# **Decision-Aware Model Learning for Actor-Critic Methods: When Theory Does Not Meet Practice**

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## **Abstract**

Actor-Critic methods are a prominent class of modern reinforcement learning algorithms based on the classic Policy Iteration procedure. Despite many successful cases, Actor-Critic methods tend to require a gigantic number of experiences and can be very unstable. Recent approaches have advocated learning and using a world model to improve sample efficiency and reduce reliance on the value function estimate. However, learning an accurate dynamics model of the world remains challenging, often requiring computationally costly and data-hungry models. More recent work has shown that learning an everywhere accurate model is unnecessary and often detrimental to the overall task; instead, the agent should improve the world model on task-critical regions. For example, in Iterative Value-Aware Model Learning, the authors extend model-based value iteration by incorporating the value function (estimate) into the model loss function, showing the novel model objective reflects improved performance in the end task. Therefore, it seems natural to expect that model-based Actor-Critic methods can benefit equally from learning valueaware models, improving overall task performance, or reducing the need for large, expensive models. However, we show empirically that combining Actor-Critic and value-aware model learning can be quite difficult and that naive approaches such as maximum likelihood estimation often achieve superior performance with less computational cost. Our results suggest that, despite theoretical guarantees, learning a value-aware model in continuous domains does not ensure better performance on the overall task.

# 1 Introduction

Actor-Critic (AC) methods [17, 19, 26, 40, 41] are a prominent class of model-free reinforcement learning (RL) algorithms based on the classic Policy Iteration procedure. The method consists in iterating over two main steps: evaluating the agent's policy (updating the value function estimate of the expected policy returns), and improving the current policy. Combined with recent advances in deep neural network function approximators [16], AC methods have obtained impressive results in many challenging sequential decision making problems such as playing Atari games from image pixel input [40] and learning complex robot gaits in simulation [22].

Recently, there has been a growing interest in extending AC methods by progressively learning and using a model of the environment dynamics [7, 8, 10, 15, 23]. The use of a dynamics model (a.k.a. world model) has been shown to greatly improve sample-efficiency [27, 32, 39], an important aspect in environments with costly actions (which are arguably more common when one ventures outside of simulation-based tasks, such as in robotics and industrial applications). Using a world model can also reduce the algorithm's reliance on the quality of the estimated value-function through mechanisms

such as multistep bootstrapping. Moreover, recent work shows that learning a world model is often easier than finding an accurate value function approximation [9], increasing the stability of RL methods. Finally, having access to a world model unlocks different learning modalities, such as learning value functions in Sobolev spaces [10].

Yet learning a world model introduces its own challenges. For instance, the model class may be *misspecified* [24], meaning that the function approximator used cannot accurately represent the true dynamics everywhere on the state space (or even in most of it). In such cases, by attempting to improve the average accuracy standard model learning approaches such as Maximum Likelihood Estimation (MLE) may sub-utilize the model capacity and fail at aiding policy learning.

Decision-aware model learning (DAML) [1, 11, 13, 14] tackles this problem by taking the decision making objective into account when optimizing for the world model. Iterative value-aware model learning [13] (IterVAML), for instance, introduces a novel model loss function which incorporates the current estimate of the value function. Under assumptions on the sample collection, model space, and value function space, the authors of IterVAML were able to theoretically link the performance of a model-based agent as a function of, among other things, the value-aware model-error (in particular they have shown that the lower that error, the closer the resulting policy is to the optimal one).¹ Although promising in theory, neither the IterVAML work or any subsequent work validated the result in practical deep RL settings.

Given the above discussion, it seems just natural to expect that one can boost the performance of model-based Actor-Critic (MBAC) methods by incorporating value-awareness into model learning. Guided by that reasoning, in this work we provide an empirical analysis of VAML in the deep RL setting, with neural network models in continuous control environments. We assess the core claims of VAML in carefully constructed artificial settings while varying the capacity of the neural network model. Then, we reformulate IterVAML, originally devised as an approximate value iteration method, as an approximate policy iteration algorithm, thus obtaining a value-aware MBAC method. To our surprise, we found that value-aware learning does not provide a clear and consistent advantage over MLE in our controlled artificial settings. Yet we find some evidence of VAML being advantageous in dynamical systems common to many deep RL benchmarks. However, upon combining value-aware learning and model-based policy improvement, we find that the resulting agent is too unstable and that switching to MLE provides comparable, and sometimes better, performance at lower computational cost. Our results suggest that, despite theoretical guarantees, learning a value-aware model in continuous domains does not ensure better performance on the overall task when compared with conventional likelihood-based model learning methods such as MLE. We speculate that some of the assumptions behind the IterVAML framework may not transfer to the deep RL setting and that poorly learned values may negatively impact model optimization.

The rest of this paper is organized as follows. Section 2 delineates related work on model-based actor-critic methods and decision-aware model learning. Section 3 lays out important background on Actor-Critic methods and value-aware model learning. Section 4 introduces our proposed adaptation of IterVAML to the Actor-Critic setting. Section 5 introduces our proposed experiments and discusses the positive and negative results from each. Finally, section 6 concludes with a discussion of the possible explanations for the gap between theory and practice, while also pointing to future research directions to expand our limited understanding of these issues.

## 2 Related work

**Model-based Actor-Critic methods.** There has been a growing interest in extending AC methods by progressively learning and using a model of the environment dynamics. The Dyna framework [36] lays the foundation many model-based methods by using the model to generate virtual experiences for use in model-free methods. One of the most successful instantiations of this paradigm in deep RL is the Model-Based Policy Optimization (MBPO) algorithm [23]. MBPO extends the Soft Actor-Critic (SAC) algorithm [19] (an off-policy, model-free AC method) by generating short model-based rollouts branched from real experiences that are then mixed together to augment the experience replay buffer.

<sup>&</sup>lt;sup>1</sup>The other relevant quantities in the performance bound are the number of samples and the regression error when learning the value function. Since these are inherent to any RL algorithm, we emphasize here the value-aware error.

MBPO is successful in increasing the sample-efficiency of SAC, but learns its model via maximum likelihood, ignoring performance on the end task.

Another prominent line of work in model-based AC methods leverages differentiable models to calculate the gradient of final performance in a policy gradient framework. Stochastic Value Gradients (SVG) uses reparameterizable models to calculate analytical policy gradients using real experiences (no virtual samples are generated). SAC-SVG [3] and Model-Augmented Actor-Critic [8] expand this concept by using model gradients and virtual experiences in the policy update of SAC. Dreamer [21] uses many of the same ideas, but its model operates in a compressed state space extracted from pixel observations using variational methods. Only Dreamer, however, incorporates some aspect of the decision-making task by optimizing its model to predict rewards, but not full returns.

Another way to exploit model derivatives is in learning action-values. In Model-based Action-Gradient-Estimator (MAGE) [10], the authors also exploit reparameterizable models to compute action-value gradients used to learn critics in Sobolev space. Built upon the TD3 [17] AC method, MAGE manages to learn better critics that increase sample-efficiency over the model-free TD3.

**Decision-aware model learning.** The authors of Value-aware Model Learning (VAML) [14] argue that optimizing a probabilistic model loss (as in MLE) is overkill since it does not take into account the end RL task. They show, theoretically and empirically, that incorporating the value function structure in the model cost produces better results when the model capacity is restricted. However, VAML's loss function uses a pessimistic formulation that requires an additional search over the value function space. IterVAML [13] relaxes this formulation by using the current value function estimate, produced along the course of the RL algorithm, in the model loss. The authors show, theoretically, that the value-aware model loss impacts the end task performance, thus optimizing it should lead to better results. Both VAML and IterVAML lack an in-depth empirical analysis with deep RL models and complex benchmarks.

In the policy gradient domain, Gradient-aware Model-based Policy Search (GAMPS) [11] optimizes its model to minimize an upper bound on the error between the true policy gradient and the model-based estimate. However, GAMPS does not build upon an AC method since it uses its model to approximate action-values via Monte Carlo methods using long virtual rollouts. In model-predictive control (MPC), End-to-end MPC [2] leverages learned models in online planning with receding horizon rollouts. The entire architecture is trained end-to-end, naturally incorporating the end task performance into model learning. However, the method does not learn a parameterized policy and has to replan for every action selection.

# 3 Background

We consider the agent-environment interaction modeled as a Markov Decision Process [38]  $(S, A, \mathcal{P}^*, \mathcal{R}^*, \rho, \gamma)$ . At every timestep  $t \in \mathbb{N}$ , the agent observes the current state  $\mathbf{s}_t \in S$  from the set of possible states. It may then select an action  $\mathbf{a}_t \in A$  from the set of possible actions to perform in the environment. The environment then transitions to the next state  $\mathbf{s}_{t+1} \sim \mathcal{P}^*(\cdot \mid \mathbf{s}_t, \mathbf{a}_t)$ , by sampling from the transition probability kernel, and emits a reward signal  $r_{t+1} \sim \mathcal{R}^*(\cdot \mid \mathbf{s}_t, \mathbf{a}_t)$ . We assume the initial state is sampled from some initial state distribution,  $\mathbf{s}_0 \sim \rho$ .

We overload notation to let  $r(\mathbf{s}, \mathbf{a}) = \mathbb{E}_{r \sim \mathcal{R}^*(\mathbf{s}, \mathbf{a})}[r]$  denote the expected immediate reward from  $(\mathbf{s}, \mathbf{a})$ . The agent's objective is to select actions that produce the highest cumulative discounted rewards, or *return*, from the initial state:  $\mathbb{E}[\sum_{t=0}^{\infty} \gamma^t r(\mathbf{s}_t, \mathbf{a}_t)]$ , where  $\gamma \in (0, 1)$  defines the agent's degree of preference for immediate against delayed rewards.

## 3.1 Actor-Critic methods

Actor-Critic methods approach the RL problem by searching for a  $policy \pi(\mathbf{a} \mid \mathbf{s})$ , an action distribution conditioned on states, that induces the highest return. The general approach starts with an initial policy estimate  $\pi_0$  and then iterates over two main steps:  $policy \ evaluation$  and  $policy \ improvement$ .

Policy evaluation consists of computing the policy's *action-value function*: the expected return from each state when committing to an initial action,  $Q^{\pi}(\mathbf{s}, \mathbf{a}) = \mathbb{E}_{\pi}[\sum_{t=0}^{\infty} \gamma^{t} r(\mathbf{s}_{t}, \mathbf{a}_{t}) \, | \, \mathbf{s}_{0} = \mathbf{s}, \mathbf{a}_{0} = \mathbf{a}]$ . One can perform policy evaluation in theory by starting with an initial guess  $Q_{0}$  and repeatedly

applying to it the Bellman operator  $T^{\pi}$ ,

$$(T^{\pi}Q)(\mathbf{s}, \mathbf{a}) = r(\mathbf{s}, \mathbf{a}) + \gamma \mathbb{E}_{\mathbf{s}' \sim \mathcal{P}(\mathbf{s}, \mathbf{a})}[V(\mathbf{s}')], \qquad (1)$$

where  $V(\mathbf{s}) = \mathbb{E}_{\mathbf{a} \sim \pi(\mathbf{s})}[Q(\mathbf{s}, \mathbf{a})]$ . The sequence  $(Q_0, Q_1, Q_2, \ldots)$  generated by this procedure is guaranteed to converge (in infinity norm) since the operator is a contraction and its unique fixed point is the policy's true value function,  $Q^{\pi}$  [38].

Policy improvement consists of computing a policy which maximizes the estimated action-value in each state. For the special case of deterministic policies, this step consists of setting  $\pi(\mathbf{s}) = \arg\max_{\mathbf{a}\in\mathcal{A}}Q^{\pi}(\mathbf{s},\mathbf{a})$  everywhere in the state space. This procedure is guaranteed to produce a policy as good as, or better than, the original [37]. In the general case of stochastic policies, policy improvement can be cast as an optimization problem in the space of policies

$$\pi_{k+1} \leftarrow \arg\max_{\pi \in \Pi} \underset{\mathbf{s} \sim \nu}{\mathbb{E}} \left[ \underset{\mathbf{a} \sim \pi}{\mathbb{E}} [Q^{\pi_k}(\mathbf{s}, \mathbf{a})] \right],$$
 (2)

where  $\nu(\mathbf{s})$  is some state distribution.

The names "actor" and "critic" come from the intuitive role that each component plays: the policy chooses actions, hence it's the "actor"; the value function evaluates the policy, hence it's known as the "critic".

Actor-Critic methods in deep RL [16] update neural network estimators  $\pi_{\theta}$  and  $Q_{\phi}$  for actor and critic respectively (where  $\theta \in \mathbb{R}^n$  and  $\phi \in \mathbb{R}^d$  denote the parameters). In this setting, the evaluation and improvement steps described above are casted as optimization problems w.r.t. the networks' parameters , which are updated via stochastic gradient descent (SGD) [33]. For instance, many methods performance policy evaluation by turning the value update into a regression problem:

$$\phi_{k+1} \leftarrow \arg\min_{\phi} \underset{\mathbf{s}, \mathbf{a}, r, \mathbf{s}' \sim \mathcal{D}}{\mathbb{E}} \left[ \left( Q_{\phi}(\mathbf{s}, \mathbf{a}) - \left( r + \gamma Q_{\phi}(\mathbf{s}', \pi_{\theta}(\mathbf{s}')) \right)^{2} \right], \tag{3}$$

where  $\mathcal{D}$  is some dataset of collected experiences. Due to the nonlinear nature of neural networks, deep AC methods have no convergence guarantees to optimal policies and value functions. However, the representation capacity and flexibility of neural networks allowed tackling many new problems (e.g., continuous-action domains and learning from pixels) which were previously too challenging for classic methods.

## 3.2 Value-aware model-learning

Model-based RL adds one more function approximator to be estimated from the available data: a *model* of the transition dynamics,  $\hat{\mathcal{P}} \approx \mathcal{P}^*$ . In IterVAML [13], the model is used as a proxy for the real dynamics in the Bellman optimality operator

$$(T^*Q)(\mathbf{s}, \mathbf{a}) = r(\mathbf{s}, \mathbf{a}) + \gamma \mathbb{E}_{\mathbf{s}' \sim \mathcal{P}^*(\mathbf{s}, \mathbf{a})}[V(\mathbf{s}')], \tag{4}$$

where  $V(\mathbf{s}) = \arg \max_{\mathbf{a}} Q(\mathbf{s}, \mathbf{a})$ . Akin to the Bellman operator, the optimality operator is also a contraction, however its unique fixed point is the optimal action-value function,  $Q^*(\mathbf{s}, \mathbf{a}) = \arg \max_{\pi} Q^{\pi}(\mathbf{s}, \mathbf{a})$ . This operator is used in the *value iteration* procedure, which computes the value of the optimal policy directly instead of alternating between policy evaluation and policy improvement. Similar to actor-critic methods, approximate value iteration (AVI) algorithms use parametric estimators and sampling in practice.

Since the model is used for AVI, IterVAML optimizes for the error between  $T^*Q$  and  $\hat{T}^*Q$ ,

$$\left\| (\mathcal{P}^* - \hat{\mathcal{P}})V \right\|_{2,\nu}^2 \doteq \mathbb{E}_{\mathbf{s},\mathbf{a} \sim \nu} \left[ \left| \int \left( \mathcal{P}^*(\mathbf{s}' \mid \mathbf{s}, \mathbf{a}) - \hat{\mathcal{P}}(\mathbf{s}' \mid \mathbf{s}, \mathbf{a}) \right) V(\mathbf{s}') d\mathbf{s}' \right| \right], \tag{5}$$

where  $\nu$  is some state-action distribution and V is defined as in eq. (4). In contrast, the model loss function used in MLE ignores the structure of the current value estimate:

$$\mathcal{L}_{\text{MLE}}(\mathcal{P}) \doteq \underset{\mathbf{s}, \mathbf{a} \sim \nu}{\mathbb{E}} \left[ \underset{\mathbf{s}' \sim \mathcal{P}^*(\mathbf{s}, \mathbf{a})}{\mathbb{E}} \left[ -\log \mathcal{P}(\mathbf{s}' \mid \mathbf{s}, \mathbf{a}) \right] \right]. \tag{6}$$

The authors of IterVAML argue that minimizing the error in eq. (5) leads to better models for AVI, especially when the model set  $\mathcal{M}$  does not contain the true dynamics,  $\mathcal{P}^*$ . A shortcoming of this formulation is the difficulty of implementing it in continuous action environments, since the argmax underlying the state-value in eq. (5) is difficult to compute.

#### **Algorithm 1:** Value-Aware MBAC

```
Input: Initial parameters \theta_0, \phi_0, \psi_0 for actor, critic and model respectively; number of iterations K; model interval M

Output: Stochastic policy

1 \mathcal{D}^{(0)} \leftarrow \emptyset

2 for k = 0, 1, \dots, K - 1 do

3 Generate training set \{(\mathbf{s}_i, \mathbf{a}_i, r_i, \mathbf{s}_i')\}_{i=1}^n by following \pi_{\theta_k} in the environment.

4 \mathcal{D}^{(k+1)} \leftarrow \mathcal{D}^{(k)} \cup \{(\mathbf{s}_i, \mathbf{a}_i, r_i, \mathbf{s}_i')\}_{i=1}^n

5 \psi_{k+1} \leftarrow \psi_k

6 if k \% M then

7 \sqsubseteq Find \psi_{k+1} by minimizing eq. (9) w.r.t. model parameters

8 Find \phi_{k+1} by approximate policy evaluation via eq. (7) using \mathcal{D}^{(k+1)} and \mathcal{P}_{\psi_{k+1}}

9 \sqsubseteq Find \theta_{k+1} by approximate policy improvement via eq. (2) using Q_{\phi_{k+1}}^{\pi} and \mathcal{D}^{(k+1)}

10 return \pi_{\theta_K}
```

# 4 Policy iteration with value-aware models

We now present our adaptation of IterVAML as a value-aware model-based AC method.

#### 4.1 Model-augmented value learning

We adopt the *policy evaluation* version of IterVAML as a generic procedure for learning the value function in an Actor-Critic algorithm.<sup>2</sup> Given an initial guess  $Q_0$ , the algorithm generates a sequence  $(Q_0,Q_1,\ldots)$  by repeatedly applying the update  $Q_{k+1}\approx \hat{T}^\pi Q_k$ . Here,  $\hat{T}^\pi$  is the same as eq. (1) with the parametric model  $\mathcal{P}_\psi$  substituted for  $\mathcal{P}^*$ . Similar to most AC methods, we approximate the theoretical formulation as a regression problem. Effectively, this is a modification of eq. (3) with virtual next-state samples

$$\phi_{k+1} \leftarrow \arg\min_{\phi} \mathbb{E}_{\mathbf{s}, \mathbf{a} \sim \mathcal{D}} \left[ \left( Q_{\phi}(\mathbf{s}, \mathbf{a}) - \left( r(\mathbf{s}, \mathbf{a}) + \gamma \mathbb{E}_{\mathbf{s}' \sim \mathcal{P}_{\psi}(\mathbf{s}, \mathbf{a})} [Q_{\phi}(\mathbf{s}', \pi_{\theta}(\mathbf{s}'))] \right) \right)^{2} \right], \quad (7)$$

assuming knowledge of the reward function (which we do in our experiments in the next section).

#### 4.2 Value-aware model optimization

Considering the approximate model-based Policy Evaluation procedure described above, we optimize the model to minimize the difference between  $T^{\pi}Q_k$  and  $\hat{T}^{\pi}Q_k$ , where  $Q_k$  is the current iterate of the API algorithm. Thus, we define the *value-aware error* incurred by a model  $\mathcal{P}$  as

$$c_{2,\nu}^{2}(\mathcal{P}, V_{k}) \doteq \|(\mathcal{P}^{*} - \mathcal{P})V_{k}\|_{2,\nu}^{2}$$

$$= \underset{\mathbf{s}, \mathbf{a} \sim \nu}{\mathbb{E}} \left[ \left| \int (\mathcal{P}^{*}(\mathbf{s}' \mid \mathbf{s}, \mathbf{a}) - \mathcal{P}(\mathbf{s}' \mid \mathbf{s}, \mathbf{a}))V_{k}(\mathbf{s}')d\mathbf{s}' \right|^{2} \right], \tag{8}$$

where  $V_k$  is defined as in eq. (1) and  $\nu$  is some state-action distribution. This is identical to the cost defined in IterVAML, except that the current policy is used in the computation of  $V_k$ .

We assume access to limited samples from the distribution of states and actions and its corresponding next-states (sampled from the transition dynamics  $\mathcal{P}^*$ ) in the form of a replay buffer  $\mathcal{D} = \{(\mathbf{s}_i, \mathbf{a}_i, \mathbf{s}_i')\}_{i=1}^N$ . Thus, we minimize the following cost w.r.t. the model

$$\mathcal{L}_{\text{VAML}}(\mathcal{P}, V) = \frac{1}{N} \sum_{(\mathbf{s}_i, \mathbf{a}_i, \mathbf{s}_i') \in \mathcal{D}} \left| V(\mathbf{s}_i') - \underset{\mathbf{s}' \sim \mathcal{P}(\mathbf{s}_i, \mathbf{a}_i)}{\mathbb{E}} [V(\mathbf{s}')] \right|^2.$$
(9)

<sup>&</sup>lt;sup>2</sup>See section 3 of IterVAML's supplementary material.

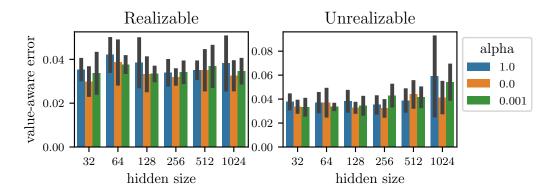


Figure 1: Results on the artificial environment.

#### 4.3 Model-based Actor-Critic

Algorithm 1 summarizes the overall method, which essentially adds a model learning step (lines 5-8) and virtual samples for the critic update (line 9) to an otherwise model-free AC method. Our approach is similar to MBPO [23] with 1-step rollouts, except we don't store virtual experiences in the replay buffer and instead sample fresh ones in every critic update. We use Adam [25] as the gradient-based optimizer for lines 7, 8, and 9 to find model, critic and actor parameters respectively in each iteration.<sup>3</sup>

Since algorithm 1 is an off-policy method, we adopt the Soft Actor-Critic [19] formulation of API to have stable actor and critic updates and encourage exploration. This amounts to adding policy entropy coefficients to model, actor and critic loss functions (due to the definition of the state-value function in maximum entropy RL), but does not alter the underlying reasoning behind each update.<sup>4</sup>

# 5 Experiments

Here we perform an empirical analysis of value-aware model learning in the deep RL setting. Throughout all our experiments, we use simple Multilayer Perceptrons (MLPs) for the model parameterization, mapping state and action vectors to the means and variances of a diagonal Gaussian distribution. The distribution is used for sampling an estimated difference between the current state and the predicted next one (similar to residual connections in deep learning). For gradient estimation of the value-aware error defined in eq. (8), we use the pathwise derivative estimator w.r.t. the model's parameters [35]. Code for our experiments is freely available and open-source.<sup>5</sup>

#### 5.1 Unrealizable vs. realizable domains

In this experiment we evaluate one of the underlying premises of VAML: that optimizing for value-aware error will yield better models when there is inherent model approximation error. To test this hypothesis, we took the following steps.

We defined an artificial environment where the transition dynamics are given by a randomly initialized 2-layer MLP (same architecture as described in the previous section). We initialized the model with the same architecture of the dynamics (but different parameters), for the realizable case, and with one less hidden layer for the unrealizable case (so that the model cannot fully capture the real dynamics). We then initialized a random uniform policy and collected two sets of data in the fake environment: one for training (50 thousand transitions) and one for testing (one thousand transitions). For the value function, we randomly initialized an MLP with one hidden layer mapping state vectors to scalar values. We then optimized the model via SGD for several epochs with early stopping on a validation

<sup>&</sup>lt;sup>3</sup>Actor and critic updates use only one stochastic gradient step on each invocation of lines 9 and 10.

<sup>&</sup>lt;sup>4</sup>See section 4.1 of the SAC paper for theoretical foundations and definition of the soft Bellman operator.

<sup>&</sup>lt;sup>5</sup>A Git repository will be linked upon publication.

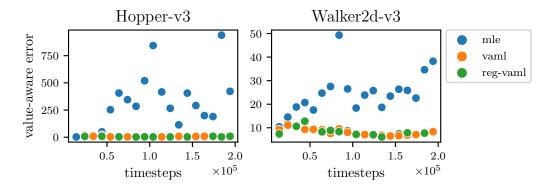


Figure 2: Value-aware error incurred by models trained via different methods in different environments.

set (taken as a subset of the training subset). Finally, we computed the empirical value-aware error of the learned models in the test set.

In our experiments, we notice that the Gaussian variance learned by value-aware models tends to collapse towards zero. To counteract this, we used a model loss that combines the value-aware and maximum likelihood losses.

$$\mathcal{L}_{\text{MODEL}}(\mathcal{P}_{\psi}, V) = \alpha \mathcal{L}_{\text{MLE}}(\mathcal{P}_{\psi}) + (1 - \alpha) \mathcal{L}_{\text{VAML}}(\mathcal{P}_{\psi}, V), \qquad (10)$$

where  $\alpha \in [0, 1]$ . In what follows, we also refer to  $\alpha$  in eq. (10) as the MLE coefficient.

Figure 1 shows results across different sizes of the hidden layers in the dynamics MLP, where error bars denote one standard deviation across five repetitions of each experiment and 'alpha' is the MLE coefficient. The realizable setting results are somewhat surprising, with VAML beating MLE by a small margin even though the true dynamics are in the model class. As alluded to before, we notice, upon closer inspection, that the Gaussian variance learned by VAML tends to 0, therefore the slight advantage might be simply due to the value-aware model never sampling values too far from the mean. On the other hand, VAML provides a narrow and inconsistent advantage over MLE, with highly overlapping error bars in most cases. Therefore, we cannot ascertain that VAML is better than MLE in this artificial setting.

#### **5.2** Value-aware error optimization in practice

Our intent in this experiment is to evaluate the feasibility of optimizing the value-aware error in unknown environments, without yet incorporating model-based policy improvements. Thus, we optimize models on data gathered during training runs of the SAC algorithm, without using the model to influence Actor-Critic updates. We consider two environments from the OpenAI Gym [6] toolkit for RL research: Hopper-v3 and Walker2d-v3. We run SAC on each environment for 200 thousand timesteps and save the policy, value function and replay buffer at different timesteps. We use these to check how well we can fit value-aware models at different training phases, since data collection and value function structure change over the course of the algorithm.

Figure 2 compares the value-aware error of models learned via different methods. We add a variation called "regularized VAML" (shortened to "reg-vam" in the plot legends) and used MLE coefficient of 0.001. The results show a trend of increasing value-aware error over the course of the algorithm when the model is trained via MLE. On the other hand, value-aware models keep the error under control throughout training; a promising sign that there's a qualitative difference between models learned via different methods.

#### 5.3 Model-based Actor-Critic with value-awareness

In this experiment we deploy algorithm 1 in two continuous control environments from OpenAI Gym commonly used in deep RL: InvertedPendulum-v2 and Pusher-v2. <sup>6</sup> Our aim was to test if

<sup>&</sup>lt;sup>6</sup>We chose lower dimensional tasks due to computation budget restrictions.

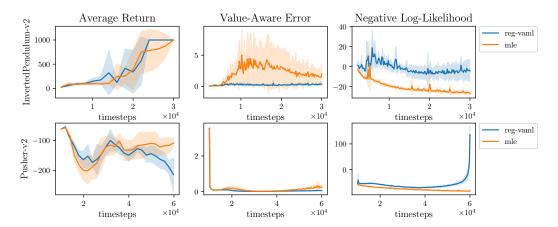


Figure 3: Model-based AC results on InvertedPendulum-v2 and Pusher-v2

minimizing the model's value-aware error translated into improved performance in the end task. Thus, we fix all hyperparameters except for the MLE coefficient in the model loss, for which we considered two values:  $\alpha=1$  (model training via MLE) and  $\alpha=0.001$ , linearly decaying towards 0 throughout training (regularized VAML). We chose to regularize VAML to keep the Gaussian variance from collapsing to zero, which rendered updates unstable.

Figure 3 shows the results in the InvertedPendulum-v2 (top) and Pusher-v2 (bottom) environments. Lines denote the average across 4 independent runs of the algorithm for each configuration. Shaded regions denote one standard deviation of results. We can see that VAML was able to successfully achieve a lower value-aware error compared to MLE throughout the majority of training. We can also see that the value-aware model is not too far behind in negative log-likelihood. However, the end task performance of the agent using MLE-based model learning is as good as (if not better, as in the case of Pusher-v2) the performance of the agent using VAML. Failing to establish a significant difference between the two model-learning methods in these simple environments, we cannot ascertain that VAML provides an advantage over conventional likelihood-based methods in a MBAC framework.

## 6 Conclusions and future work

In this work we adapted the ideas of VAML to the Actor-Critic framework. We showed that, despite promising theoretical results and preliminary experiments, VAML does not translate well to the deep RL setting, with conventional MLE-based approaches yielding comparable, or better, end task performance.

Despite these negative results, there are interesting research directions to further our understanding of the underlying issues with VAML in its current formulation. One concern with the approach in algorithm 1 is that it is too unstable as a model-based method (we observed that its performance is sometimes worse than SAC). Stabilizing this base algorithm by conservatively updating the policy or model [31], or incorporating epistemic uncertainty in model learning with randomized prior functions, [28] may provide a more solid foundation upon which to compare VAML and MLE-based approaches.

Our results call for a better understanding of the assumptions underlying IterVAML. <sup>7</sup> The paper's theoretical analysis assumes data collected in each iteration is independent of all the others, which is clearly not the case in an approximate policy iteration setting. Moreover the analysis also assumes the value function is independent of the data and bounded. We also suspect that the interplay between model and critic may destabilize training (in an already unstable actor-critic framework). We suggest that the original VAML formulation [14] may be more promising since it decouples the value used in learning the model from the one used for policy improvement. Moreover, the VAML loss function may be amenable to optimization via adversarial methods [4] and has a connection to the Wasserstein distance between model and true dynamics [5].

<sup>&</sup>lt;sup>7</sup>See Assumptions 1 and 3 of the IterVAML work.

# Acknowledgments and Disclosure of Funding

This work was partly supported by the CAPES grant 88887.339578/2019-00 (first author), FAPESP grant 2016/22900-1 (second author), the CNPq grants 304012/2019-0 (third author) and 307979/2018-0 (fourth author), and CAPES finance code 001.

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# A IterVAML's performance bound

We restate here the error propagation theorem from IterVAML which motivated this work.

Theorem 1 (IterVAML) Consider a sequence of action-value functions  $(\hat{Q}_k)_{k=0}^K$ , and their corresponding  $(\hat{V}_k)_{k=0}^K$ , each of which is defined as  $\hat{V}_k(\mathbf{s}) = \max_{\mathbf{a}} \hat{Q}_k(\mathbf{s}, \mathbf{a})$ . Suppose that the MDP is such that the expected rewards are  $R_{max}$ -bounded, and  $\hat{Q}_0$  is initialized such that it is  $V_{max} \leq \frac{R_{max}}{1-\gamma}$ -bounded. Let  $\varepsilon_k = T^*_{\hat{\mathcal{P}}(k+1)} \hat{Q}_k - \hat{Q}_{k+1}$  (regression error) and  $e_k = (\mathcal{P}^* - \hat{\mathcal{P}}^{(k+1)}) \hat{V}_k$  (modeling error) for  $k = 0, 1, \ldots, K-1$ . Let  $\pi_K$  be the greedy policy w.r.t.  $\hat{Q}_K$ , i.e.,  $\pi_K(\mathbf{s}) = \arg\max_{\mathbf{a}} \hat{Q}_K(\mathbf{s}, \mathbf{a})$  for all  $\mathbf{s} \in \mathcal{S}$ . Consider probability distributions  $\rho, \nu \in \mathcal{M}(\mathcal{S} \times \mathcal{A})$ . We have

$$\|Q^* - Q_K^{\pi}\|_{1,\rho} \le \frac{2\gamma}{(1-\gamma)^2} \left[ \overline{C}(\rho,\nu) \max_{0 \le k \le K-1} (\|\varepsilon_k\|_{2,\nu} + \gamma \|e_k\|_{2,\nu}) + 2\gamma^K R_{max} \right].$$

Recall that the theorem above is valid for an approximate Value Iteration setting, whereas in this work we deal with the approximate Policy Iteration setting. Furthermore, the modeling error in our setting considers state values as  $\hat{V}_k(\mathbf{s}) = \mathbb{E}_{\mathbf{a} \sim \pi_k}[\hat{Q}_k(\mathbf{s}, \mathbf{a})]$ .