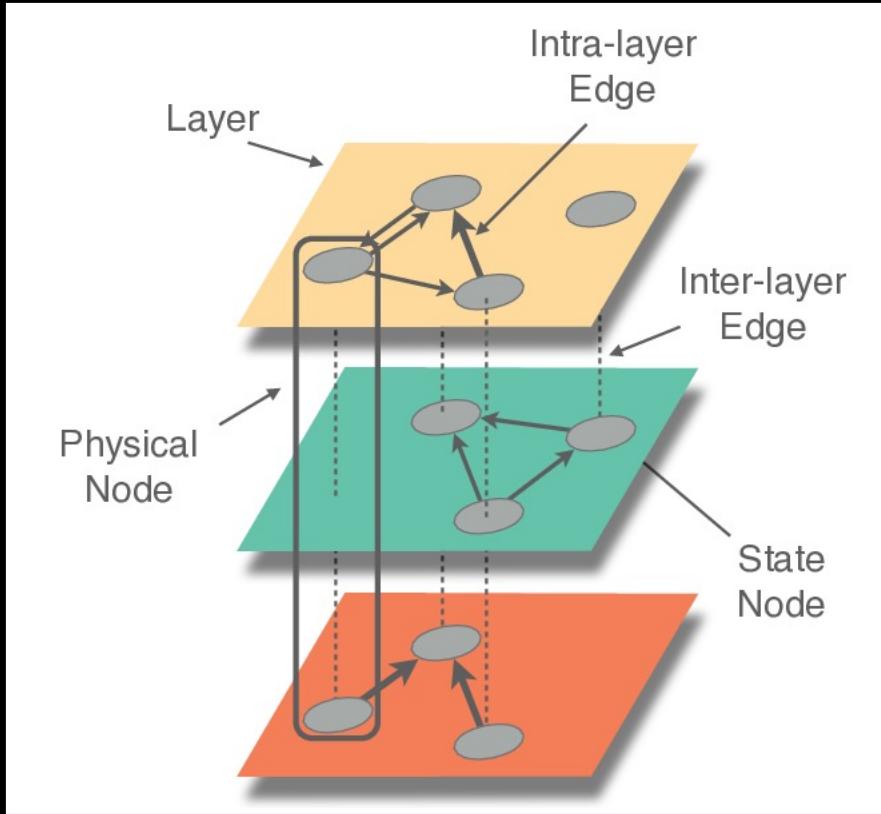
*Oxford Centre for Industrial and Applied Mathematics, Mathematical Institute, University of Oxford,  
Oxford OX2 6GG, UK*

### The structure and dynamics of multilayer networks



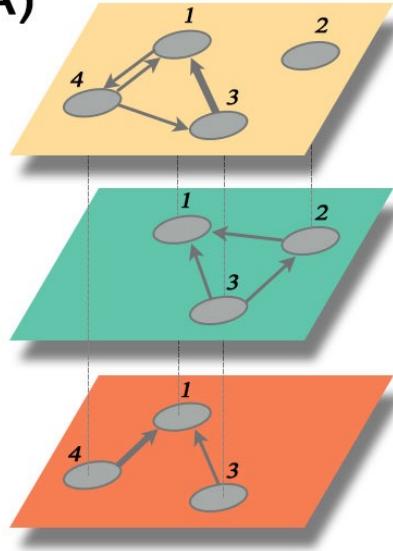
S. Boccaletti<sup>a,b,\*</sup>, G. Bianconi<sup>c</sup>, R. Criado<sup>d,e</sup>, C.I. del Genio<sup>f,g,h</sup>,  
J. Gómez-Gardeñes<sup>i</sup>, M. Romance<sup>d,e</sup>, I. Sendiña-Nadal<sup>j,e</sup>, Z. Wang<sup>k,l</sup>,  
M. Zanin<sup>m,n</sup>

De Domenico et al. 2013, PRE  
Kivela et al. 2014, J. Complex Net  
Boccaletti et al. 2014, Physics Reports



#### 4 components:

- layers (patches, interaction types, time points)
- nodes (physical vs state)
- intralayer links
- **interlayer links**

**A)****L1**

1	2	3	4
1			
2			
3	●		
4	●	●	

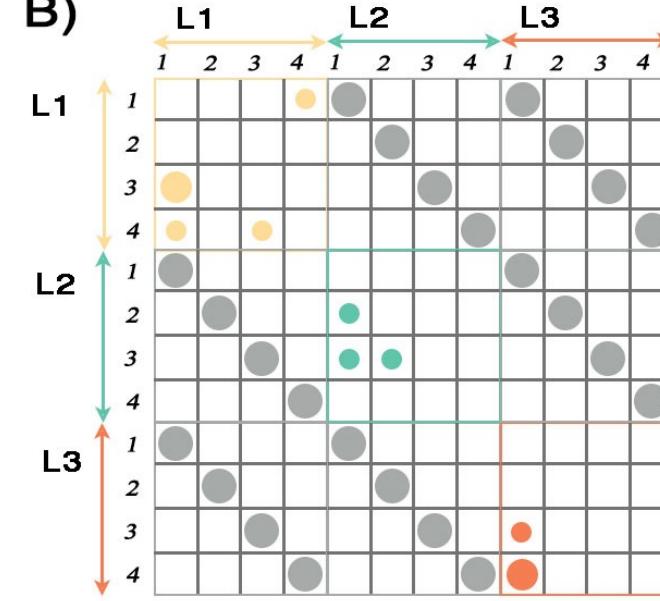
**L2**

1	2	3	4
1			
2	●		
3	●	●	
4			

**L3**

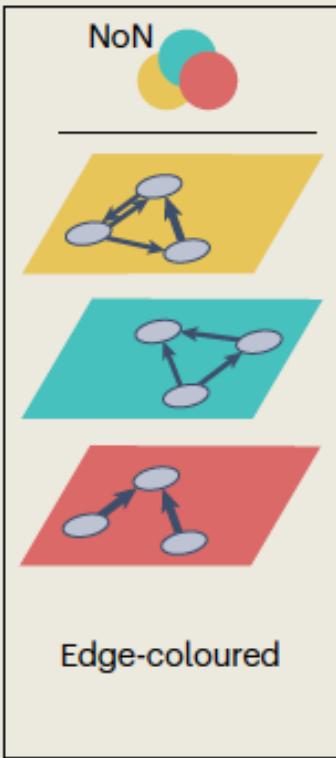
1	2	3	4
1			
2			
3	●		
4	●		

**Interconnected  
Multiplex Network**

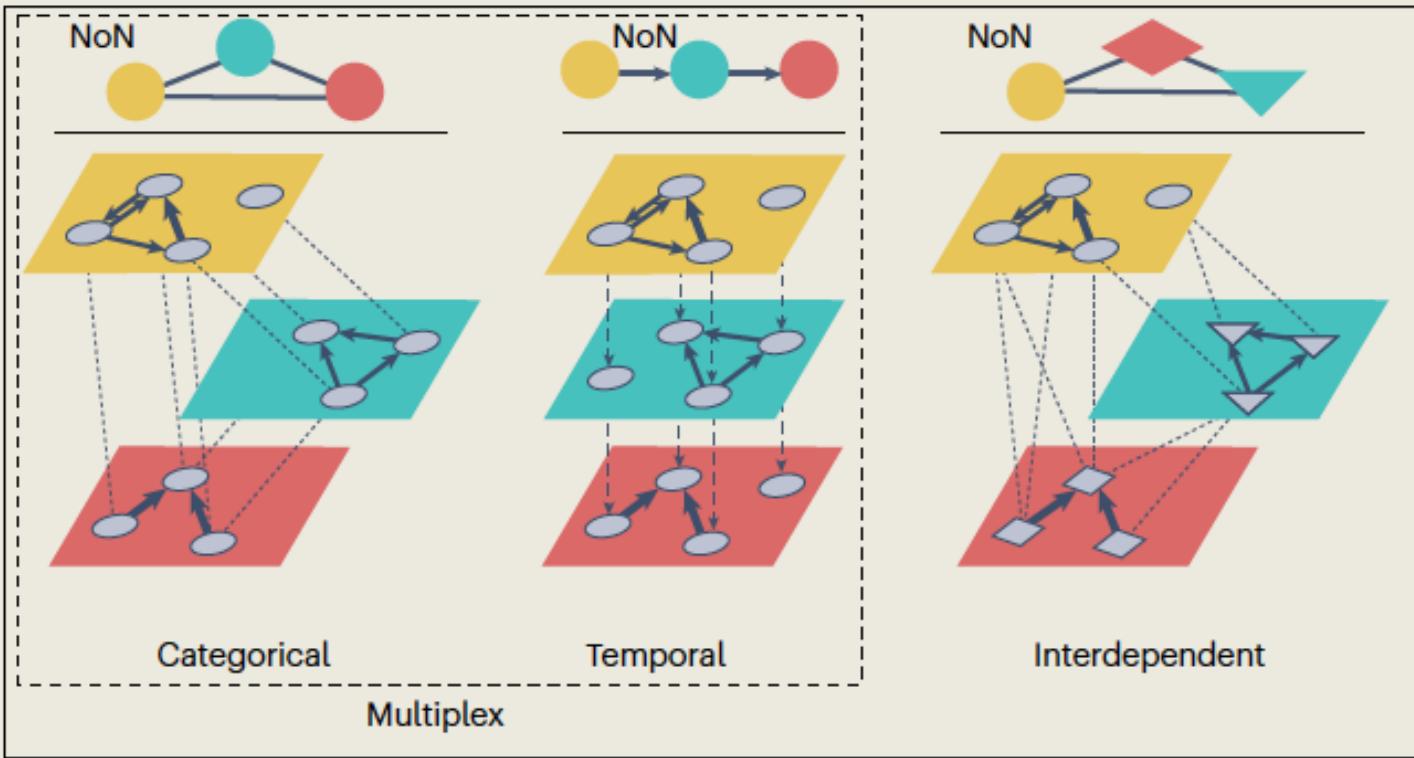
**B)**

**Supra-adjacency Matrix**

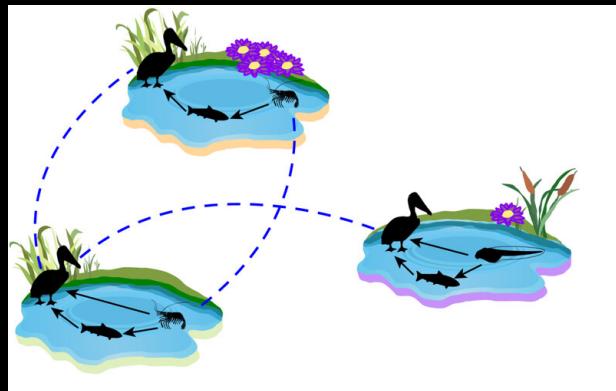
## Non-interconnected



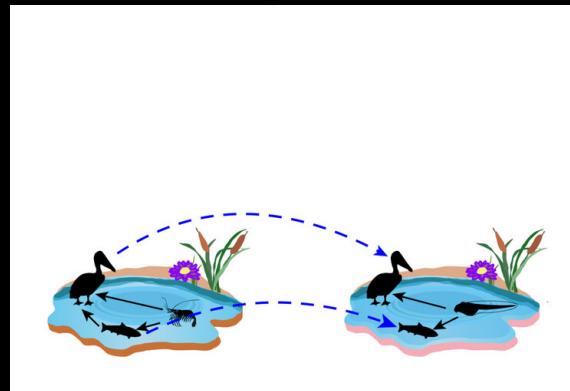
## Interconnected



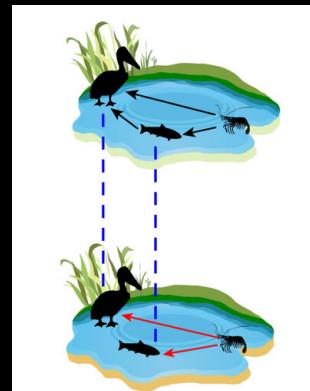
Spatial



Temporal



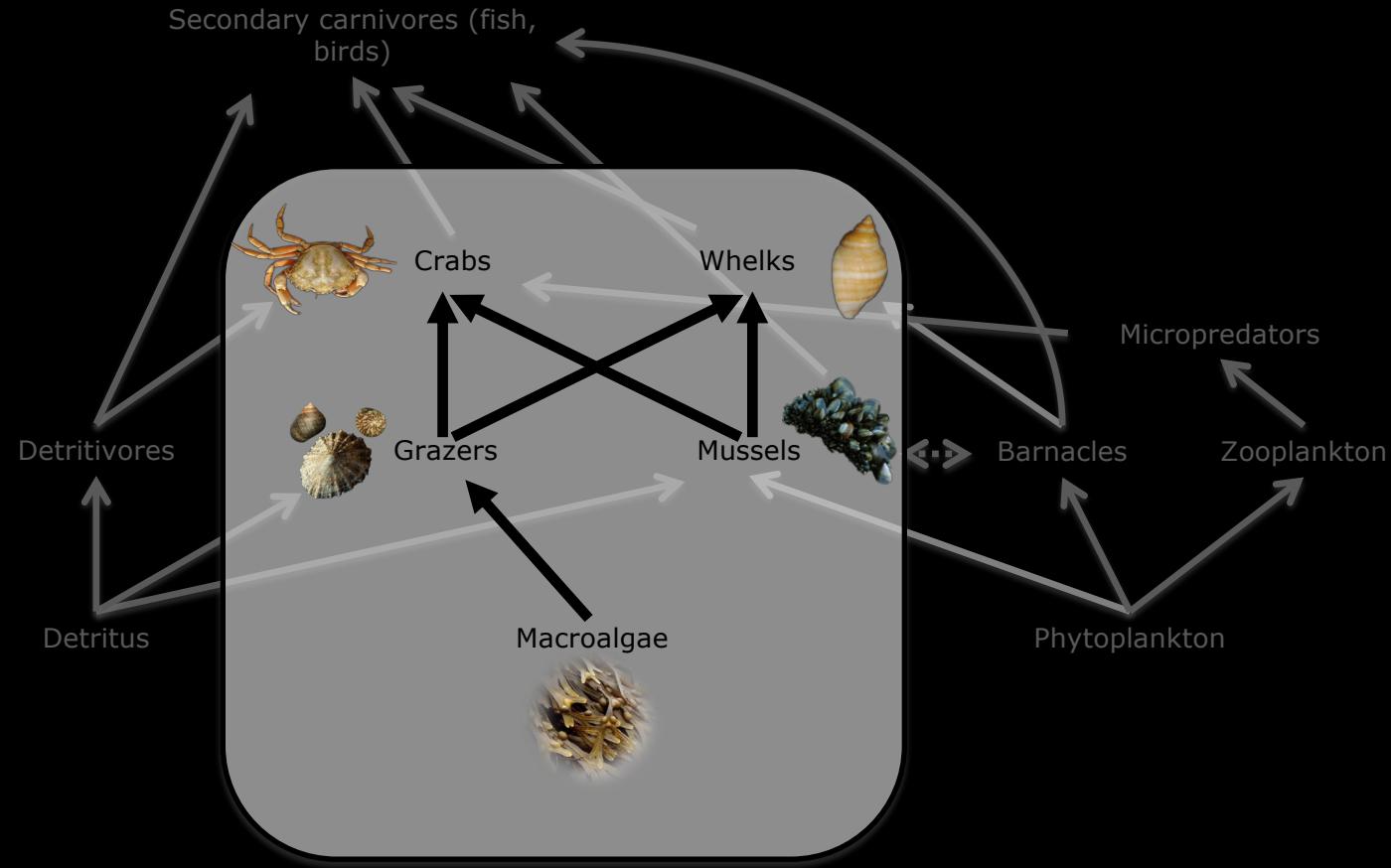
Multi-interactions

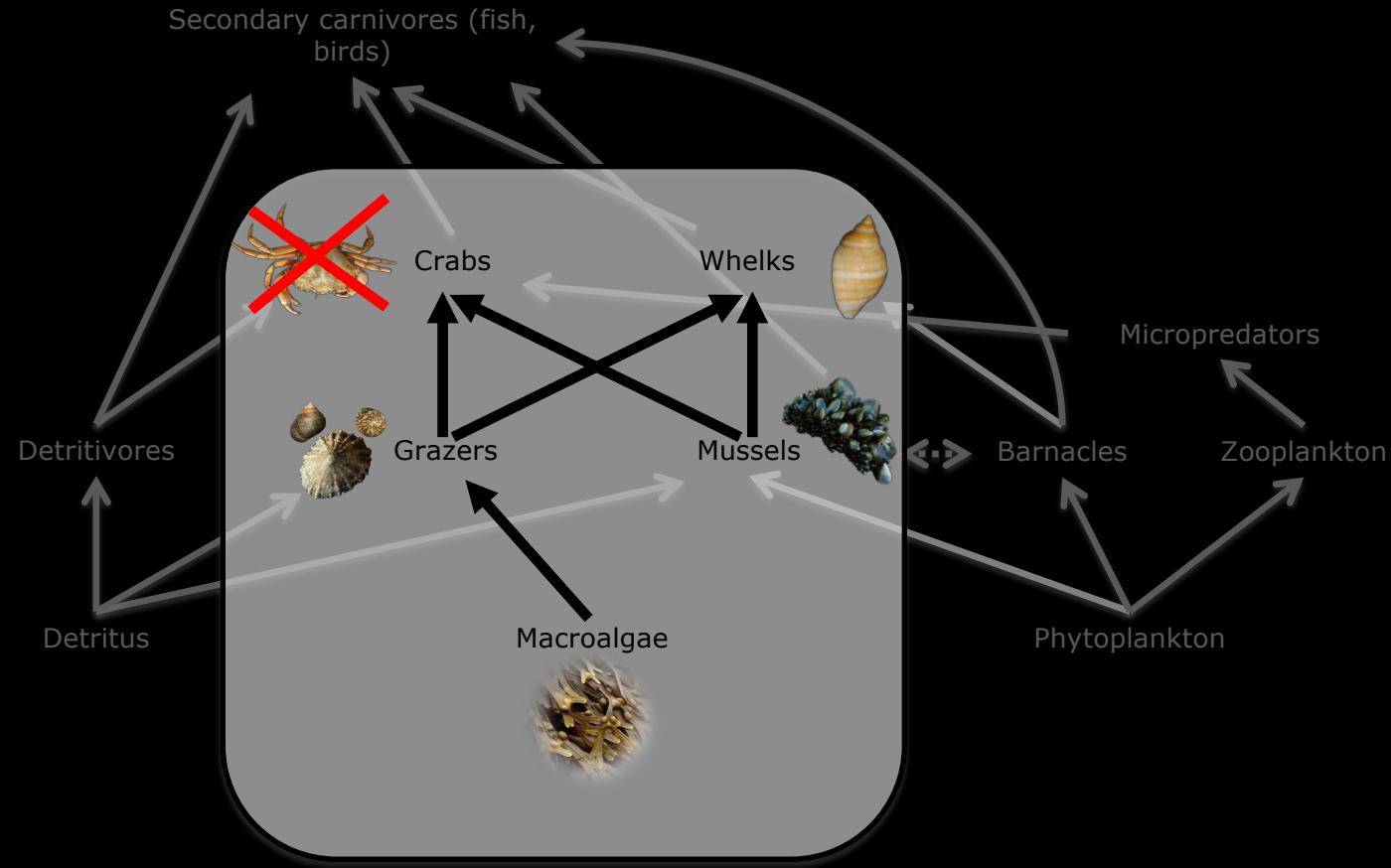


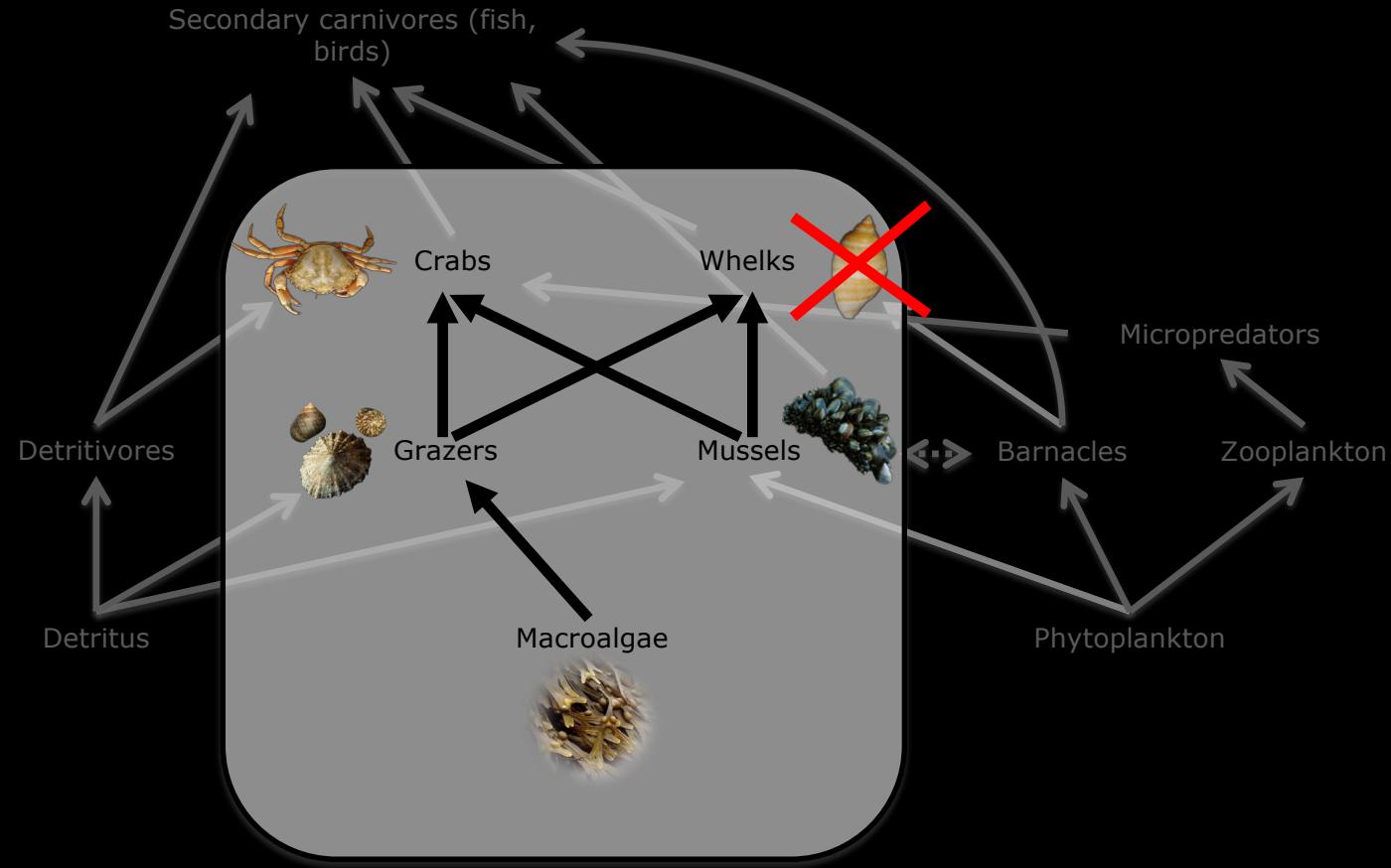
multi-interaction networks

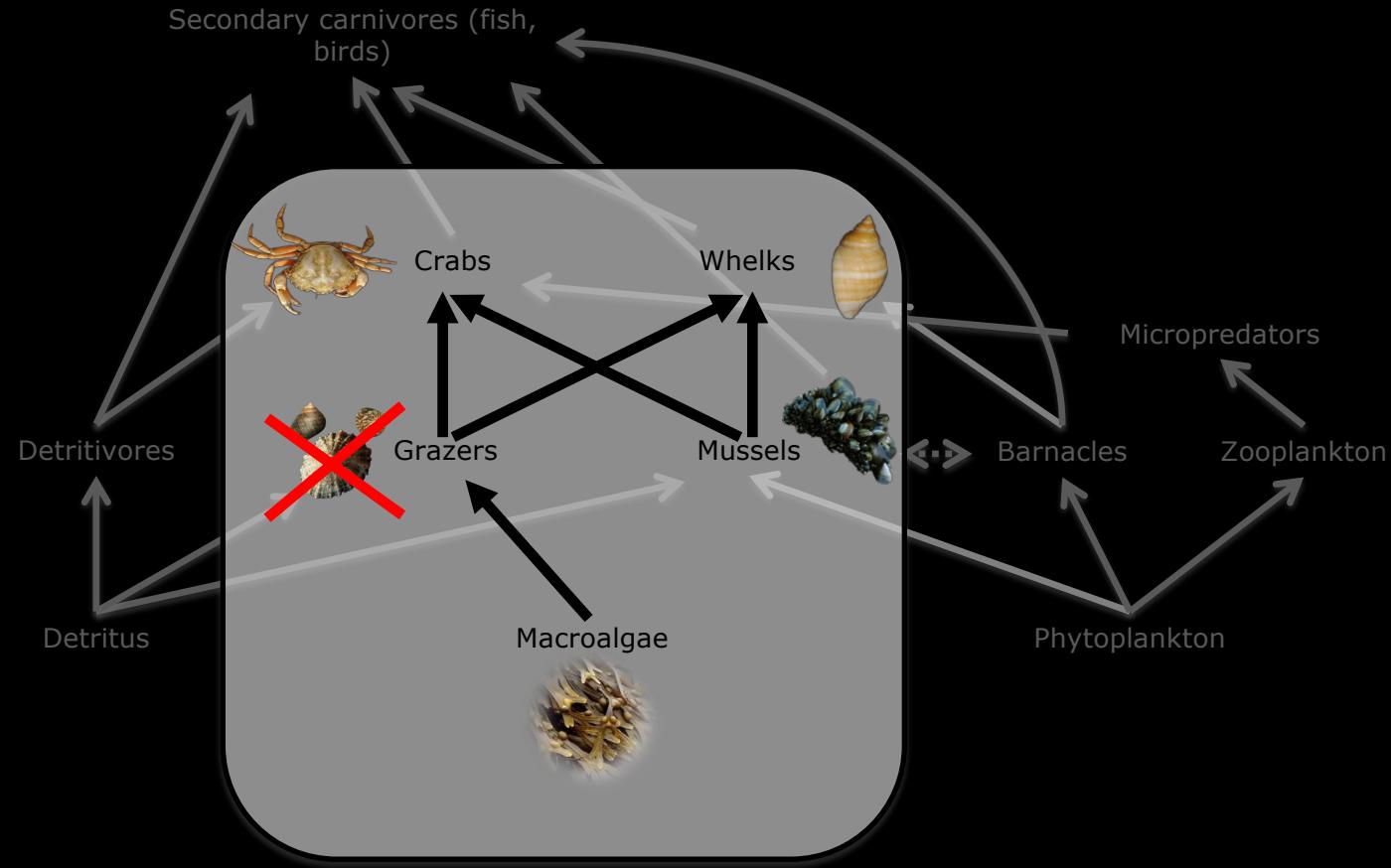


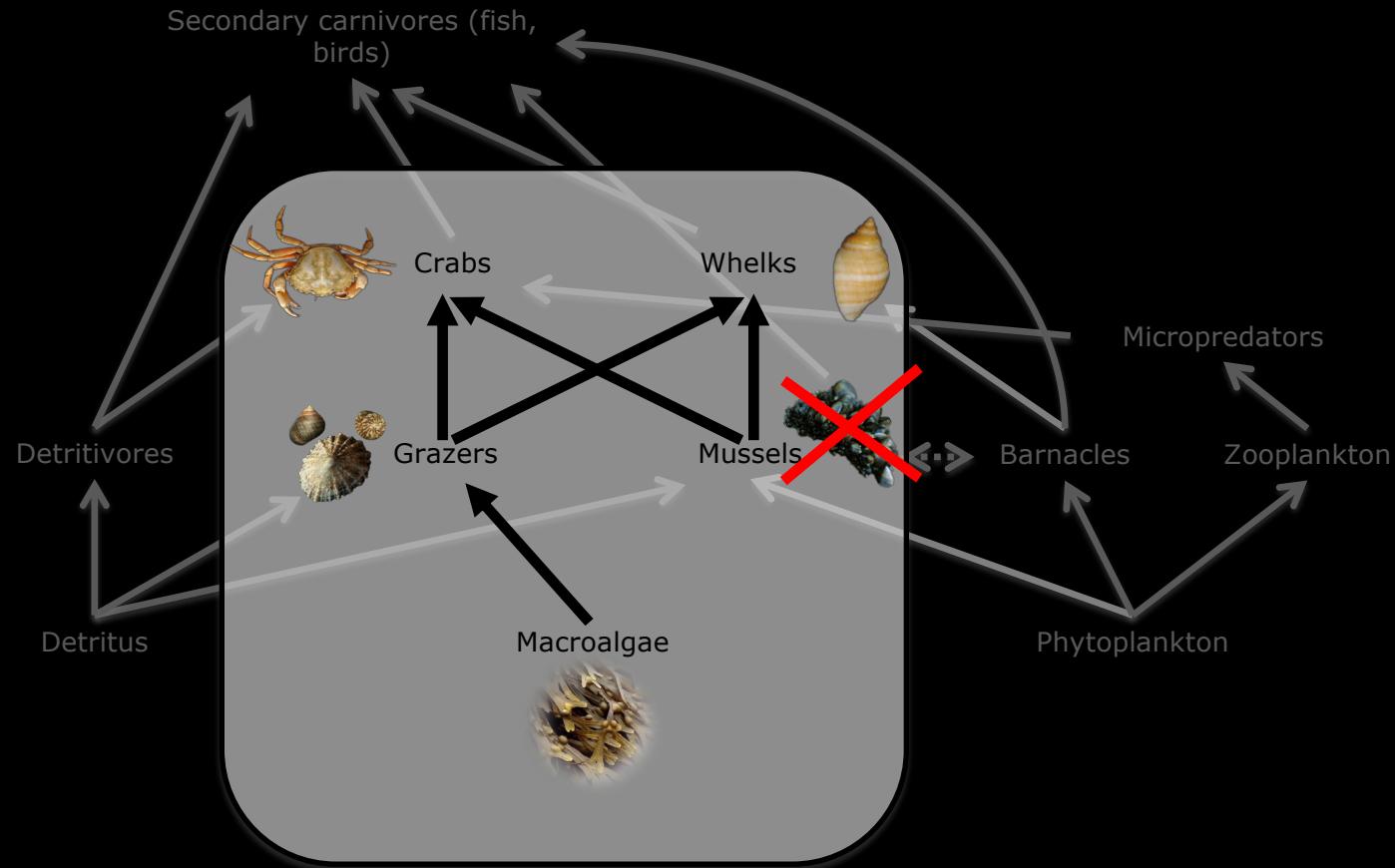
@ian Donohue

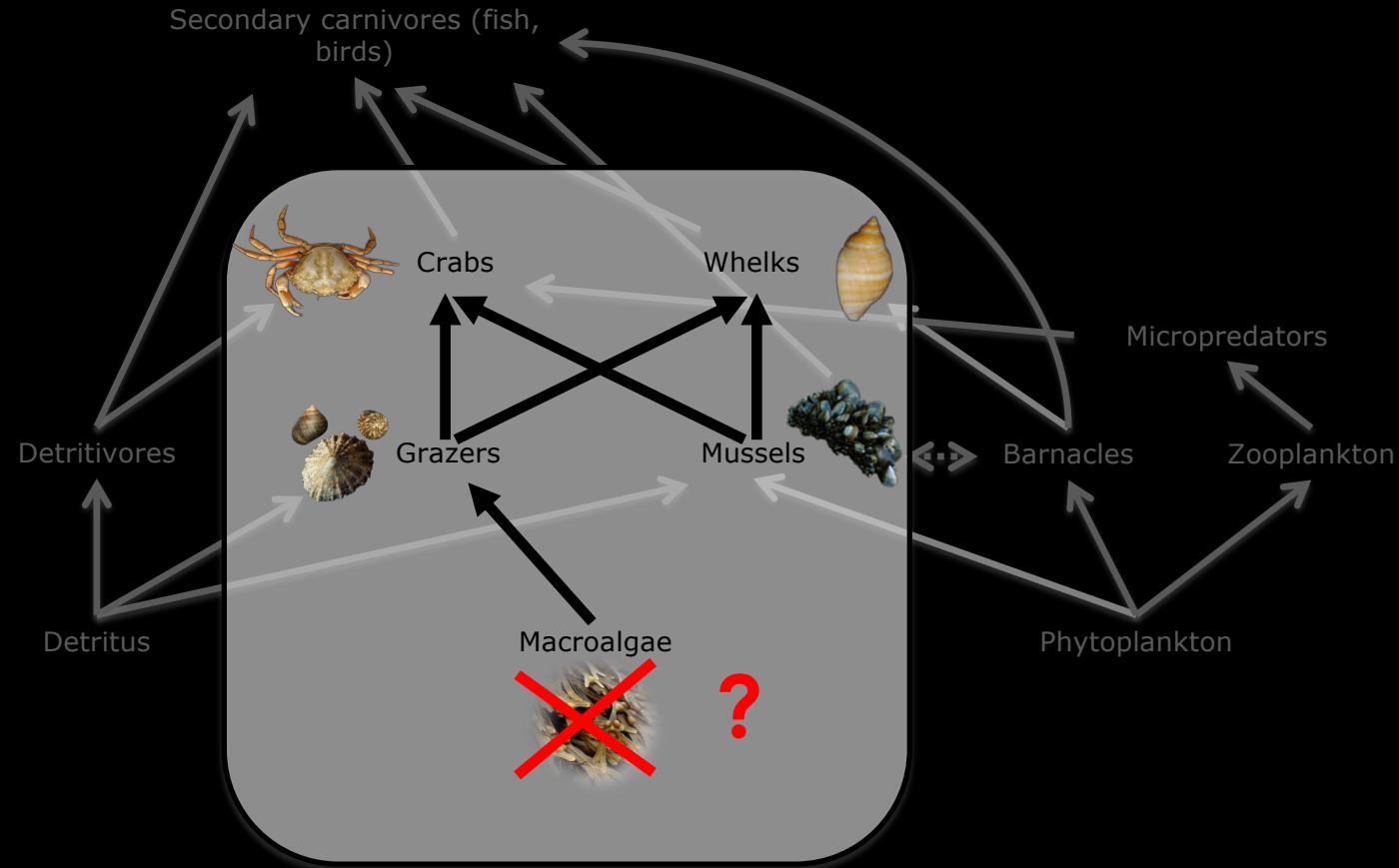


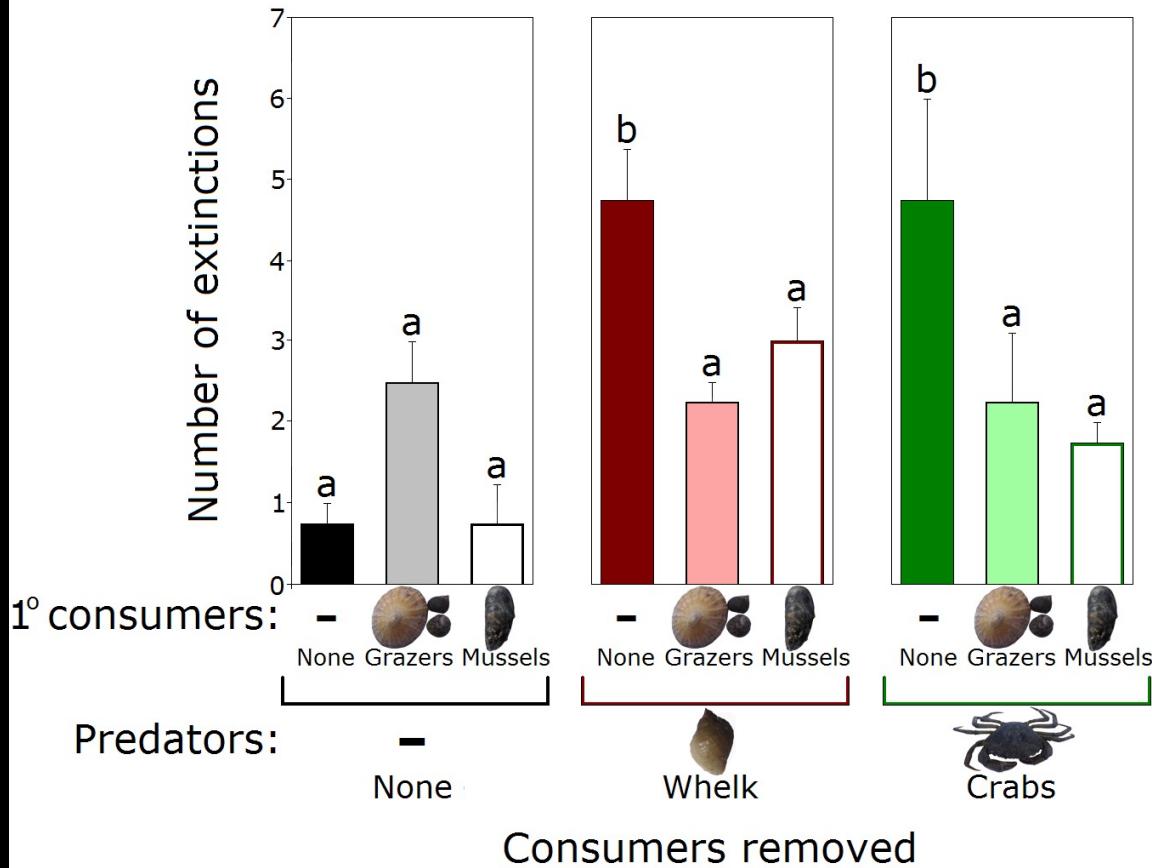












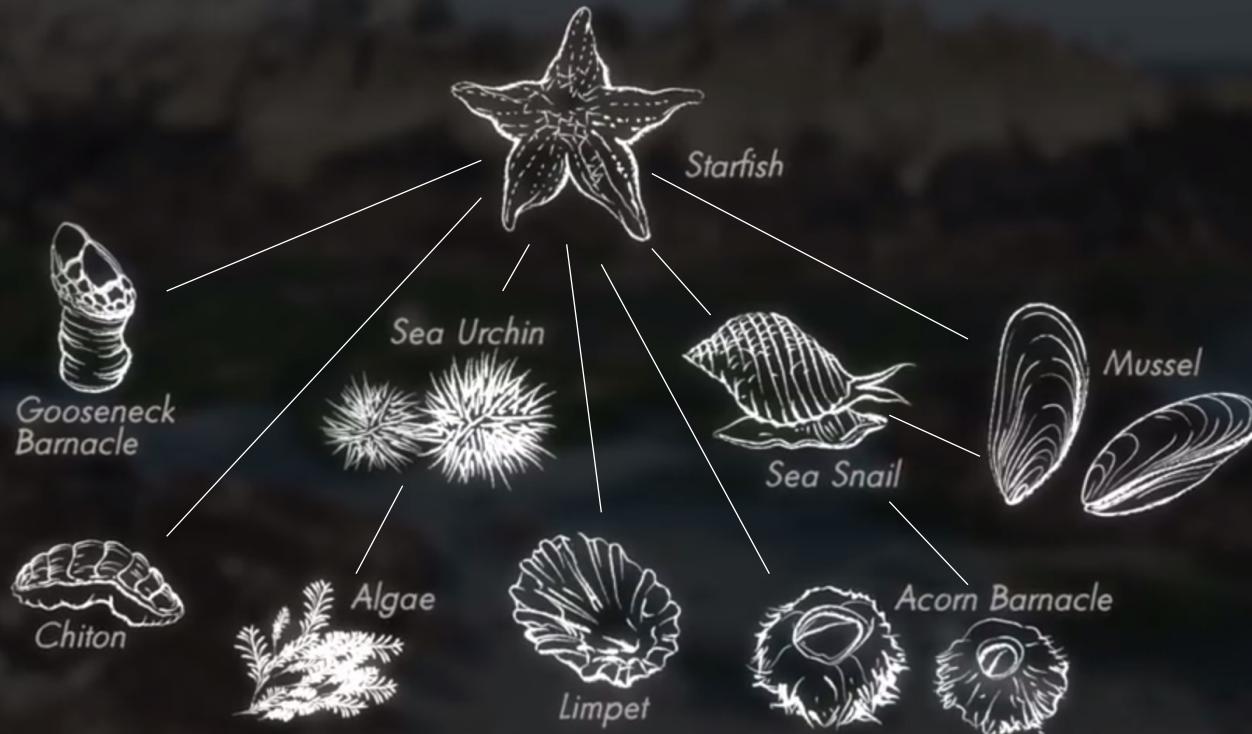
1/3 of the macroalgal taxa lost following the removal of either predator species

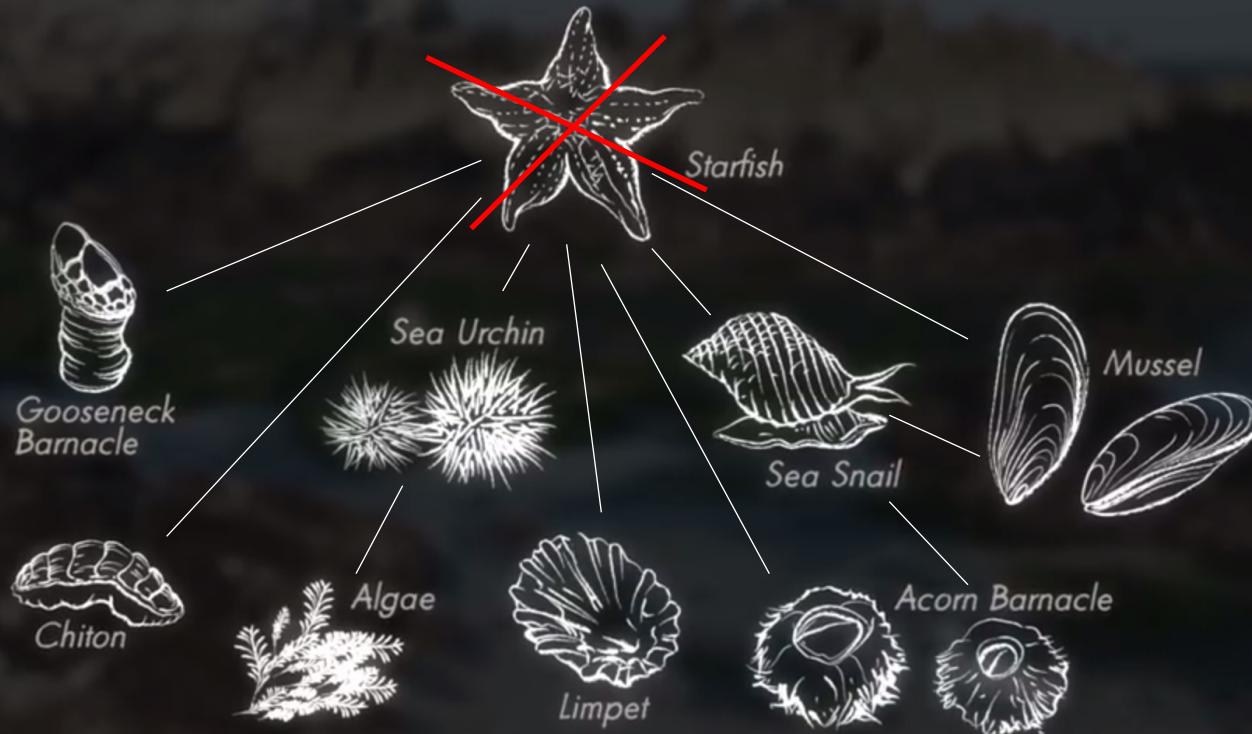
an order of magnitude greater than in models

e.g. Ebenman *et al.* 2006  
Eklöf and Ebenman 2006  
Quince *et al.* 2005  
Petchey *et al.* 2008



Robert Paine  
Credit: Alamy. Telegraph obituary





15 species initially



hhmi biointeractive

« Some Animals Are More Equal than Others: Keystone Species and Trophic Cascades »

7 species after 1.5 year



hhmi biointeractive

« Some Animals Are More Equal than Others: Keystone Species and Trophic Cascades »

1 species after 7 years



→ puzzling discrepancy between observations  
and the prediction of most theoretical models



feeding interactions



@Evie Wieters



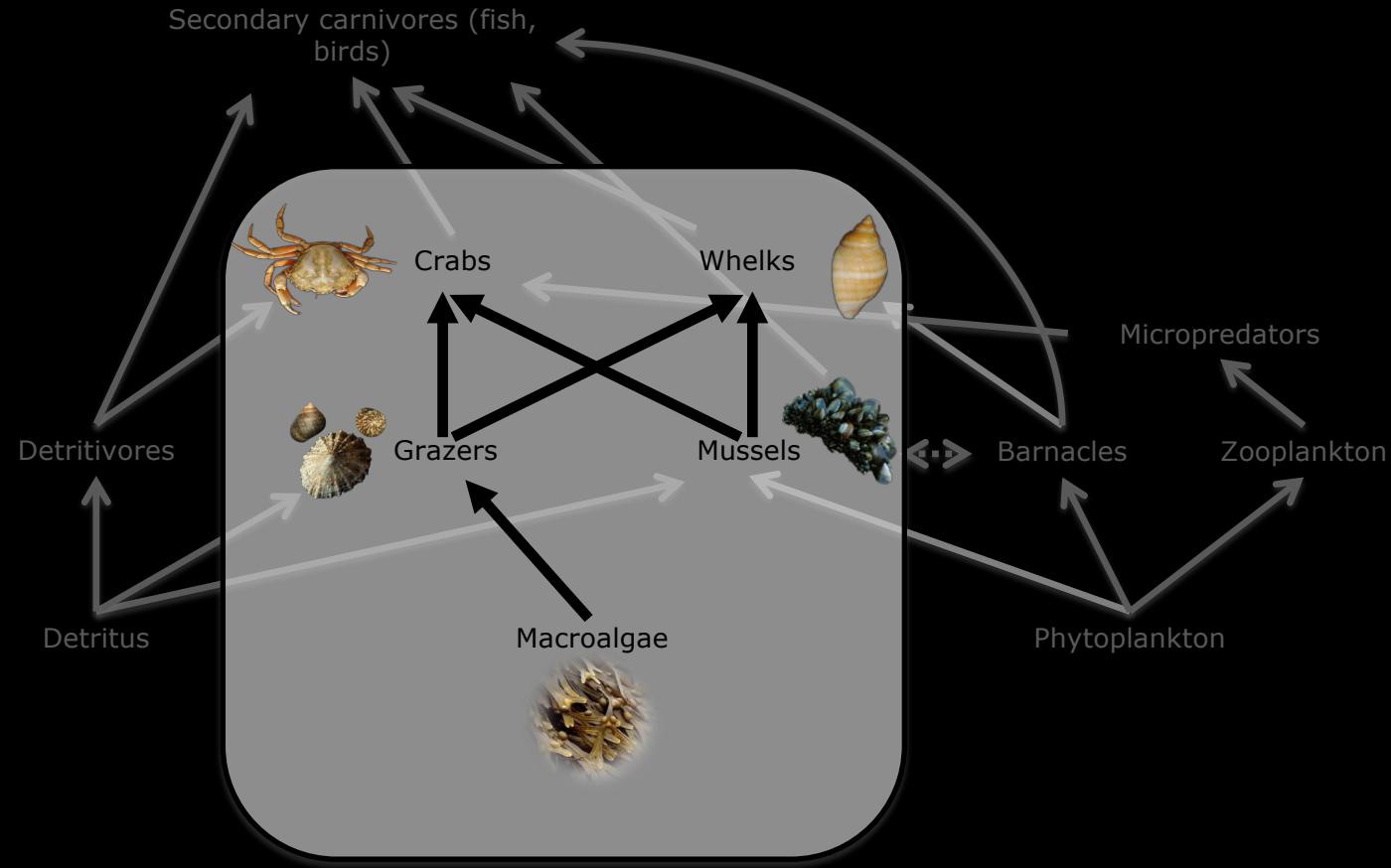
@Evie Wieters

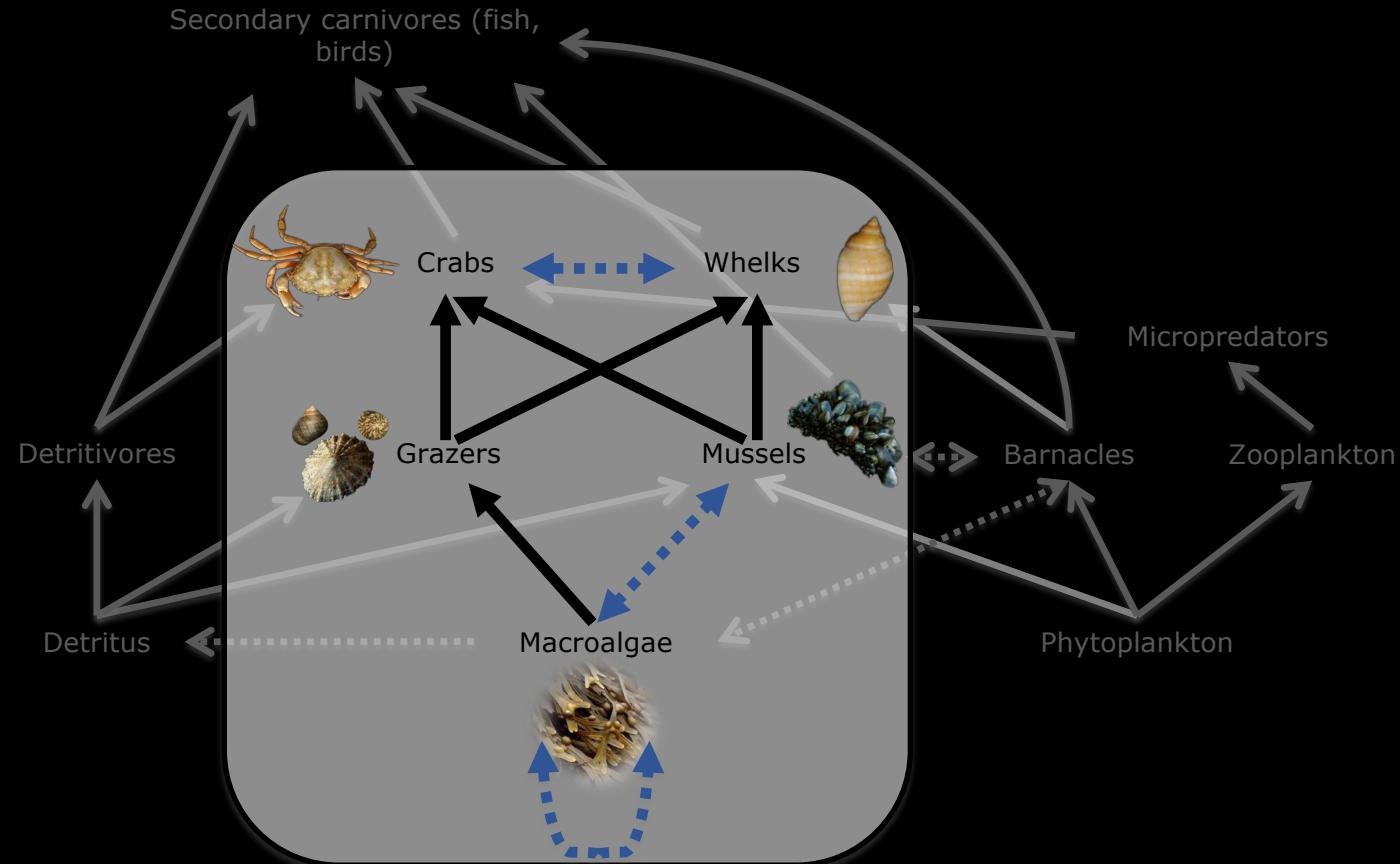


@Evie Wieters



@Evie Wieters





dynamical model  
[bioenergetic consumer-resource model]

$$\frac{dB_i}{dt} = r_i \left(1 - \frac{B_i}{K_i}\right) B_i + e B_i \sum_j F_{ij} - \sum_k F_{ki} B_k - x_i B_i$$

Yodzis and Innes 1992  
Brose et al. 2005, 2006  
Stouffer et al. 2011

$$\frac{dB_i}{dt} = \underbrace{r_i \left(1 - \frac{B_i}{K_i}\right) B_i}_{\text{growth}} + \underbrace{e B_i \sum_j F_{ij}}_{\text{consumption (eats)}} - \underbrace{\sum_k F_{ki} B_k}_{\text{consumption (is eaten)}} - \underbrace{x_i B_i}_{\text{metabolism}}$$

primary  
producers      non-primary  
producers

Yodzis and Innes 1992  
Brose et al. 2005, 2006  
Stouffer et al. 2011

$$\frac{dB_i}{dt} = r_i \left(1 - \frac{B_i}{K_i}\right) B_i + e B_i \sum_j F_{ij} - \sum_k F_{ki} B_k - x_i B_i$$

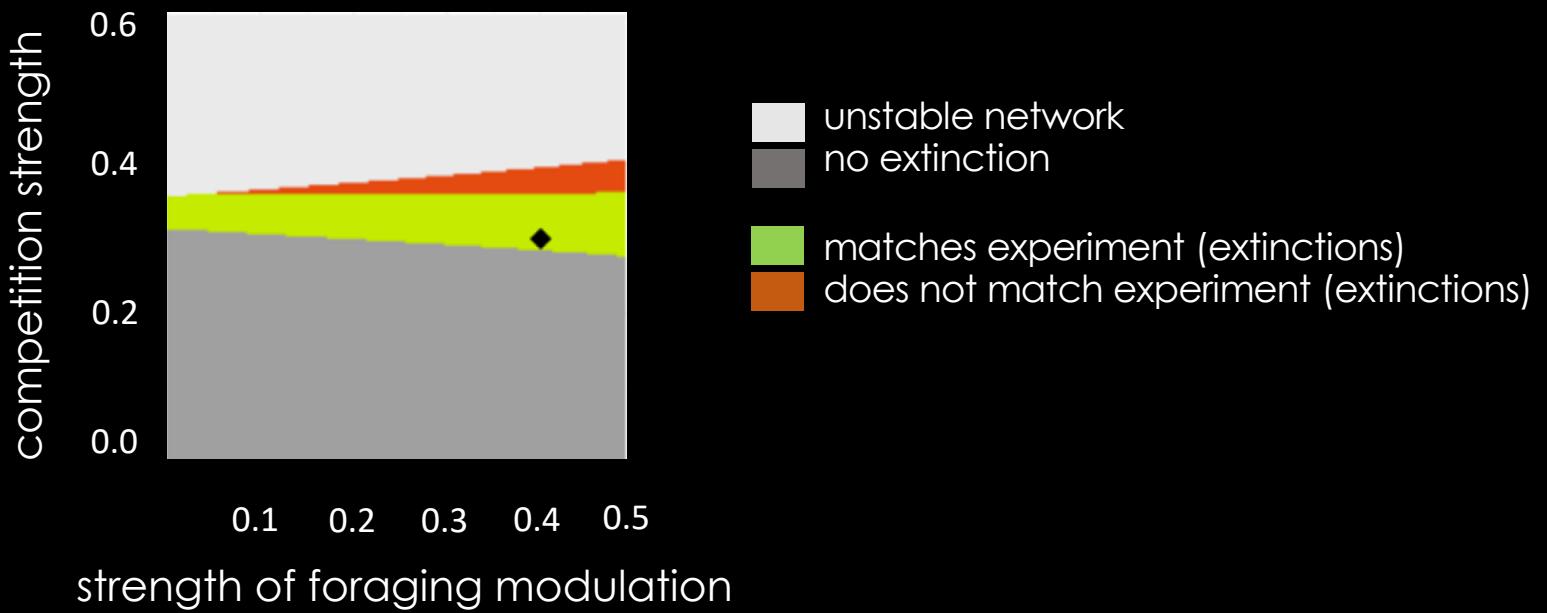

  
 growth      consumption (eats)      consumption (is eaten)      metabolism

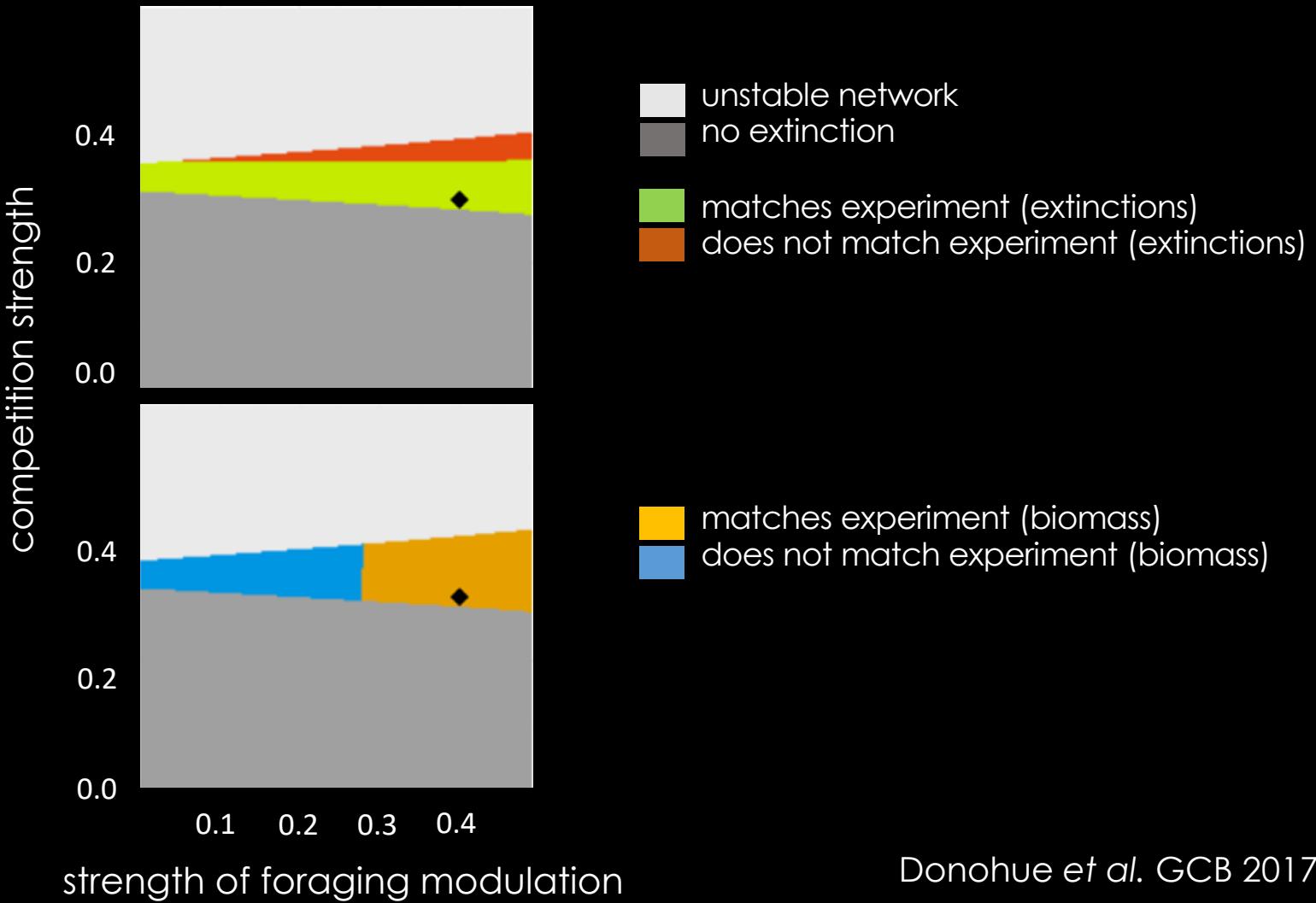
$$F_{ij} = \frac{w_i b_{ij} B_j^{1+q}}{1 + w_i h_i \sum_k b_{ik} B_k^{1+q}}$$

Yodzis and Innes 1992  
 Brose *et al.* 2005, 2006  
 Stouffer *et al.* 2011

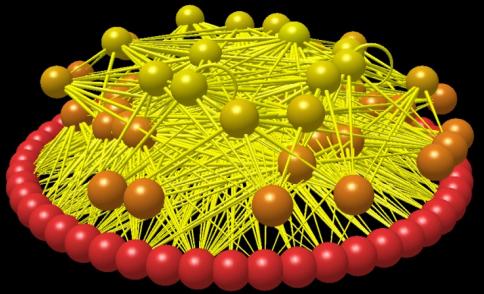
dynamical model  
[bioenergetic consumer-resource model]

+ non-trophic interactions  
competition for space  
foraging modulation

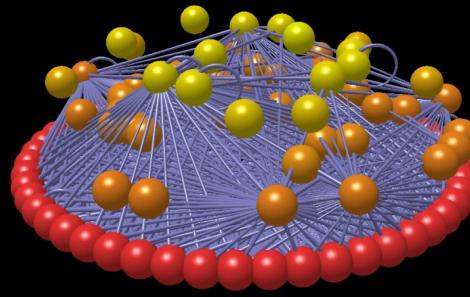


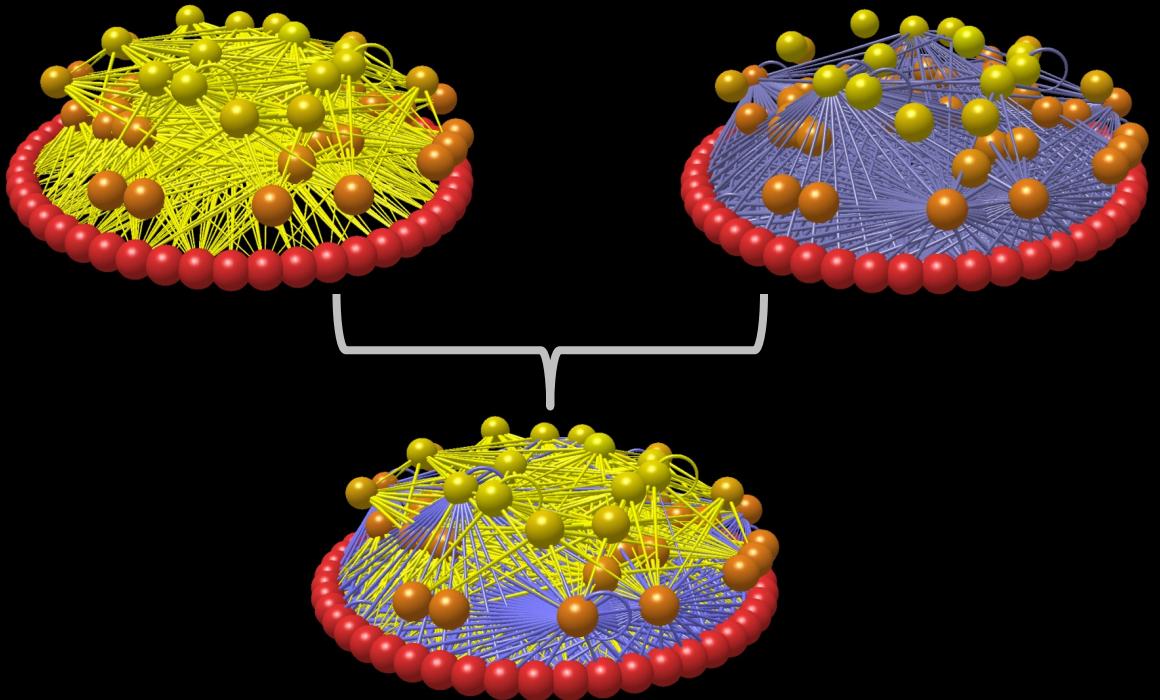


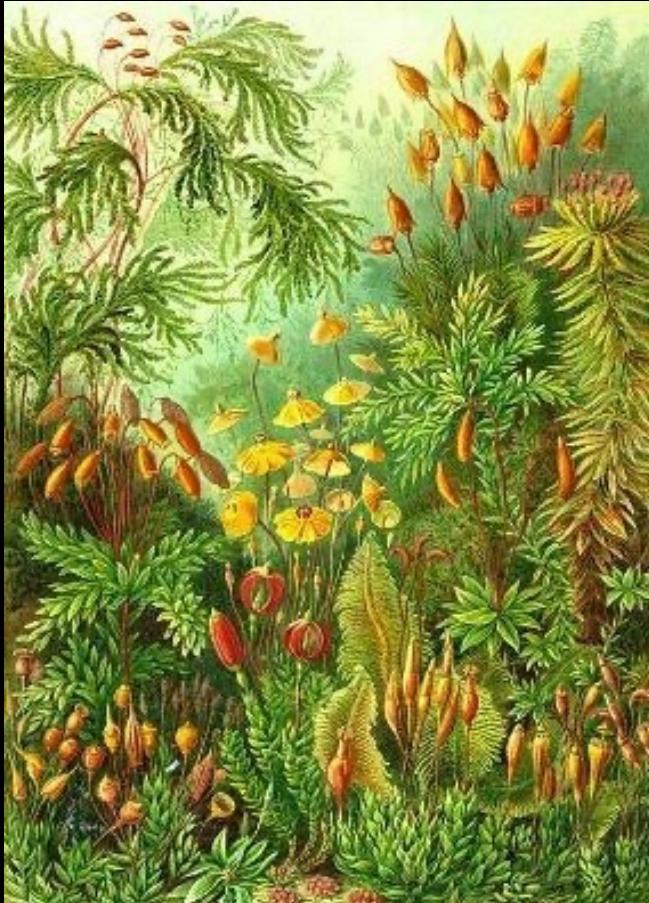
The diversity of interaction types is needed to reproduce the results of the experiments



-







« So dependent on each other  
in so complex a manner »

Charles Darwin, 1859

DARWIN'S "ENTANGLED BANK" (HAECKEL, CIRCA 1904)

# A need for **integrating** several interaction types in ecological network studies

Berlow et al. 2004

Ings et al. 2009

Olff et al. 2009

Fontaine et al. 2011

Kéfi et al. 2012

How does the diversity of interaction types affect functioning?

dynamical model  
[bioenergetic consumer-resource model]  
+ non-trophic interactions

- Competition for space
- Predator interference
- Recruitment facilitation
- Refuge provisioning
- Positive and negative effects on survival

# Simulations

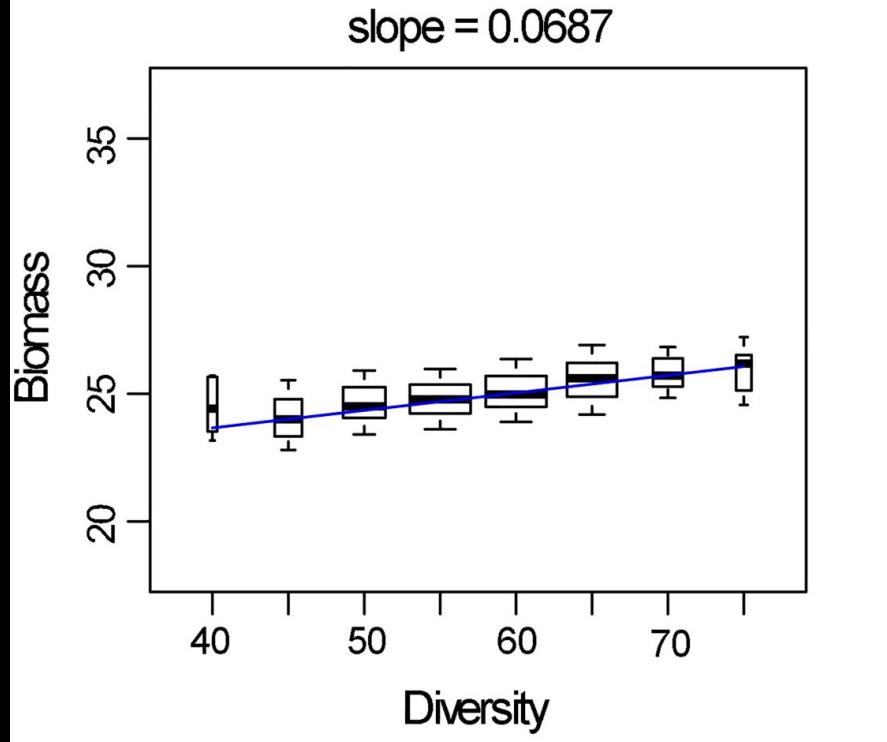
Niche model for food web skeleton, 100 species incl. 20 plants  
Plug NTI ‘links randomly’  
Run dynamics with and without NTI



Calculate species diversity and total biomass

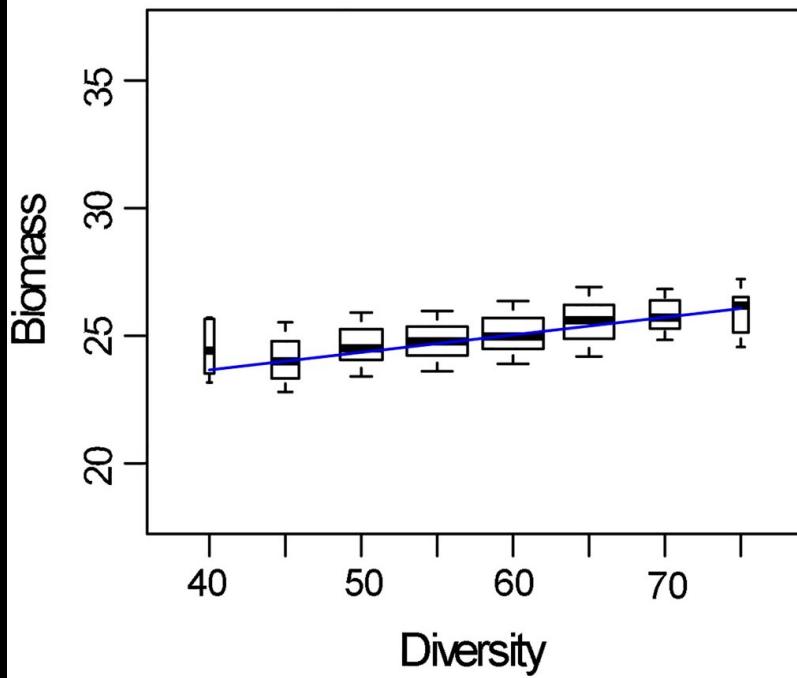
# One interaction type (trophic)

slope = 0.0687



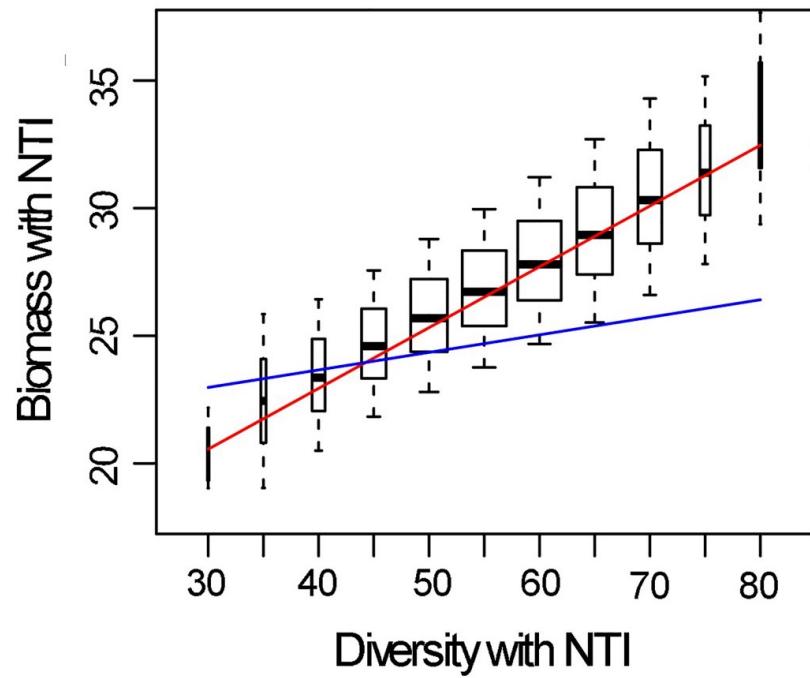
## One interaction type (trophic)

slope = 0.0687



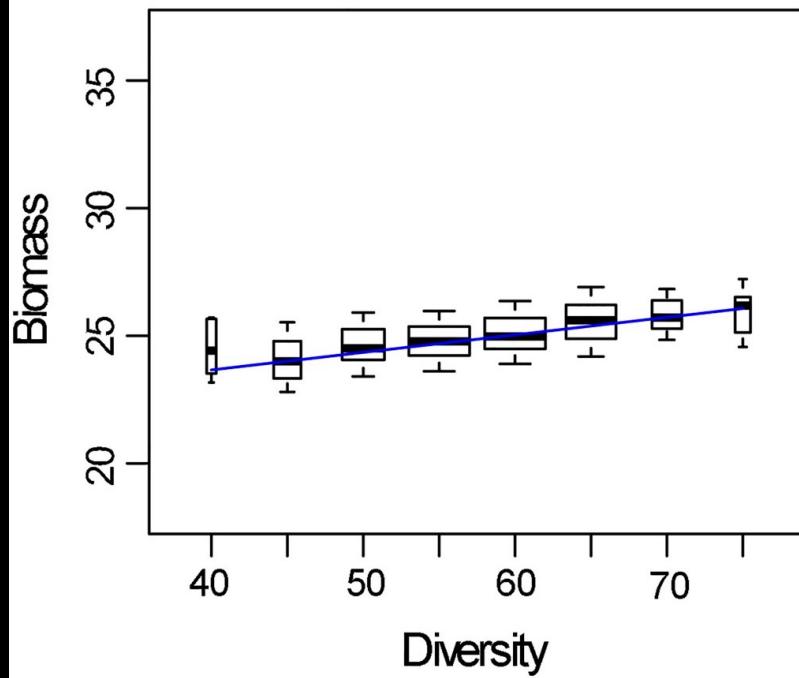
## Diverse interactions types (multiplex)

slope = 0.238



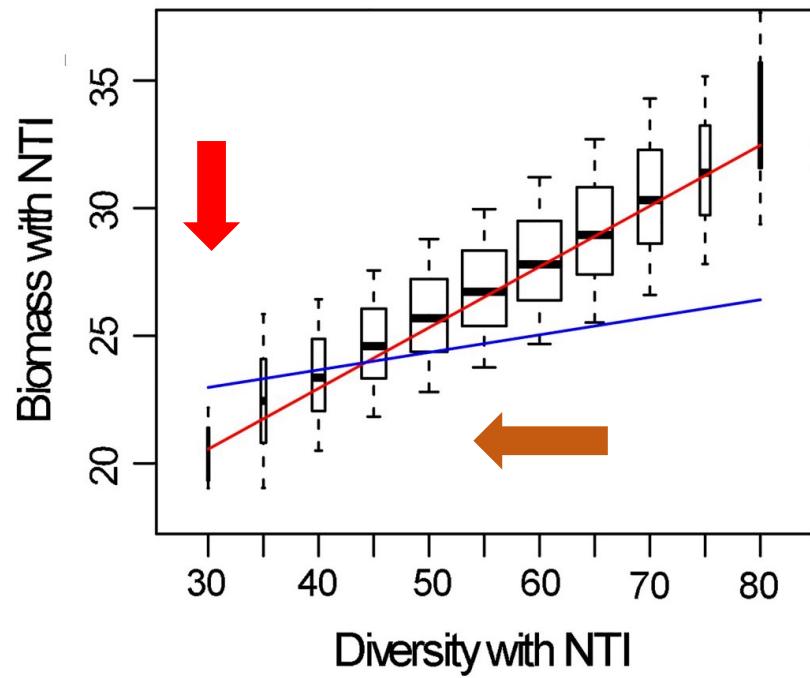
## One interaction type (trophic)

slope = 0.0687



## Diverse interactions types (multiplex)

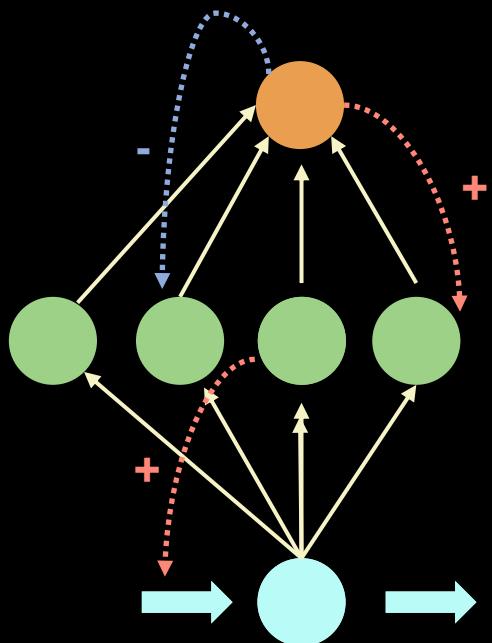
slope = 0.238



NTIs affect species diversity, community functioning and their relationship

How do different interaction types map  
onto each other?

What's the relative abundance of different interaction types?



multiplex ecological network

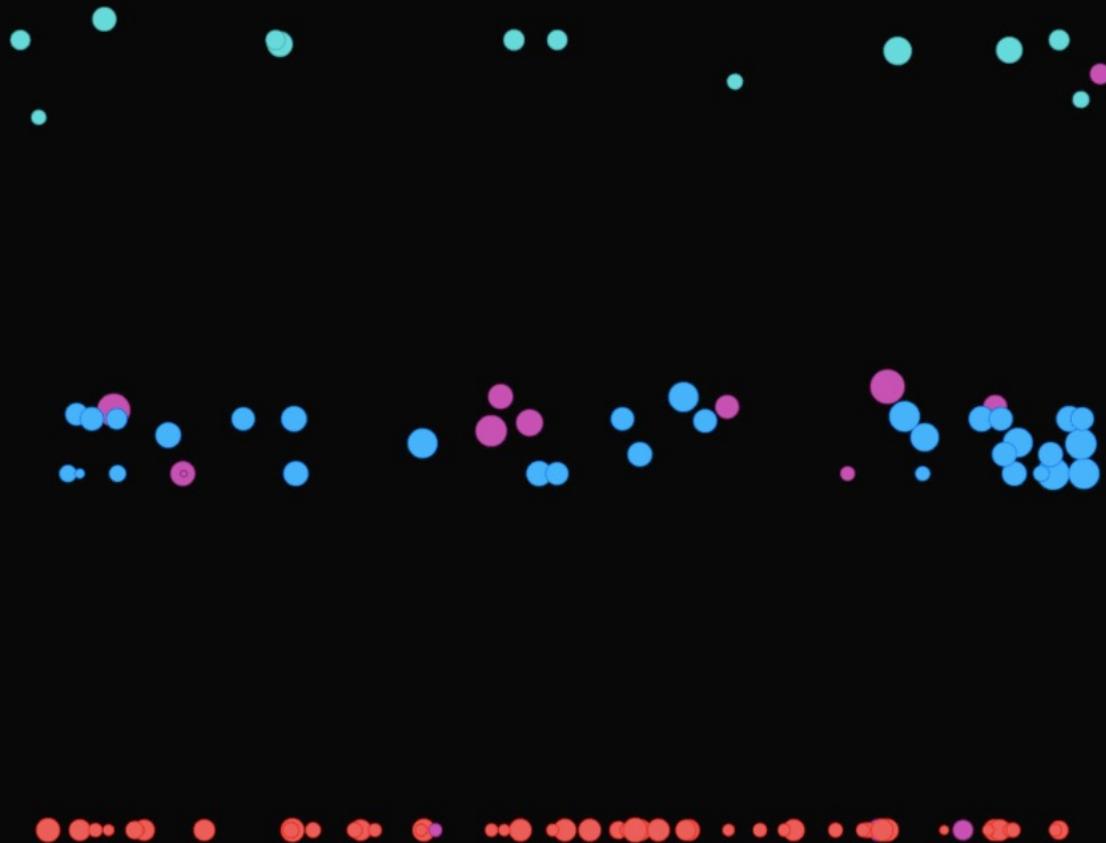


Sergio Navarrete,  
Evie Wieters

Kéfi et al. 2015



# CHILEAN MARINE ECOLOGICAL NETWORK



TL

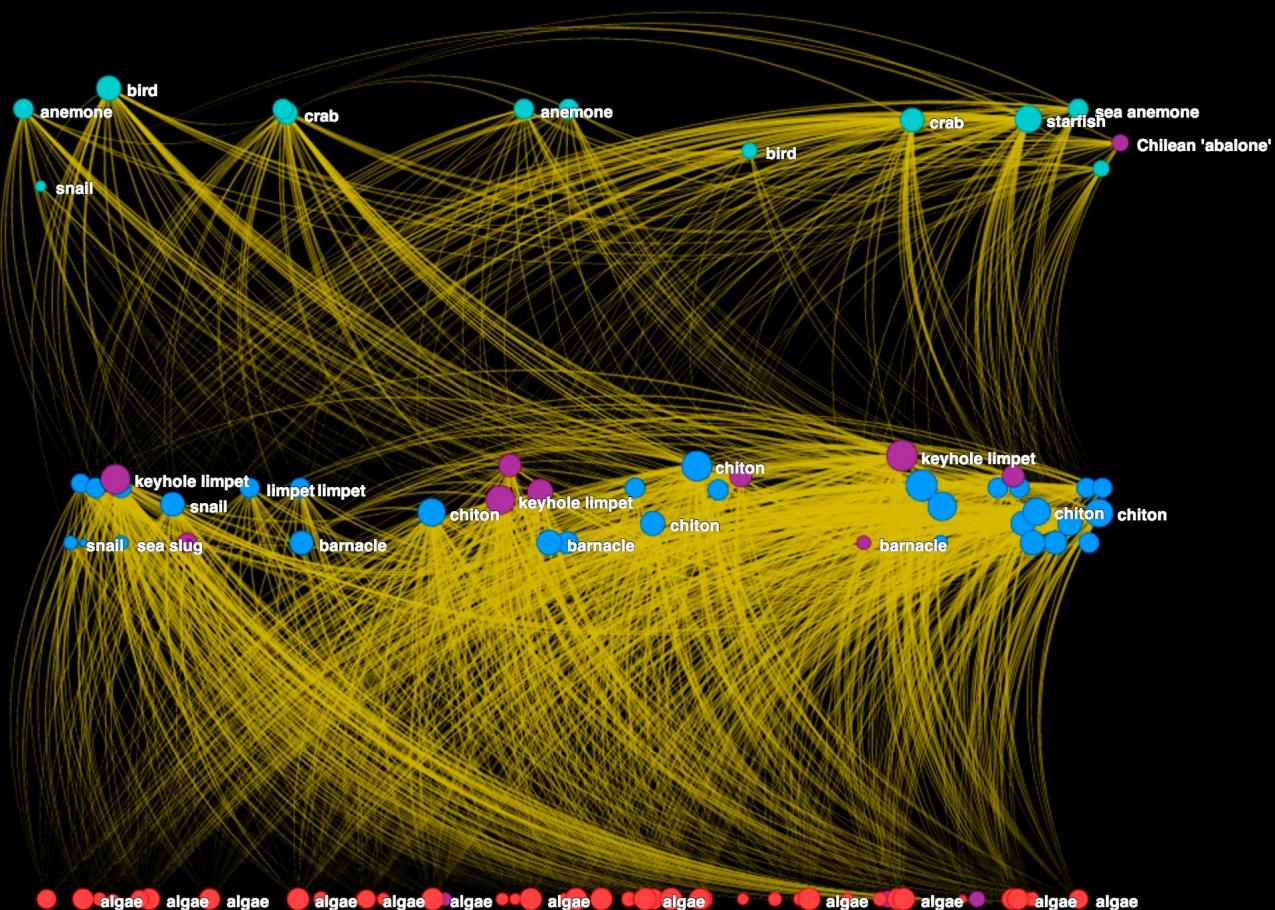
Rand

Kéfi et al. 2015 Ecology





# CHILEAN MARINE FOOD WEB



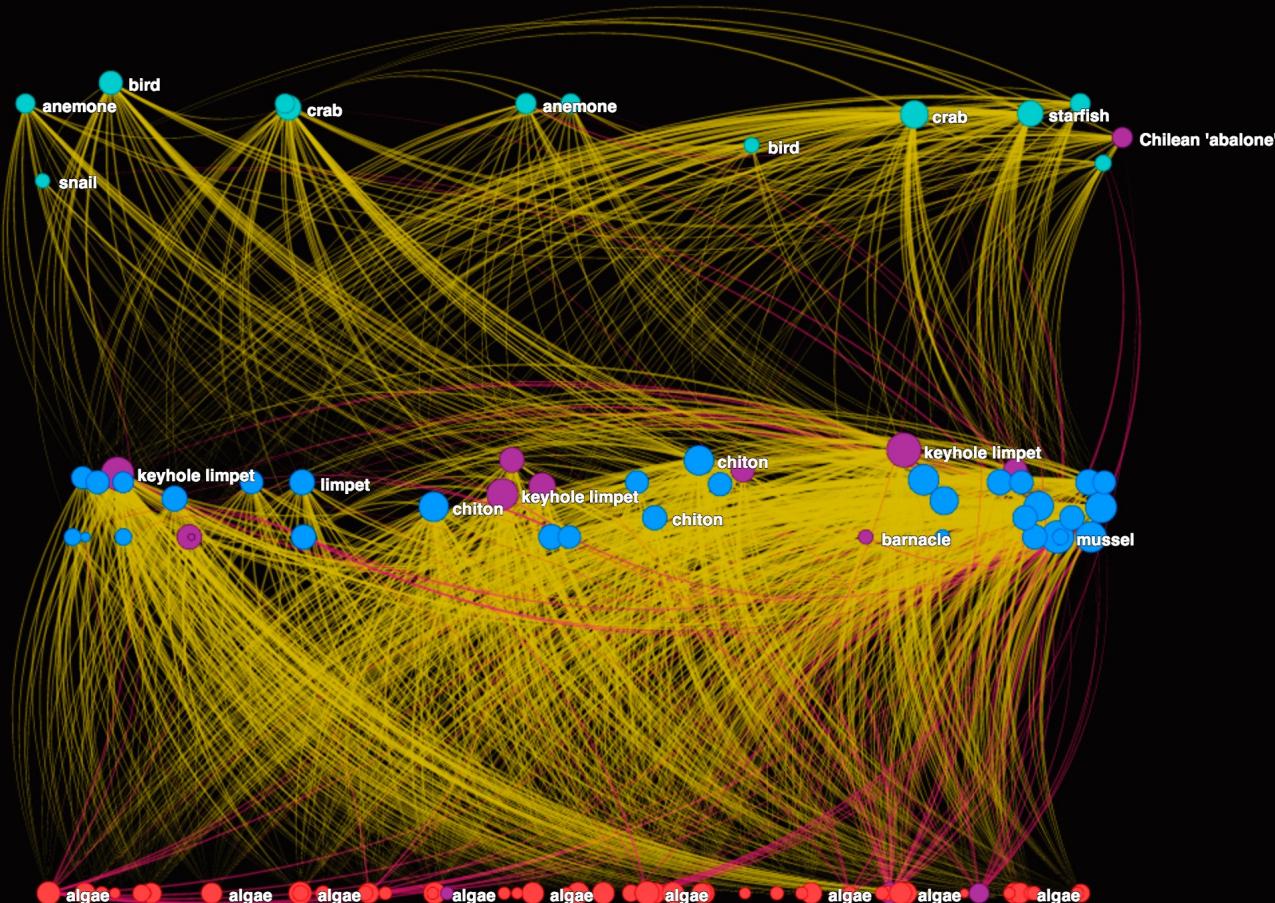
TL

Rand

NODES 104	
46	Basal
32	Intermediate
12	Top
14	zHarvested

1 2

# CHILEAN MARINE ECOLOGICAL NETWORK



NODES 104

46	Basal
32	Intermediate
12	Top
14	zHarvested

EDGES 1611

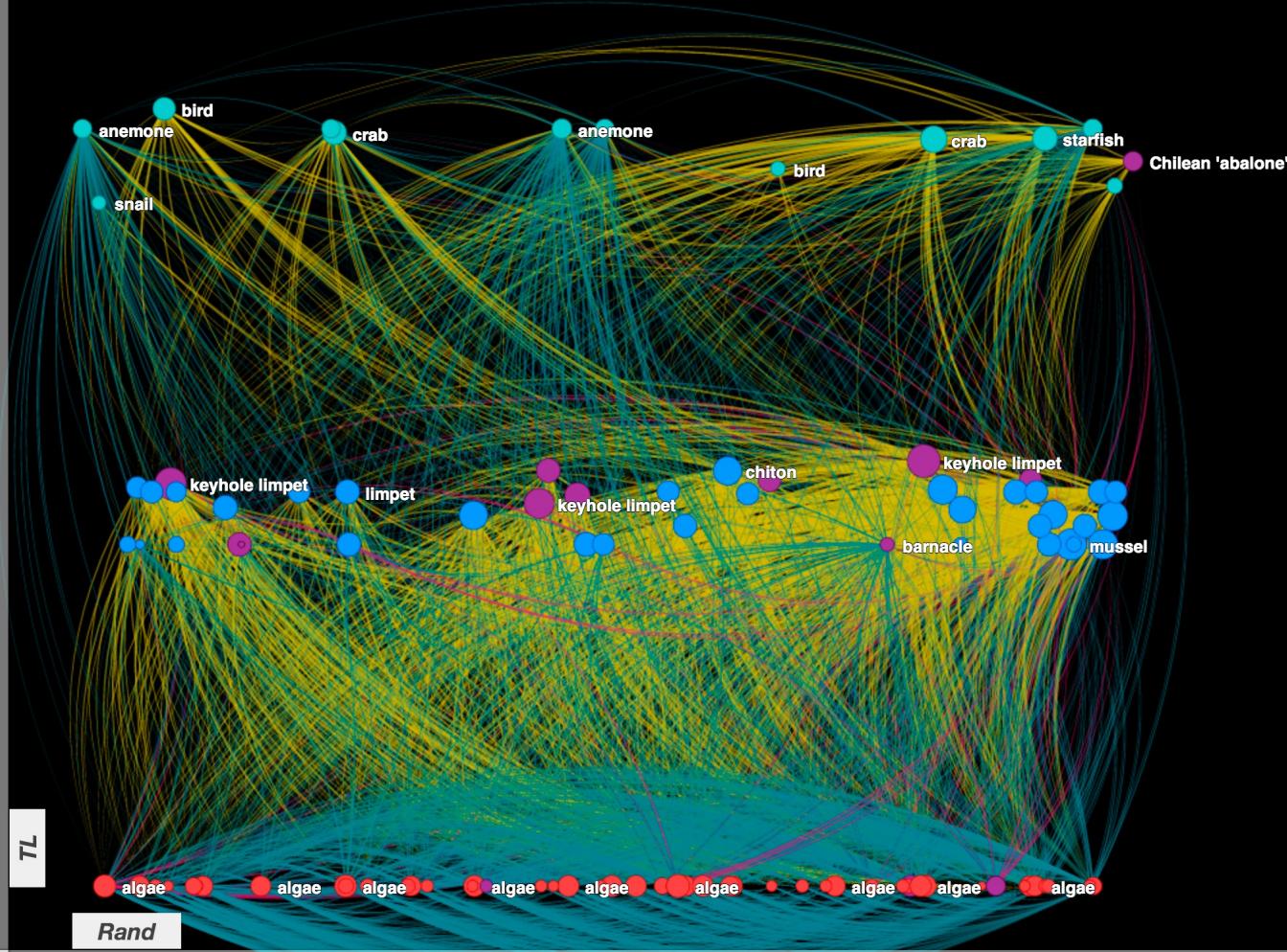
1456	Feeding
155	Non-Feeding Positive

1 2 3

TL

Rand

# CHILEAN MARINE ECOLOGICAL NETWORK



NODES 104	
46	Basal
32	Intermediate
12	Top
14	zHarvested
EDGES 4720	
1424	Feeding
3141	Non-Feeding Negative
155	Non-Feeding Positive

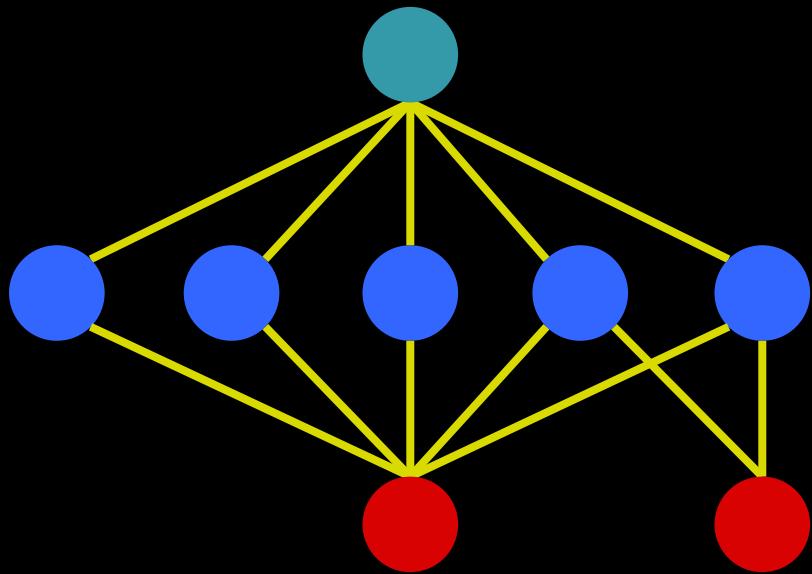
1 2 3

Do species collapse into a smaller set of  
multiplex clusters?

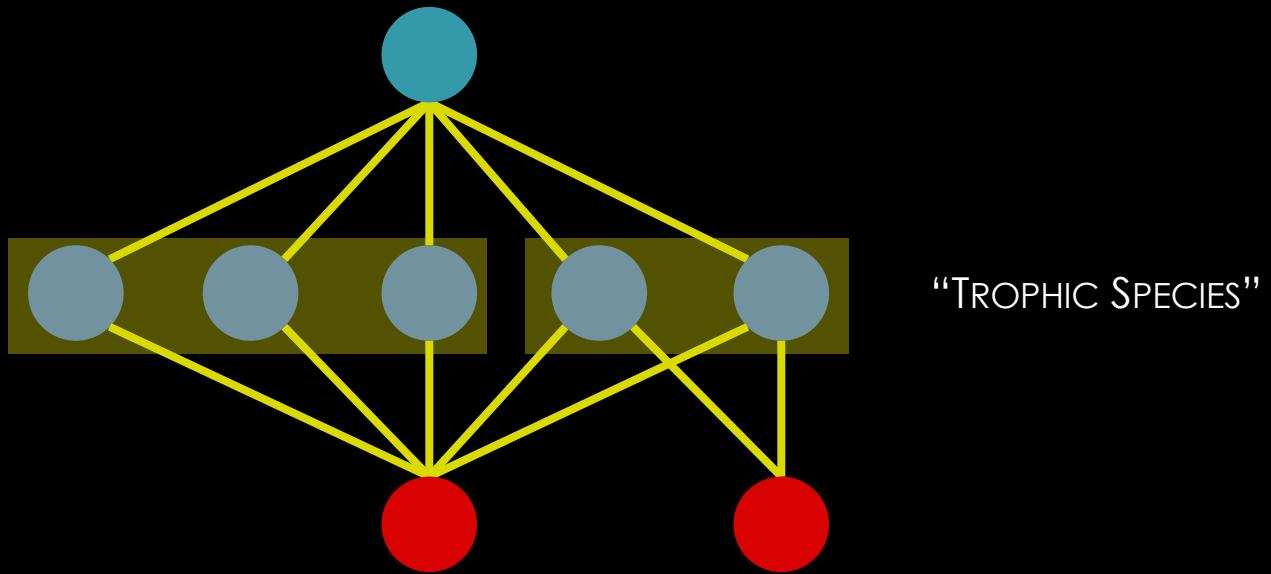
# stochastic block model

Newman and Leicht 2007  
Daudin *et al.* 2008  
Miele *et al.* 2014

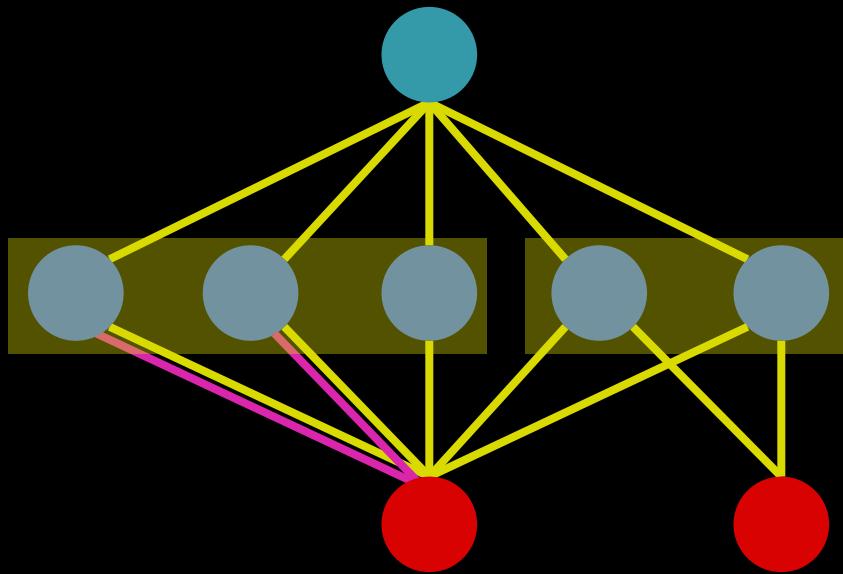
 FEEDING



 FEEDING



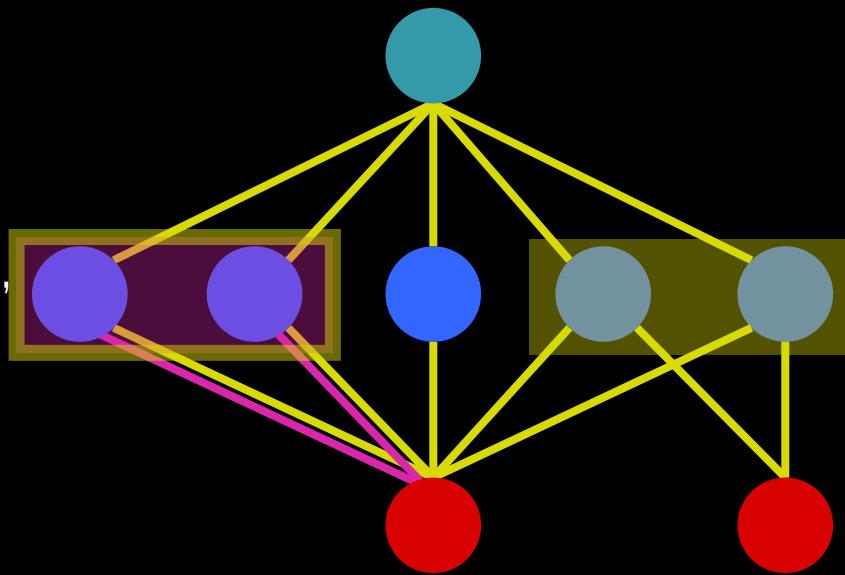
 FEEDING  
 FACILITATION



“TROPHIC SPECIES”  
(1 DIMENSION)

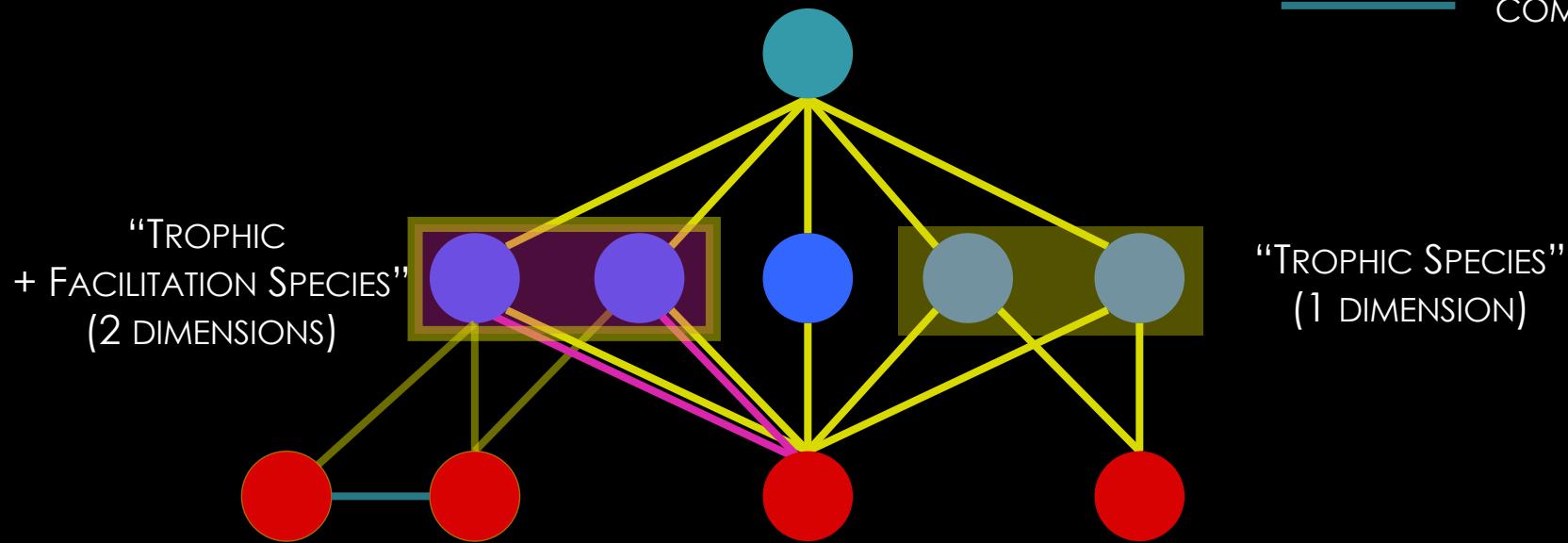
 FEEDING  
 FACILITATION

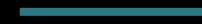
“TROPHIC  
+ FACILITATION SPECIES”  
(2 DIMENSIONS)

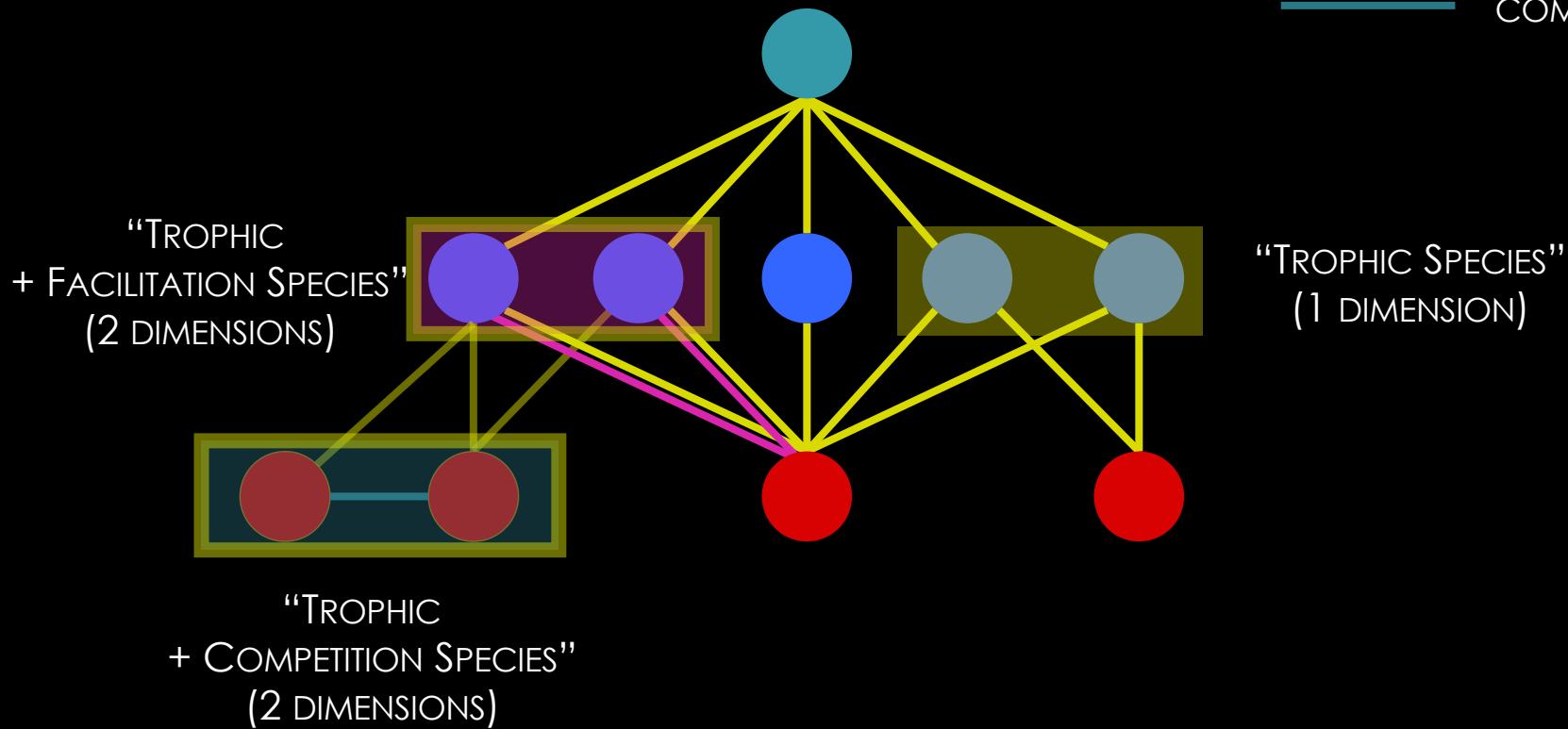


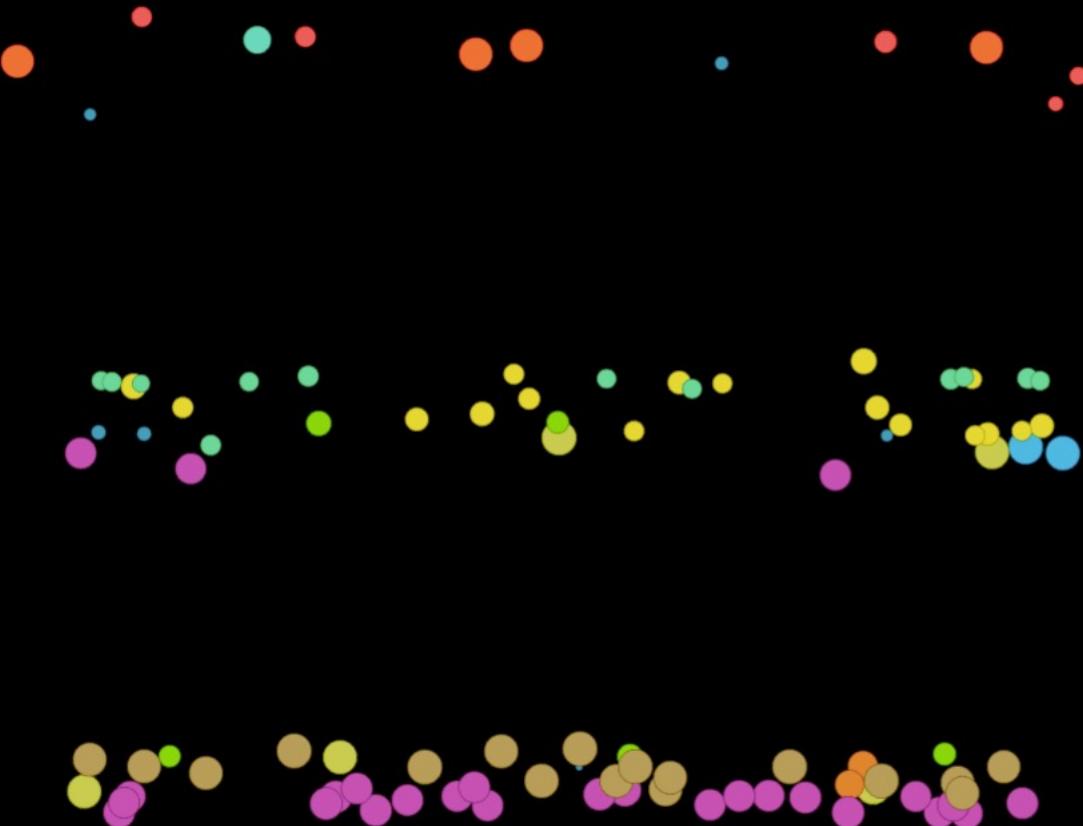
“TROPHIC SPECIES”  
(1 DIMENSION)

 FEEDING  
 FACILITATION  
 COMPETITION



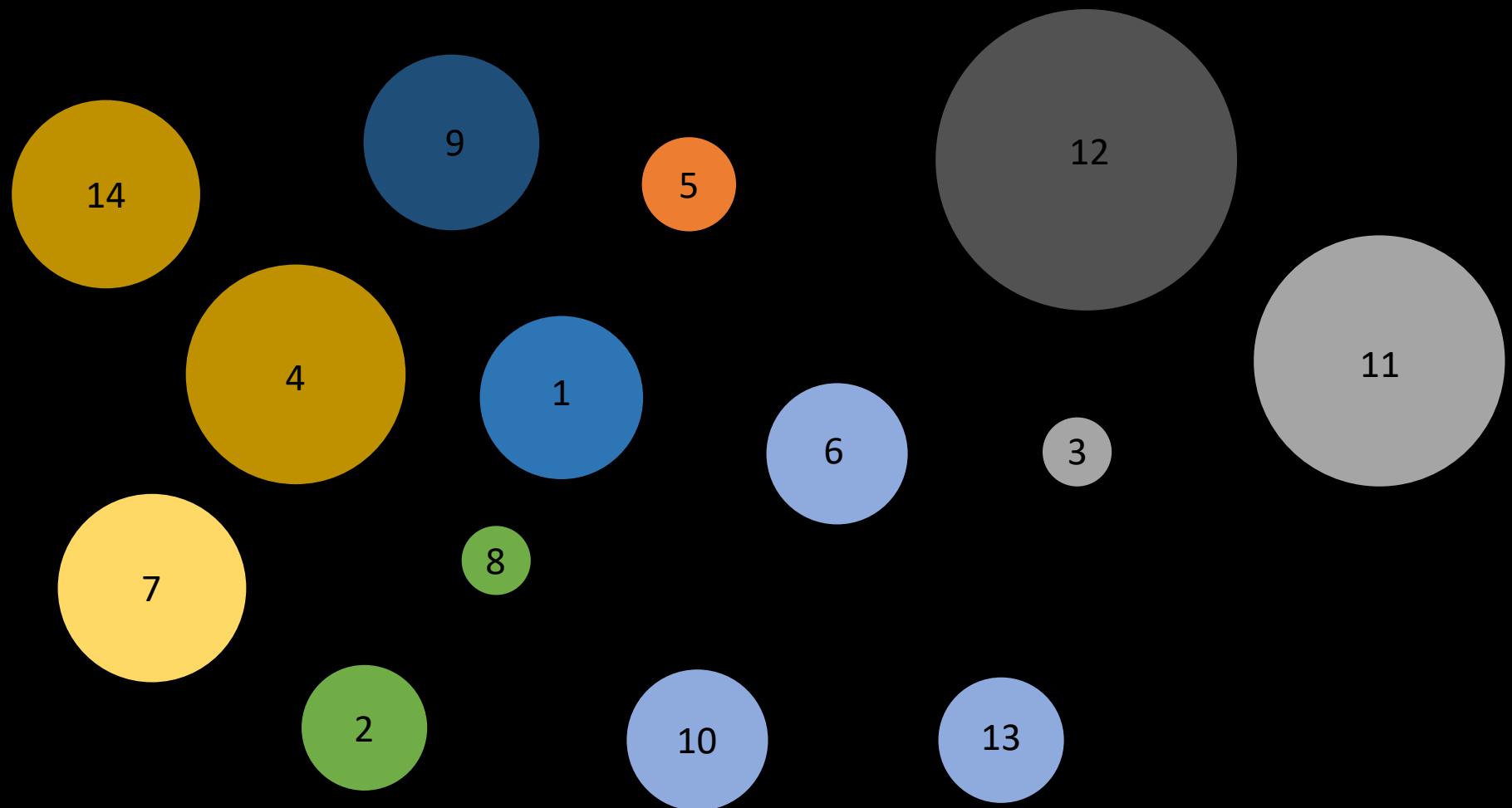
 FEEDING  
 FACILITATION  
 COMPETITION





1 2 3 4 5





Trophic Out

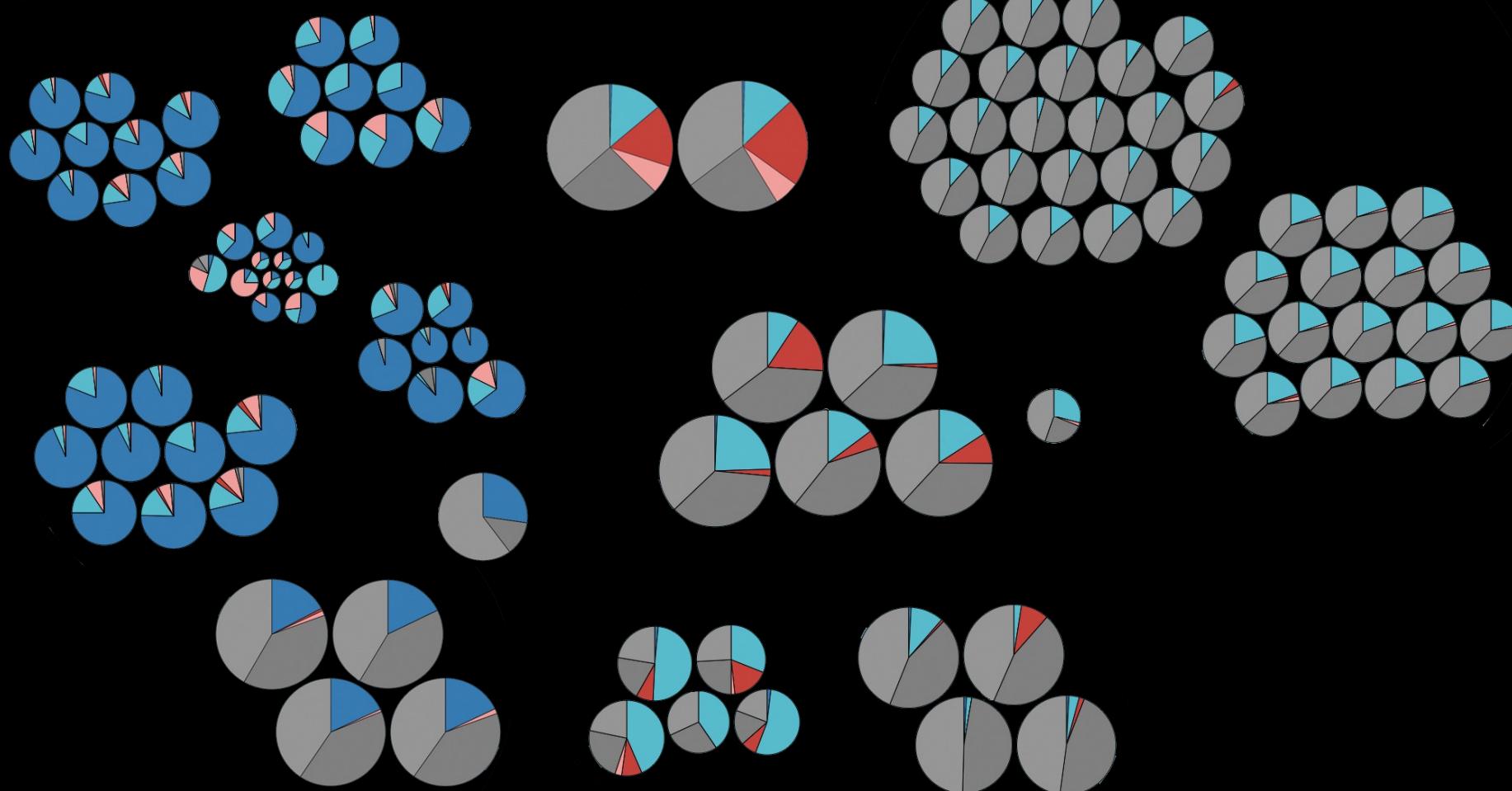
Trophic In

Positive Out

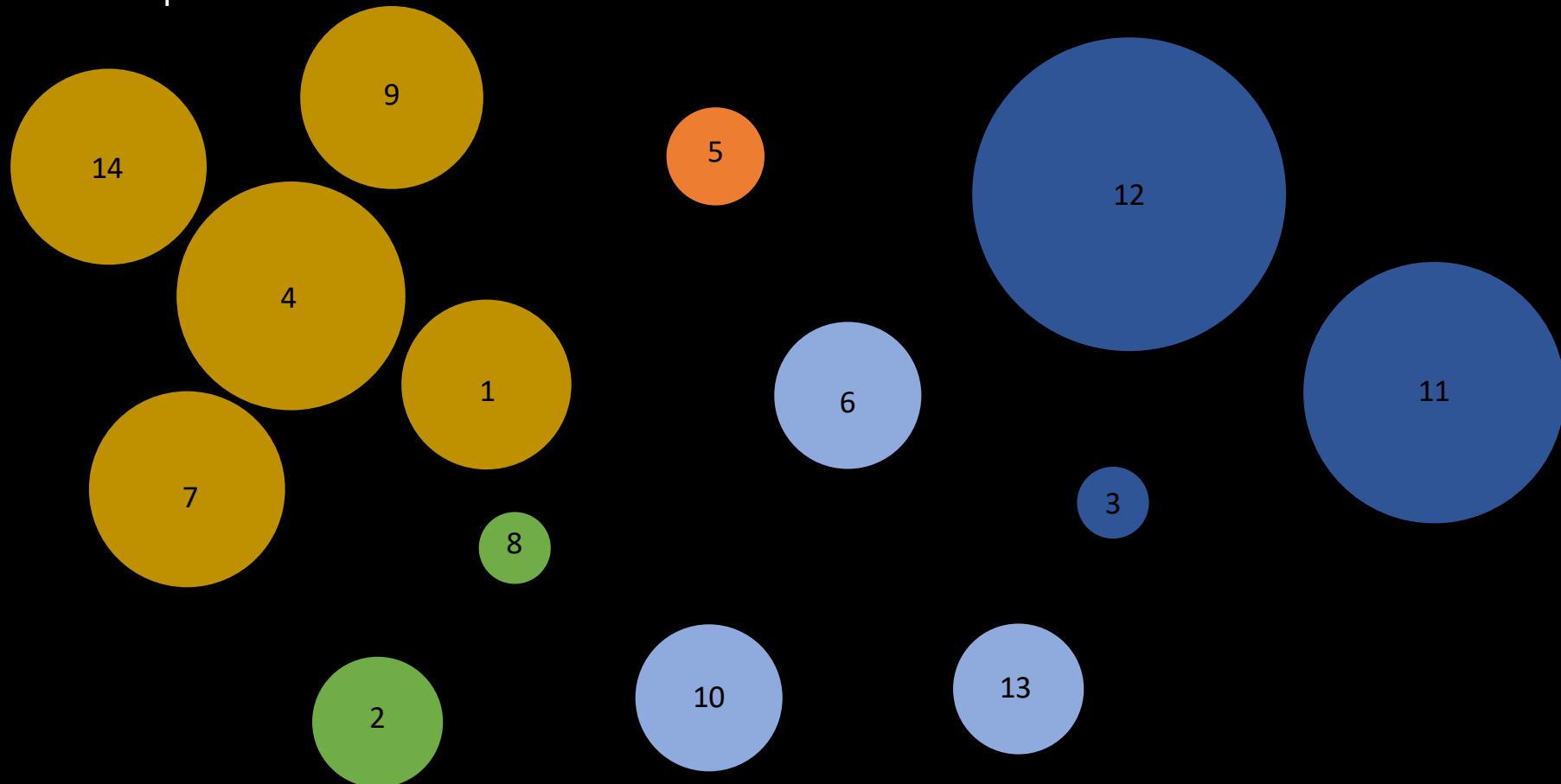
Positive In

Negative Out

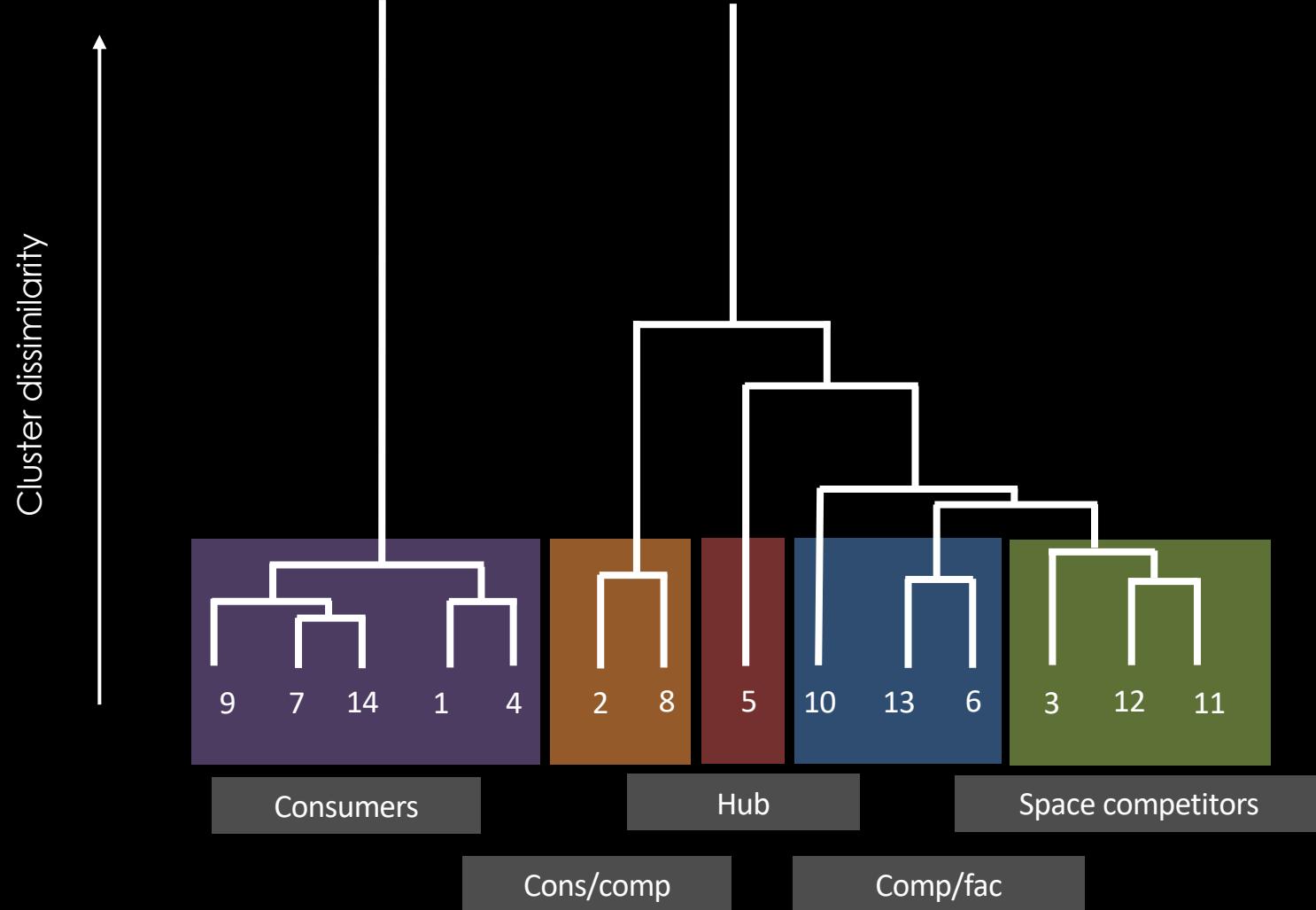
Negative In



# 14 multiplex clusters



Species collapse into a small set of  
multiplex clusters



What are the functional consequences of  
the 3-dimensional connectivity pattern?

dynamical model  
[bioenergetic consumer-resource model]  
+ non-trophic interactions

- Competition for space
- Predator interference
- Recruitment facilitation
- Refuge provisioning
- Positive and negative effects on survival

# Simulations

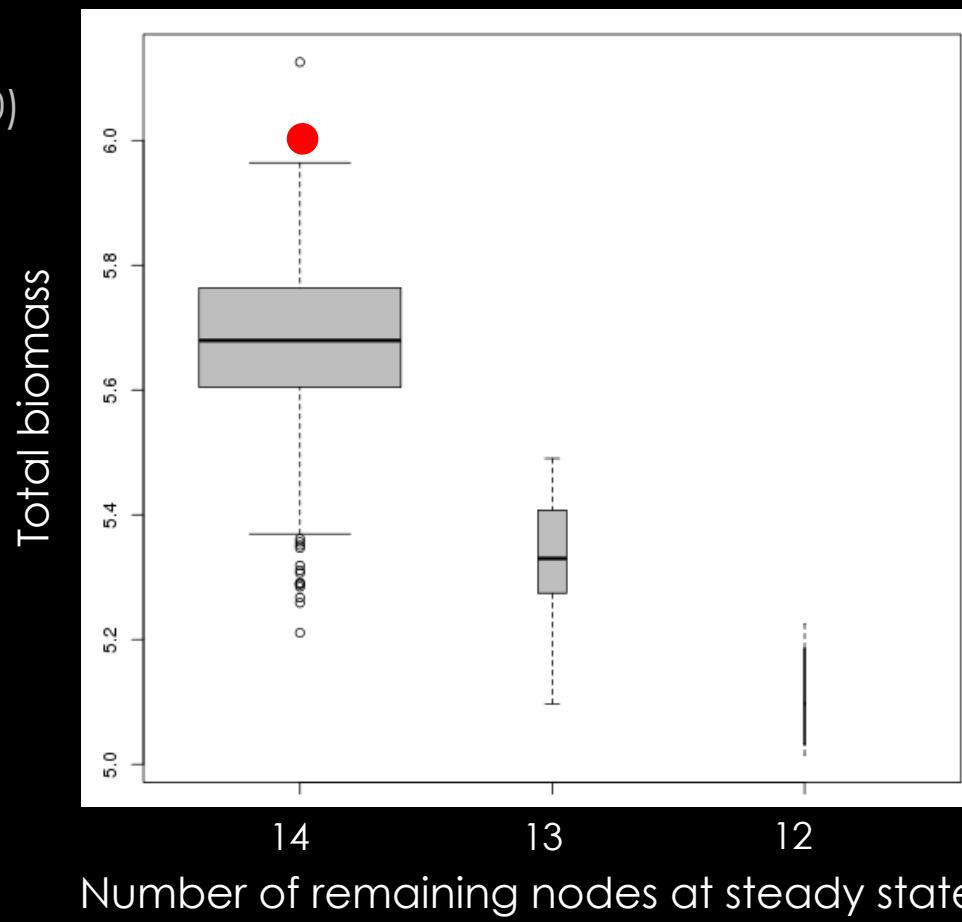
**14 nodes**  
('typical' species of  
the cluster)

- 
- (i) Connectivity of the Chilean web
  - (ii) 500 random networks  
(keep degree sequence)



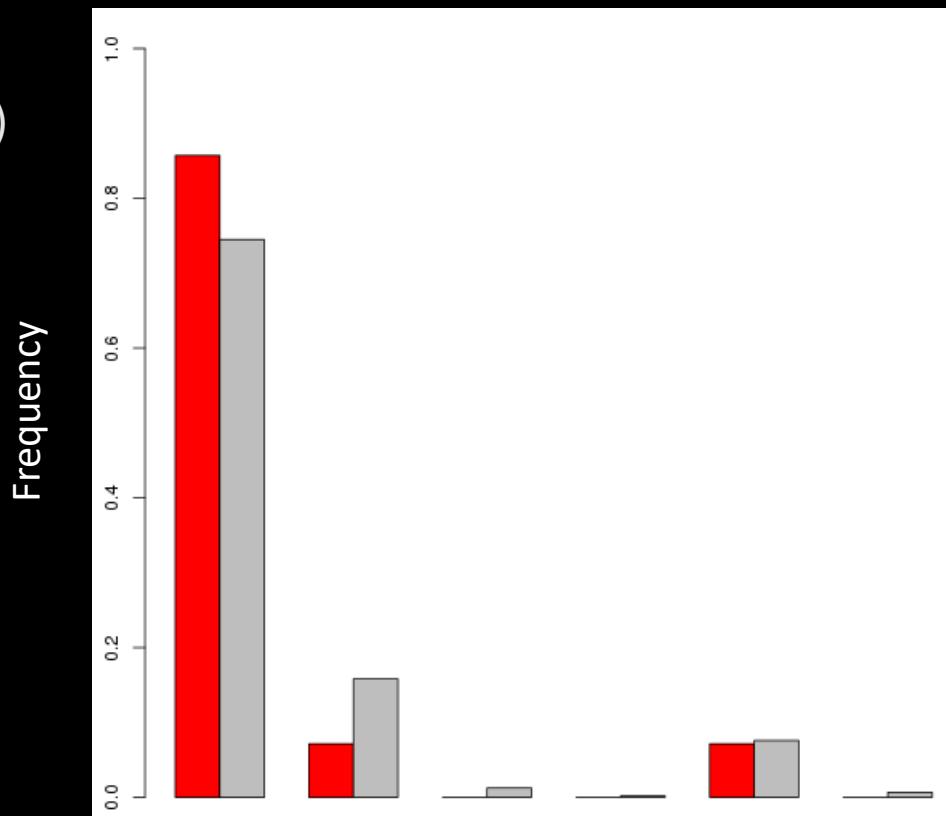
Calculate species diversity and total biomass

Chilean web  
Random webs (500)



Chilean web

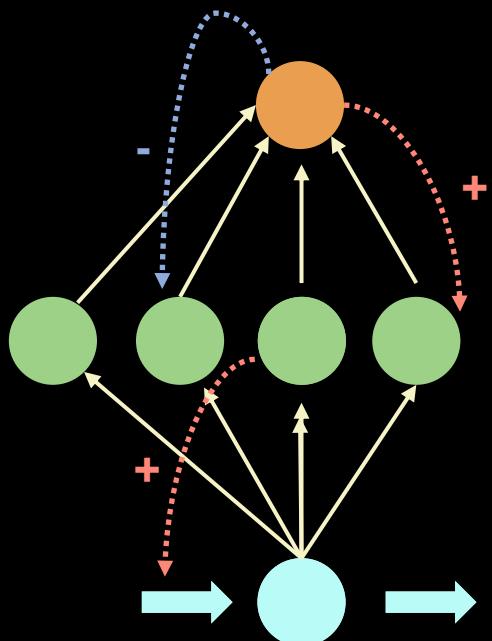
Random webs (500)



Differential number of clusters after primary extinction

The specific 3-dimentional signature of the clusters  
in the Chilean web promotes:

- high species persistence
- high total biomass
- tends to decrease the number of secondary extinctions

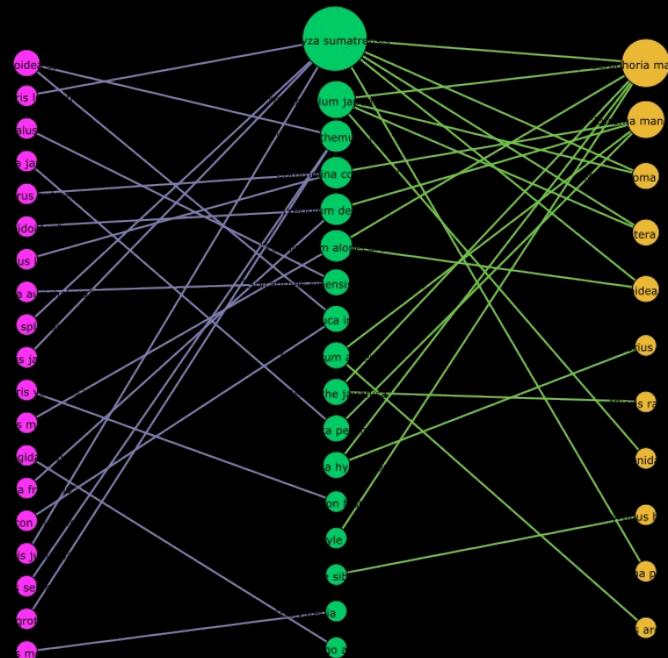


multiplex networks

Herbivores

Plants

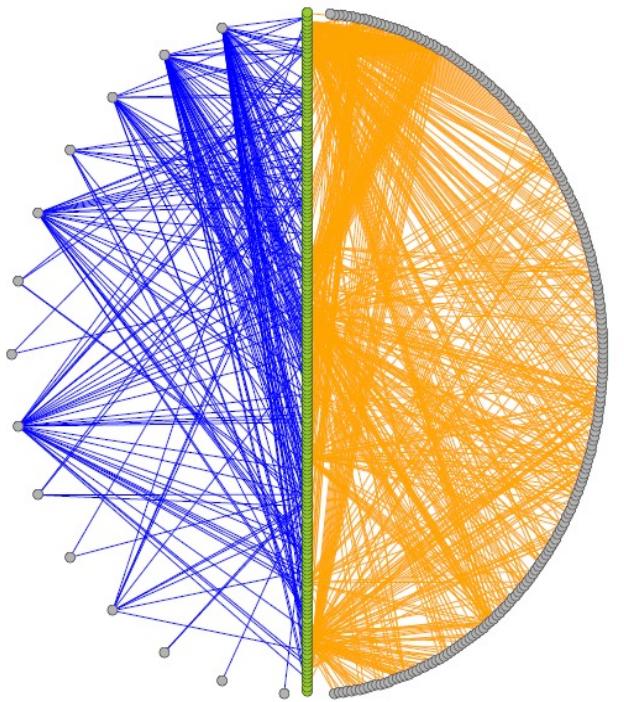
Pollinators



multipartite networks

# Doñana Biological Reserve, Spain

Antagonistic Plants Mutualistic



390 species  
(170 plants, 180 pollinators, 26 dispersors, 14  
herbivores)

## 2 layers

798 interactions (578 mutualistic, 220 antagonistic)

binary and quantitative links

# Doñana Biological Reserve, Spain

**How are different interactions combined in natural communities?  
How does that affect stability?**

**Two metrics:**

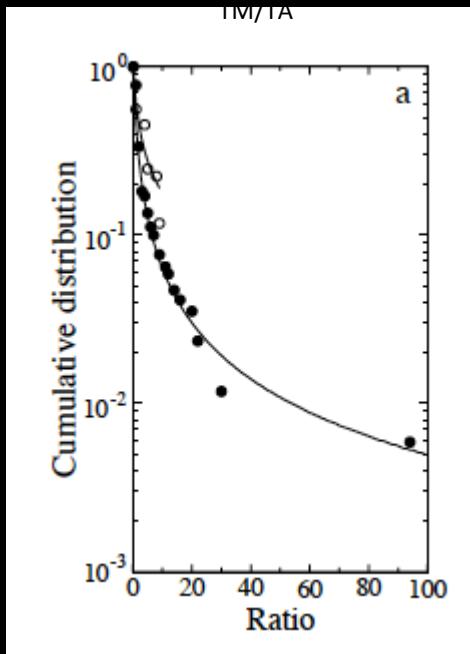
- the presence of the simplest module  
(a plant with a mutualistic and an antagonistic link)
- the ratio of the total number of mutualistic to antagonistic interactions per plant species, TM/TA

Null model:

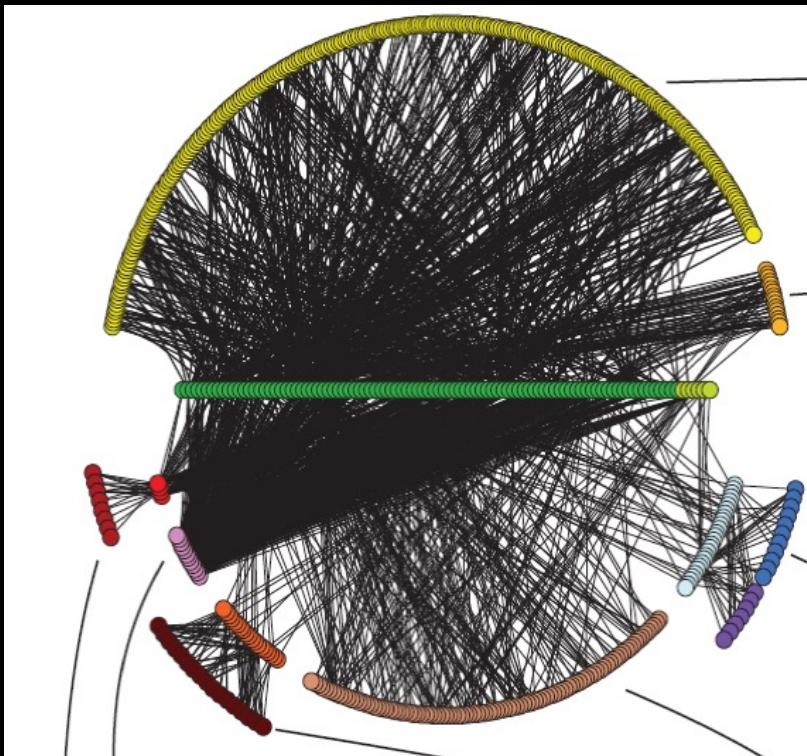
randomize links keeping the nb of links of animal constant (i.e. randomization with respect to the plants)

# Doñana Biological Reserve, Spain

- a few plants are involved in many modules and have a high ratio TM/TA
- very heterogeneous multilayer role of species
- promotes diversity (model)



# Norwood farm, Somerset, UK



560 taxa  
(plants + 11 groups of animals)

## 7 sub-networks

1501 interactions (trophic, mutualistic, parasitic)

# Norwood farm, Somerset, UK

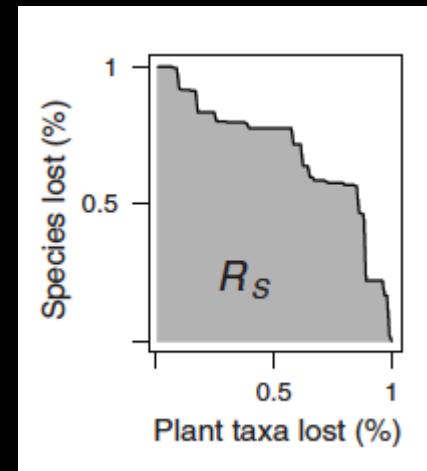
**How does the robustness of different species interaction networks vary?**

**robustness:**

sequential (random) removal of plant species

→ some sub-networks (layers) are more robust than others

→ Identification of **keystone plants** (that have the most important cascading effects)



# Key results

- Different layers have different structural properties
  - Different layers have different robustness
  - → id of key species that create a disprop amount of secondary extinctions
- 
- species have different roles in different layers
  - A few species have disproportional multiplex roles

multi-interaction networks

multilayer ecological networks

temporal networks

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RESEARCH ARTICLE

Journal of Animal Ecology



## Core-periphery dynamics in a plant-pollinator network

Vincent Miele<sup>1</sup> | Rodrigo Ramos-Jiliberto<sup>2</sup> | Diego P. Vázquez<sup>3,4,5</sup>

### How does species role change through time?

Dynamic stochastic Block model (on 6 years of data)

- Core-periphery structure stable through time
- But role of species variable through time

spatial networks

ARTICLE

DOI: [10.1038/s41467-017-02658-y](https://doi.org/10.1038/s41467-017-02658-y)

OPEN

# Multilayer networks reveal the spatial structure of seed-dispersal interactions across the Great Rift landscapes

Sérgio Timóteo<sup>1</sup>, Marta Correia<sup>1</sup>, Susana Rodríguez-Echeverría<sup>1</sup>, Helena Freitas<sup>1</sup> & Ruben Heleno<sup>1</sup>

seed-dispersal interactions across the Gorongosa National Park, Mozambique

- id of highly versatile species that disperse many plant species across multiple habitats
- Not predicted by monolayer approaches

# « Complexity begets stability »

Odum 1953  
MacArthur 1955  
Elton 1958



Robert May

PRINCETON  
LANDMARKS  
IN BIOLOGY

STABILITY AND  
COMPLEXITY IN  
**M O D E L  
ECOSYSTEMS**



WITH A NEW INTRODUCTION BY THE AUTHOR

ROBERT M.  
**MAY**

« In general mathematical models of multispecies communities, complexity tends to beget instability »

Robert May, 1973

« The task, therefore, is to elucidate the **devious strategies** which make for stability in enduring natural systems »

COMPLEX ECOLOGICAL COMMUNITIES  
MANY SPECIES  
MANY INTERACTION TYPES  
SPATIO-TEMPORAL DYNAMICS

Thank you very much for your attention



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