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LING723

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Homework #1 – Written Portion

*{Academic honesty note: I worked on question #2 and compared answers for #1 with Alan Mischler. The program code turned in for this assignment was completed on my own.}*

Probability

1. A fair coin is tossed three times. What is the probability that exactly two heads occur, given that:

a. The first outcome was a head?

$$\begin{aligned} P(\text{HHT}|\text{H}) &= P(\text{H}=3, \text{T}=2|\text{H}) + P(\text{T}=3, \text{H}=2) \\ &= \frac{1}{4} + \frac{1}{4} = \underline{\frac{1}{2}} \end{aligned}$$

b. The first outcome was a tail?

$$\begin{aligned} P(\text{HHT}|\text{T}) &= P(\text{H}=2, \text{H}=3|\text{T}) \\ &= (\frac{1}{2})(\frac{1}{2}) = \underline{\frac{1}{4}} \end{aligned}$$

c. The first two outcomes were heads?

$$P(\text{HHT}|\text{HH}) = \underline{\frac{1}{2}}$$

d. The first outcome was a head and the third outcome was a head?

$$P(\text{HHT}|\text{H}=1, \text{H}=3) = \underline{\frac{1}{2}}$$

2. Marie is getting married tomorrow, at an outdoor ceremony in the desert. In recent years, it has rained only 5 days each year. Unfortunately, the weatherman has predicted rain for tomorrow. When it actually rains, the weatherman correctly forecasts rain 90% of the time. When it doesn't rain, he incorrectly forecasts rain 10% of the time. What is the probability that it will rain on the day of Marie's wedding?

Probability of a forecast of rain =>

$$P(F) = (5/365)(.9) + (360/365)(.1)$$

Probability of rain with a forecast =>

$$P(R|F) = P(R \text{ when } F)/P(F)$$

$$((5/365)(.9))/((5/365)(.9)+(360/365)(.1)) = \underline{\underline{1/9 \text{ or } 11\%}}$$

Extra credit limerick:

We've taught computers so much  
I worry they may be a crutch  
    When they can teach themselves  
    The language of the elves  
I know that they know too much!