

The Demographic Transition

Ömer Özak

Department of Economics
Southern Methodist University

Economic Growth and Comparative Development

Phases of Development: Standard of Living

- The Malthusian Epoch

Phases of Development: Standard of Living

- The Malthusian Epoch
- The Post-Malthusian Regime

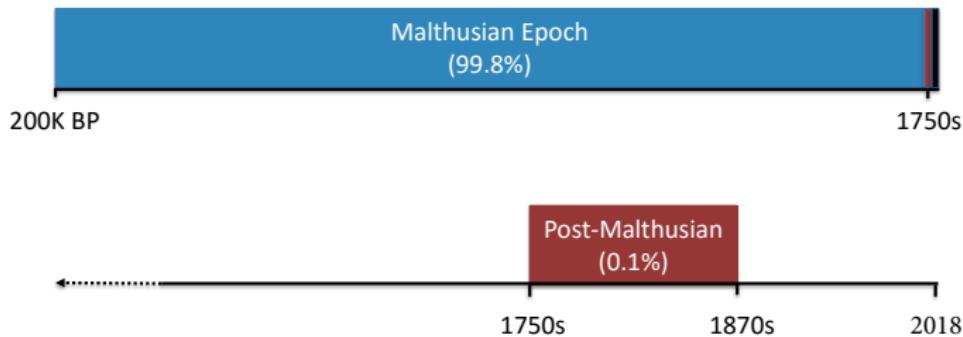
Phases of Development: Standard of Living

- The Malthusian Epoch
- The Post-Malthusian Regime
- The Modern Growth Regime

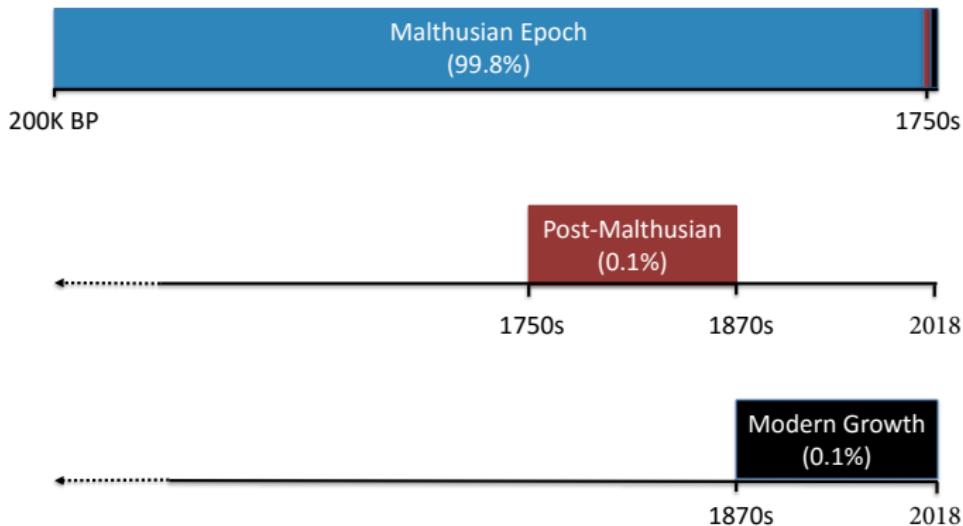
Phases of Development: Timeline of the Most Developed Economies



Phases of Development: Timeline of the Most Developed Economies



Phases of Development: Timeline of the Most Developed Economies



The Demographic Transition

- The positive relationship between income and population is reversed

The Demographic Transition

- The positive relationship between income and population is reversed
- Fertility, mortality and population growth decline very rapidly

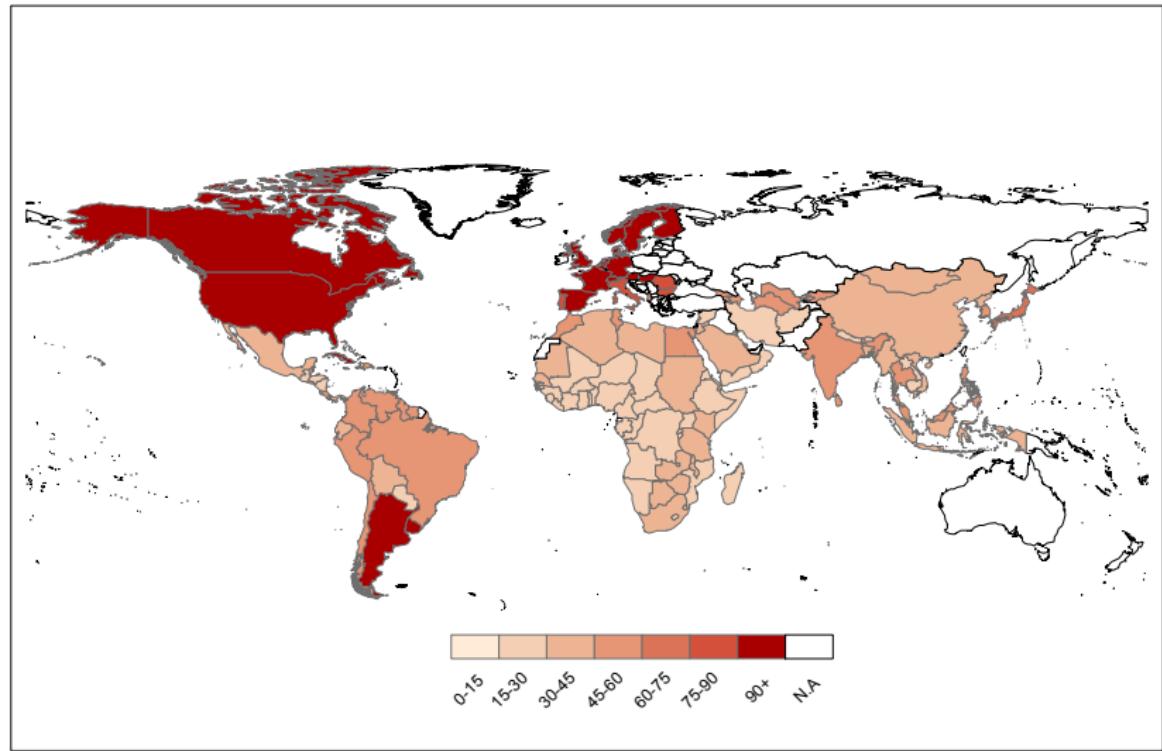
The Demographic Transition

- The positive relationship between income and population is reversed
- Fertility, mortality and population growth decline very rapidly
- The impact of technological progress on output per capita are no longer counterbalanced by population growth

The Demographic Transition

- The positive relationship between income and population is reversed
- Fertility, mortality and population growth decline very rapidly
- The impact of technological progress on output per capita are no longer counterbalanced by population growth
- Transition to Modern Growth

Variation in years elapsed since the Onset of the Fertility Decline



The Demographic Transition – Definitions

- Crude Birth Rate (CBR) or Birth Rate

The Demographic Transition – Definitions

- Crude Birth Rate (CBR) or Birth Rate
 - total number of live births per 1,000 in a population in a period

The Demographic Transition – Definitions

- Crude Birth Rate (CBR) or Birth Rate
 - total number of live births per 1,000 in a population in a period
- Crude Death Rate (CDR) or Death Rate

The Demographic Transition – Definitions

- Crude Birth Rate (CBR) or Birth Rate
 - total number of live births per 1,000 in a population in a period
- Crude Death Rate (CDR) or Death Rate
 - total number of deaths per 1,000 in a population in a period

The Demographic Transition – Definitions

- Crude Birth Rate (CBR) or Birth Rate
 - total number of live births per 1,000 in a population in a period
- Crude Death Rate (CDR) or Death Rate
 - total number of deaths per 1,000 in a population in a period
- Rate of Natural Increase (RNI)

The Demographic Transition – Definitions

- Crude Birth Rate (CBR) or Birth Rate
 - total number of live births per 1,000 in a population in a period
- Crude Death Rate (CDR) or Death Rate
 - total number of deaths per 1,000 in a population in a period
- Rate of Natural Increase (RNI)

$$RNI = CBR - CDR$$

The Demographic Transition – Definitions

- Crude Birth Rate (CBR) or Birth Rate
 - total number of live births per 1,000 in a population in a period
- Crude Death Rate (CDR) or Death Rate
 - total number of deaths per 1,000 in a population in a period
- Rate of Natural Increase (RNI)

$$RNI = CBR - CDR$$

⇒ population growth excluding migration

The Demographic Transition – Definitions

- Total Fertility Rate (TFR)

The Demographic Transition – Definitions

- Total Fertility Rate (TFR)
 - average number of children that would be born to a woman over her lifetime if

The Demographic Transition – Definitions

- Total Fertility Rate (TFR)

- average number of children that would be born to a woman over her lifetime if
 - She experienced the exact current age-specific fertility rates through her lifetime

The Demographic Transition – Definitions

- Total Fertility Rate (TFR)

- average number of children that would be born to a woman over her lifetime if
 - She experienced the exact current age-specific fertility rates through her lifetime
 - She survived from birth to the end of her reproductive life (15-44/9)

The Demographic Transition – Definitions

- Total Fertility Rate (TFR)
 - average number of children that would be born to a woman over her lifetime if
 - She experienced the exact current age-specific fertility rates through her lifetime
 - She survived from birth to the end of her reproductive life (15-44/9)
- Net reproduction rate (NRR)

The Demographic Transition – Definitions

- Total Fertility Rate (TFR)

- average number of children that would be born to a woman over her lifetime if
 - She experienced the exact current age-specific fertility rates through her lifetime
 - She survived from birth to the end of her reproductive life (15-44/9)

- Net reproduction rate (NRR)

- number of daughters a woman would have in her lifetime if she were subject to prevailing age-specific fertility and mortality rates in the given year

The Demographic Transition – Definitions

- Total Fertility Rate (TFR)

- average number of children that would be born to a woman over her lifetime if
 - She experienced the exact current age-specific fertility rates through her lifetime
 - She survived from birth to the end of her reproductive life (15-44/9)

- Net reproduction rate (NRR)

- number of daughters a woman would have in her lifetime if she were subject to prevailing age-specific fertility and mortality rates in the given year
 - She experienced the exact current age-specific fertility rates

The Demographic Transition – Definitions

- Total Fertility Rate (TFR)

- average number of children that would be born to a woman over her lifetime if
 - She experienced the exact current age-specific fertility rates through her lifetime
 - She survived from birth to the end of her reproductive life (15-44/9)

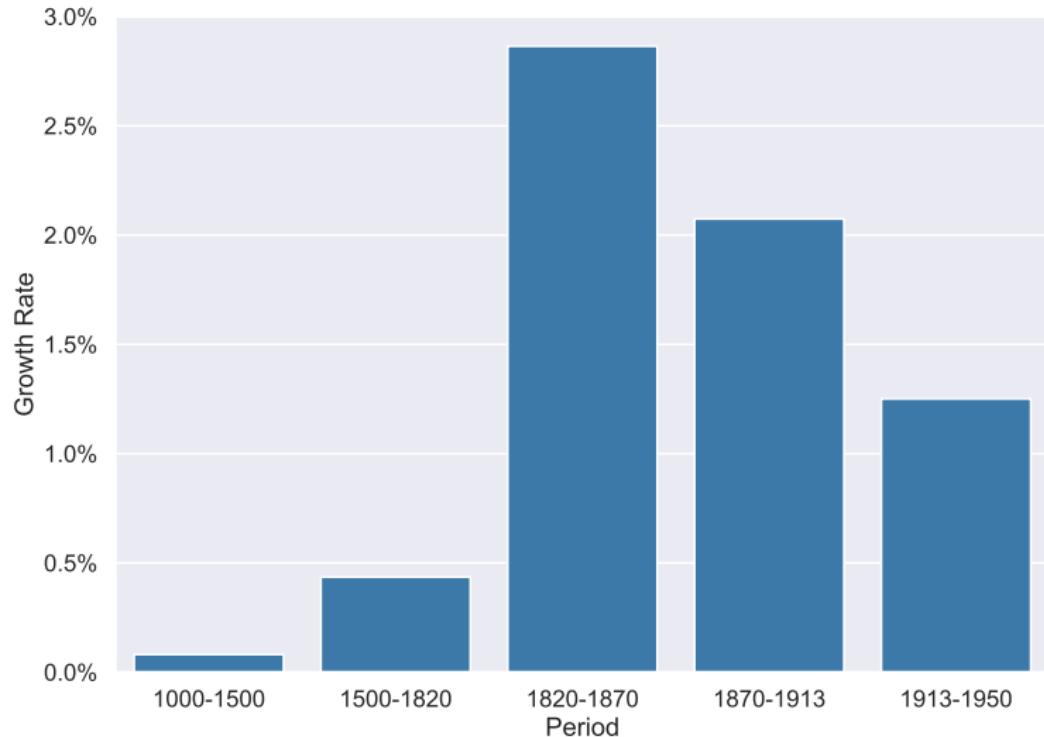
- Net reproduction rate (NRR)

- number of daughters a woman would have in her lifetime if she were subject to prevailing age-specific fertility and mortality rates in the given year
 - She experienced the exact current age-specific fertility rates
 - She experienced the exact current age-specific mortality rates

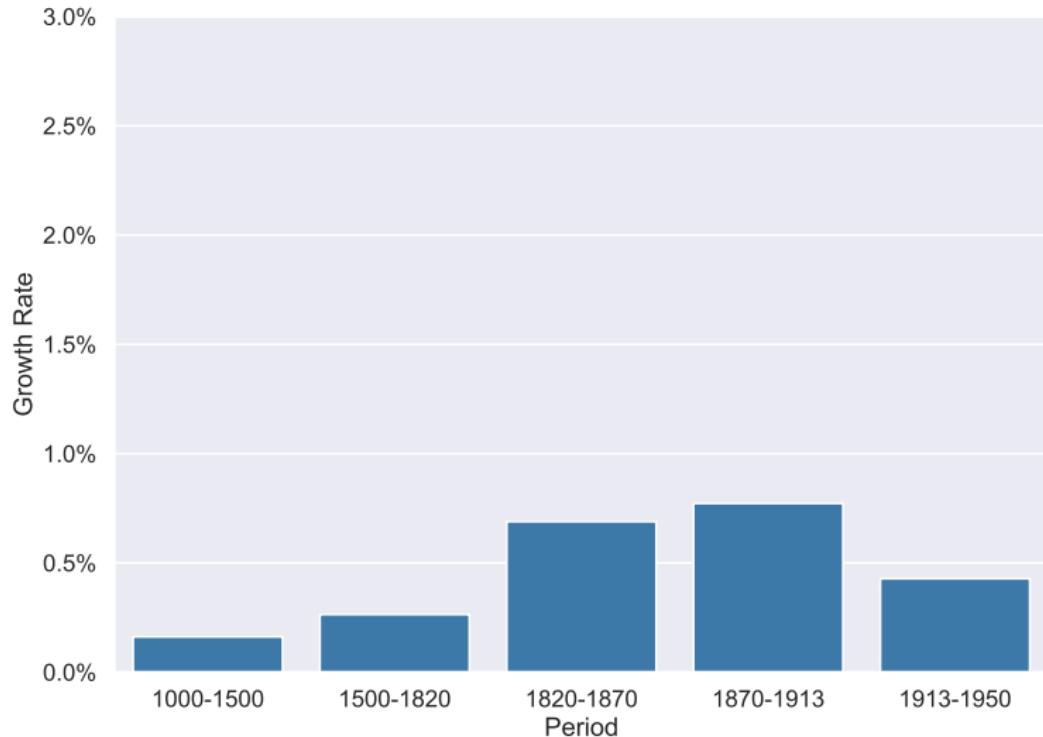
The Demographic Transition – Definitions

- Total Fertility Rate (TFR)
 - average number of children that would be born to a woman over her lifetime if
 - She experienced the exact current age-specific fertility rates through her lifetime
 - She survived from birth to the end of her reproductive life (15-44/9)
- Net reproduction rate (NRR)
 - number of daughters a woman would have in her lifetime if she were subject to prevailing age-specific fertility and mortality rates in the given year
 - She experienced the exact current age-specific fertility rates
 - She experienced the exact current age-specific mortality rates
- TFR & NRR are synthetic rates

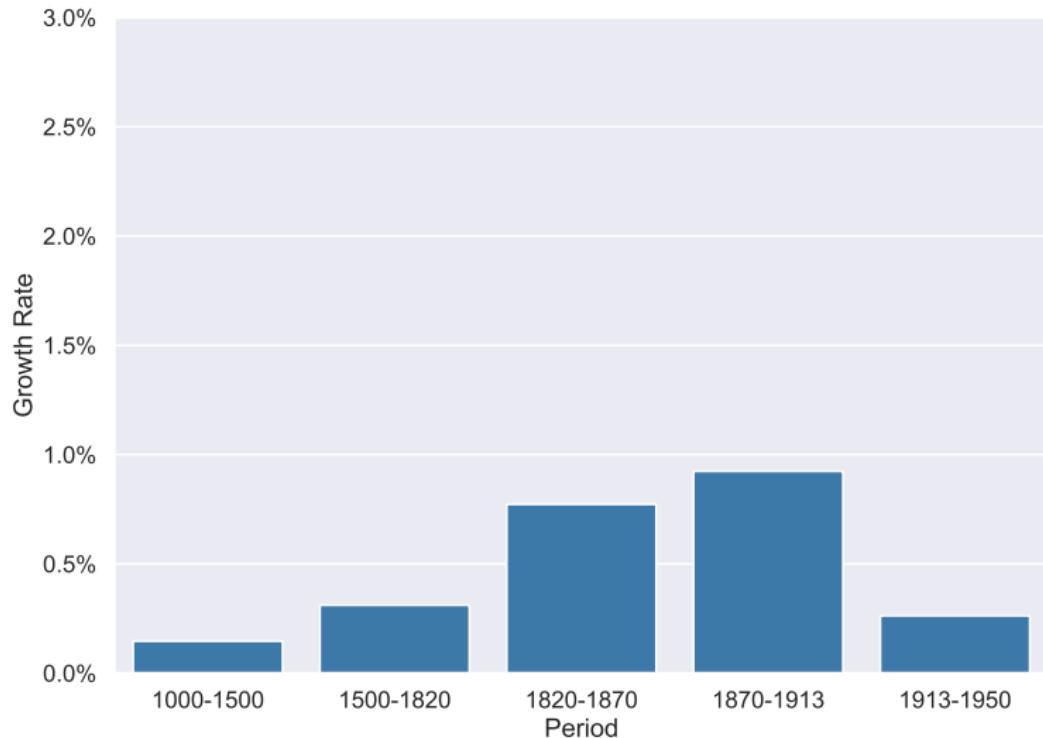
Early Fertility Decline – Western Offshoots



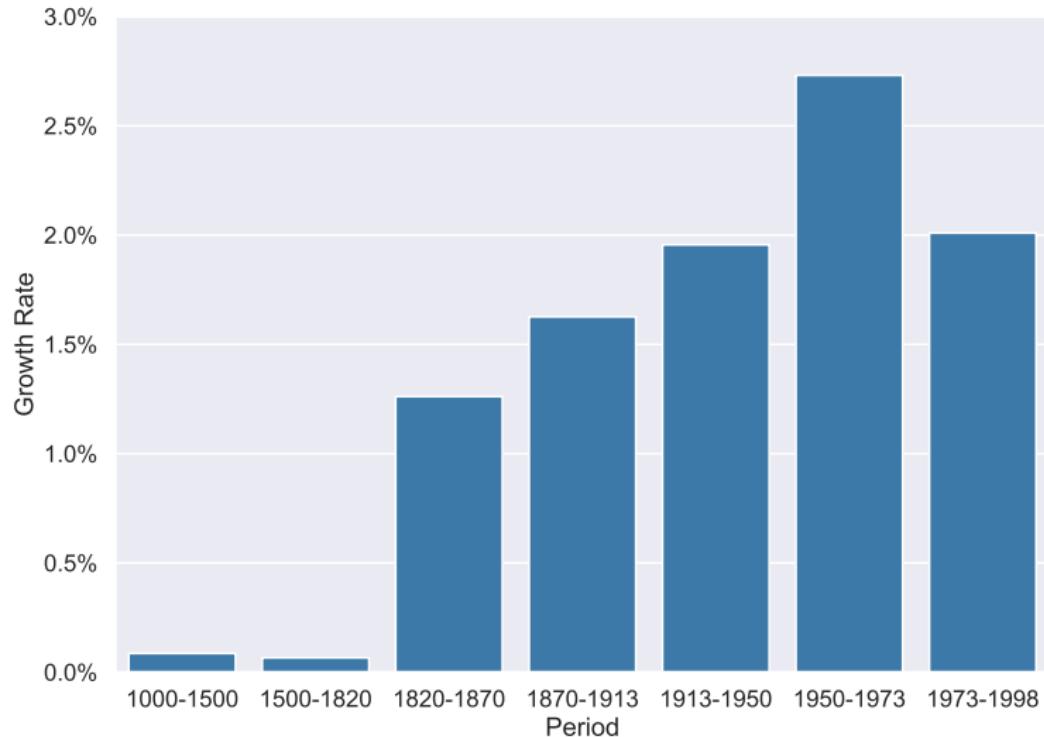
Early Fertility Decline – Western Europe



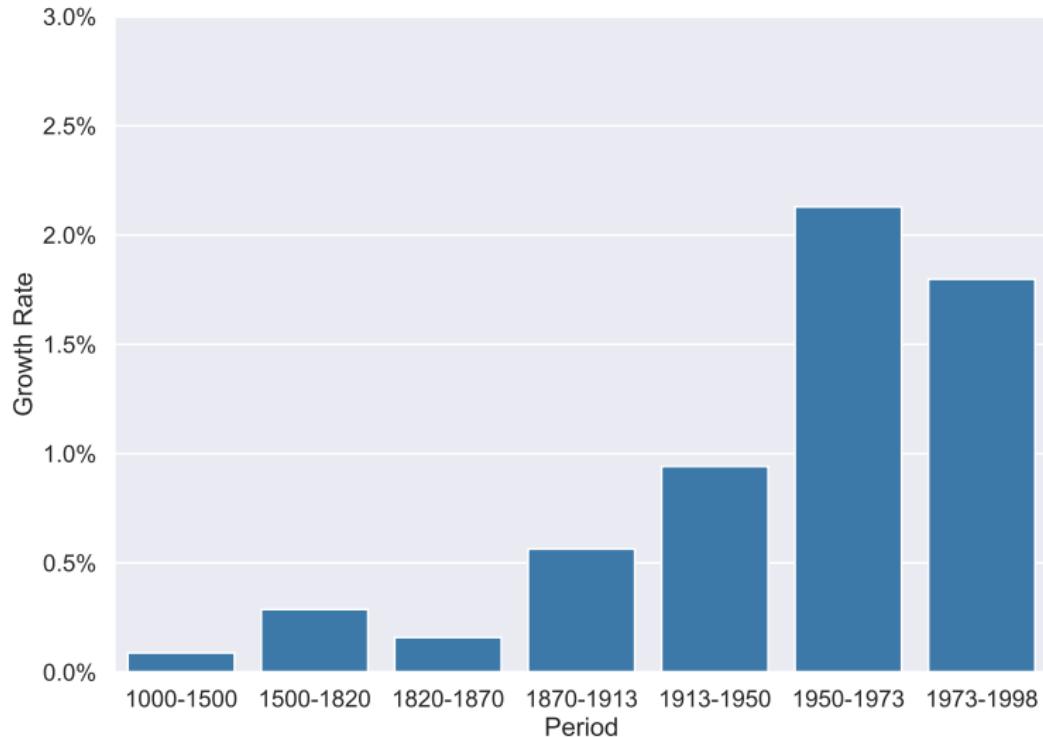
Early Fertility Decline – Eastern Europe



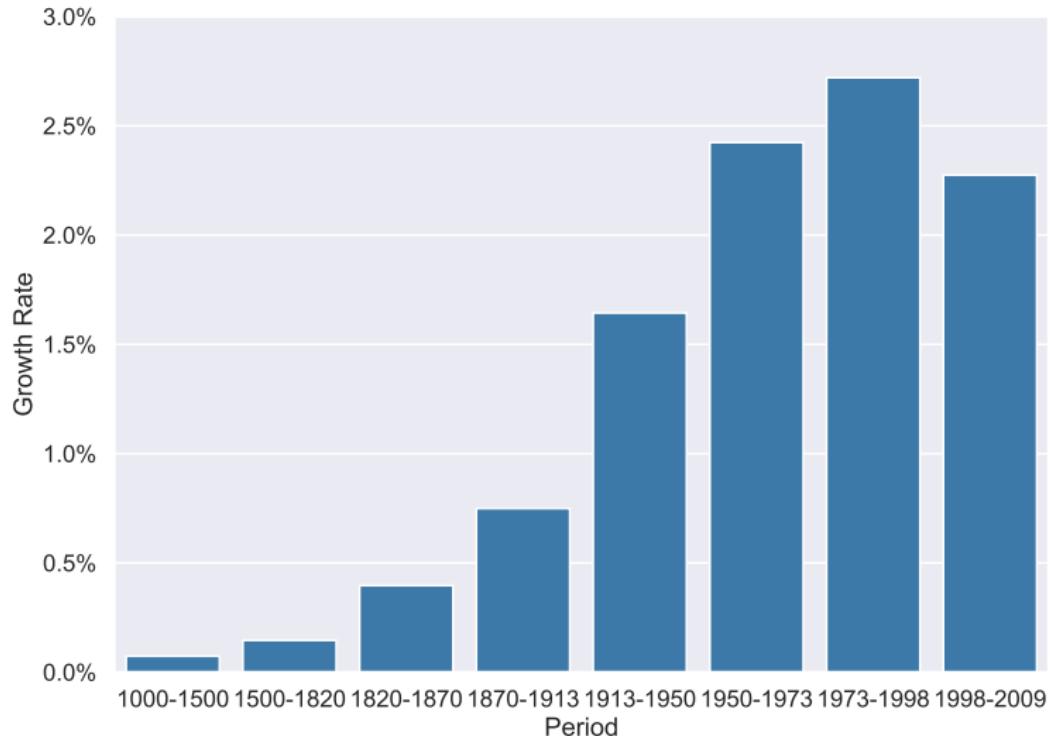
Late Fertility Decline – Latin America



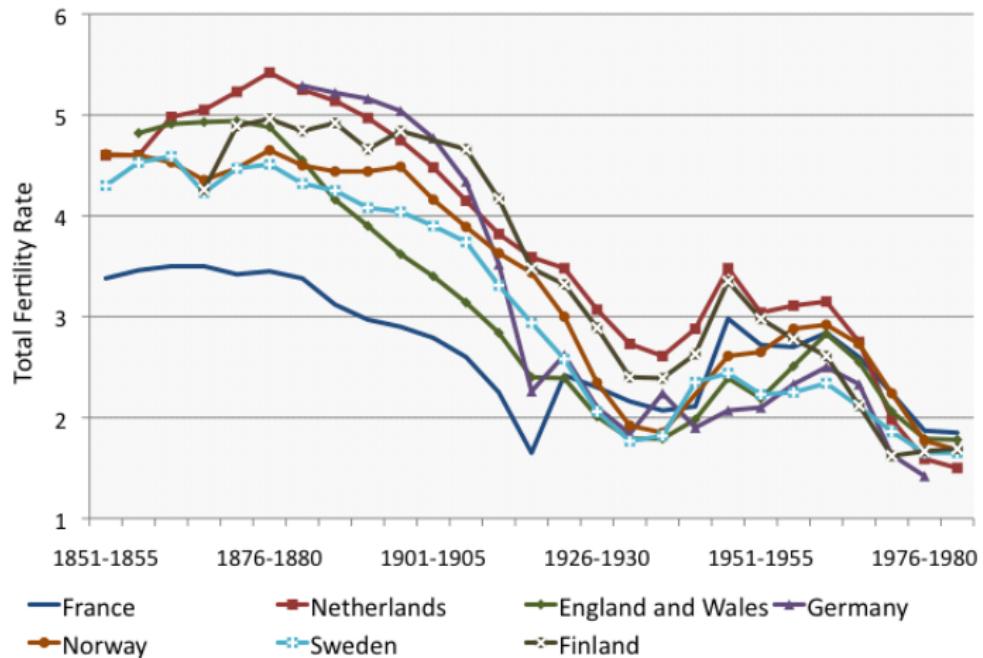
Late Fertility Decline – Asia



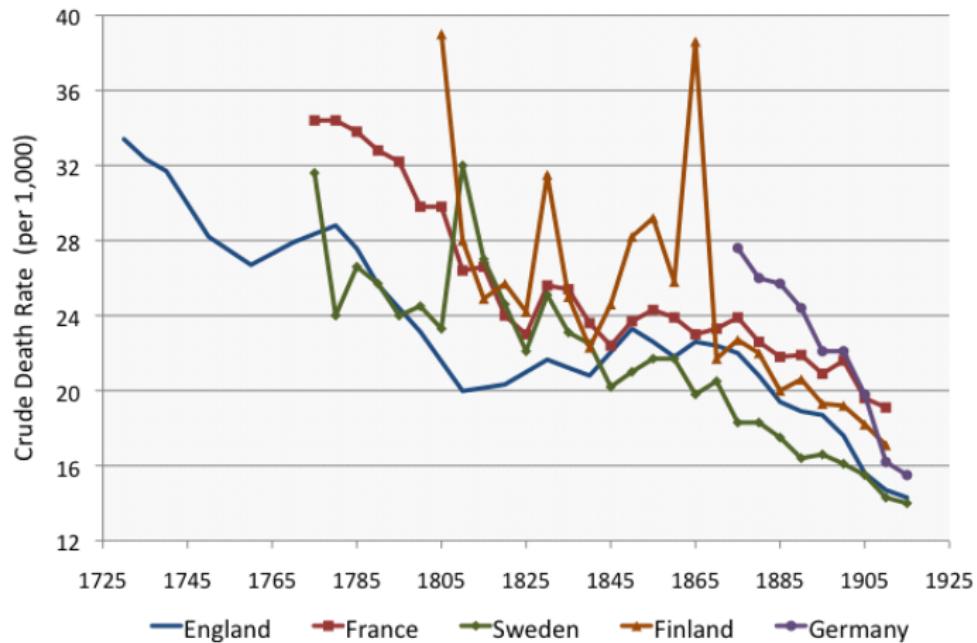
Late Fertility Decline – Africa



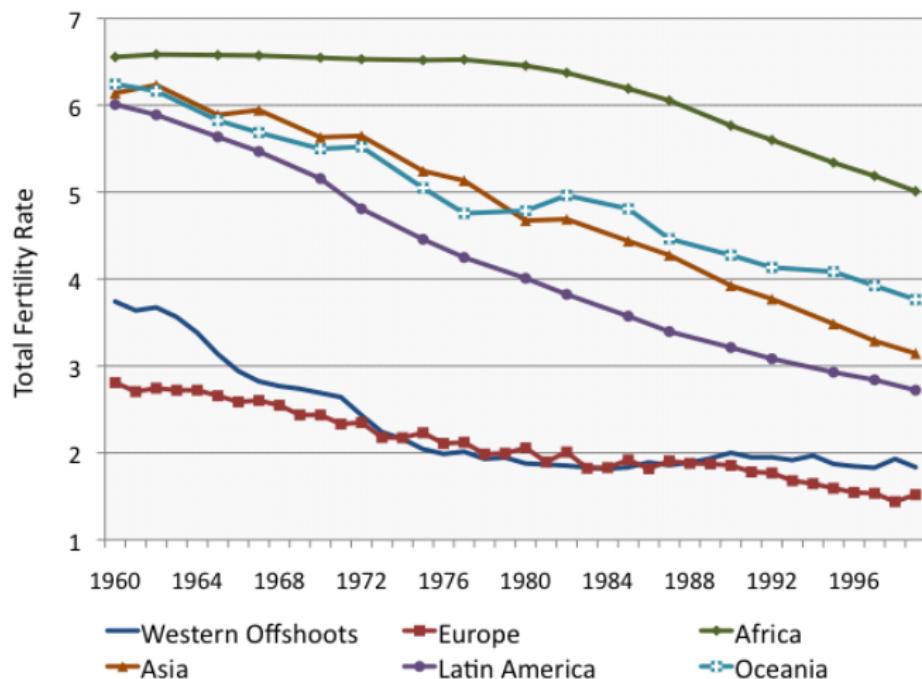
The Demographic Transition in Western Europe: Total Fertility Rates



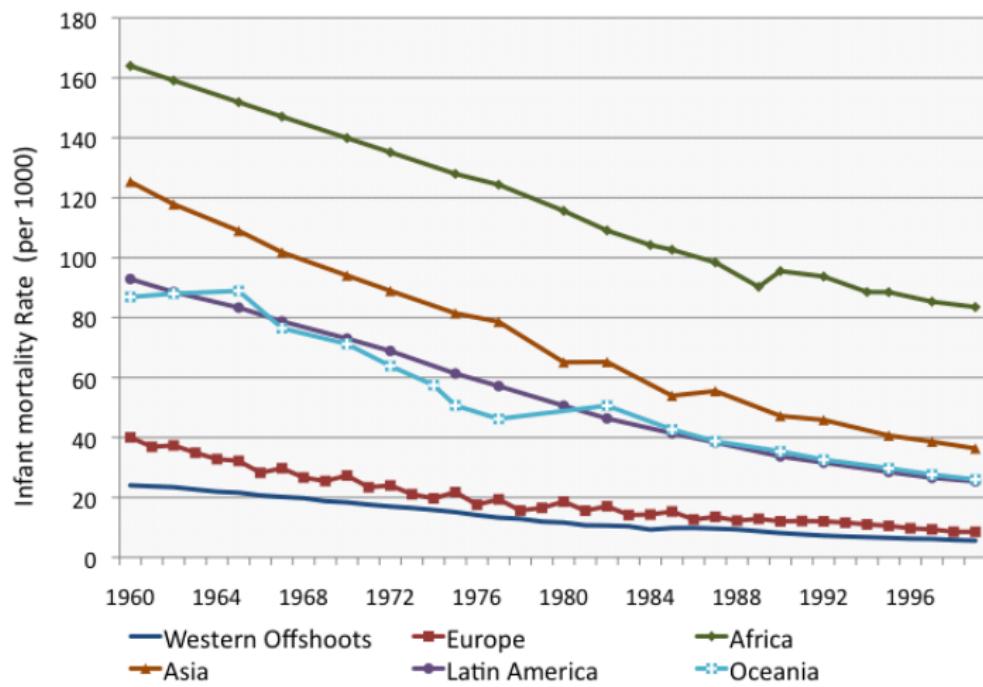
Mortality Decline Western Europe: 1730-1920



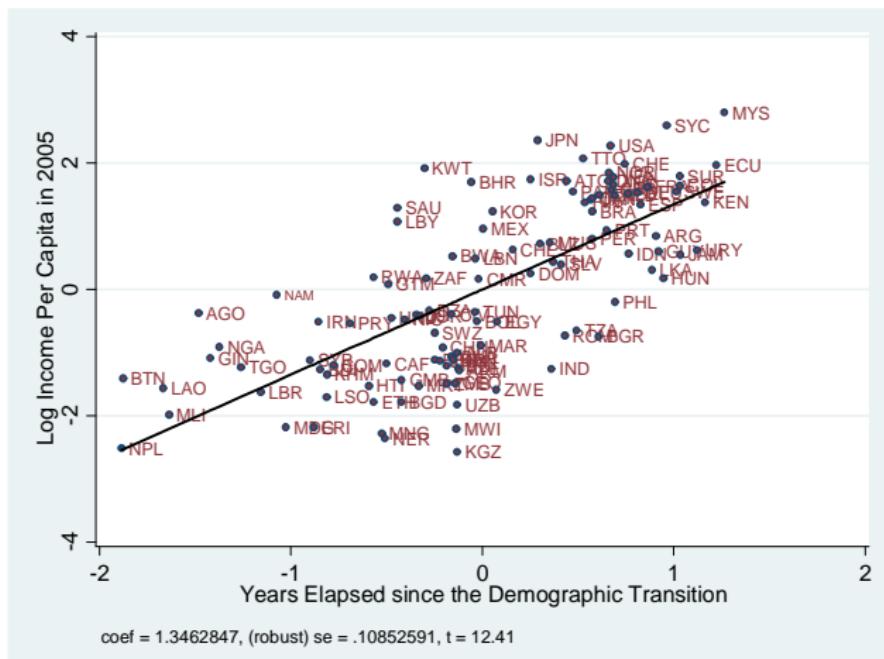
The Evolution of Total Fertility Rate across Regions, 1960-1999



Decline in infant mortality rates across regions, 1960-1999



Timing of the Demographic Transition and Current Income per Capita



Theories of the Demographic Transition

Theories of the Demographic Transition

- The Rise in Income (Becker, 1960)

Theories of the Demographic Transition

- The Rise in Income (Becker, 1960)
 - The cost of raising children is primarily parental time

Theories of the Demographic Transition

- The Rise in Income (Becker, 1960)
 - The cost of raising children is primarily parental time
 - The rise in income increased the opportunity cost of raising children

Theories of the Demographic Transition

- The Rise in Income (Becker, 1960)
 - The cost of raising children is primarily parental time
 - The rise in income increased the opportunity cost of raising children ⇒ reduction in fertility (Becker, 1960)

Theories of the Demographic Transition

- The Rise in Income (Becker, 1960)
 - The cost of raising children is primarily parental time
 - The rise in income increased the opportunity cost of raising children ⇒ reduction in fertility (Becker, 1960)
- The income elasticity of child quality is larger than that of quantity

Theories of the Demographic Transition

- The Rise in Income (Becker, 1960)
 - The cost of raising children is primarily parental time
 - The rise in income increased the opportunity cost of raising children ⇒ reduction in fertility (Becker, 1960)
- The income elasticity of child quality is larger than that of quantity
 - The rise in income

Theories of the Demographic Transition

- The Rise in Income (Becker, 1960)
 - The cost of raising children is primarily parental time
 - The rise in income increased the opportunity cost of raising children ⇒ reduction in fertility (Becker, 1960)
- The income elasticity of child quality is larger than that of quantity
 - The rise in income ⇒ substitution of child quality for quantity

Theories of the Demographic Transition

- The Rise in Income (Becker, 1960)
 - The cost of raising children is primarily parental time
 - The rise in income increased the opportunity cost of raising children ⇒ reduction in fertility (Becker, 1960)
- The income elasticity of child quality is larger than that of quantity
 - The rise in income ⇒ substitution of child quality for quantity ⇒ reduction in fertility (Becker and Lewis, JPE 1973)

Theories of the Demographic Transition

- The Rise in Income (Becker, 1960)
 - The cost of raising children is primarily parental time
 - The rise in income increased the opportunity cost of raising children ⇒ reduction in fertility (Becker, 1960)
- The income elasticity of child quality is larger than that of quantity
 - The rise in income ⇒ substitution of child quality for quantity ⇒ reduction in fertility (Becker and Lewis, JPE 1973)
- The Decline in Child Mortality

Theories of the Demographic Transition

- The Rise in Income (Becker, 1960)
 - The cost of raising children is primarily parental time
 - The rise in income increased the opportunity cost of raising children ⇒ reduction in fertility (Becker, 1960)
- The income elasticity of child quality is larger than that of quantity
 - The rise in income ⇒ substitution of child quality for quantity ⇒ reduction in fertility (Becker and Lewis, JPE 1973)
- The Decline in Child Mortality
 - Decline in child mortality enabled families to attain their desirable number of children with lower number of births

Theories of the Demographic Transition

- The Rise in Income (Becker, 1960)
 - The cost of raising children is primarily parental time
 - The rise in income increased the opportunity cost of raising children ⇒ reduction in fertility (Becker, 1960)
- The income elasticity of child quality is larger than that of quantity
 - The rise in income ⇒ substitution of child quality for quantity ⇒ reduction in fertility (Becker and Lewis, JPE 1973)
- The Decline in Child Mortality
 - Decline in child mortality enabled families to attain their desirable number of children with lower number of births
 - The mortality decline

Theories of the Demographic Transition

- The Rise in Income (Becker, 1960)
 - The cost of raising children is primarily parental time
 - The rise in income increased the opportunity cost of raising children ⇒ reduction in fertility (Becker, 1960)
- The income elasticity of child quality is larger than that of quantity
 - The rise in income ⇒ substitution of child quality for quantity ⇒ reduction in fertility (Becker and Lewis, JPE 1973)
- The Decline in Child Mortality
 - Decline in child mortality enabled families to attain their desirable number of children with lower number of births
 - The mortality decline ⇒ reduction in fertility

Theories of the Demographic Transition

Theories of the Demographic Transition

- The Old-Age Security Hypothesis (Caldwell, 1976)

Theories of the Demographic Transition

- The Old-Age Security Hypothesis (Caldwell, 1976)
 - Children is a form of investment good (in the absence of access to financial markets)

Theories of the Demographic Transition

- The Old-Age Security Hypothesis (Caldwell, 1976)
 - Children is a form of investment good (in the absence of access to financial markets)
 - Development of financial markets reduced the demand for children as an investment good

Theories of the Demographic Transition

- The Old-Age Security Hypothesis (Caldwell, 1976)
 - Children is a form of investment good (in the absence of access to financial markets)
 - Development of financial markets reduced the demand for children as an investment good ⇒ reduction in fertility

Theories of the Demographic Transition

- The Old-Age Security Hypothesis (Caldwell, 1976)
 - Children is a form of investment good (in the absence of access to financial markets)
 - Development of financial markets reduced the demand for children as an investment good ⇒ reduction in fertility
- The Decline in the Gender Wage Gap (Galor-Weil, AER 1996))

Theories of the Demographic Transition

- The Old-Age Security Hypothesis (Caldwell, 1976)
 - Children is a form of investment good (in the absence of access to financial markets)
 - Development of financial markets reduced the demand for children as an investment good ⇒ reduction in fertility
- The Decline in the Gender Wage Gap (Galor-Weil, AER 1996))
 - The process of development decreased the gender wage gap

Theories of the Demographic Transition

- The Old-Age Security Hypothesis (Caldwell, 1976)
 - Children is a form of investment good (in the absence of access to financial markets)
 - Development of financial markets reduced the demand for children as an investment good ⇒ reduction in fertility
- The Decline in the Gender Wage Gap (Galor-Weil, AER 1996))
 - The process of development decreased the gender wage gap
 - The rise in the relative wages of women increased the opportunity cost of raising children more than family income

Theories of the Demographic Transition

- The Old-Age Security Hypothesis (Caldwell, 1976)
 - Children is a form of investment good (in the absence of access to financial markets)
 - Development of financial markets reduced the demand for children as an investment good ⇒ reduction in fertility
- The Decline in the Gender Wage Gap (Galor-Weil, AER 1996))
 - The process of development decreased the gender wage gap
 - The rise in the relative wages of women increased the opportunity cost of raising children more than family income
⇒ reduction in fertility

Theories of the Demographic Transition

Theories of the Demographic Transition

- The Rise Human Capital Formation: (Galor-Weil, AER 2000)

Theories of the Demographic Transition

- The Rise Human Capital Formation: (Galor-Weil, AER 2000)
 - The rise in the industrial demand for human capital induced human capital formation

Theories of the Demographic Transition

- The Rise Human Capital Formation: (Galor-Weil, AER 2000)
 - The rise in the industrial demand for human capital induced human capital formation
 - The presence of a budget constraint

Theories of the Demographic Transition

- The Rise Human Capital Formation: (Galor-Weil, AER 2000)
 - The rise in the industrial demand for human capital induced human capital formation
 - The presence of a budget constraint \Rightarrow substitution of child quality for quantity

Theories of the Demographic Transition

- The Rise Human Capital Formation: (Galor-Weil, AER 2000)
 - The rise in the industrial demand for human capital induced human capital formation
 - The presence of a budget constraint \Rightarrow substitution of child quality for quantity \Rightarrow reduction in fertility

The Rise in Income - Main Hypothesis

The Rise in Income - Main Hypothesis

- The cost of raising children is primarily parental time

The Rise in Income - Main Hypothesis

- The cost of raising children is primarily parental time
 - The rise in income increased the opportunity cost of raising children

The Rise in Income - Main Hypothesis

- The cost of raising children is primarily parental time
 - The rise in income increased the opportunity cost of raising children
⇒ reduction in fertility (Becker, 1960)

The Rise in Income - Main Hypothesis

- The cost of raising children is primarily parental time
 - The rise in income increased the opportunity cost of raising children
⇒ reduction in fertility (Becker, 1960)
- The income elasticity of child quality is larger than that of quantity

The Rise in Income - Main Hypothesis

- The cost of raising children is primarily parental time
 - The rise in income increased the opportunity cost of raising children
⇒ reduction in fertility (Becker, 1960)
- The income elasticity of child quality is larger than that of quantity
 - The rise in income

The Rise in Income - Main Hypothesis

- The cost of raising children is primarily parental time
 - The rise in income increased the opportunity cost of raising children
⇒ reduction in fertility (Becker, 1960)
- The income elasticity of child quality is larger than that of quantity
 - The rise in income ⇒ substitution of child quality for quantity

The Rise in Income - Main Hypothesis

- The cost of raising children is primarily parental time
 - The rise in income increased the opportunity cost of raising children
⇒ reduction in fertility (Becker, 1960)
- The income elasticity of child quality is larger than that of quantity
 - The rise in income ⇒ substitution of child quality for quantity
⇒ reduction in fertility (Becker and Lewis, JPE 1973)

The Rise in Income: Income and Fertility (Again!)

- Child rearing is time-intensive

The Rise in Income: Income and Fertility (Again!)

- Child rearing is time-intensive
- Household's Budget constraint

$$y\tau n + c \leq y$$

The Rise in Income: Income and Fertility (Again!)

- Child rearing is time-intensive
- Household's Budget constraint

$$y\tau n + c \leq y$$

- $y \equiv$ household's income

The Rise in Income: Income and Fertility (Again!)

- Child rearing is time-intensive
- Household's Budget constraint

$$y\tau n + c \leq y$$

- $y \equiv$ household's income
- $c \equiv$ household's consumption

The Rise in Income: Income and Fertility (Again!)

- Child rearing is time-intensive
- Household's Budget constraint

$$y\tau n + c \leq y$$

- $y \equiv$ household's income
- $c \equiv$ household's consumption
- $n \equiv$ household's children

The Rise in Income: Income and Fertility (Again!)

- Child rearing is time-intensive
- Household's Budget constraint

$$y\tau n + c \leq y$$

- $y \equiv$ household's income
- $c \equiv$ household's consumption
- $n \equiv$ household's children
- $\tau \equiv$ time cost per child

The Rise in Income: Income and Fertility (Again!)

- Child rearing is time-intensive
- Household's Budget constraint

$$y\tau n + c \leq y$$

- $y \equiv$ household's income
- $c \equiv$ household's consumption
- $n \equiv$ household's children
- $\tau \equiv$ time cost per child
- $y\tau \equiv$ opportunity cost of raising a child

The Rise in Income: Income and Fertility (Again!)

- Child rearing is time-intensive
- Household's Budget constraint

$$y\tau n + c \leq y$$

- $y \equiv$ household's income
- $c \equiv$ household's consumption
- $n \equiv$ household's children
- $\tau \equiv$ time cost per child
- $y\tau \equiv$ opportunity cost of raising a child
- Equivalently

$$c \leq y(1 - \tau n)$$

- $1 \equiv$ household's time endowment

The Rise in Income: Income and Fertility (Again!)

- Child rearing is time-intensive
- Household's Budget constraint

$$y\tau n + c \leq y$$

- $y \equiv$ household's income
- $c \equiv$ household's consumption
- $n \equiv$ household's children
- $\tau \equiv$ time cost per child
- $y\tau \equiv$ opportunity cost of raising a child
- Equivalently

$$c \leq y(1 - \tau n)$$

- $1 \equiv$ household's time endowment
- $(1 - \tau n) \equiv$ labor force participation

The Rise in Income: Income and Fertility (Again!)

- Child rearing is time-intensive
- Household's Budget constraint

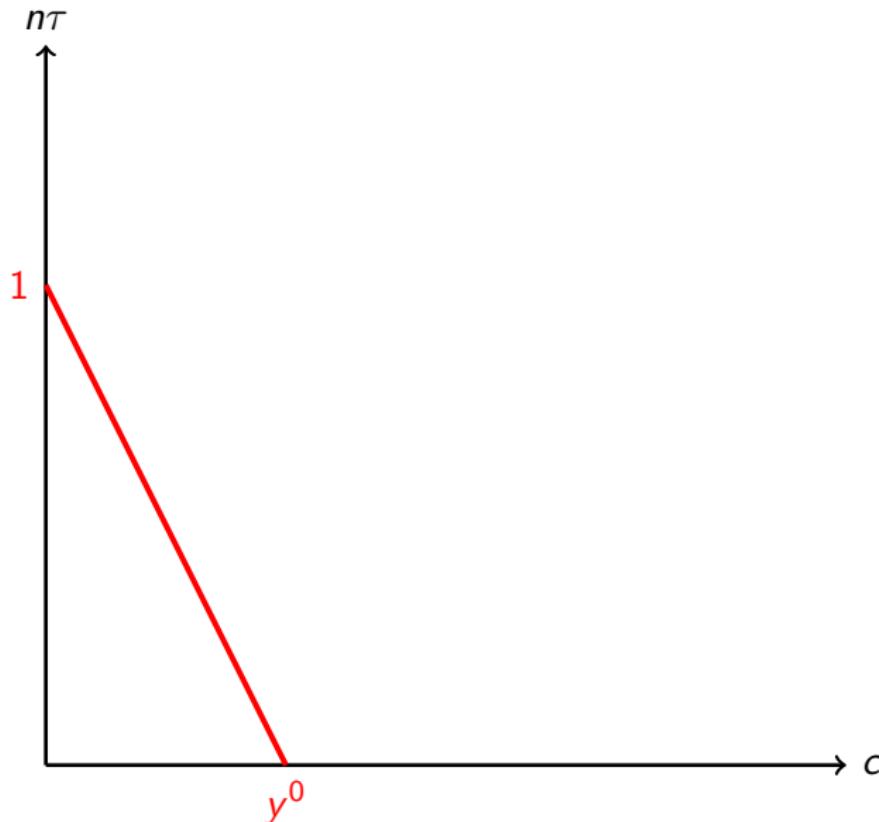
$$y\tau n + c \leq y$$

- $y \equiv$ household's income
- $c \equiv$ household's consumption
- $n \equiv$ household's children
- $\tau \equiv$ time cost per child
- $y\tau \equiv$ opportunity cost of raising a child
- Equivalently

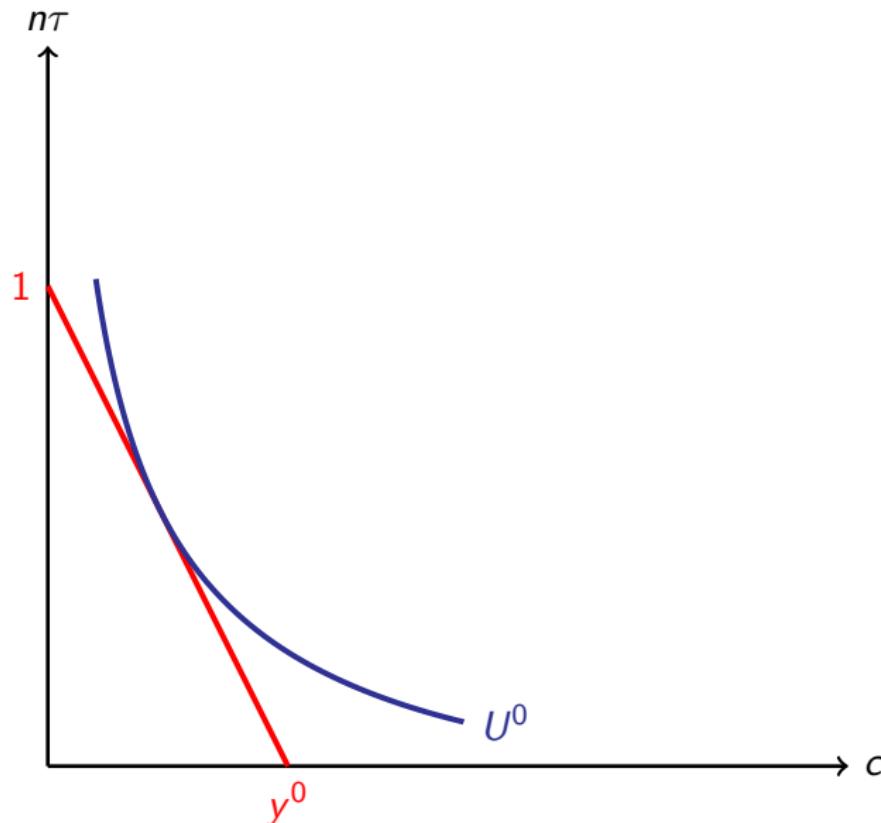
$$c \leq y(1 - \tau n)$$

- $1 \equiv$ household's time endowment
- $(1 - \tau n) \equiv$ labor force participation
- $\tau n \equiv$ time spent raising children

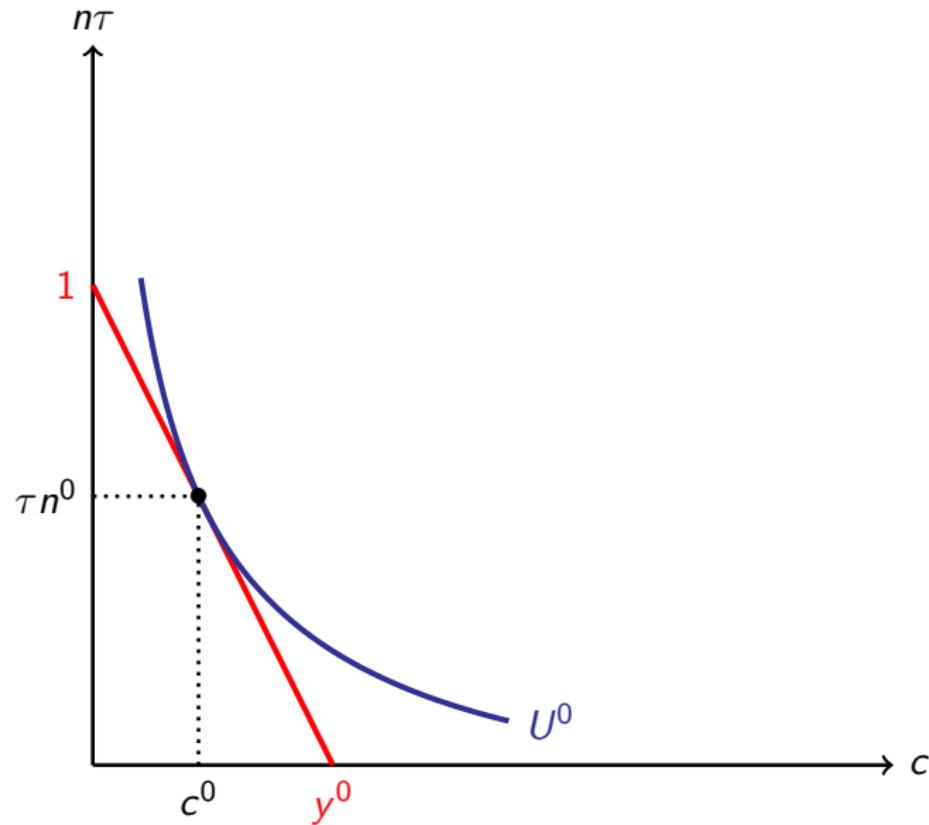
Rise in Income: Optimal Choice



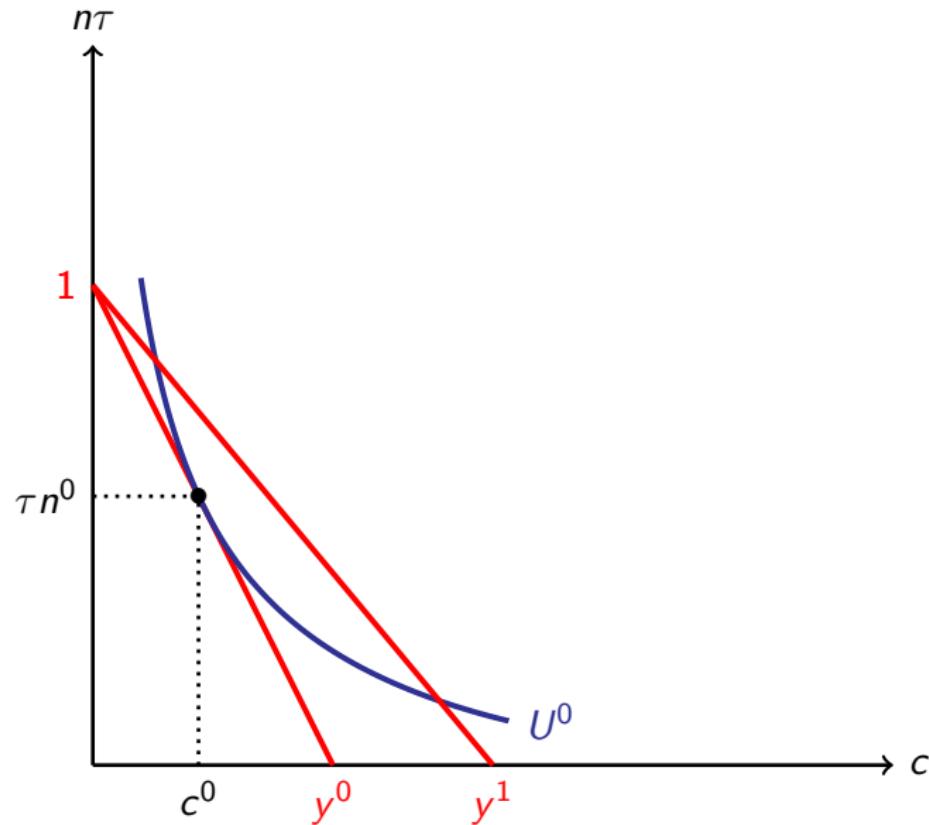
Rise in Income: Optimal Choice



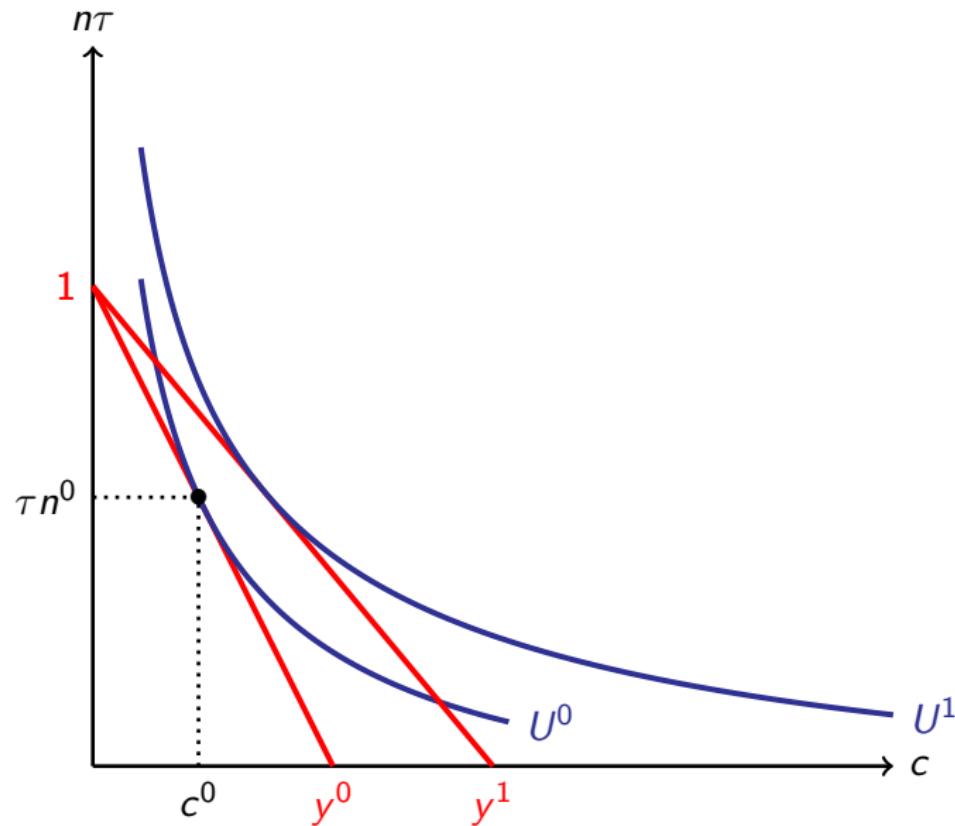
Rise in Income: Optimal Choice



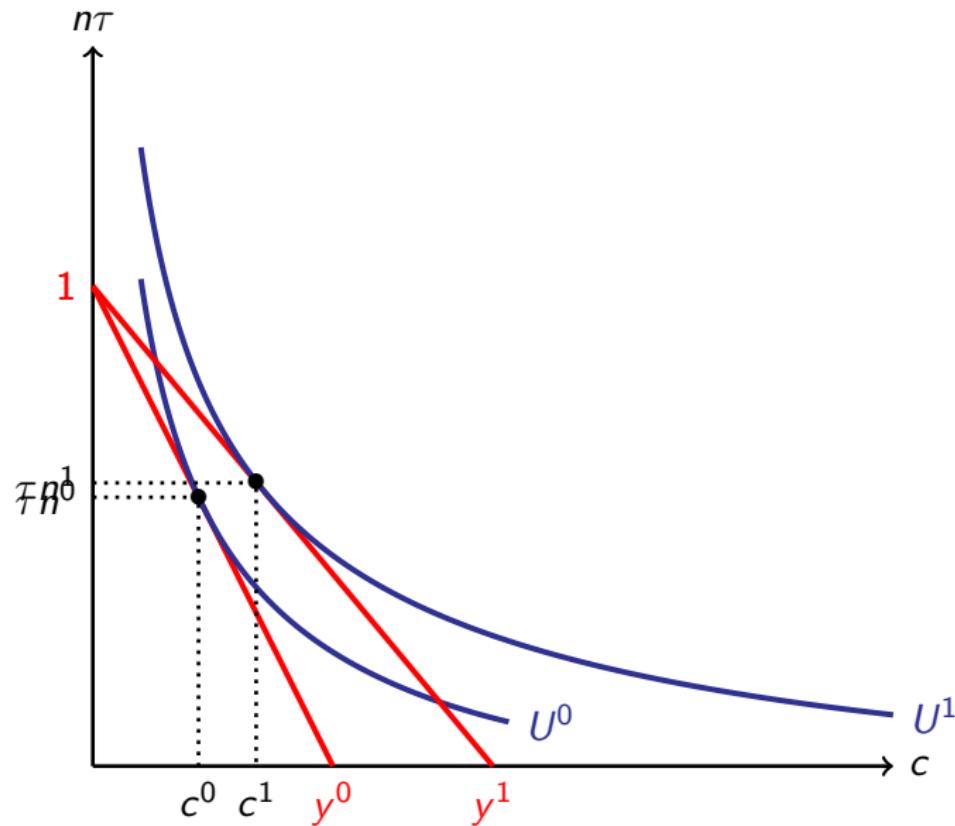
Rise in Income: Optimal Choice



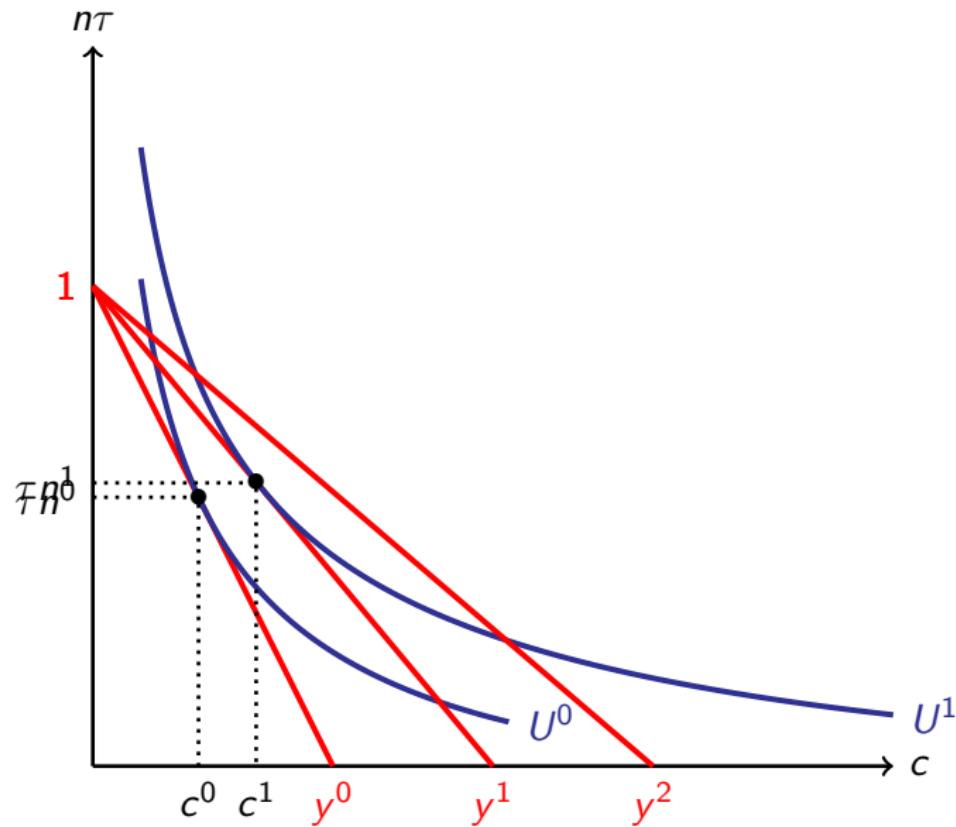
Rise in Income: Optimal Choice



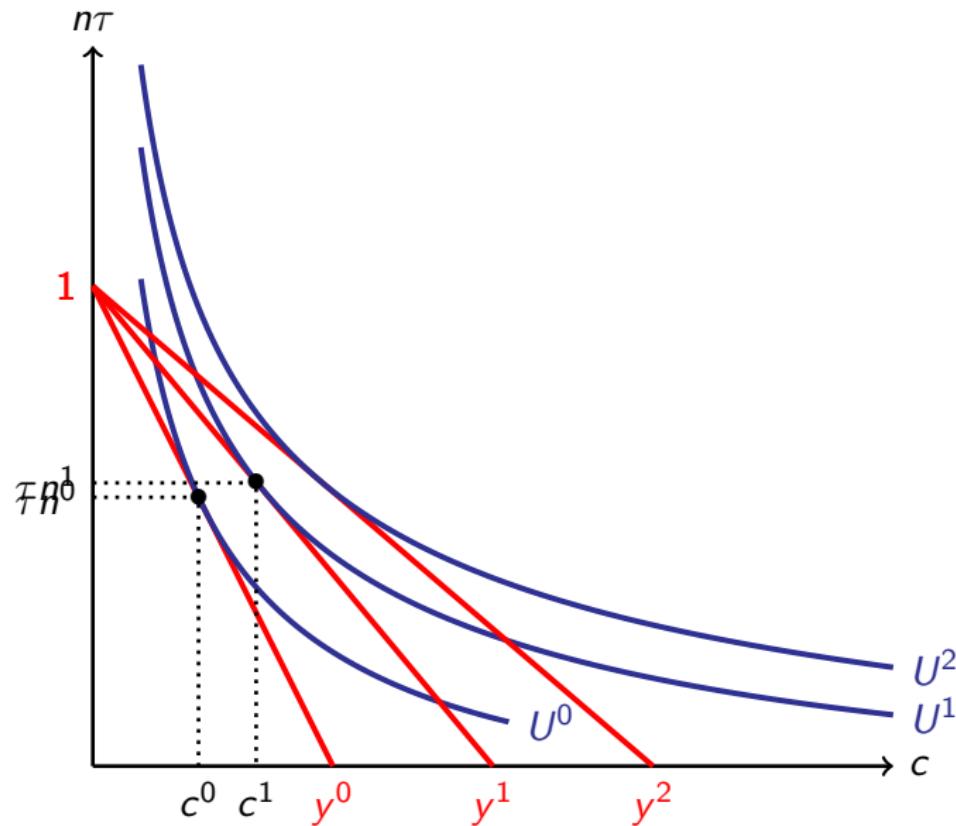
Rise in Income: Optimal Choice



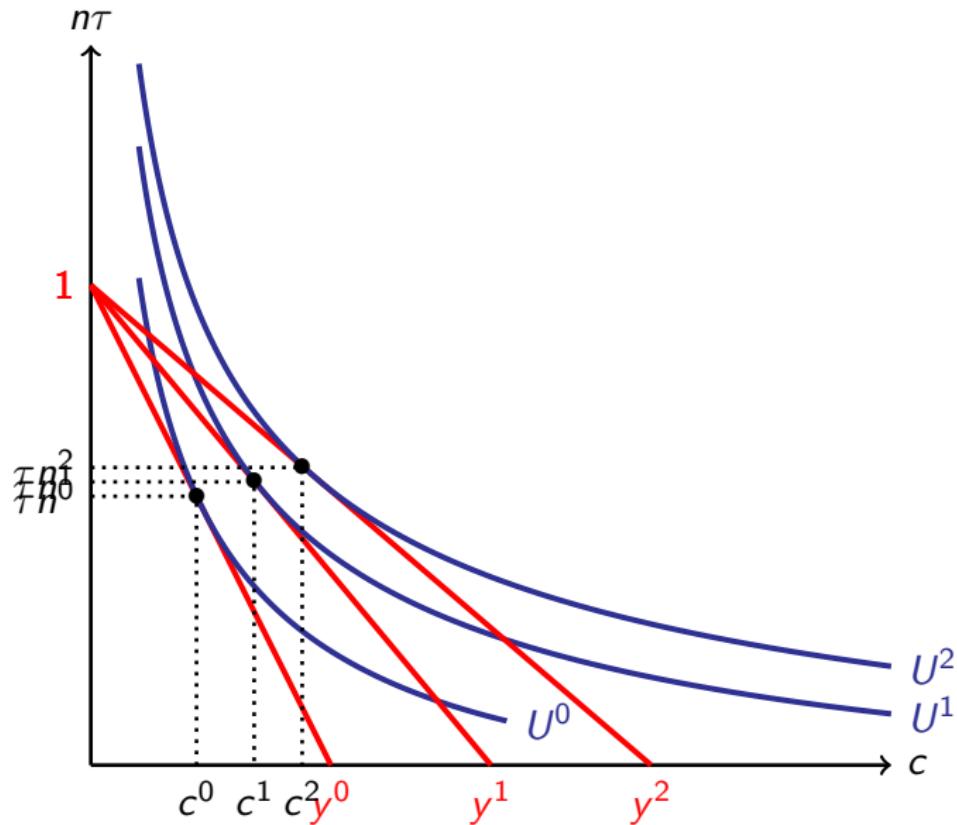
Rise in Income: Optimal Choice



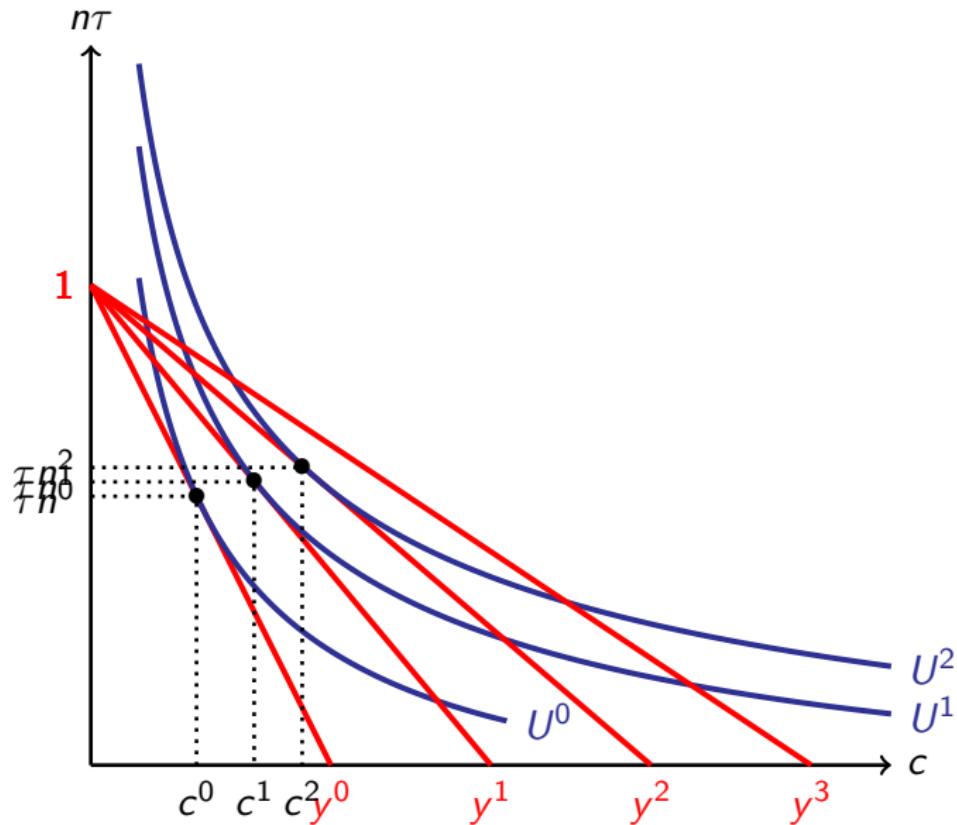
Rise in Income: Optimal Choice



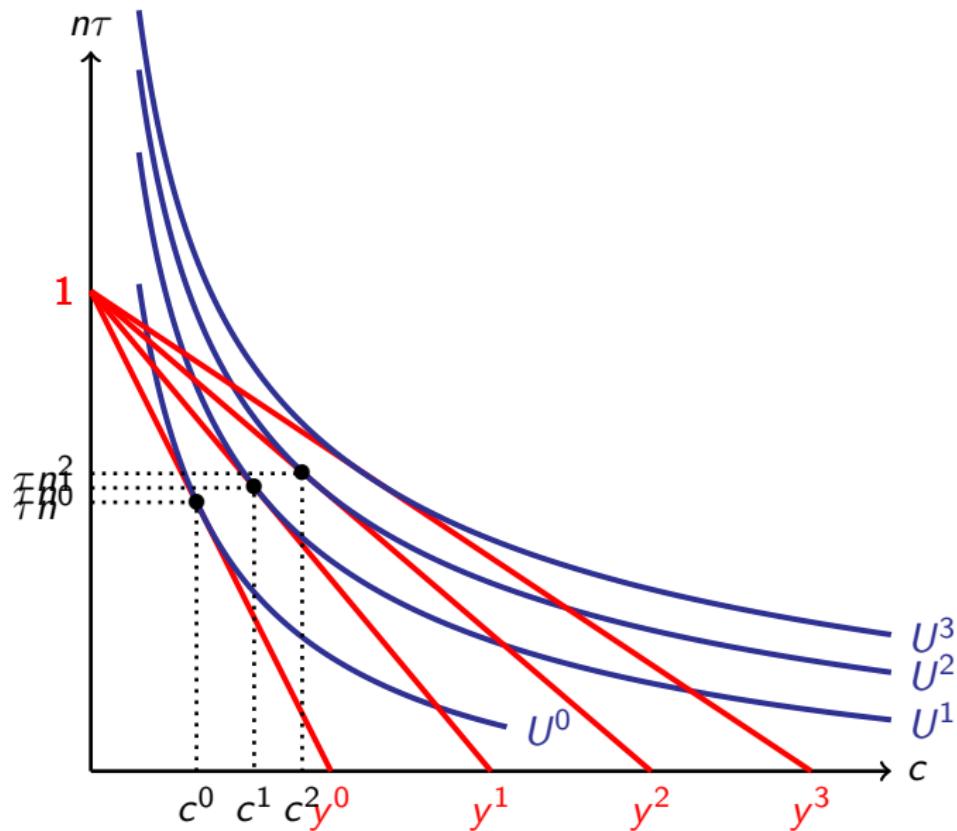
Rise in Income: Optimal Choice



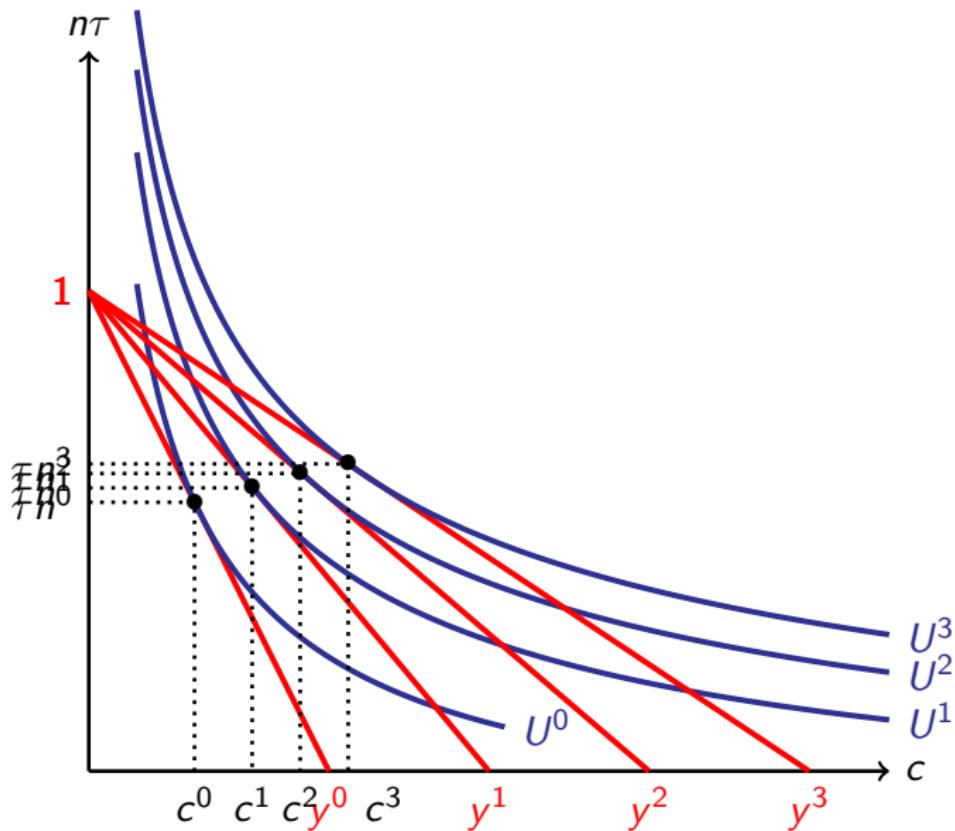
Rise in Income: Optimal Choice



Rise in Income: Optimal Choice



Rise in Income: Optimal Choice



The Rise in Income: Mechanism

- The rise in income generates two conflicting effects:

The Rise in Income: Mechanism

- The rise in income generates two conflicting effects:
 - An income effect:

The Rise in Income: Mechanism

- The rise in income generates two conflicting effects:
 - An income effect:

$$y\tau n + c \leq [y] \uparrow$$

The Rise in Income: Mechanism

- The rise in income generates two conflicting effects:

- An income effect:

$$y\tau n + c \leq [y] \uparrow$$

- More income can be devoted to raising children

The Rise in Income: Mechanism

- The rise in income generates two conflicting effects:
 - An income effect:

$$y\tau n + c \leq [y] \uparrow$$

- More income can be devoted to raising children
- operates towards $n \uparrow$

The Rise in Income: Mechanism

- The rise in income generates two conflicting effects:

- An income effect:

$$y\tau n + c \leq [y] \uparrow$$

- More income can be devoted to raising children
 - operates towards $n \uparrow$

- A substitution effect:

The Rise in Income: Mechanism

- The rise in income generates two conflicting effects:

- An income effect:

$$y\tau n + c \leq [y] \uparrow$$

- More income can be devoted to raising children
 - operates towards $n \uparrow$

- A substitution effect:

$$\uparrow [y\tau]n + c \leq y$$

The Rise in Income: Mechanism

- The rise in income generates two conflicting effects:

- An income effect:

$$y\tau n + c \leq [y] \uparrow$$

- More income can be devoted to raising children
 - operates towards $n \uparrow$

- A substitution effect:

$$\uparrow [y\tau]n + c \leq y$$

- The opportunity cost of raising children increases

The Rise in Income: Mechanism

- The rise in income generates two conflicting effects:

- An income effect:

$$y\tau n + c \leq [y] \uparrow$$

- More income can be devoted to raising children
 - operates towards $n \uparrow$

- A substitution effect:

$$\uparrow [y\tau]n + c \leq y$$

- The opportunity cost of raising children increases
 - operates towards $n \downarrow$

The Rise in Income: Mechanism

- The substitution effect dominates at a higher level of income

The Rise in Income: Mechanism

- The substitution effect dominates at a higher level of income
- As income increases fertility declines

The Rise in Income: Mechanism

- The substitution effect dominates at a higher level of income
- As income increases fertility declines
- Fertility declines in the process of development

The Rise in Income - Theoretical Evaluation

- Preference-based theory (unattractive)

The Rise in Income - Theoretical Evaluation

- Preference-based theory (unattractive)
 - Innate bias against child quantity beyond a certain level of income - non-refutable

The Rise in Income - Theoretical Evaluation

- Preference-based theory (unattractive)
 - Innate bias against child quantity beyond a certain level of income - non-refutable
 - Non-robust (e.g., the class of homothetic preferences will not trigger a fertility decline)

The Rise in Income - Homothetic Preferences

- Preferences:

$$u = n^\gamma c^{(1-\gamma)} \quad 0 < \gamma < 1$$

The Rise in Income - Homothetic Preferences

- Preferences:

$$u = n^\gamma c^{(1-\gamma)} \quad 0 < \gamma < 1$$

- Budget constraint

$$y\tau n + c \leq y$$

The Rise in Income - Homothetic Preferences

- Preferences:

$$u = n^\gamma c^{(1-\gamma)} \quad 0 < \gamma < 1$$

- Budget constraint

$$y\tau n + c \leq y$$

- Optimization: (fraction γ of income is spent on children and $(1 - \gamma)$ on consumption)

The Rise in Income - Homothetic Preferences

- Preferences:

$$u = n^\gamma c^{(1-\gamma)} \quad 0 < \gamma < 1$$

- Budget constraint

$$y\tau n + c \leq y$$

- Optimization: (fraction γ of income is spent on children and $(1 - \gamma)$ on consumption)

$$\begin{aligned} y\tau n &= \gamma y \\ c &= (1 - \gamma)y \end{aligned}$$

The Rise in Income - Homothetic Preferences

- Optimal number of children

$$n = \gamma/\tau$$

The Rise in Income - Homothetic Preferences

- Optimal number of children

$$n = \gamma/\tau$$

- The rise in income has no effect on fertility, i.e.,

$$|\text{Income effect}| = |\text{Substitution effect}|$$

The Rise in Income - Homothetic Preferences

- Optimal number of children

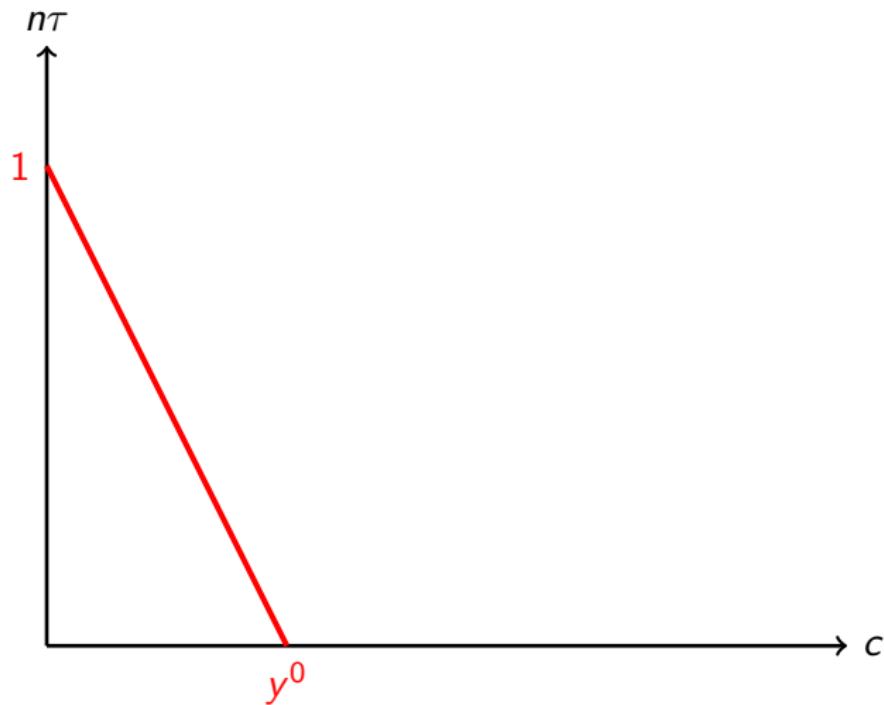
$$n = \gamma/\tau$$

- The rise in income has no effect on fertility, i.e.,

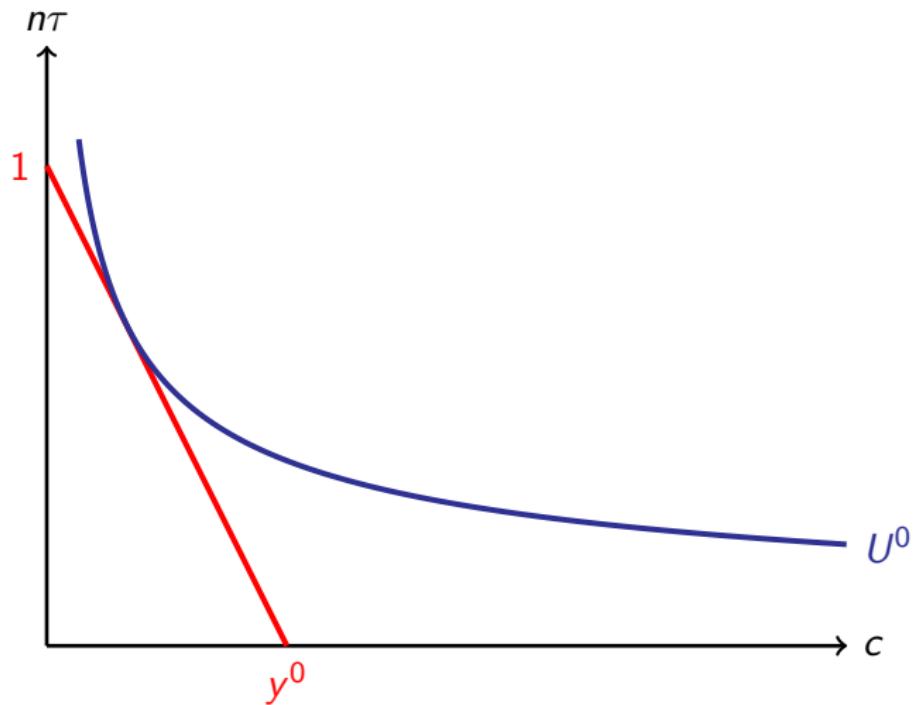
$$|\text{Income effect}| = |\text{Substitution effect}|$$

- Fertility is unaffected by the process of development

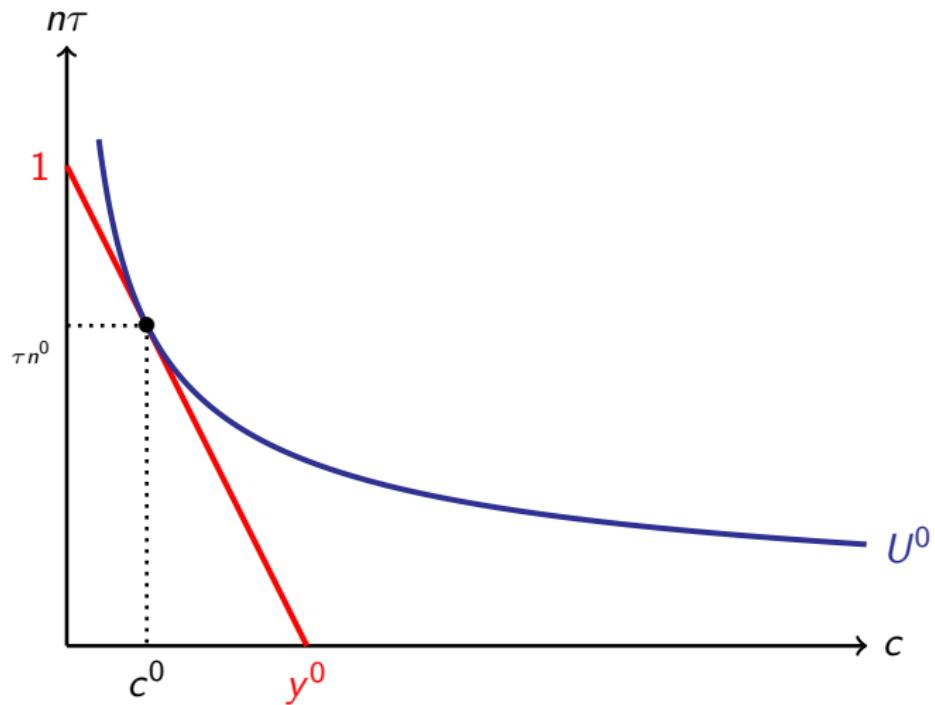
The Rise in Income - Homothetic Preferences



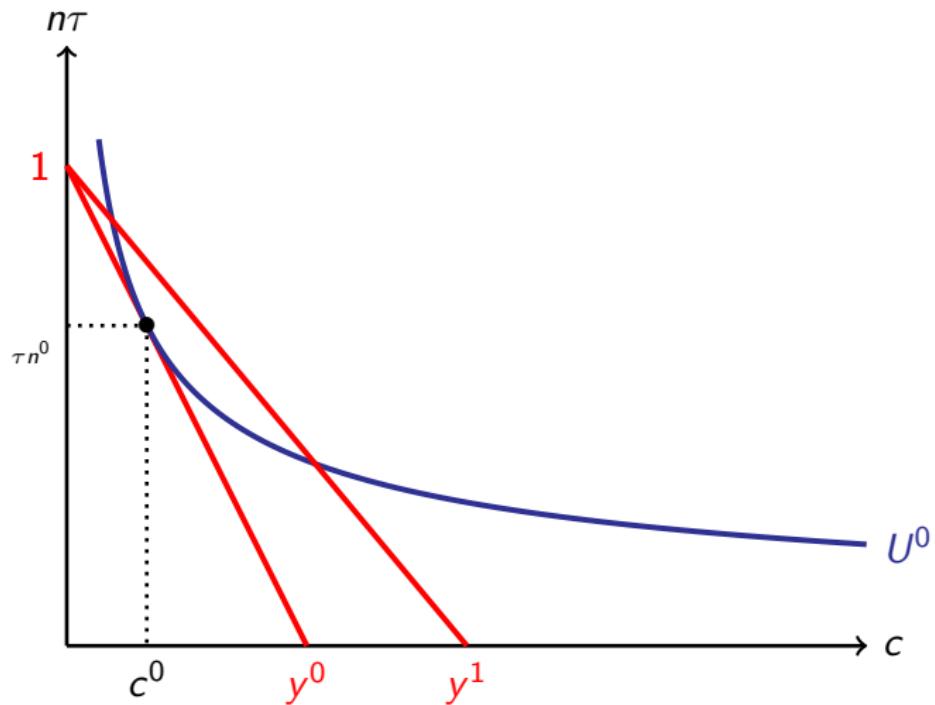
The Rise in Income - Homothetic Preferences



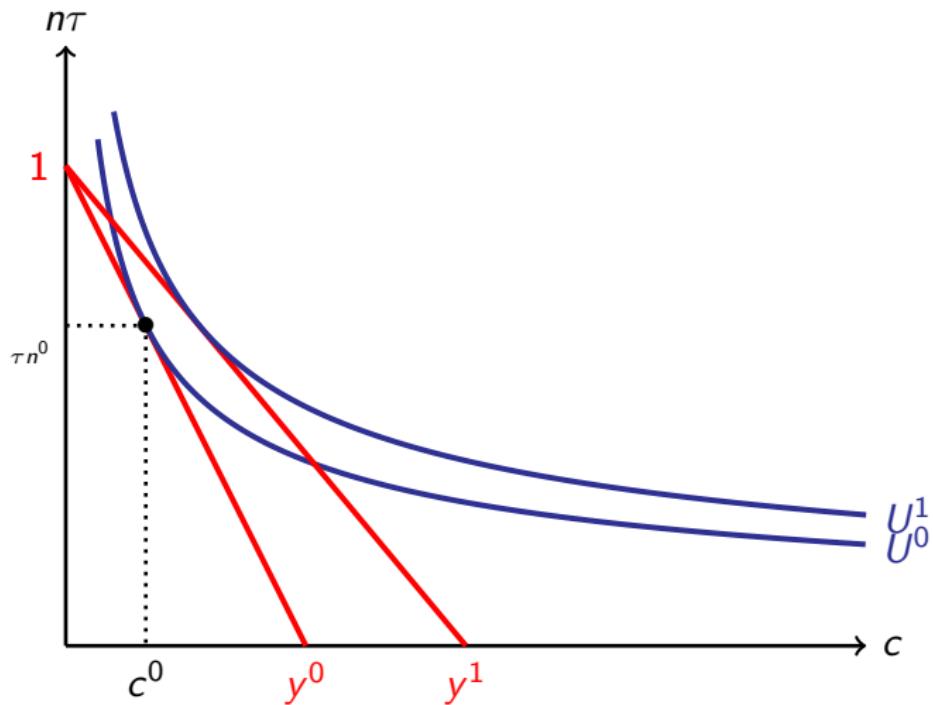
The Rise in Income - Homothetic Preferences



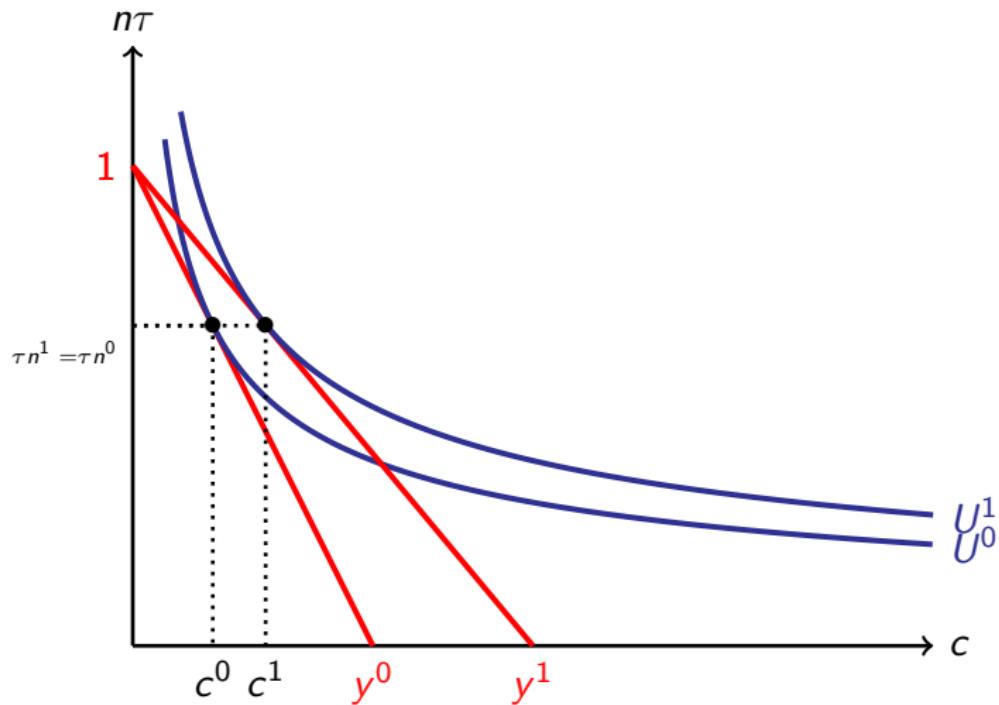
The Rise in Income - Homothetic Preferences



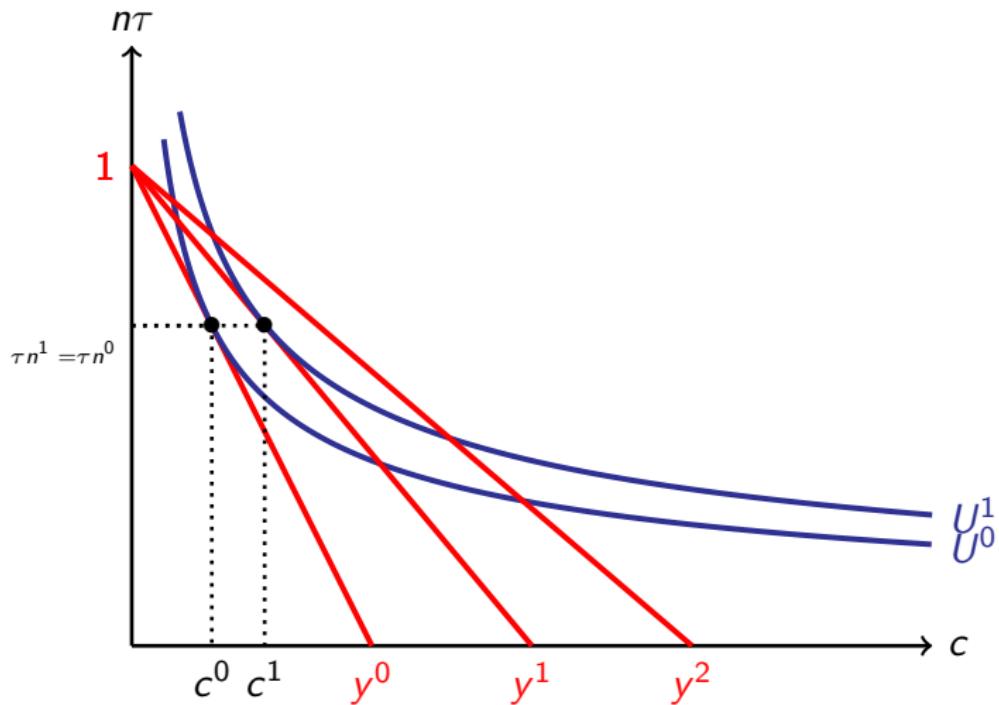
The Rise in Income - Homothetic Preferences



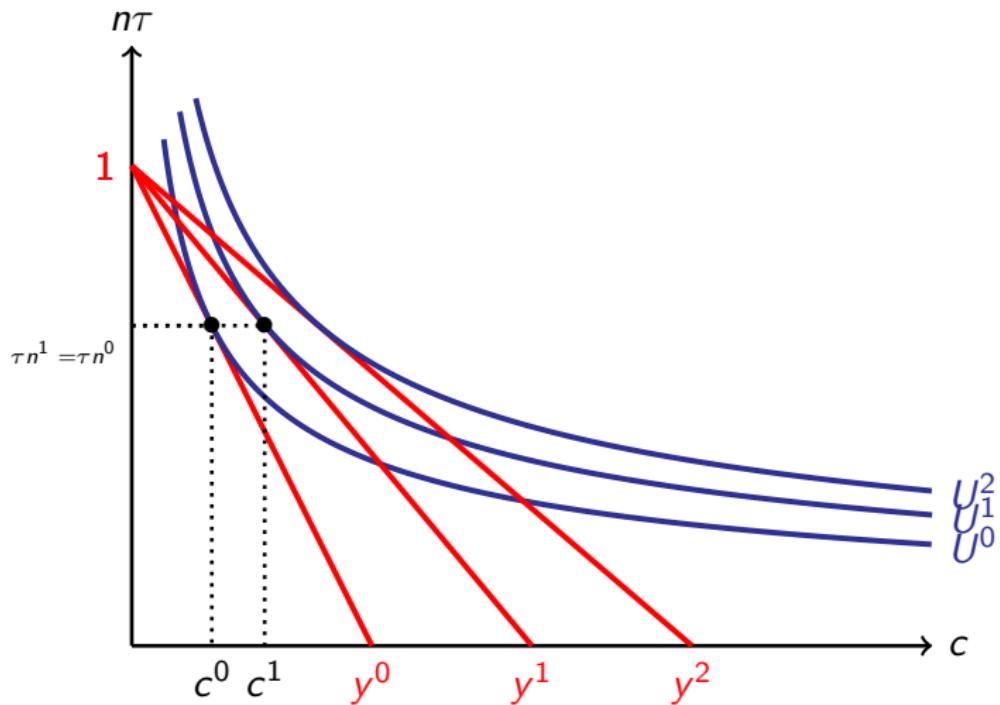
The Rise in Income - Homothetic Preferences



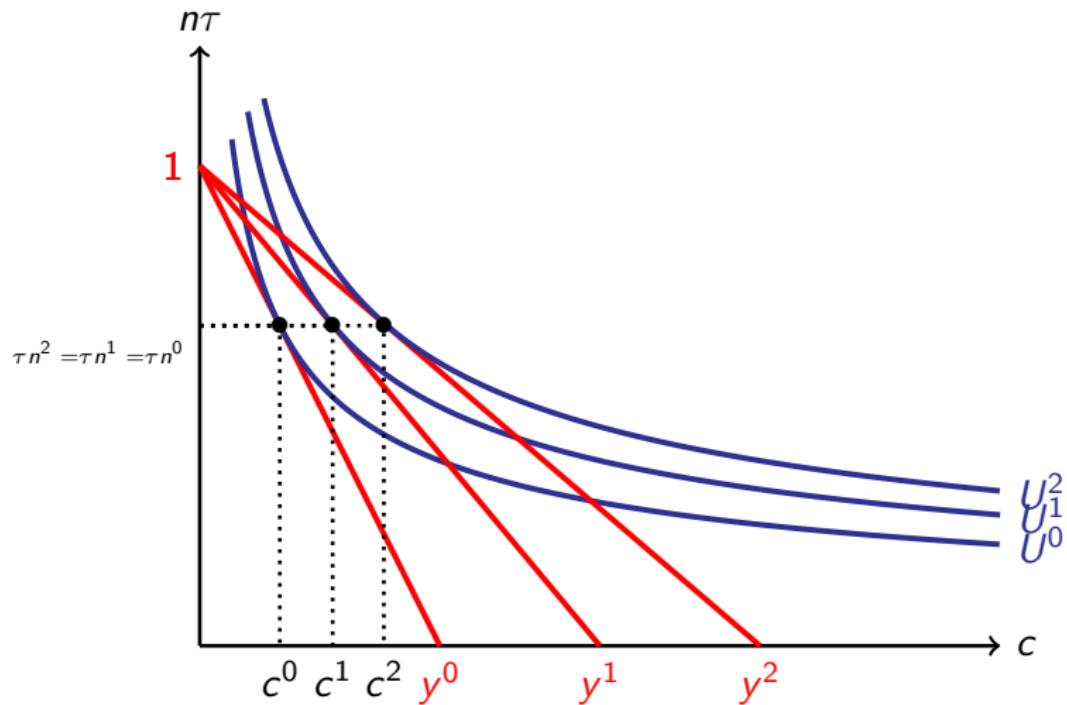
The Rise in Income - Homothetic Preferences



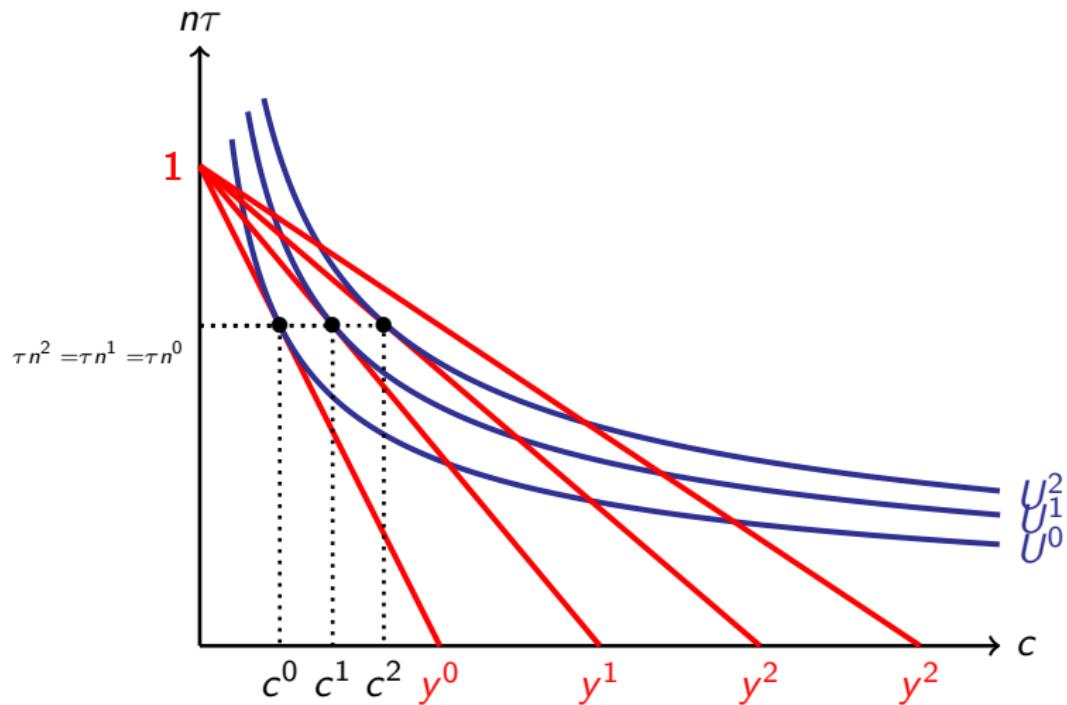
The Rise in Income - Homothetic Preferences



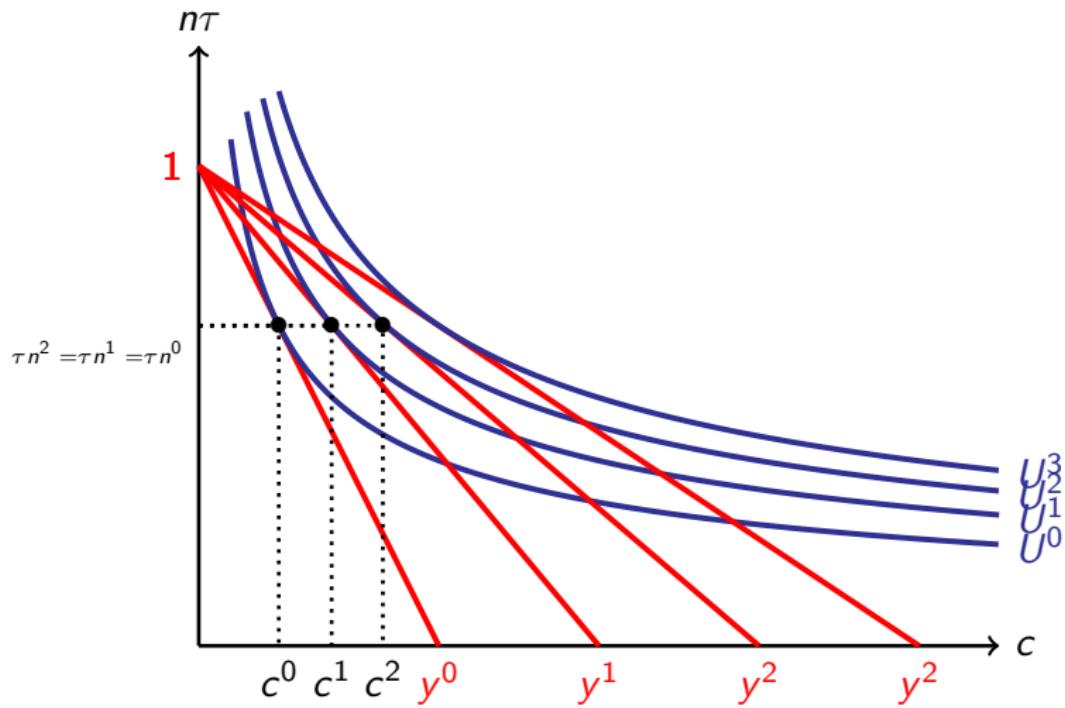
The Rise in Income - Homothetic Preferences



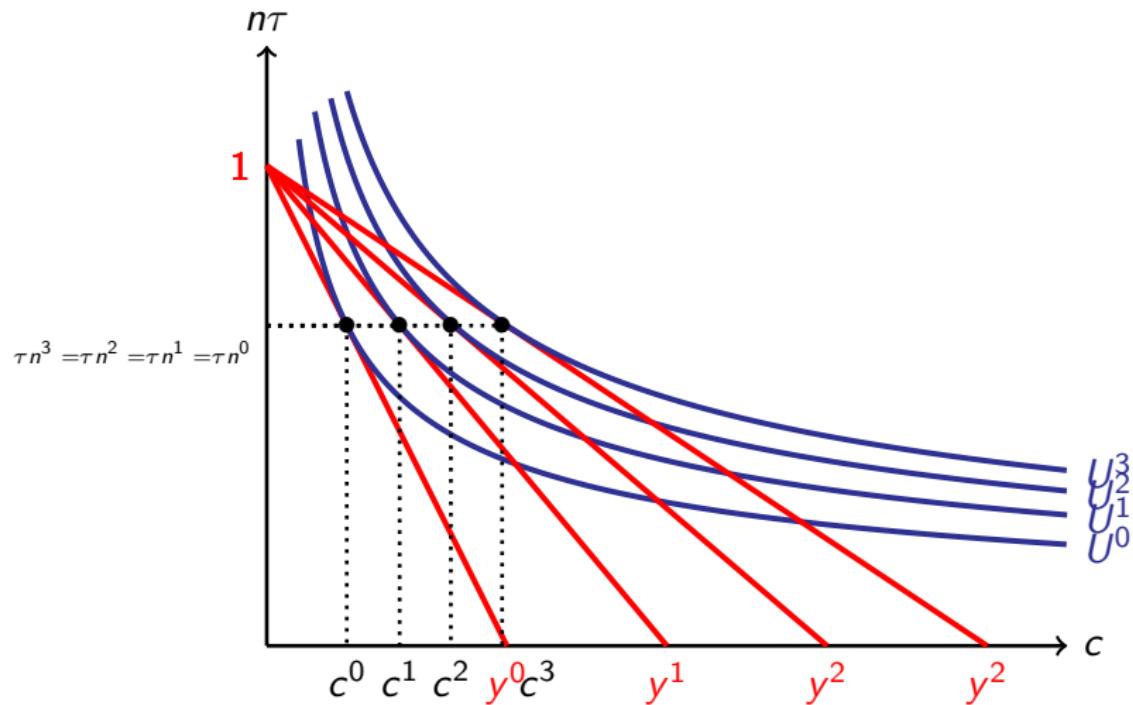
The Rise in Income - Homothetic Preferences



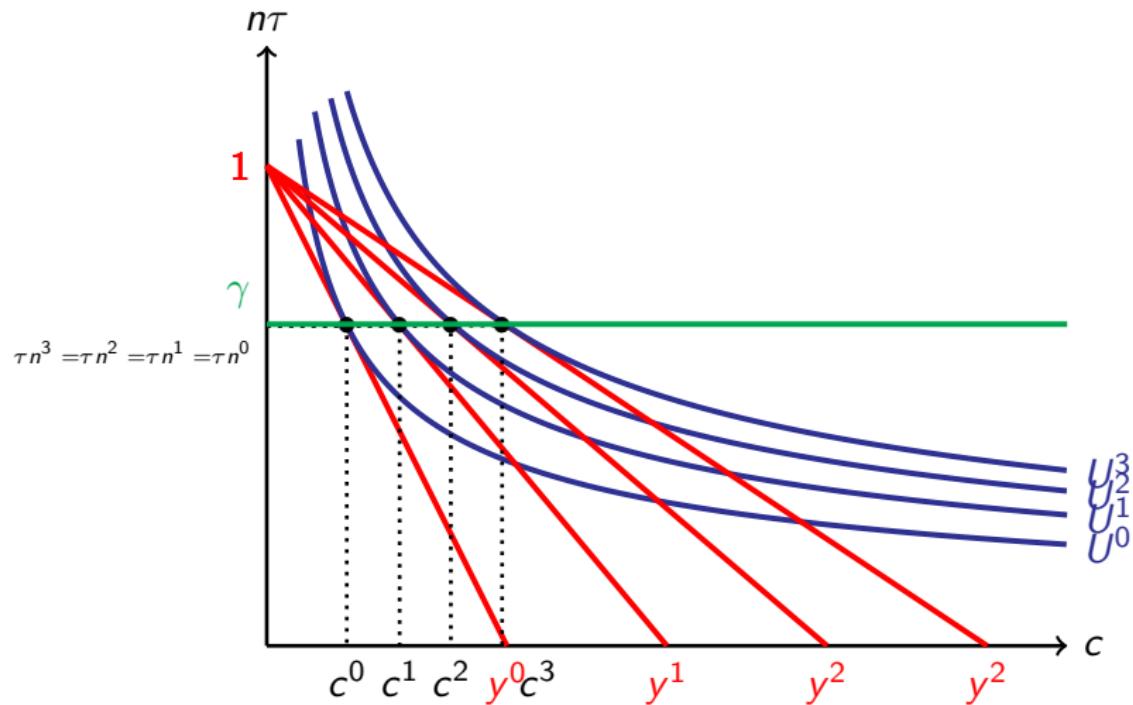
The Rise in Income - Homothetic Preferences



The Rise in Income - Homothetic Preferences



The Rise in Income - Homothetic Preferences



The Rise in Income: Testable predictions

- Across countries that are similar in sociocultural characteristics (and thus in noneconomic factors that may affect fertility decisions), the timing of the fertility decline is inversely related to the level of income per capita.

The Rise in Income: Testable predictions

- Across countries that are similar in sociocultural characteristics (and thus in noneconomic factors that may affect fertility decisions), the timing of the fertility decline is inversely related to the level of income per capita.
- Within an economy, the number of (surviving) children across households is inversely related to their levels of income.

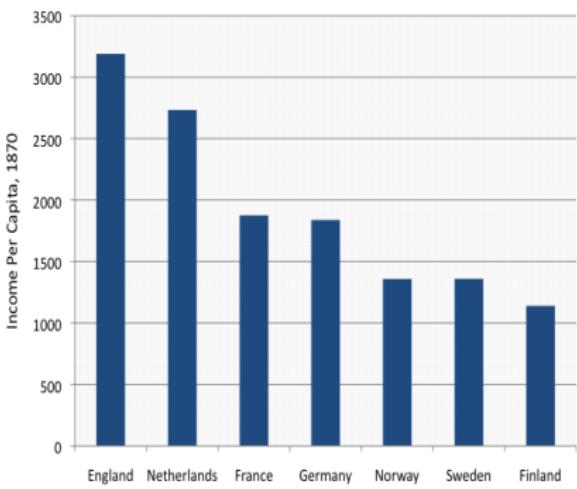
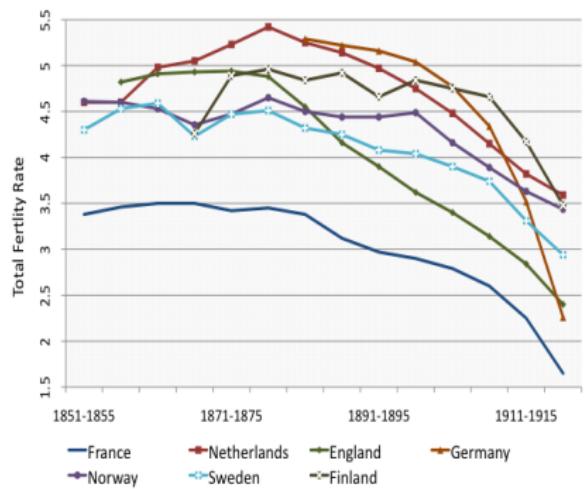
The Rise in Income: Refuting Cross Country Evidence

- Cross Section of Countries (1870-2000) - Income per worker was positively associated with fertility rates, accounting for mortality rates and education (Murtin 2013).

The Rise in Income: Refuting Cross Country Evidence

- Cross Section of Countries (1870-2000) - Income per worker was positively associated with fertility rates, accounting for mortality rates and education (Murtin 2013).
- Western Europe (1870s) The DT occurred among countries that differed significantly in their income per capita.

Simultaneous DT across European Countries that Differ in Income per Capita



The Rise in Income: Refuting Evidence from Individual Countries

- France (1876–96) Income per capita had a positive effect on fertility rates during France's demographic transition, accounting for education, the gender literacy gap, and mortality rates (Murphy 2015)

The Rise in Income: Refuting Evidence from Individual Countries

- France (1876–96) Income per capita had a positive effect on fertility rates during France's demographic transition, accounting for education, the gender literacy gap, and mortality rates (Murphy 2015)
- England (During the DT): The force associated with the rise in income would have led to an increase in fertility rates (Fernandez-Villaverde 2001)

The Rise in Income: Refuting Evidence from Individual Countries

- France (1876–96) Income per capita had a positive effect on fertility rates during France's demographic transition, accounting for education, the gender literacy gap, and mortality rates (Murphy 2015)
- England (During the DT): The force associated with the rise in income would have led to an increase in fertility rates (Fernandez-Villaverde 2001)
- England (1630s) Reproductive success increases with income (Clark and Hamilton JEH 2006)

The Decline in Child Mortality - Main Hypothesis

The Decline in Child Mortality - Main Hypothesis

- Parents generate utility from the number of surviving children

The Decline in Child Mortality - Main Hypothesis

- Parents generate utility from the number of surviving children
- A decline in child mortality permits parents to reach a given level of surviving children with lower fertility

The Decline in Child Mortality - Main Hypothesis

- Parents generate utility from the number of surviving children
- A decline in child mortality permits parents to reach a given level of surviving children with lower fertility
- The decline in mortality triggered the subsequent decline in fertility

The Decline in Mortality – Mechanism

The Decline in Mortality – Mechanism

- Preferences:

$$u = n^\gamma c^{(1-\gamma)} \quad 0 < \gamma < 1$$

The Decline in Mortality – Mechanism

- Preferences:

$$u = n^\gamma c^{(1-\gamma)} \quad 0 < \gamma < 1$$

- $c \equiv$ household's consumption

The Decline in Mortality – Mechanism

- Preferences:

$$u = n^\gamma c^{(1-\gamma)} \quad 0 < \gamma < 1$$

- $c \equiv$ household's consumption
- $n \equiv$ household's surviving children

The Decline in Mortality – Mechanism

- Preferences:

$$u = n^\gamma c^{(1-\gamma)} \quad 0 < \gamma < 1$$

- $c \equiv$ household's consumption
- $n \equiv$ household's surviving children

- Survival children

$$n = \theta n^b$$

The Decline in Mortality – Mechanism

- Preferences:

$$u = n^\gamma c^{(1-\gamma)} \quad 0 < \gamma < 1$$

- $c \equiv$ household's consumption
- $n \equiv$ household's surviving children

- Survival children

$$n = \theta n^b$$

- $\theta \equiv$ probability of a child to survive infancy

The Decline in Mortality – Mechanism

- Preferences:

$$u = n^\gamma c^{(1-\gamma)} \quad 0 < \gamma < 1$$

- $c \equiv$ household's consumption
- $n \equiv$ household's surviving children

- Survival children

$$n = \theta n^b$$

- $\theta \equiv$ probability of a child to survive infancy
- $n^b \equiv$ household's children born

The Decline in Mortality – Mechanism

The Decline in Mortality – Mechanism

- Budget constraint

$$y\tau n + c \leq y$$

The Decline in Mortality – Mechanism

- Budget constraint

$$y\tau n + c \leq y$$

- $y \equiv$ household's income

The Decline in Mortality – Mechanism

- Budget constraint

$$y\tau n + c \leq y$$

- $y \equiv$ household's income
- $c \equiv$ household's consumption

The Decline in Mortality – Mechanism

- Budget constraint

$$y\tau n + c \leq y$$

- $y \equiv$ household's income
- $c \equiv$ household's consumption
- $\tau \equiv$ time cost of raising a surviving child

The Decline in Mortality – Mechanism

- Budget constraint

$$y\tau n + c \leq y$$

- $y \equiv$ household's income
- $c \equiv$ household's consumption
- $\tau \equiv$ time cost of raising a surviving child
- $y\tau \equiv$ opportunity cost of raising a surviving child

The Decline in Mortality – Mechanism

- Optimization: (fraction γ of income is spent on children and $(1 - \gamma)$ on consumption)

The Decline in Mortality – Mechanism

- Optimization: (fraction γ of income is spent on children and $(1 - \gamma)$ on consumption)

$$\begin{aligned}y\tau n &= \gamma y \\c &= (1 - \gamma)y\end{aligned}$$

The Decline in Mortality – Mechanism

- Optimization: (fraction γ of income is spent on children and $(1 - \gamma)$ on consumption)

$$\begin{aligned}y\tau n &= \gamma y \\c &= (1 - \gamma)y\end{aligned}$$

- Optimal number of surviving children (NRR)

$$n = \gamma/\tau$$

The Decline in Mortality – Mechanism

- Optimization: (fraction γ of income is spent on children and $(1 - \gamma)$ on consumption)

$$\begin{aligned}y\tau n &= \gamma y \\c &= (1 - \gamma)y\end{aligned}$$

- Optimal number of surviving children (NRR)

$$n = \gamma/\tau$$

- Optimal fertility (# of successful pregnancies - TFR)

$$n^b = n/\theta = \gamma/(\tau\theta)$$

The Decline in Mortality – Testable Predictions

- Child mortality rate, $(1 - \theta)$, has a positive effect on TFR

The Decline in Mortality – Testable Predictions

- Child mortality rate, $(1 - \theta)$, has a positive effect on TFR
- Child mortality rate, $(1 - \theta)$, has no effect on NRR

The Decline in Child Mortality

- Worldwide: NRR and TFR plummet jointly during the demographic transition (Lehr 2009). But the theory does not predict a decline in NRR

The Decline in Child Mortality

- Worldwide: NRR and TFR plummet jointly during the demographic transition (Lehr 2009). But the theory does not predict a decline in NRR
- NRR does not decline unless:

The Decline in Child Mortality

- Worldwide: NRR and TFR plummet jointly during the demographic transition (Lehr 2009). But the theory does not predict a decline in NRR
- NRR does not decline unless:
 - There exists a precautionary demand for children

The Decline in Child Mortality

- Worldwide: NRR and TFR plummet jointly during the demographic transition (Lehr 2009). But the theory does not predict a decline in NRR
- NRR does not decline unless:
 - There exists a precautionary demand for children
 - RA with respect to fertility > RA with respect to consumption

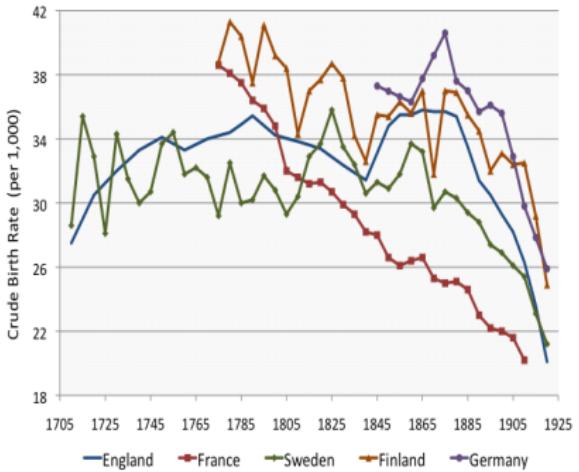
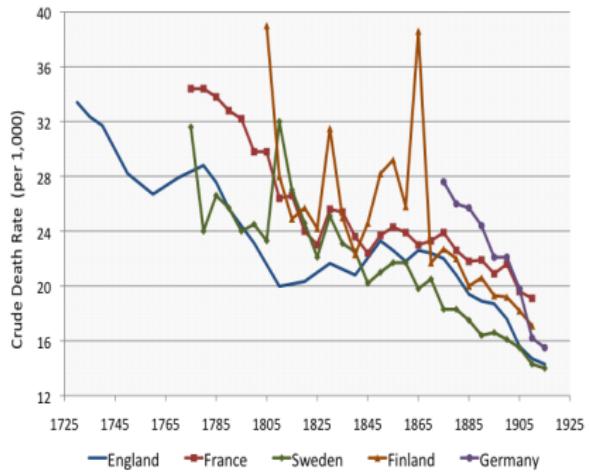
The Decline in Child Mortality

- Worldwide: NRR and TFR plummet jointly during the demographic transition (Lehr 2009). But the theory does not predict a decline in NRR
- NRR does not decline unless:
 - There exists a precautionary demand for children
 - RA with respect to fertility > RA with respect to consumption
 - Replacement fertility is insignificant (empirical estimates 0.2–0.6)

The Decline in Child Mortality

- Worldwide: NRR and TFR plummet jointly during the demographic transition (Lehr 2009). But the theory does not predict a decline in NRR
- NRR does not decline unless:
 - There exists a precautionary demand for children
 - RA with respect to fertility > RA with respect to consumption
 - Replacement fertility is insignificant (empirical estimates 0.2–0.6)
 - Resources saved from investment in non-surviving children are not channeled towards higher fertility

The Decline in Mortality and Fertility - Evidence



The Decline in Child Mortality – Challenges to the Theory

- Worldwide: NRR and TFR plummets jointly during the demographic transition. But the theory does not predict a decline in NRR

The Decline in Child Mortality – Challenges to the Theory

- Worldwide: NRR and TFR plummets jointly during the demographic transition. But the theory does not predict a decline in NRR
- US, France, and Some LDCs: The decline in mortality did not precede the decline in fertility

The Decline in Child Mortality – Challenges to the Theory

- Worldwide: NRR and TFR plummets jointly during the demographic transition. But the theory does not predict a decline in NRR
- US, France, and Some LDCs: The decline in mortality did not precede the decline in fertility
- Western Europe: No change in the patterns of mortality decline at the time of the sharp decline in fertility

The Decline in Child Mortality – Challenges to the Theory

- Worldwide: NRR and TFR plummets jointly during the demographic transition. But the theory does not predict a decline in NRR
- US, France, and Some LDCs: The decline in mortality did not precede the decline in fertility
- Western Europe: No change in the patterns of mortality decline at the time of the sharp decline in fertility
- England: The decline in mortality started in the 1730s (140 years before the fertility decline) and was accompanied by a steady increase in fertility rates until 1800

The Decline in Mortality: Refuting Evidence from Individual Countries

- France (1876–96): Mortality rate had no effect on fertility during France's demographic transition, accounting for education, income, and the gender literacy gap. (Murphy 2009)

The Decline in Mortality: Refuting Evidence from Individual Countries

- France (1876–96): Mortality rate had no effect on fertility during France's demographic transition, accounting for education, income, and the gender literacy gap. (Murphy 2009)
- England (1861–1951): The force associated with the decline in child mortality would have led to an increase in fertility rates (Fernandez-Villaverde 2001; Doepke 2005)

The Old-Age Security Hypothesis

The Old-Age Security Hypothesis

- Children is a form of investment good (in the absence of capital markets)

The Old-Age Security Hypothesis

- Children is a form of investment good (in the absence of capital markets)
- The development of financial markets reduced the demand for children for investment purposes and triggered a decline in fertility

The Old-Age Security Hypothesis - Challenges to the Theory

- The decline in the importance of old-age support is unlikely to be a major force behind the significant reduction in fertility – at a rate of 30–50% – during the demographic transition:

The Old-Age Security Hypothesis - Challenges to the Theory

- The decline in the importance of old-age support is unlikely to be a major force behind the significant reduction in fertility – at a rate of 30–50% – during the demographic transition:
 - Rare examples in nature of offspring that support their parents in old age

The Old-Age Security Hypothesis - Challenges to the Theory

- The decline in the importance of old-age support is unlikely to be a major force behind the significant reduction in fertility – at a rate of 30–50% – during the demographic transition:
 - Rare examples in nature of offspring that support their parents in old age
- Institutions supporting individuals in their old age were formed well before the demographic transition

The Old-Age Security Hypothesis - Challenges to the Theory

- The decline in the importance of old-age support is unlikely to be a major force behind the significant reduction in fertility – at a rate of 30–50% – during the demographic transition:
 - Rare examples in nature of offspring that support their parents in old age
- Institutions supporting individuals in their old age were formed well before the demographic transition
 - England (16th century) Parents did not rely on support from children in their old age (Pelling and Smith 1991)

The Old-Age Security Hypothesis - Challenges to the Theory

- The decline in the importance of old-age support is unlikely to be a major force behind the significant reduction in fertility – at a rate of 30–50% – during the demographic transition:
 - Rare examples in nature of offspring that support their parents in old age
- Institutions supporting individuals in their old age were formed well before the demographic transition
 - England (16th century) Parents did not rely on support from children in their old age (Pelling and Smith 1991)
- Prior to the demographic transition, richer individuals who presumably had better access to financial markets, had larger number of surviving children

The Decline in the Gender Wage Gap

The Decline in the Gender Wage Gap

- The inevitable rise in the relative wages of women in the process of development

The Decline in the Gender Wage Gap

- The inevitable rise in the relative wages of women in the process of development
 - increases the opportunity cost of raising children more than family income

The Decline in the Gender Wage Gap

- The inevitable rise in the relative wages of women in the process of development
 - increases the opportunity cost of raising children more than family income
⇒ reduction in fertility

Mechanism: I. Development and Women's Wages

Mechanism: I. Development and Women's Wages

- Female-Biased Technical change

Mechanism: I. Development and Women's Wages

- Female-Biased Technical change
 - Mechanization and advanced technologies have complemented mental tasks more than physical tasks

Mechanism: I. Development and Women's Wages

- Female-Biased Technical change

- Mechanization and advanced technologies have complemented mental tasks more than physical tasks
- Women have physiological comparative advantage in mental (rather than physical) tasks

Mechanism: I. Development and Women's Wages

- Female-Biased Technical change

- Mechanization and advanced technologies have complemented mental tasks more than physical tasks
- Women have physiological comparative advantage in mental (rather than physical) tasks

⇒ The process of development has (inevitably) increased the productivity of women relative to men:

Mechanism: I. Development and Women's Wages

- Female-Biased Technical change

- Mechanization and advanced technologies have complemented mental tasks more than physical tasks
- Women have physiological comparative advantage in mental (rather than physical) tasks

⇒ The process of development has (inevitably) increased the productivity of women relative to men:

$$\text{Economic Development} \implies (w^F/w^M) \uparrow$$

Mechanism: I. Development and Women's Wages

- Female-Biased Technical change

- Mechanization and advanced technologies have complemented mental tasks more than physical tasks
- Women have physiological comparative advantage in mental (rather than physical) tasks

⇒ The process of development has (inevitably) increased the productivity of women relative to men:

$$\text{Economic Development} \implies (w^F/w^M) \uparrow$$

- $w^F \equiv$ women's wages

Mechanism: I. Development and Women's Wages

- Female-Biased Technical change

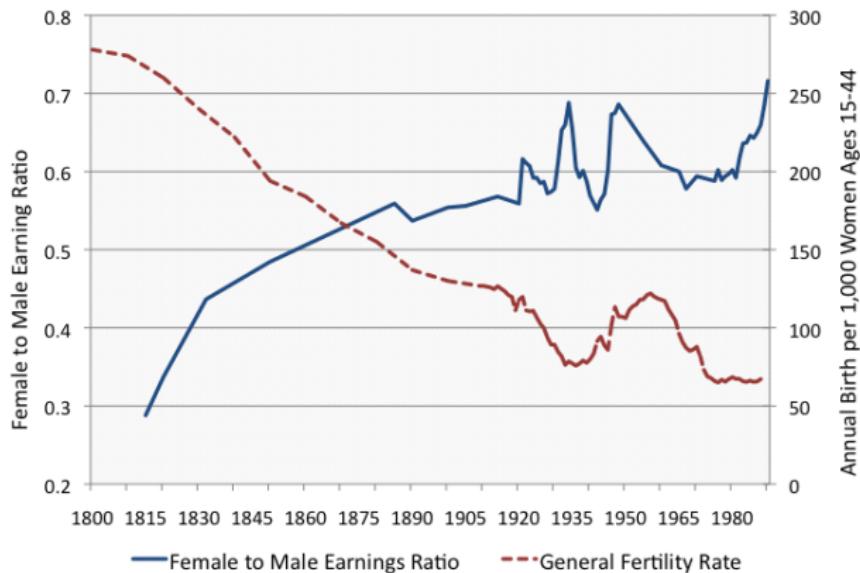
- Mechanization and advanced technologies have complemented mental tasks more than physical tasks
- Women have physiological comparative advantage in mental (rather than physical) tasks

⇒ The process of development has (inevitably) increased the productivity of women relative to men:

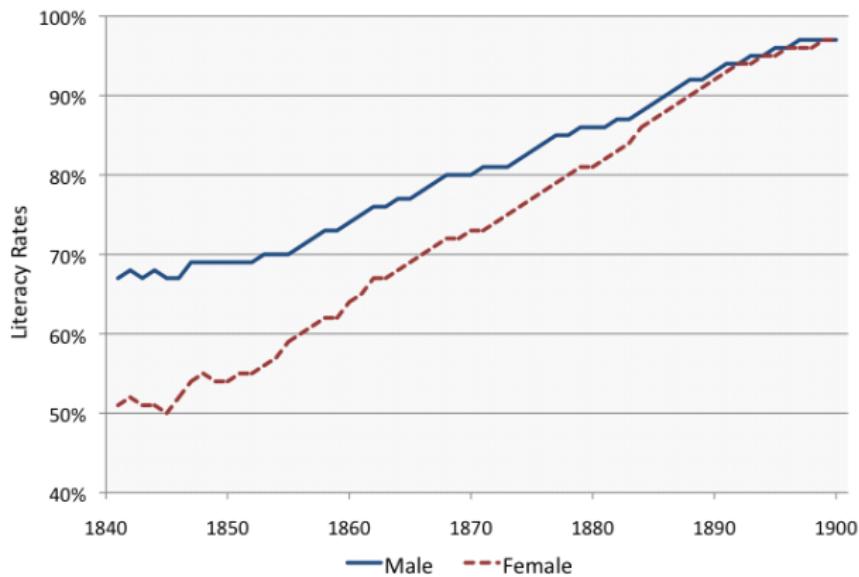
$$\text{Economic Development} \implies (w^F/w^M) \uparrow$$

- w^F ≡ women's wages
- w^M ≡ men's wages

Evolution of the Gender Earnings Ratio - US



Evolution of the Gender Literacy Gap - England



Mechanism: Women's Relative Wages and Fertility

Mechanism: Women's Relative Wages and Fertility

- Child rearing is time-intensive

Mechanism: Women's Relative Wages and Fertility

- Child rearing is time-intensive
- Women are the prime care-takers engaged in child rearing

Mechanism: Women's Relative Wages and Fertility

- Child rearing is time-intensive
- Women are the prime care-takers engaged in child rearing
- Budget constraint (if only women raise children)

$$w^F \tau n + c \leq w^M + w^F$$

Mechanism: Women's Relative Wages and Fertility

- Child rearing is time-intensive
- Women are the prime care-takers engaged in child rearing
- Budget constraint (if only women raise children)

$$w^F \tau n + c \leq w^M + w^F$$

- $w^F + w^M \equiv$ household's income

Mechanism: Women's Relative Wages and Fertility

- Child rearing is time-intensive
- Women are the prime care-takers engaged in child rearing
- Budget constraint (if only women raise children)

$$w^F \tau n + c \leq w^M + w^F$$

- $w^F + w^M \equiv$ household's income
- $c \equiv$ household's consumption

Mechanism: Women's Relative Wages and Fertility

- Child rearing is time-intensive
- Women are the prime care-takers engaged in child rearing
- Budget constraint (if only women raise children)

$$w^F \tau n + c \leq w^M + w^F$$

- $w^F + w^M \equiv$ household's income
- $c \equiv$ household's consumption
- $n \equiv$ household's (surviving) children

Mechanism: Women's Relative Wages and Fertility

- Child rearing is time-intensive
- Women are the prime care-takers engaged in child rearing
- Budget constraint (if only women raise children)

$$w^F \tau n + c \leq w^M + w^F$$

- $w^F + w^M \equiv$ household's income
- $c \equiv$ household's consumption
- $n \equiv$ household's (surviving) children
- $\tau \equiv$ time cost per child

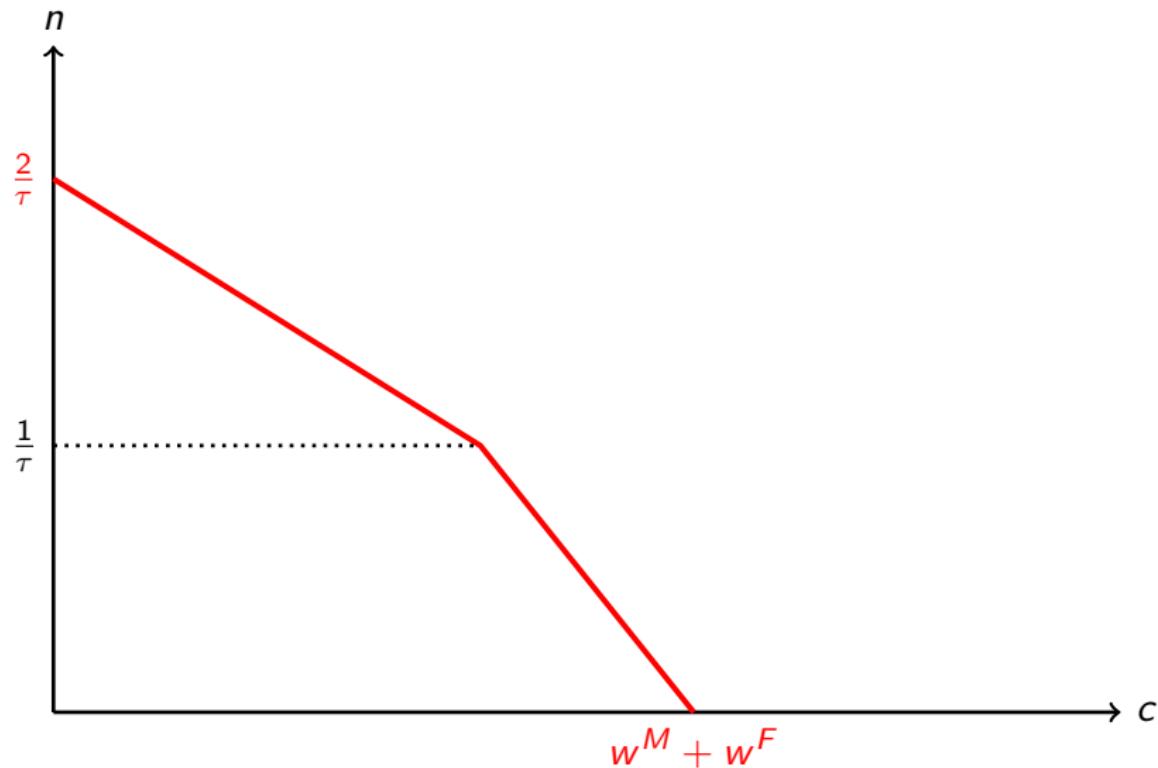
Mechanism: Women's Relative Wages and Fertility

- Child rearing is time-intensive
- Women are the prime care-takers engaged in child rearing
- Budget constraint (if only women raise children)

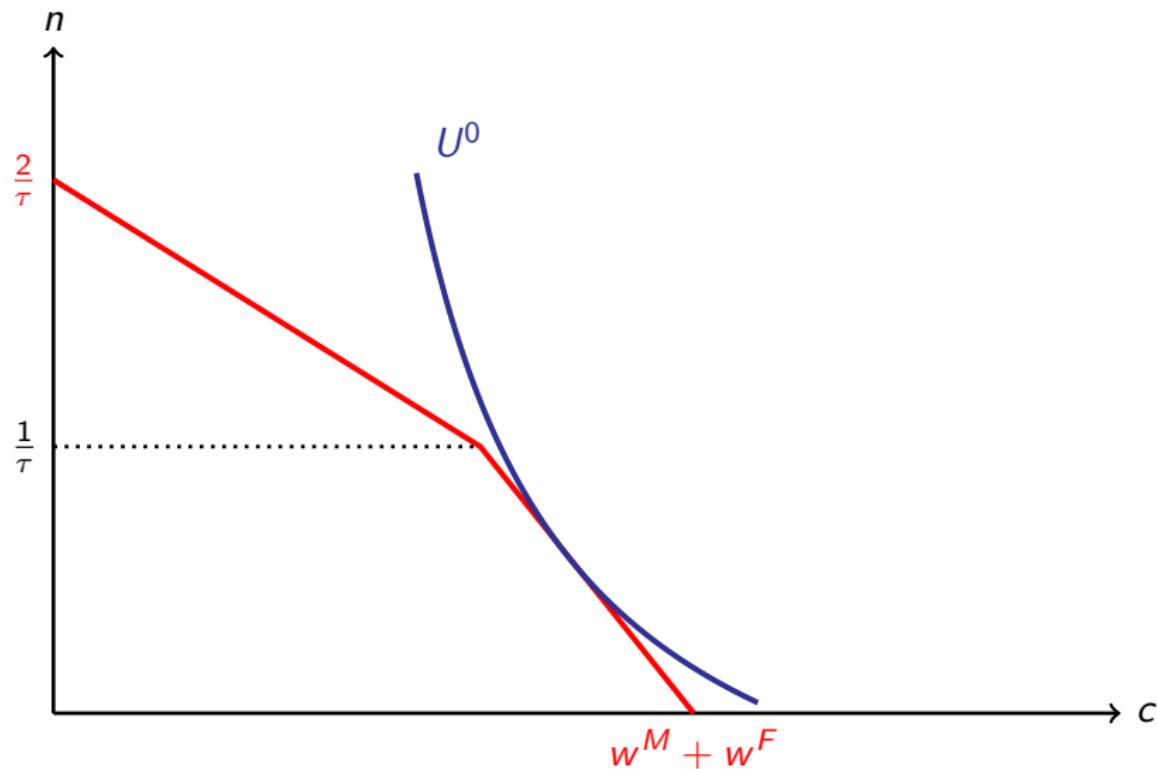
$$w^F \tau n + c \leq w^M + w^F$$

- $w^F + w^M \equiv$ household's income
- $c \equiv$ household's consumption
- $n \equiv$ household's (surviving) children
- $\tau \equiv$ time cost per child
- $w^F \tau \equiv$ opportunity cost of raising a child

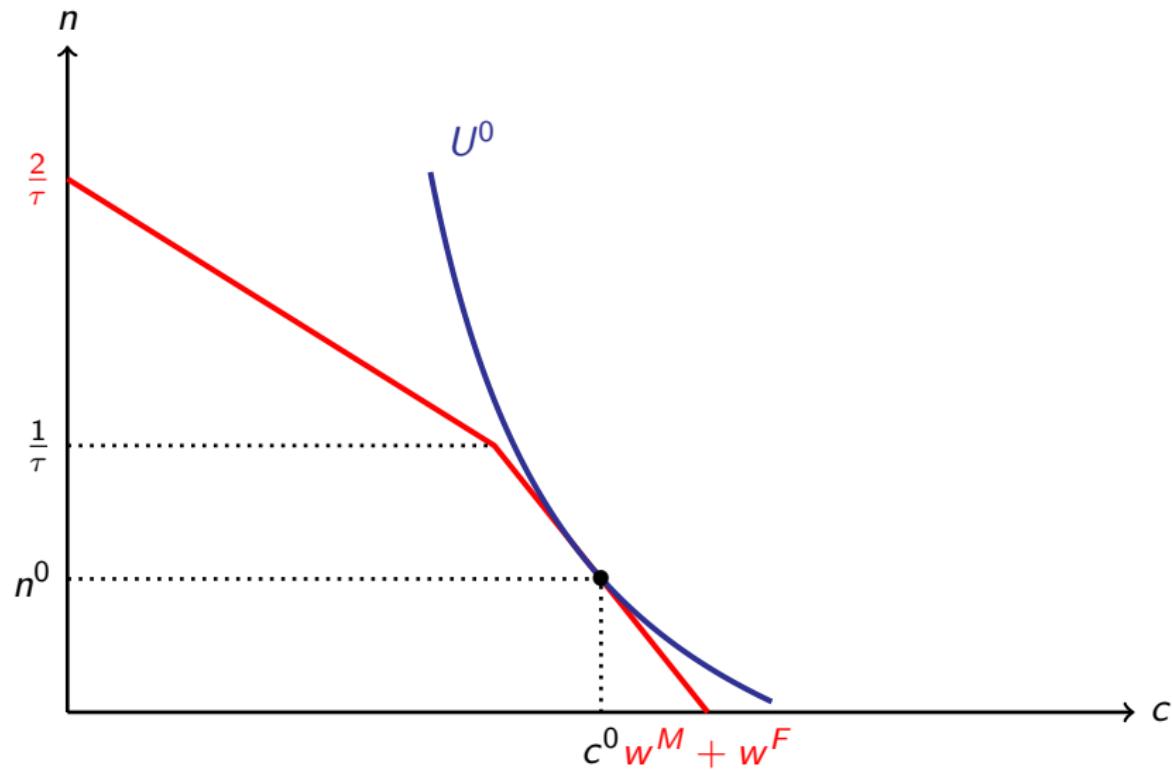
Mechanism: Women's Relative Wages and Fertility



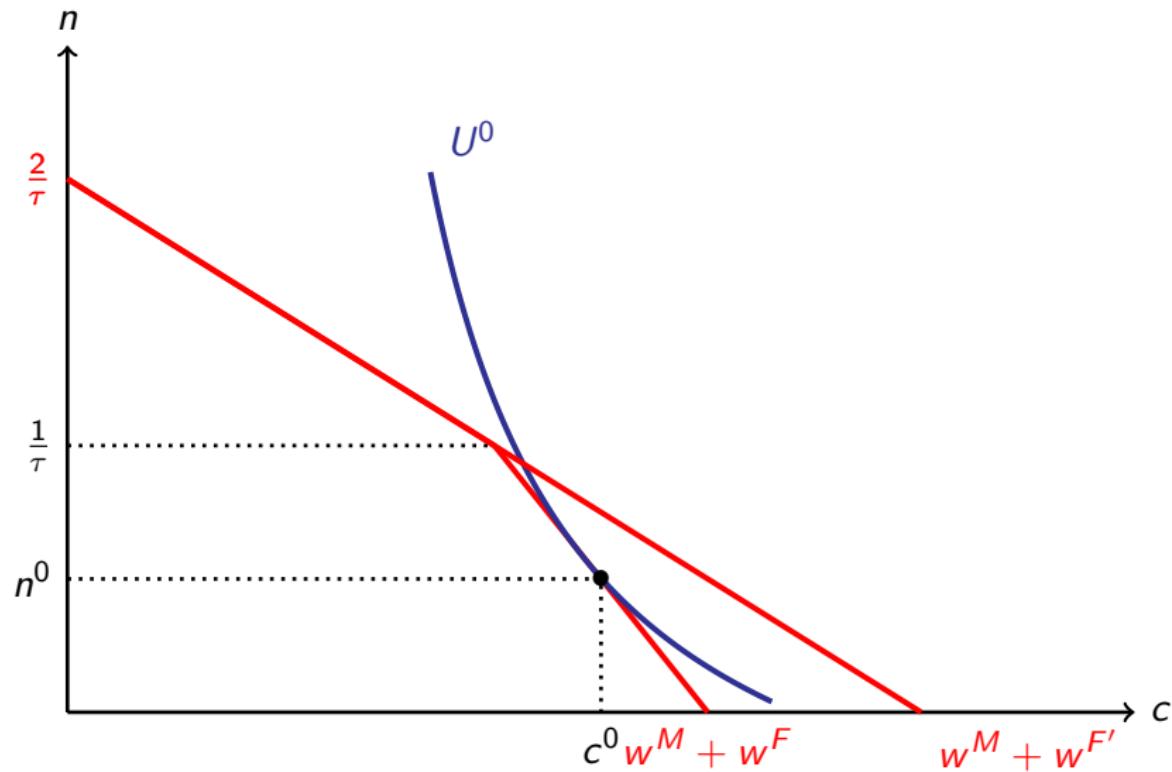
Mechanism: Women's Relative Wages and Fertility



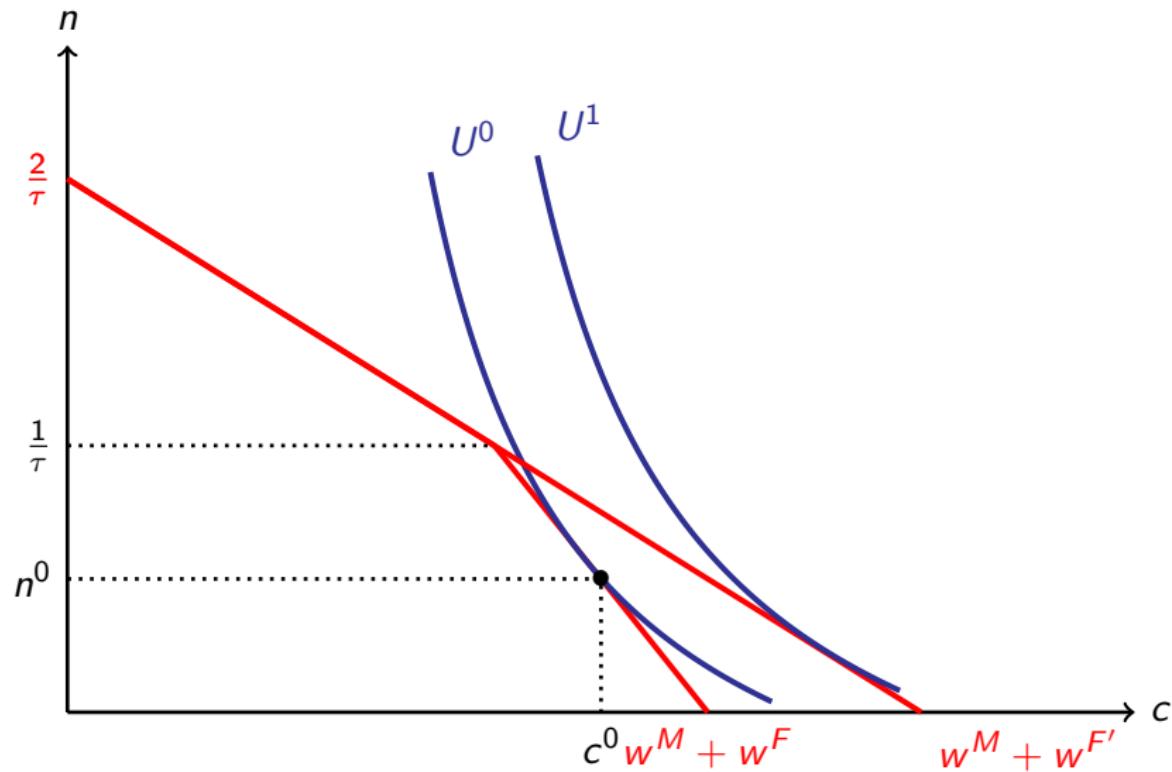
Mechanism: Women's Relative Wages and Fertility



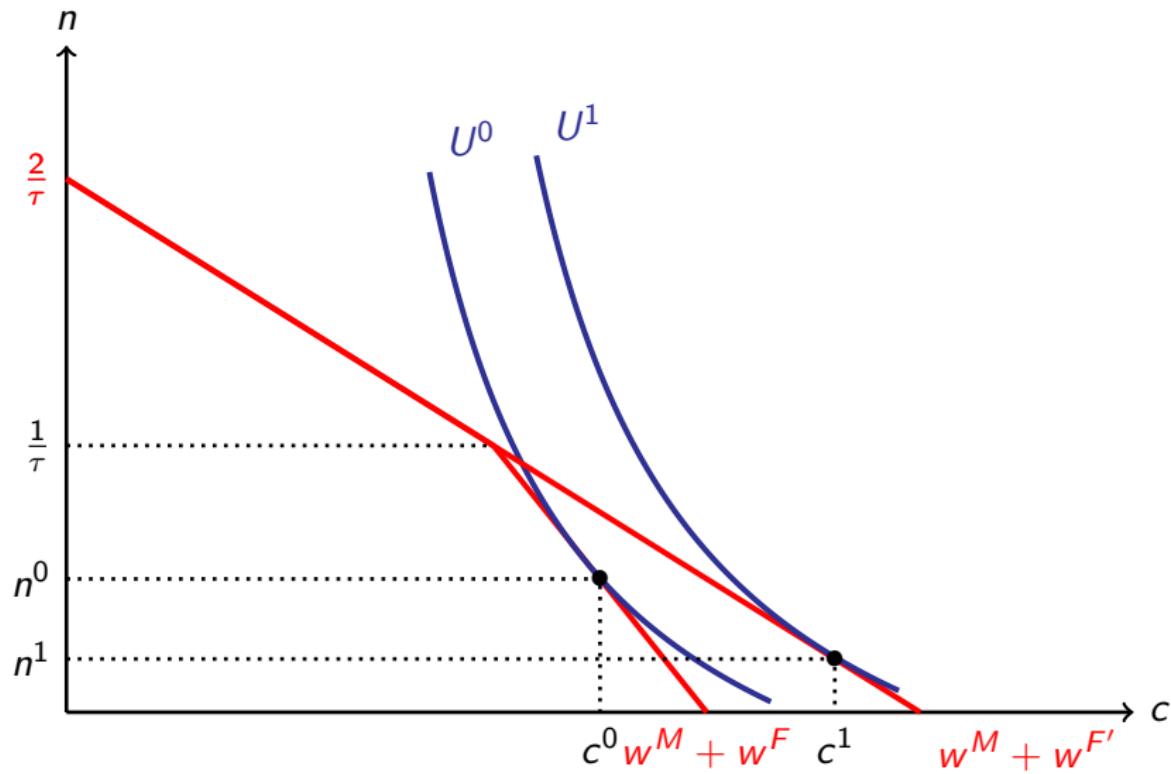
Mechanism: Women's Relative Wages and Fertility



Mechanism: Women's Relative Wages and Fertility



Mechanism: Women's Relative Wages and Fertility



Mechanism: Women's Relative Wages and Fertility

Mechanism: Women's Relative Wages and Fertility

- The rise in women's wages, w^F , generates two conflicting effects:

Mechanism: Women's Relative Wages and Fertility

- The rise in women's wages, w^F , generates two conflicting effects:
 - An income effect:

$$w^F \tau n + c \leq w^M + [w^F] \uparrow$$

Mechanism: Women's Relative Wages and Fertility

- The rise in women's wages, w^F , generates two conflicting effects:
 - An income effect:

$$w^F \tau n + c \leq w^M + [w^F] \uparrow$$

- More income for raising children

Mechanism: Women's Relative Wages and Fertility

- The rise in women's wages, w^F , generates two conflicting effects:

- An income effect:

$$w^F \tau n + c \leq w^M + [w^F] \uparrow$$

- More income for raising children \implies operates towards $n \uparrow$

Mechanism: Women's Relative Wages and Fertility

- The rise in women's wages, w^F , generates two conflicting effects:

- An income effect:

$$w^F \tau n + c \leq w^M + [w^F] \uparrow$$

- More income for raising children \implies operates towards $n \uparrow$

- A substitution effect:

$$\uparrow [w^F \tau] n + c \leq w^M + w^F$$

Mechanism: Women's Relative Wages and Fertility

- The rise in women's wages, w^F , generates two conflicting effects:

- An income effect:

$$w^F \tau n + c \leq w^M + [w^F] \uparrow$$

- More income for raising children \implies operates towards $n \uparrow$

- A substitution effect:

$$\uparrow [w^F \tau] n + c \leq w^M + w^F$$

- Opportunity cost of children increases

Mechanism: Women's Relative Wages and Fertility

- The rise in women's wages, w^F , generates two conflicting effects:

- An income effect:

$$w^F \tau n + c \leq w^M + [w^F] \uparrow$$

- More income for raising children \implies operates towards $n \uparrow$

- A substitution effect:

$$\uparrow [w^F \tau] n + c \leq w^M + w^F$$

- Opportunity cost of children increases \implies operates towards $n \downarrow$

Mechanism: Women's Relative Wages and Fertility

- The rise in women's wages, w^F , generates two conflicting effects:

- An income effect:

$$w^F \tau n + c \leq w^M + [w^F] \uparrow$$

- More income for raising children \implies operates towards $n \uparrow$

- A substitution effect:

$$\uparrow [w^F \tau] n + c \leq w^M + w^F$$

- Opportunity cost of children increases \implies operates towards $n \downarrow$

- A rise in men's wages generate only an income effect

Mechanism: Women's Relative Wages and Fertility

- The rise in women's wages, w^F , generates two conflicting effects:

- An income effect:

$$w^F \tau n + c \leq w^M + [w^F] \uparrow$$

- More income for raising children \implies operates towards $n \uparrow$

- A substitution effect:

$$\uparrow [w^F \tau] n + c \leq w^M + w^F$$

- Opportunity cost of children increases \implies operates towards $n \downarrow$

- A rise in men's wages generate only an income effect

$$w^F \tau n + c \leq [w^M] \uparrow + [w^F]$$

The Decline in the Gender Wage Gap

- If women work and raise children, an increase in w^F increases the opportunity cost of raising children more than family income,

The Decline in the Gender Wage Gap

- If women work and raise children, an increase in w^F increases the opportunity cost of raising children more than family income, i.e.,

$$w^F \uparrow \implies |\text{Income effect}| < |\text{Substitution effect}|$$

$$\implies n \downarrow \text{ (even if preferences are homothetic)}$$

The Decline in the Gender Wage Gap

- If women work and raise children, an increase in w^F increases the opportunity cost of raising children more than family income, i.e.,

$$w^F \uparrow \implies |\text{Income effect}| < |\text{Substitution effect}|$$

$$\implies n \downarrow \text{ (even if preferences are homothetic)}$$

- A rise in men's wages generate only an income effect

The Decline in the Gender Wage Gap

- If women work and raise children, an increase in w^F increases the opportunity cost of raising children more than family income, i.e.,

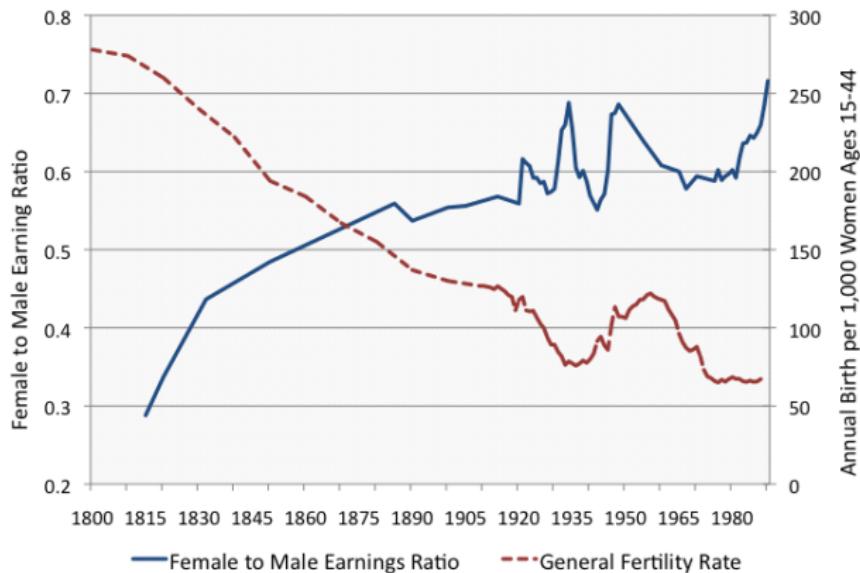
$$w^F \uparrow \implies |\text{Income effect}| < |\text{Substitution effect}|$$

$$\implies n \downarrow \text{ (even if preferences are homothetic)}$$

- A rise in men's wages generate only an income effect

$$w^M \uparrow \implies n \uparrow$$

Women's Relative Wages and Fertility - US



Women's Relative Wages and Fertility - Evidence

- US (1970s): $w^F \uparrow \implies n \downarrow$ & $w^M \uparrow \implies n \uparrow$ (Heckman and Walker ECT
79)

Women's Relative Wages and Fertility - Evidence

- US (1970s): $w^F \uparrow \implies n \downarrow$ & $w^M \uparrow \implies n \uparrow$ (Heckman and Walker ECT
79)
- Sweden's demographic transition: $(w^F/w^M) \uparrow \implies n \downarrow$ (Schultz 1985)

Women's Relative Wages and Fertility - Evidence

- US (1970s): $w^F \uparrow \implies n \downarrow$ & $w^M \uparrow \implies n \uparrow$ (Heckman and Walker ECT 79)
- Sweden's demographic transition: $(w^F/w^M) \uparrow \implies n \downarrow$ (Schultz 1985)
- France (1876–1896): reduction in the gender literacy gap had an adverse effect on fertility, accounting for income per capita, educational attainment, and mortality rates (Murphy 2015)

The Rise in the Demand for Human Capital - Main Thesis

The Rise in the Demand for Human Capital - Main Thesis

- The acceleration in the rate of technological progress in the 2nd phase of industrialization increased the demand for human capital

The Rise in the Demand for Human Capital - Main Thesis

- The acceleration in the rate of technological progress in the 2nd phase of industrialization increased the demand for human capital
 - education enabled individuals to cope with a rapidly changing technological environment

The Rise in the Demand for Human Capital - Main Thesis

- The acceleration in the rate of technological progress in the 2nd phase of industrialization increased the demand for human capital
 - education enabled individuals to cope with a rapidly changing technological environment
- The rise in the demand for human capital induced a substitution of quality for quantity of children triggering a demographic transition

The Rise in the Demand for Human Capital - Main Thesis

- The acceleration in the rate of technological progress in the 2nd phase of industrialization increased the demand for human capital
 - education enabled individuals to cope with a rapidly changing technological environment
- The rise in the demand for human capital induced a substitution of quality for quantity of children triggering a demographic transition
 - ⇒ reduction in fertility

The Model - Preferences

$$u = (1 - \gamma) \ln c + \gamma [\ln n + \beta \ln h]$$

The Model - Preferences

$$u = (1 - \gamma) \ln c + \gamma [\ln n + \beta \ln h]$$

- c \equiv consumption

The Model - Preferences

$$u = (1 - \gamma) \ln c + \gamma [\ln n + \beta \ln h]$$

- $c \equiv$ consumption
- $n \equiv$ (surviving) children

The Model - Preferences

$$u = (1 - \gamma) \ln c + \gamma [\ln n + \beta \ln h]$$

- $c \equiv$ consumption
- $n \equiv$ (surviving) children
- $h \equiv$ quality (human capital) of each child

The Model - Preferences

$$u = (1 - \gamma) \ln c + \gamma [\ln n + \beta \ln h]$$

- $c \equiv$ consumption
- $n \equiv$ (surviving) children
- $h \equiv$ quality (human capital) of each child
- $\beta \equiv$ degree of preference for child quality;

The Model - Preferences

$$u = (1 - \gamma) \ln c + \gamma [\ln n + \beta \ln h]$$

- $c \equiv$ consumption
- $n \equiv$ (surviving) children
- $h \equiv$ quality (human capital) of each child
- $\beta \equiv$ degree of preference for child quality; $\beta < 1$

The Model - Budget Constraint

$$yn(\tau^q + \tau^e e) + c \leq y$$

The Model - Budget Constraint

$$yn(\tau^q + \tau^e e) + c \leq y$$

- $y \equiv$ household potential income

The Model - Budget Constraint

$$yn(\tau^q + \tau^e e) + c \leq y$$

- y \equiv household potential income
- τ^q \equiv fraction of the household's unit-time endowment required to raise a child, regardless of quality

The Model - Budget Constraint

$$yn(\tau^q + \tau^e e) + c \leq y$$

- y \equiv household potential income
- τ^q \equiv fraction of the household's unit-time endowment required to raise a child, regardless of quality
- τ^e \equiv fraction of the household's unit-time endowment required for each unit of education per child

The Model - Budget Constraint

$$yn(\tau^q + \tau^e e) + c \leq y$$

- y \equiv household potential income
- τ^q \equiv fraction of the household's unit-time endowment required to raise a child, regardless of quality
- τ^e \equiv fraction of the household's unit-time endowment required for each unit of education per child
- $(\tau^q + \tau^e e)$ \equiv time cost of raising a child with a level of education (quality)
 e

The Model - Budget Constraint

$$yn(\tau^q + \tau^e e) + c \leq y$$

- y \equiv household potential income
- τ^q \equiv fraction of the household's unit-time endowment required to raise a child, regardless of quality
- τ^e \equiv fraction of the household's unit-time endowment required for each unit of education per child
- $(\tau^q + \tau^e e)$ \equiv time cost of raising a child with a level of education (quality) e
- $y(\tau^q + \tau^e e)$ \equiv opportunity cost of raising a child with quality e

The Model - Human Capital Formation

$$h = h(e, g)$$

The Model - Human Capital Formation

$$h = h(e, g)$$

- $h_e(e, g) > 0$ & $h_{ee}(e, g) < 0$

The Model - Human Capital Formation

$$h = h(e, g)$$

- $h_e(e, g) > 0$ & $h_{ee}(e, g) < 0$
 - HC is increasing (at decreasing rates) in the parental time investment in the education of the child

The Model - Human Capital Formation

$$h = h(e, g)$$

- $h_e(e, g) > 0 \text{ & } h_{ee}(e, g) < 0$
 - HC is increasing (at decreasing rates) in the parental time investment in the education of the child
- $h_g(e, g) < 0 \text{ & } h_{gg}(e, g) > 0$

The Model - Human Capital Formation

$$h = h(e, g)$$

- $h_e(e, g) > 0$ & $h_{ee}(e, g) < 0$
 - HC is increasing (at decreasing rates) in the parental time investment in the education of the child
- $h_g(e, g) < 0$ & $h_{gg}(e, g) > 0$
 - HC is decreasing in the rate of technological progress (obsolescence of HC in a changing technological environment)

The Model - Human Capital Formation

$$h = h(e, g)$$

- $h_e(e, g) > 0 \text{ & } h_{ee}(e, g) < 0$
 - HC is increasing (at decreasing rates) in the parental time investment in the education of the child
- $h_g(e, g) < 0 \text{ & } h_{gg}(e, g) > 0$
 - HC is decreasing in the rate of technological progress (obsolescence of HC in a changing technological environment)
- $h_{eg}(e, g) > 0$

The Model - Human Capital Formation

$$h = h(e, g)$$

- $h_e(e, g) > 0 \text{ & } h_{ee}(e, g) < 0$
 - HC is increasing (at decreasing rates) in the parental time investment in the education of the child
- $h_g(e, g) < 0 \text{ & } h_{gg}(e, g) > 0$
 - HC is decreasing in the rate of technological progress (obsolescence of HC in a changing technological environment)
- $h_{eg}(e, g) > 0$
 - Education lessens the obsolescence of HC in a changing technological environment

The Model - Human Capital Formation

$$h = h(e, g)$$

- $h_e(e, g) > 0 \text{ & } h_{ee}(e, g) < 0$
 - HC is increasing (at decreasing rates) in the parental time investment in the education of the child
- $h_g(e, g) < 0 \text{ & } h_{gg}(e, g) > 0$
 - HC is decreasing in the rate of technological progress (obsolescence of HC in a changing technological environment)
- $h_{eg}(e, g) > 0$
 - Education lessens the obsolescence of HC in a changing technological environment
- $h(0, g) > 0 \text{ & } \lim_{e \rightarrow 0} h_e(e, g) = \infty; \lim_{e \rightarrow \infty} h_e(e, g) = 0$

The Model - Human Capital Formation

$$h = h(e, g)$$

- $h_e(e, g) > 0 \text{ & } h_{ee}(e, g) < 0$
 - HC is increasing (at decreasing rates) in the parental time investment in the education of the child
- $h_g(e, g) < 0 \text{ & } h_{gg}(e, g) > 0$
 - HC is decreasing in the rate of technological progress (obsolescence of HC in a changing technological environment)
- $h_{eg}(e, g) > 0$
 - Education lessens the obsolescence of HC in a changing technological environment
- $h(0, g) > 0 \text{ & } \lim_{e \rightarrow 0} h_e(e, g) = \infty; \lim_{e \rightarrow \infty} h_e(e, g) = 0$
 - Basic level of human capital & interior solution

The Model - Optimization

The Model - Optimization

$$\begin{aligned} \{n, e, c\} &= \arg \max \gamma[\ln n + \beta \ln h(e, g)] + (1 - \gamma) \ln c \\ s.t. \quad & yn(\tau^q + \tau^e e) + c \leq y \end{aligned}$$

The Model - Optimization

$$\begin{aligned} \{n, e, c\} &= \arg \max \gamma[\ln n + \beta \ln h(e, g)] + (1 - \gamma) \ln c \\ s.t. \quad & yn(\tau^q + \tau^e e) + c \leq y \end{aligned}$$

since $c = y[1 - n(\tau^q + \tau^e e)]$

The Model - Optimization

$$\begin{aligned}\{n, e, c\} &= \arg \max \gamma[\ln n + \beta \ln h(e, g)] + (1 - \gamma) \ln c \\ s.t. \quad & yn(\tau^q + \tau^e e) + c \leq y\end{aligned}$$

since $c = y[1 - n(\tau^q + \tau^e e)] \iff$

The Model - Optimization

$$\begin{aligned}\{n, e, c\} &= \arg \max \gamma[\ln n + \beta \ln h(e, g)] + (1 - \gamma) \ln c \\ s.t. \quad & yn(\tau^q + \tau^e e) + c \leq y\end{aligned}$$

since $c = y[1 - n(\tau^q + \tau^e e)] \iff$

$$\{n, e\} = \arg \max \gamma[\ln n + \beta \ln h(e, g)] + (1 - \gamma) \ln y[1 - n(\tau^q + \tau^e e)]$$

Optimization

$$\{n, e\} = \arg \max \gamma[\ln n + \beta \ln h(e, g)] + (1 - \gamma) \ln y[1 - n(\tau^q + \tau^e e)]$$

Optimization

$$\{n, e\} = \arg \max \gamma[\ln n + \beta \ln h(e, g)] + (1 - \gamma) \ln y[1 - n(\tau^q + \tau^e e)]$$

- with respect to n :

Optimization

$$\{n, e\} = \arg \max \gamma[\ln n + \beta \ln h(e, g)] + (1 - \gamma) \ln y[1 - n(\tau^q + \tau^e e)]$$

- with respect to n :

$$\frac{\gamma}{n} = \frac{(1 - \gamma)y(\tau^q + \tau^e e)}{y[1 - n(\tau^q + \tau^e e)]}$$

Optimization

$$\{n, e\} = \arg \max \gamma[\ln n + \beta \ln h(e, g)] + (1 - \gamma) \ln y[1 - n(\tau^q + \tau^e e)]$$

- with respect to n :

$$\frac{\gamma}{n} = \frac{(1 - \gamma)y(\tau^q + \tau^e e)}{y[1 - n(\tau^q + \tau^e e)]}$$

$$\gamma[1 - n(\tau^q + \tau^e e)] = (1 - \gamma)(\tau^q + \tau^e e)n$$

Optimization

$$\{n, e\} = \arg \max \gamma[\ln n + \beta \ln h(e, g)] + (1 - \gamma) \ln y[1 - n(\tau^q + \tau^e e)]$$

- with respect to n :

$$\frac{\gamma}{n} = \frac{(1 - \gamma)y(\tau^q + \tau^e e)}{y[1 - n(\tau^q + \tau^e e)]}$$

$$\gamma[1 - n(\tau^q + \tau^e e)] = (1 - \gamma)(\tau^q + \tau^e e)n$$

$$n(\tau^q + \tau^e e) = \gamma$$

Optimization

$$\{n, e\} = \arg \max \gamma[\ln n + \beta \ln h(e, g)] + (1 - \gamma) \ln y[1 - n(\tau^q + \tau^e e)]$$

Optimization

$$\{n, e\} = \arg \max \gamma[\ln n + \beta \ln h(e, g)] + (1 - \gamma) \ln y[1 - n(\tau^q + \tau^e e)]$$

- with respect to e :

$$\frac{\gamma \beta h_e(e, g)}{h(e, g)} = \frac{(1 - \gamma) y n \tau^e}{y[1 - n(\tau^q + \tau^e e)]}$$

Optimization

$$\{n, e\} = \arg \max \gamma[\ln n + \beta \ln h(e, g)] + (1 - \gamma) \ln y[1 - n(\tau^q + \tau^e e)]$$

- with respect to e :

$$\frac{\gamma \beta h_e(e, g)}{h(e, g)} = \frac{(1 - \gamma) y n \tau^e}{y[1 - n(\tau^q + \tau^e e)]}$$

- since $n(\tau^q + \tau^e e) = \gamma$

Optimization

$$\{n, e\} = \arg \max \gamma[\ln n + \beta \ln h(e, g)] + (1 - \gamma) \ln y[1 - n(\tau^q + \tau^e e)]$$

- with respect to e :

$$\frac{\gamma \beta h_e(e, g)}{h(e, g)} = \frac{(1 - \gamma) y n \tau^e}{y[1 - n(\tau^q + \tau^e e)]}$$

- since $n(\tau^q + \tau^e e) = \gamma$

$$\frac{\gamma \beta h_e(e, g)}{h(e, g)} = n \tau^e$$

Optimization

$$\{n, e\} = \arg \max \gamma[\ln n + \beta \ln h(e, g)] + (1 - \gamma) \ln y[1 - n(\tau^q + \tau^e e)]$$

- with respect to e :

$$\frac{\gamma \beta h_e(e, g)}{h(e, g)} = \frac{(1 - \gamma) y n \tau^e}{y[1 - n(\tau^q + \tau^e e)]}$$

- since $n(\tau^q + \tau^e e) = \gamma$

$$\frac{\gamma \beta h_e(e, g)}{h(e, g)} = n \tau^e \implies \frac{\beta h_e(e, g)}{h(e, g)} = \frac{\tau^e}{(\tau^q + \tau^e e)}$$

Optimization

$$\{n, e\} = \arg \max \gamma[\ln n + \beta \ln h(e, g)] + (1 - \gamma) \ln y[1 - n(\tau^q + \tau^e e)]$$

- with respect to e :

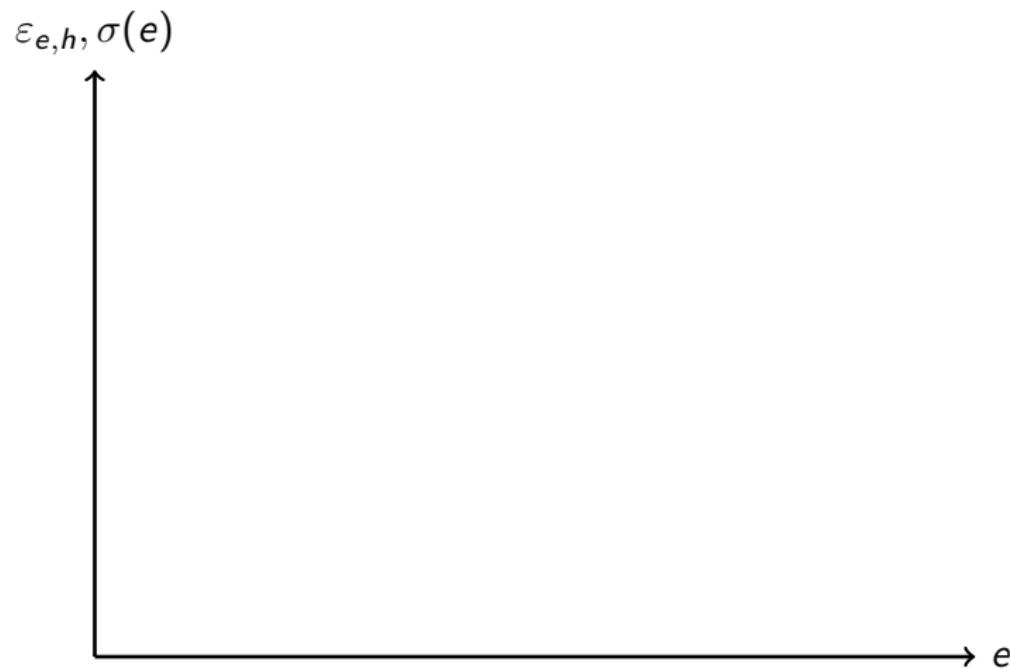
$$\frac{\gamma \beta h_e(e, g)}{h(e, g)} = \frac{(1 - \gamma) y n \tau^e}{y[1 - n(\tau^q + \tau^e e)]}$$

- since $n(\tau^q + \tau^e e) = \gamma$

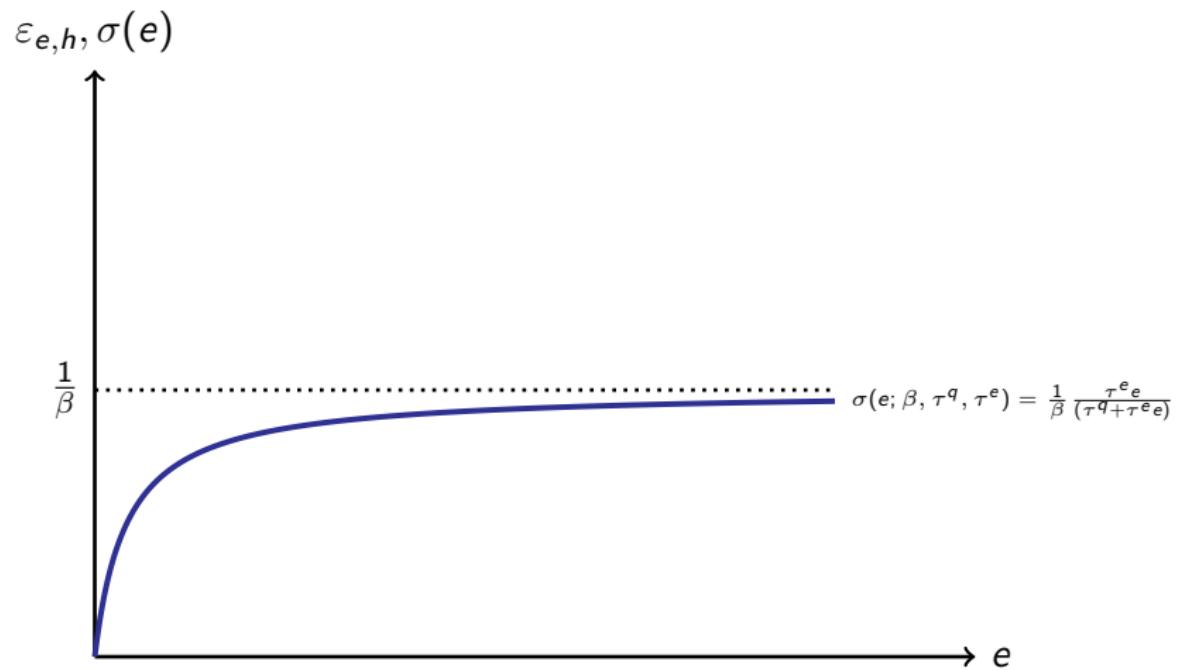
$$\frac{\gamma \beta h_e(e, g)}{h(e, g)} = n \tau^e \implies \frac{\beta h_e(e, g)}{h(e, g)} = \frac{\tau^e}{(\tau^q + \tau^e e)}$$

$$\implies \varepsilon_{h,e} \equiv \frac{h_e(e, g)e}{h(e, g)} = \frac{1}{\beta} \frac{\tau^e e}{(\tau^q + \tau^e e)} \equiv \sigma(e; \beta, \tau^q, \tau^e)$$

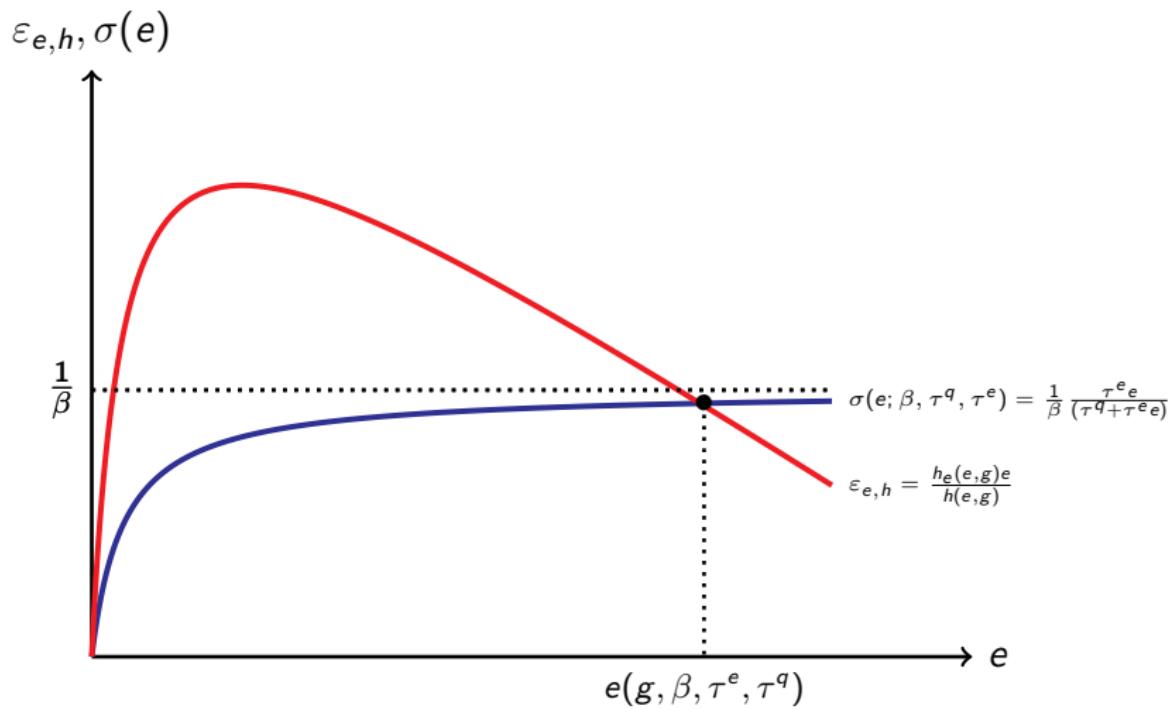
Optimal education choice



Optimal education choice



Optimal education choice



Optimization

- So,

Optimization

- So,

$$n = \gamma / (\tau^q + \tau^e e)$$

$$\tau^e h(e, g) = \beta h_e(e, g) (\tau^q + \tau^e e)$$

Optimization

- So,

$$n = \gamma / (\tau^q + \tau^e e)$$

$$\tau^e h(e, g) = \beta h_e(e, g) (\tau^q + \tau^e e)$$

⇒

Optimization

- So,

$$n = \gamma / (\tau^q + \tau^e e)$$

$$\tau^e h(e, g) = \beta h_e(e, g) (\tau^q + \tau^e e)$$

\implies

$$e = e(g, \beta, \tau^e, \tau^q),$$

$$n = \gamma / [\tau^q + \tau^e e(g, \beta, \tau^e, \tau^q)]$$

Testable Predictions - Investment in Quality

The optimal level of investment in child quality increases if:

Testable Predictions - Investment in Quality

The optimal level of investment in child quality increases if:

- The technological environment changes more rapidly

$$\partial e(g, \beta, \tau^e, \tau^q) / \partial g > 0$$

Testable Predictions - Investment in Quality

The optimal level of investment in child quality increases if:

- The technological environment changes more rapidly

$$\partial e(g, \beta, \tau^e, \tau^q) / \partial g > 0$$

- Preferences for child quality are higher

$$\partial e(g, \beta, \tau^e, \tau^q) / \partial \beta > 0$$

Testable Predictions - Investment in Quality

The optimal level of investment in child quality increases if:

- The technological environment changes more rapidly

$$\partial e(g, \beta, \tau^e, \tau^q) / \partial g > 0$$

- Preferences for child quality are higher

$$\partial e(g, \beta, \tau^e, \tau^q) / \partial \beta > 0$$

- The cost of raising a child (regardless of quality) increases

$$\partial e(g, \beta, \tau^e, \tau^q) / \partial \tau^q > 0$$

Testable Predictions - Investment in Quality

The optimal level of investment in child quality increases if:

- The technological environment changes more rapidly

$$\partial e(g, \beta, \tau^e, \tau^q) / \partial g > 0$$

- Preferences for child quality are higher

$$\partial e(g, \beta, \tau^e, \tau^q) / \partial \beta > 0$$

- The cost of raising a child (regardless of quality) increases

$$\partial e(g, \beta, \tau^e, \tau^q) / \partial \tau^q > 0$$

- The cost of educating a child decreases

$$\partial e(g, \beta, \tau^e, \tau^q) / \partial \tau^e < 0$$

Testable Predictions - Investment in Quantity

The optimal number of children decreases if:

Testable Predictions - Investment in Quantity

The optimal number of children decreases if:

- The technological environment changes more rapidly

$$\partial n / \partial g < 0$$

Testable Predictions - Investment in Quantity

The optimal number of children decreases if:

- The technological environment changes more rapidly

$$\partial n / \partial g < 0$$

- Preferences for child quality are higher

$$\partial n / \partial \beta < 0$$

Testable Predictions - Investment in Quantity

The optimal number of children decreases if:

- The technological environment changes more rapidly

$$\partial n / \partial g < 0$$

- Preferences for child quality are higher

$$\partial n / \partial \beta < 0$$

- The cost of raising a child (regardless of quality) increases

$$\partial n / \partial \tau^q < 0$$

Testable Predictions - Investment in Quantity

The optimal number of children decreases if:

- The technological environment changes more rapidly

$$\partial n / \partial g < 0$$

- Preferences for child quality are higher

$$\partial n / \partial \beta < 0$$

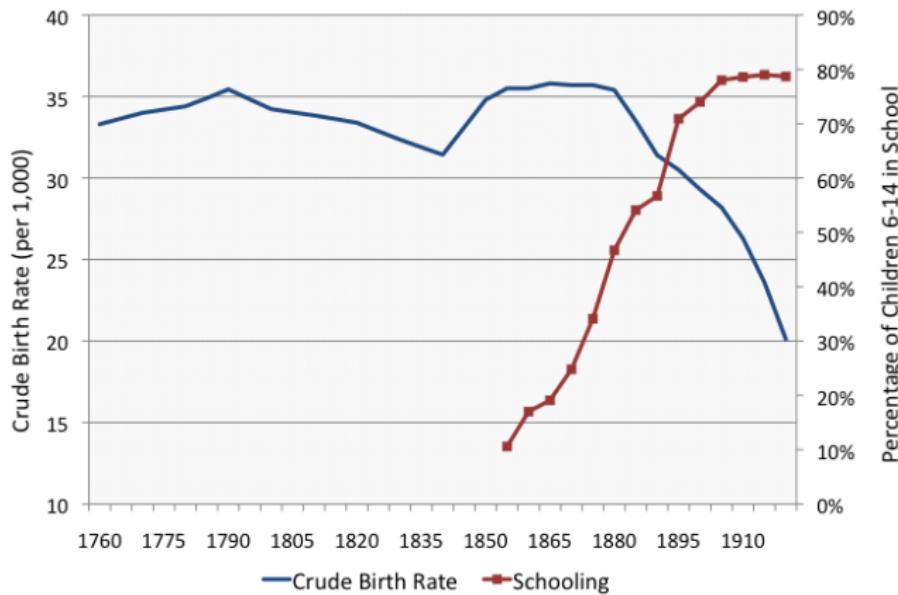
- The cost of raising a child (regardless of quality) increases

$$\partial n / \partial \tau^q < 0$$

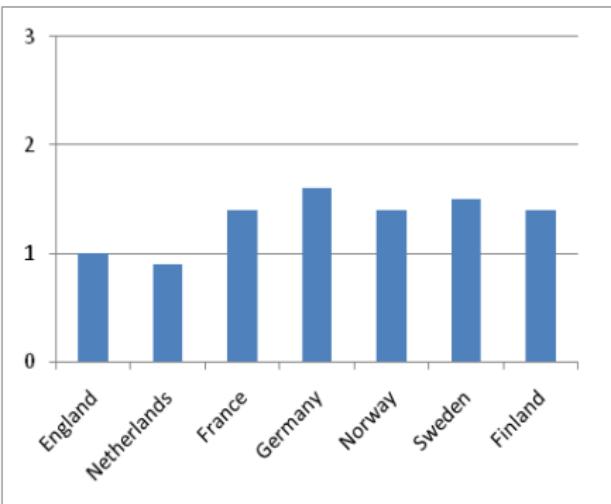
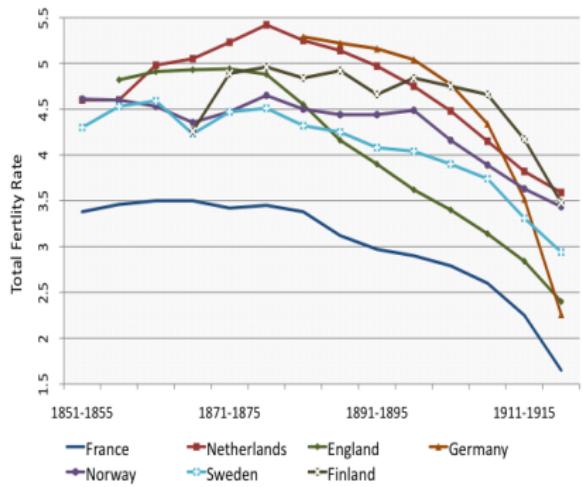
- The cost of educating a child increases and the elasticity of child quality with respect to the cost of child quality is smaller than one in absolute value

$$\partial n / \partial \tau^e < 0 \text{ if } [\partial e / \partial \tau^e][\tau^e / e] > -1$$

Human Capital Formation and the DT - England



Growth Rates 1870-1913 and DT



Supporting Evidence: Cross-Country Evidence

- Cross Section of Countries (1870-2000) - educational attainment has been negatively associated with fertility, accounting for income per worker and mortality rates (Murtin 2013).

Supporting Evidence: Cross-Country Evidence

- Cross Section of Countries (1870-2000) - educational attainment has been negatively associated with fertility, accounting for income per worker and mortality rates (Murtin 2013).
- Cross Section of Countries (1960-1999): adverse effect on net fertility of an increase in productivity in advanced stages of development, when education demand dominates (Lehr 2009)

Supporting Evidence: Evidence from Individual Countries

- US (1910s): Eradication of hookworm – a positive shock to the return to child quality - had an adverse effect on fertility (Bleakley-Lange 2009)

Supporting Evidence: Evidence from Individual Countries

- US (1910s): Eradication of hookworm – a positive shock to the return to child quality - had an adverse effect on fertility (Bleakley-Lange 2009)
- Prussia (19th century): the rise in human capital formation has had an adverse effect on fertility (Becker-Cinnirella-Woessmann 2010)

Supporting Evidence: Evidence from Individual Countries

- US (1910s): Eradication of hookworm – a positive shock to the return to child quality - had an adverse effect on fertility (Bleakley-Lange 2009)
- Prussia (19th century): the rise in human capital formation has had an adverse effect on fertility (Becker-Cinnirella-Woessmann 2010)
- France (1876–96): the level of education attainment had an adverse effect on fertility rates during France's demographic transition, accounting for income per capita, the gender literacy gap, and mortality rates. (Murphy 2015)

Supporting Evidence: Evidence from Individual Countries

- US (1910s): Eradication of hookworm – a positive shock to the return to child quality - had an adverse effect on fertility (Bleakley-Lange 2009)
- Prussia (19th century): the rise in human capital formation has had an adverse effect on fertility (Becker-Cinnirella-Woessmann 2010)
- France (1876–96): the level of education attainment had an adverse effect on fertility rates during France's demographic transition, accounting for income per capita, the gender literacy gap, and mortality rates. (Murphy 2015)
- England (1580-1871) Adverse effect of family size on children's literacy.
(Klemp-Weisdorf 2016)