

DLMs and GAMs for GOA salmon

```
library(MARSS)
library(mgcv)
library(dplyr)
library(forecast)
library(ggplot2)
library(lubridate)
library(marssTMB)
library(tidyverse)
```

Data

```
# Load salmon timeseries collapsed into DFA trend
# salm.dat <- read.csv("GOA_salmon_case_study/Data/dfa_trend.csv") %>%
#   rename(year = t, salmon_DFA = estimate)

salm.dat <- readRDS(here::here("GOA_salmon_case_study/Data/dfa_trend.rds"))

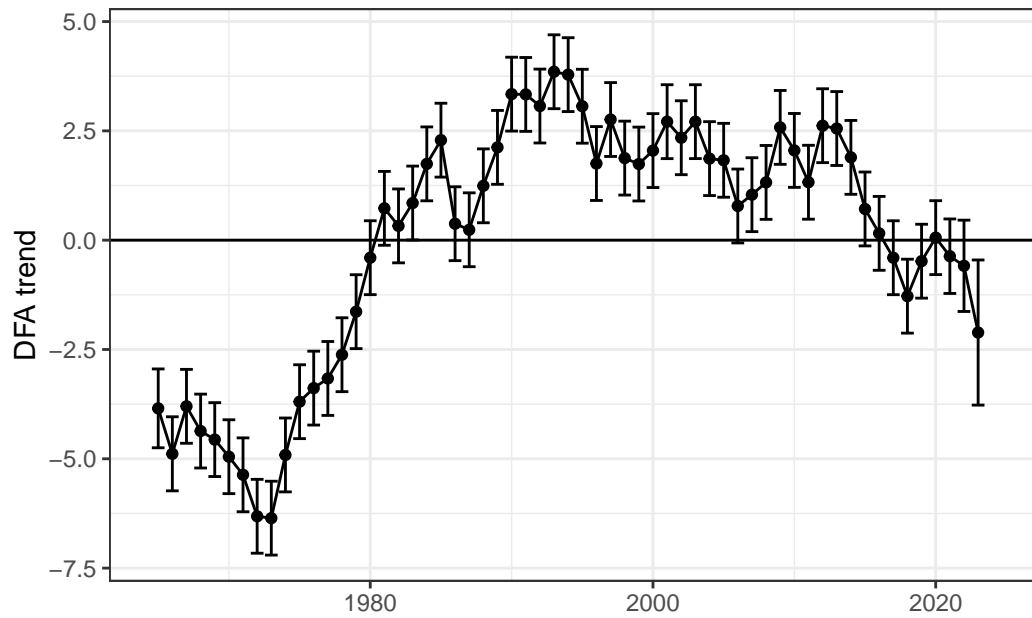
# Load 3-year running mean winter SST timeseries
# sst.dat <- read.csv("GOA_salmon_case_study/Data/winterSST_3yr_running_mean.csv") %>%
#   dplyr::select(!X)

sst.dat <- readRDS(here::here("GOA_salmon_case_study/Data/winterSST_3yr_running_mean.rds"))

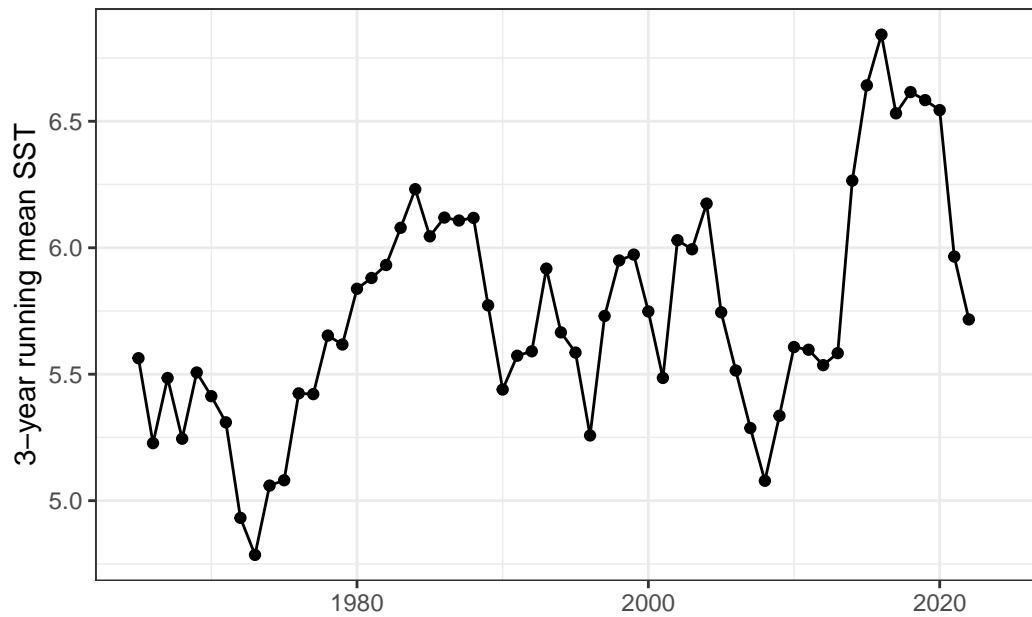
# Bind
right_join(salm.dat, sst.dat) -> dat

# Plot salmon DFA
ggplot(dat, aes(year, salmon_DFA)) +
  theme_bw() +
  geom_line() +
```

```
geom_hline(yintercept = 0) +
geom_point() +
geom_errorbar(aes(x=year, ymin=conf.low, ymax=conf.high)) +
xlab("") +
ylab("DFA trend")
```



```
# Plot sst
ggplot(dat, aes(year, sst_3yr_running_mean)) +
  theme_bw() +
  geom_line() +
  geom_point() +
  xlab("") +
  ylab("3-year running mean SST")
```



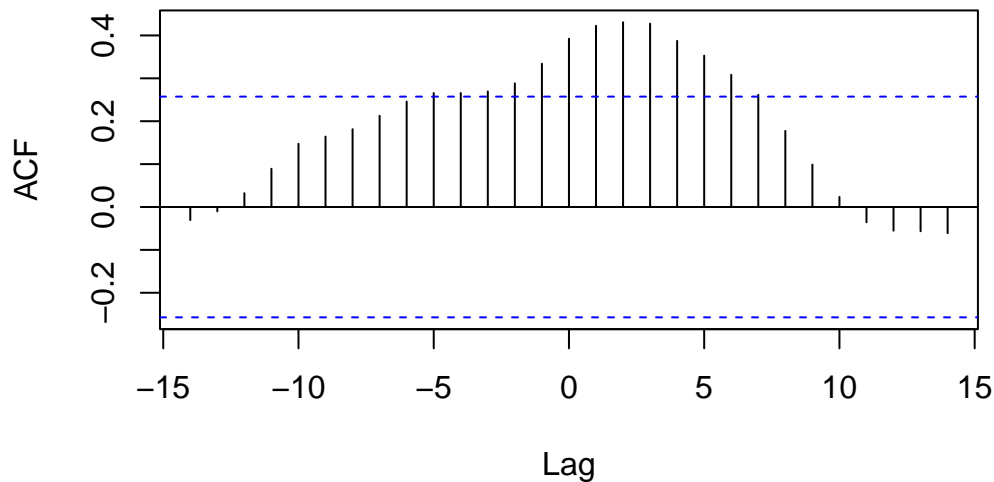
```
# Scale predictor sst
dat %>%
  mutate(z_sst = scale(sst_3yr_running_mean)) %>%
  na.omit() -> dat2
```

Evaluate lags between trend estimate (response) and response relationships. 1-3 months strongly correlated

```
sst <- as.vector(dat2$z_sst)
salmon <- as.vector(dat2$salmon_DFA)

ccf(sst, salmon)
```

sst & salmon



Use a lag of 3 months?

```
lag_n <- 0
dat2$lagged_sst <- c(rep(NA, lag_n), dat2$z_sst[1:(nrow(dat2)-lag_n)])
dat2 <- dat2[-c(1:lag_n),]
```

DLMs

Define the model.

```
m <- 2
TT <- nrow(dat2)
B <- diag(m) ## 2x2; Identity
U <- matrix(0, nrow = m, ncol = 1) ## 2x1; both elements = 0
Q <- matrix(list(0), m, m) ## 2x2; all 0 for now
diag(Q)[1] <- 0.0000001
diag(Q)[2] <- c("q.beta")
#diag(Q) <- c("q.alpha", "q.beta") ## 2x2; diag = (q1,q2)
Z <- array(NA, c(1, m, TT)) ## NxMxT; empty for now
Z[1, 1, ] <- rep(1, TT) ## Nx1; 1's for intercept
Z[1, 2, ] <- dat2$lagged_sst ## Nx1; predictor variable
A <- matrix(0) ## 1x1; scalar = 0
```

```

R <- matrix("r") ## 1x1; scalar = r
## only need starting values for regr parameters
inits_list <- list(x0 = matrix(c(0, 0), nrow = m))

## list of model matrices & vectors
mod_list <- list(B = B, U = U, Q = Q, Z = Z, A = A, R = R)

# convert response to matrix
dat_mat <- matrix(dat2$salmon_DFA, nrow = 1)

# fit the model -- crank up the maxit to ensure convergence
dlm_1 <- MARSS(dat_mat, inits = inits_list, model = mod_list,
               control = list(maxit=4000), method="TMB")

```

MARSS fit is
 Estimation method: TMB
 Estimation converged in 14 iterations.
 Log-likelihood: -111.193
 AIC: 230.3861 AICc: 231.1553

	Estimate
R.r	2.027
Q.q.beta	0.368
x0.X1	1.324
x0.X2	5.881

Initial states (x0) defined at t=0

Standard errors have not been calculated.
 Use MARSSparamCIs to compute CIs and bias estimates.

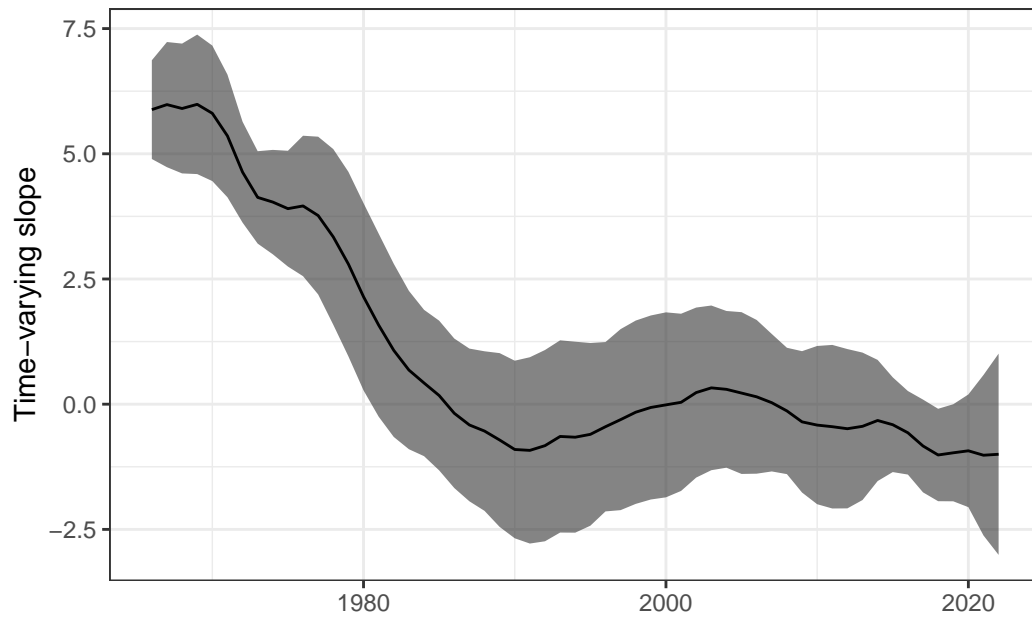
Put the state estimates back into the original dataframe and plot. The slope is generally positive, which is what we expect – and exhibits clear variation through time

```

dat2$int_est <- dlm_1$states[1,]
dat2$int_se <- dlm_1$states.se[1,]
dat2$slope_est <- dlm_1$states[2,]
dat2$slope_se <- dlm_1$states.se[2,]

ggplot(dat2, aes(year, slope_est)) +
  geom_ribbon(aes(ymin=slope_est-2*slope_se, ymax = slope_est+2*slope_se), alpha=0.6) +
  geom_line() + ylab("Time-varying slope") + xlab("") + theme_bw()

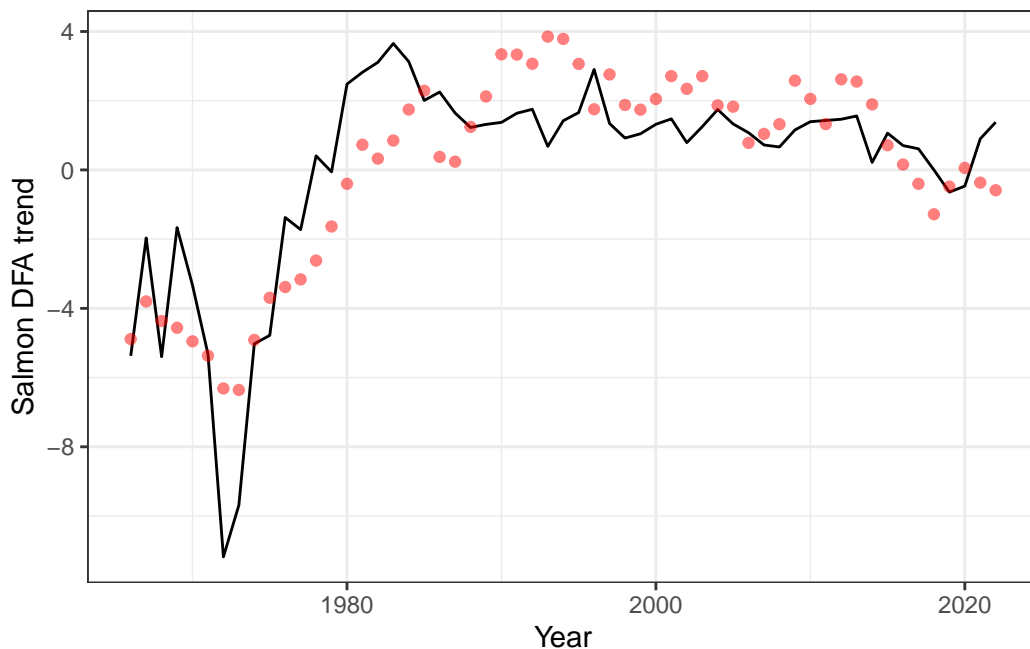
```



Plot the fitted values from the model, and some diagnostics

```
pred <- fitted(dlm_1)

dat2$pred <- pred$.fitted
ggplot(dat2, aes(year, pred)) +
  geom_line() +
  ylab("Salmon DFA trend") +
  xlab("Year") +
  theme_bw() +
  geom_point(aes(year, salmon_DFA), col="red", alpha=0.5)
```



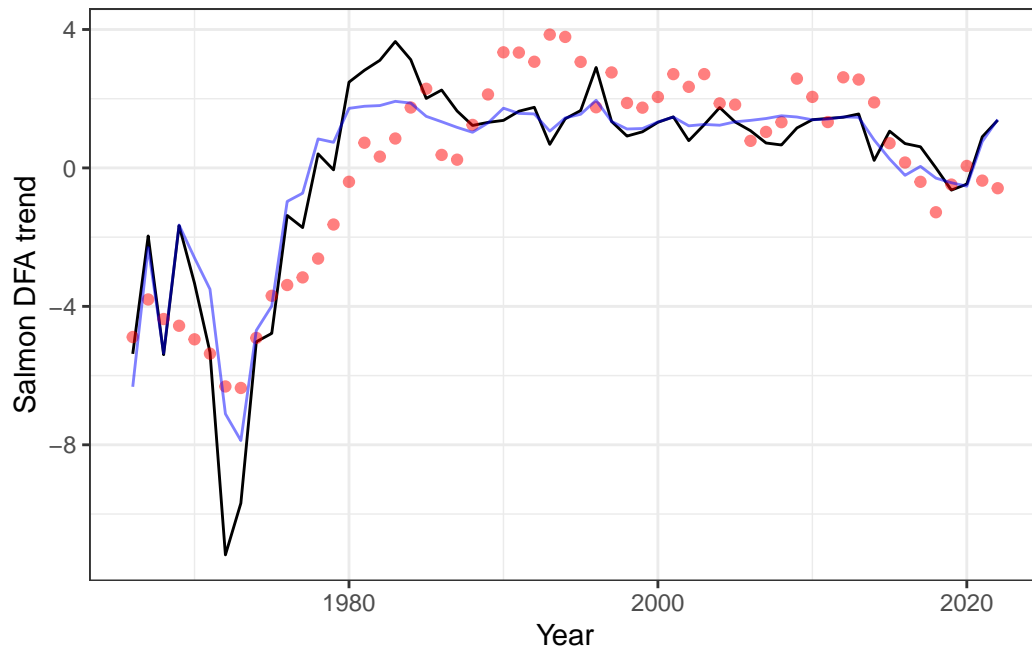
GAMs

Let's fit the same model with a GAM

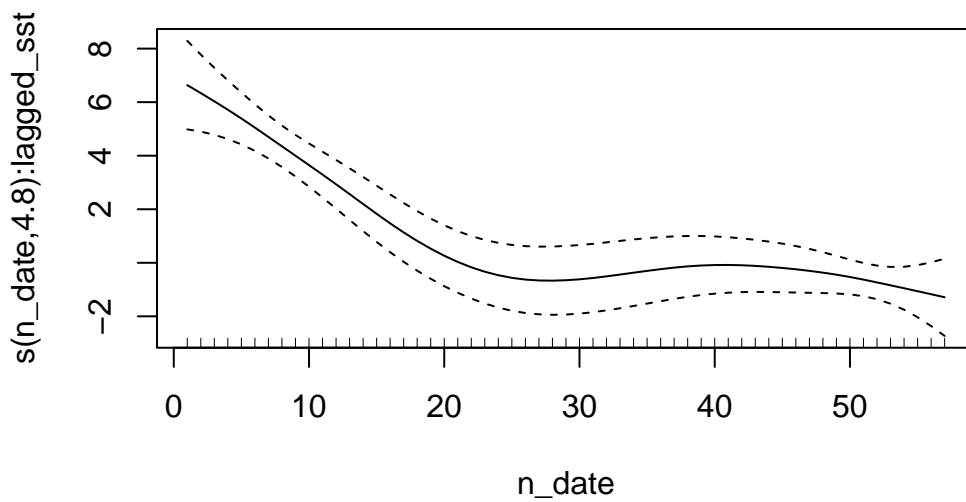
```
# The 'sp' parameter also controls the penalty on smoothing (below)
dat2$n_date <- as.numeric(as.factor(dat2$year))
gam_cr <- gam(salmon_DFA ~ s(n_date, by = lagged_sst, bs = "cr", k=nrow(dat2)),
             data = dat2)
gam_tp <- gam(salmon_DFA ~ s(n_date, by = lagged_sst, k=nrow(dat2)),
             data = dat2) # k is ignored
gam_gp <- gam_cr <- gam(salmon_DFA ~ s(n_date, by = lagged_sst, bs = "gp", k=nrow(dat2)),
                       data = dat2)

dat2$pred_gam <- predict(gam_tp)

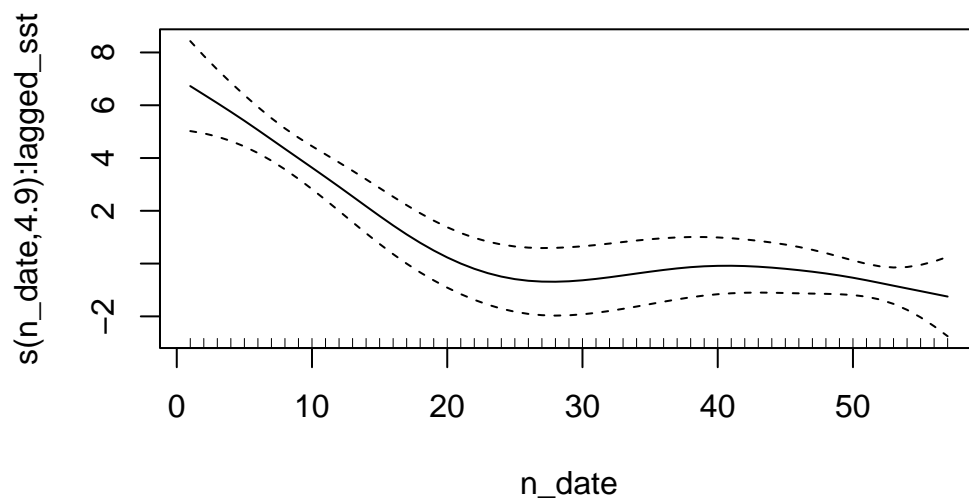
ggplot(dat2, aes(year, pred)) +
  geom_line() +
  ylab("Salmon DFA trend") +
  xlab("Year") +
  theme_bw() +
  geom_point(aes(year, salmon_DFA), col="red", alpha=0.5) +
  geom_line(aes(year, pred_gam), col="blue", alpha=0.5)
```



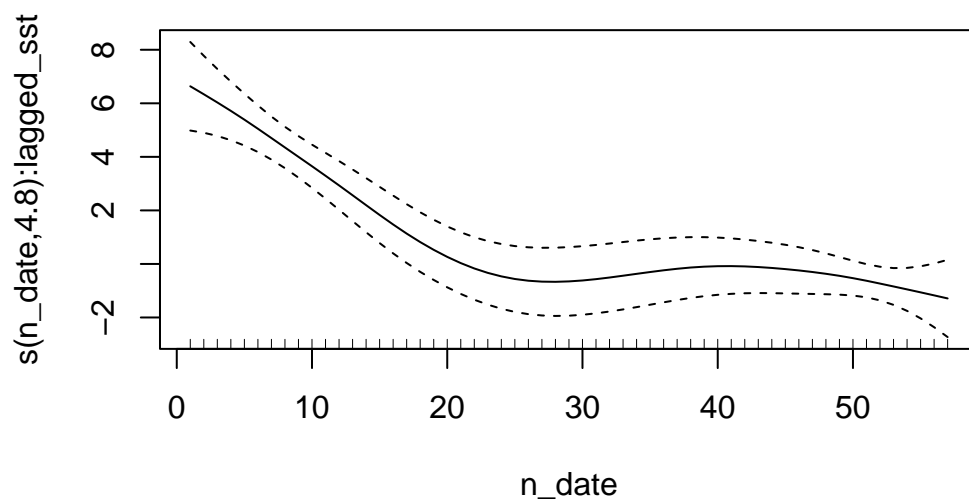
```
# extract the smooth estimates with SEs to compare to DLM
plot_cr <- plot(gam_cr, seWithMean = TRUE, n = nrow(dat2))
```




```
plot_tp <- plot(gam_tp, seWithMean = TRUE, n = nrow(dat2))
```



```
plot_gp <- plot(gam_gp, seWithMean = TRUE, n = nrow(dat2))
```

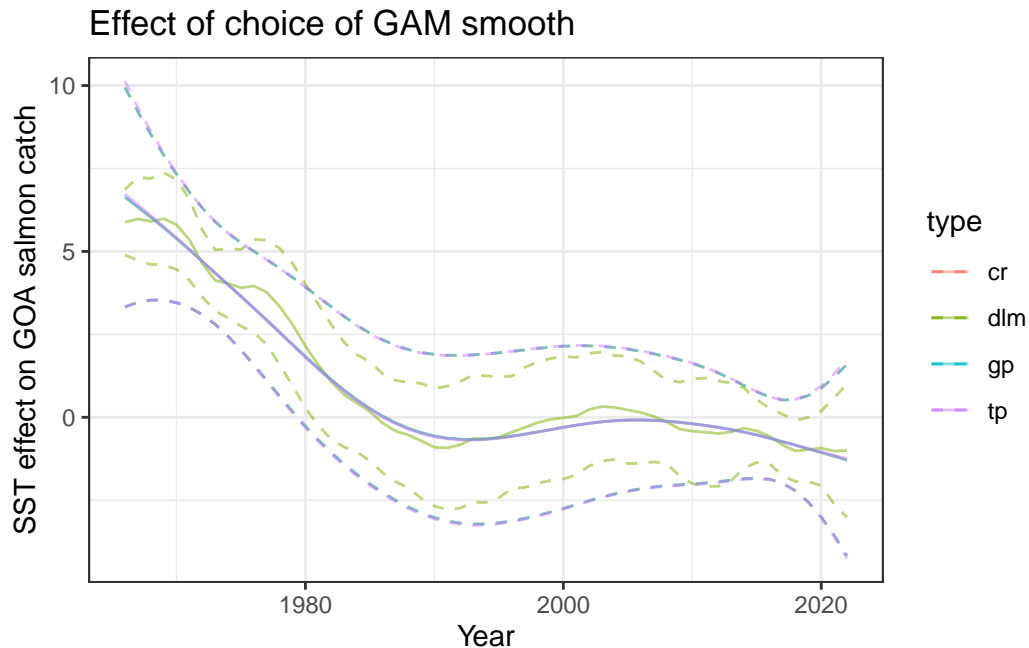


```

df_cr <- data.frame(year = dat2$year,
                    est = plot_cr[[1]]$fit,
                    se = plot_cr[[1]]$se, type="cr")
df_tp <- data.frame(year = dat2$year,
                    est = plot_tp[[1]]$fit,
                    se = plot_tp[[1]]$se, type="tp")
df_gp <- data.frame(year = dat2$year,
                    est = plot_gp[[1]]$fit,
                    se = plot_gp[[1]]$se, type="gp")
df_dlm <- data.frame(year = dat2$year,
                    est = dat2$slope_est,
                    se = dat2$slope_se, type="dlm")
df_smooth <- rbind(df_cr, df_tp, df_gp, df_dlm)

ggplot(df_smooth, aes(year, est, col=type, fill=type)) +
  geom_line(aes(year,est-2*se), alpha=0.5, linetype=2) +
  geom_line(aes(year,est+2*se), alpha=0.5, linetype=2) +
  geom_line(aes(year,est), alpha=0.5) +
  theme_bw() +
  xlab("Year") +
  ylab("SST effect on GOA salmon catch") +
  ggtitle("Effect of choice of GAM smooth")

```

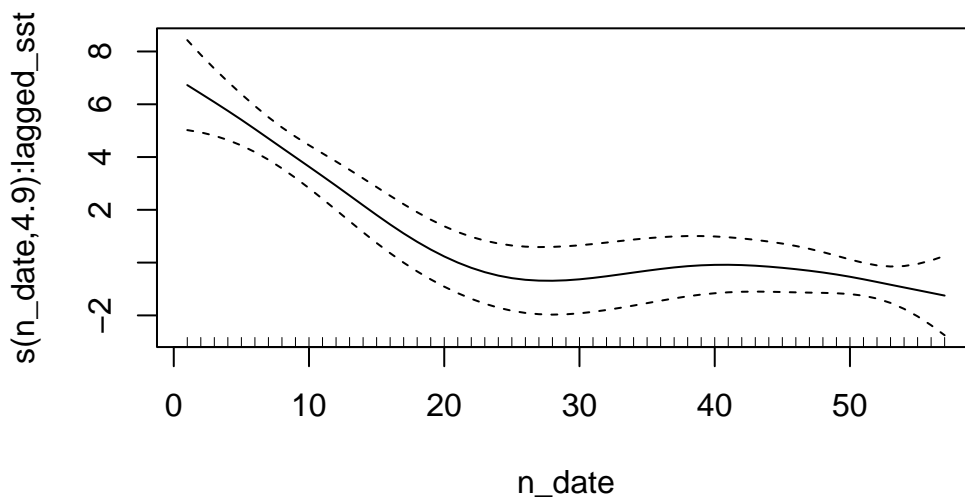


```

gam_cr30 <- gam(salmon_DFA ~ s(n_date, by = lagged_sst, bs = "cr",
                              k=nrow(dat2)), data = dat2)
gam_cr60 <- gam(salmon_DFA ~ s(n_date, by = lagged_sst, bs = "cr",
                              k=nrow(dat2),sp=16), data = dat2)
gam_cr90 <- gam(salmon_DFA ~ s(n_date, by = lagged_sst, bs = "cr",
                              k=nrow(dat2),sp=2.5), data = dat2)
gam_cr120 <- gam(salmon_DFA ~ s(n_date, by = lagged_sst, bs = "cr",
                              k=nrow(dat2),sp=0.3), data = dat2)

plot_cr30 <- plot(gam_cr30, seWithMean = TRUE, n = nrow(dat2))

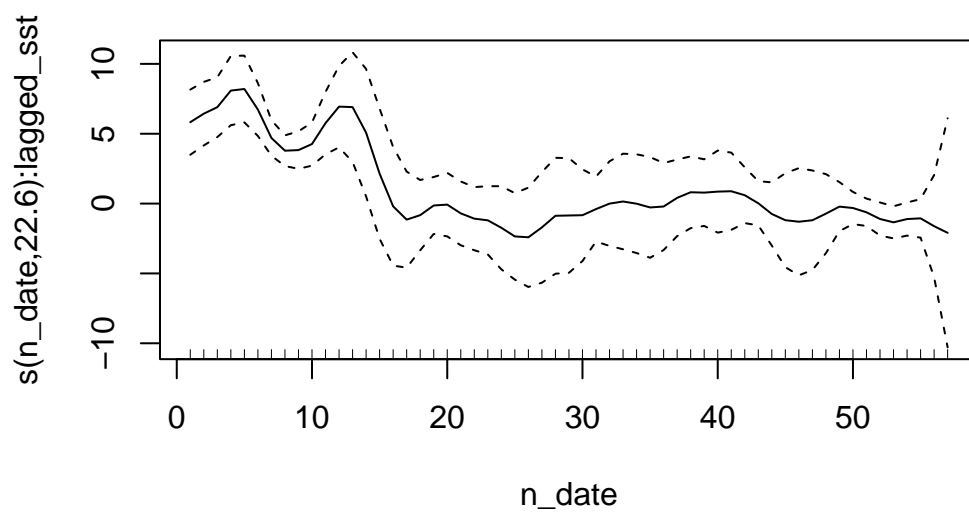
```



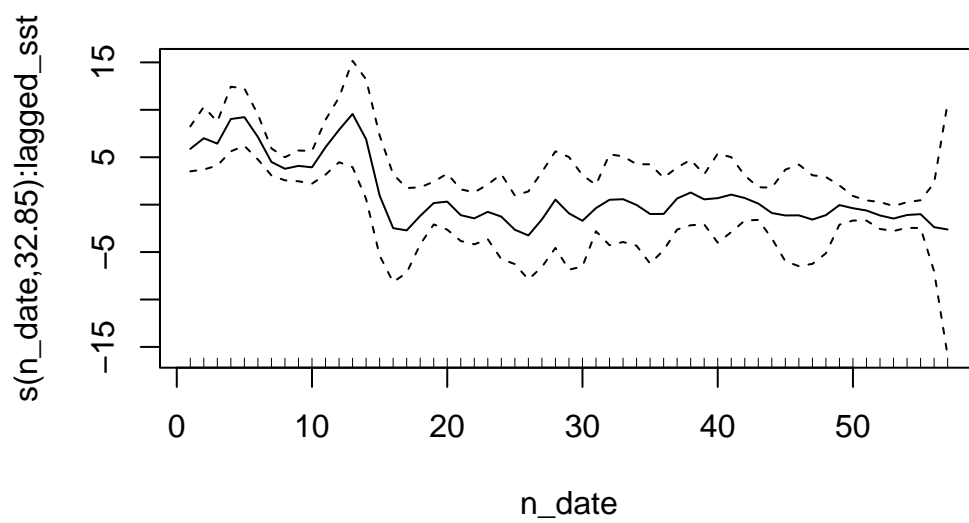
```

plot_cr60 <- plot(gam_cr60, seWithMean = TRUE, n = nrow(dat2))

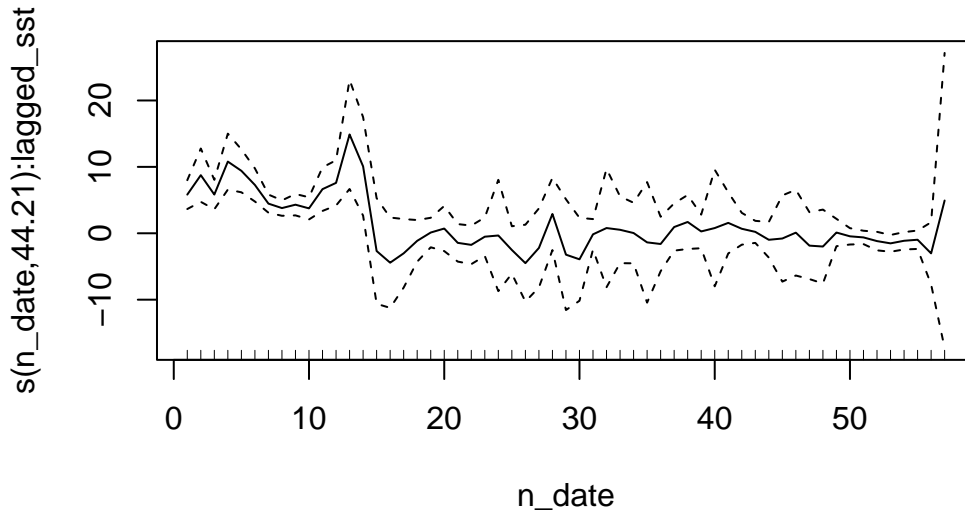
```



```
plot_cr90 <- plot(gam_cr90, seWithMean = TRUE, n = nrow(dat2))
```



```
plot_cr120 <- plot(gam_cr120, seWithMean = TRUE, n = nrow(dat2))
```



```
df_30 <- data.frame(year = dat2$year,
  est = plot_cr30[[1]]$fit,
  se = plot_cr30[[1]]$se, knots="30")
df_60 <- data.frame(year = dat2$year,
  est = plot_cr60[[1]]$fit,
  se = plot_cr60[[1]]$se, knots="60")
df_90 <- data.frame(year = dat2$year,
  est = plot_cr90[[1]]$fit,
  se = plot_cr90[[1]]$se, knots="90")
df_120 <- data.frame(year = dat2$year,
  est = plot_cr120[[1]]$fit,
  se = plot_cr120[[1]]$se, knots="120")
df_smooth <- rbind(df_30, df_60, df_90, df_120)

ggplot(df_smooth, aes(year, est, col=knots, fill=knots)) +
  geom_line(aes(year, est-2*se), alpha=0.5, linetype=2) +
  geom_line(aes(year, est+2*se), alpha=0.5, linetype=2) +
  geom_line(aes(year, est), alpha=0.5) +
  theme_bw() +
  xlab("Year") +
```

```
ylab("SST effect on GOA salmon catch") +  
ggtitle("Effect of smoothing DF on SEs")
```

