Supervision questions for Part IIa Macroeconomic Policy Easter 2012

Question 1

1 Consider the following macroeconomic model. Aggregate demand is given by:

$$y_t = m_t - p_t + v_t \tag{1}$$

and aggregate supply by:

$$y_t - y_t^p = \beta(p_t -_{t-1} p_t^e) \tag{2}$$

where y is the log of real output, y^p is the log of trend output, m is the log of the money stock, p is the log of the price level and v is the log of (constant) velocity. The subscript t indicates the time period. $t-1p_t^e$ is the expectation formed in period t-1 of what the price level will be in period t. It is assumed that the policymaker follows a rule for the stock of money of the form

$$m_t = \alpha y_{t-1} + \epsilon_t \tag{3}$$

where ϵ_t is a zero mean surprise shock to monetary policy.

- (a) Suppose expectations are formed adaptively. Write down an expression for how expectations are formed in this case and comment on the properties of this relationship.
- (b) There a single positive shock to ϵ in period t. Show diagrammatically how output and the price level return to equilibrium. Make clear what determines the speed with which equilibrium is re-established.
- (c) Suppose now expectations are formed rationally so $t_{t-1}p_t^e = E(p_t \mid I_{t-1})$. Explain what is meant by this.
- (d) What is the effect now on output and the price level of a shock to ϵ_t ?

Question 2

2 The relationship describing the evolution over time of the debt to income ratio can be written approximately as:

$$\Delta b = d + (r - g)b \tag{4}$$

where b, is the stock of national debt expressed as a proportion of nominal income, d, is the primary deficit as a proportion of nominal income, r is the real interest rate, and g is the growth rate of real income.

- (a) Explain the economic intuition and show how this relationship can be derived from the underlying budget identity of the government.
- (b) Suppose that the real interest rate is smaller than the growth rate of the economy (r < g). The initial stock of debt is positive and the government runs a primary deficit. Show in a diagram how the debt-income ratio evolves over time and explain what is happening.
- (c) Suppose now that the government runs a primary surplus. How does this alter your answer to part (b)?
- (d) Suppose now r > g. Show in a diagram how the debt ratio now evolves depending upon whether the government runs a primary deficit or primary surplus.