

# Algorithms and Analysis

## Lesson 3: *Declare your intentions (not your actions)*



*ADTs, stacks, queues, priority queues, sets, maps*

# Outline

## 1. Abstract Data Types (ADTs)

## 2. Stacks

## 3. Queues and Priority Queues

## 4. Lists, Sets and Maps

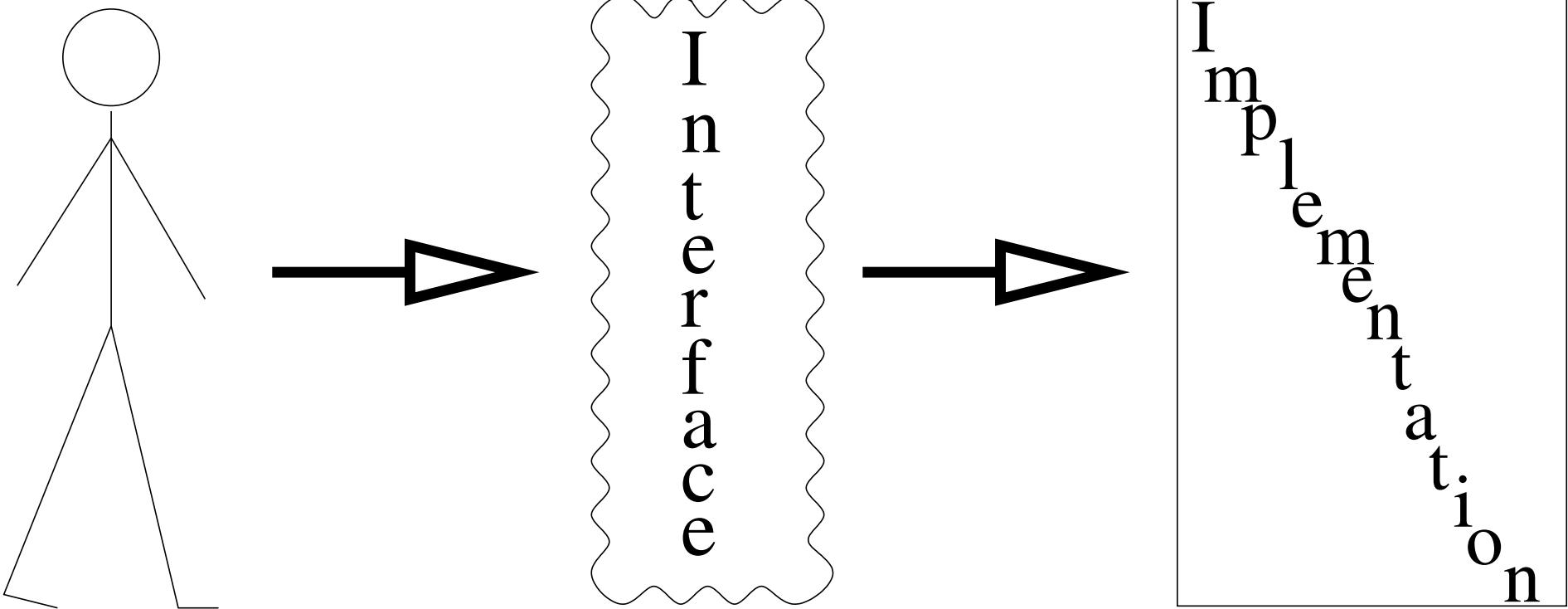
## 5. Putting it Together



# Object Oriented Programming

- OO-programming allows you to build large systems reliably
- In the OO-methodology you separate the interface from the implementation
- The **interface** is the public methods (functions) of a class
- The implementation is hidden (**encapsulated**) and may be changed without affecting how the class is used
- There exist other ways of programming, but C++ is designed to support the OO-methodology—for building systems it is brilliant

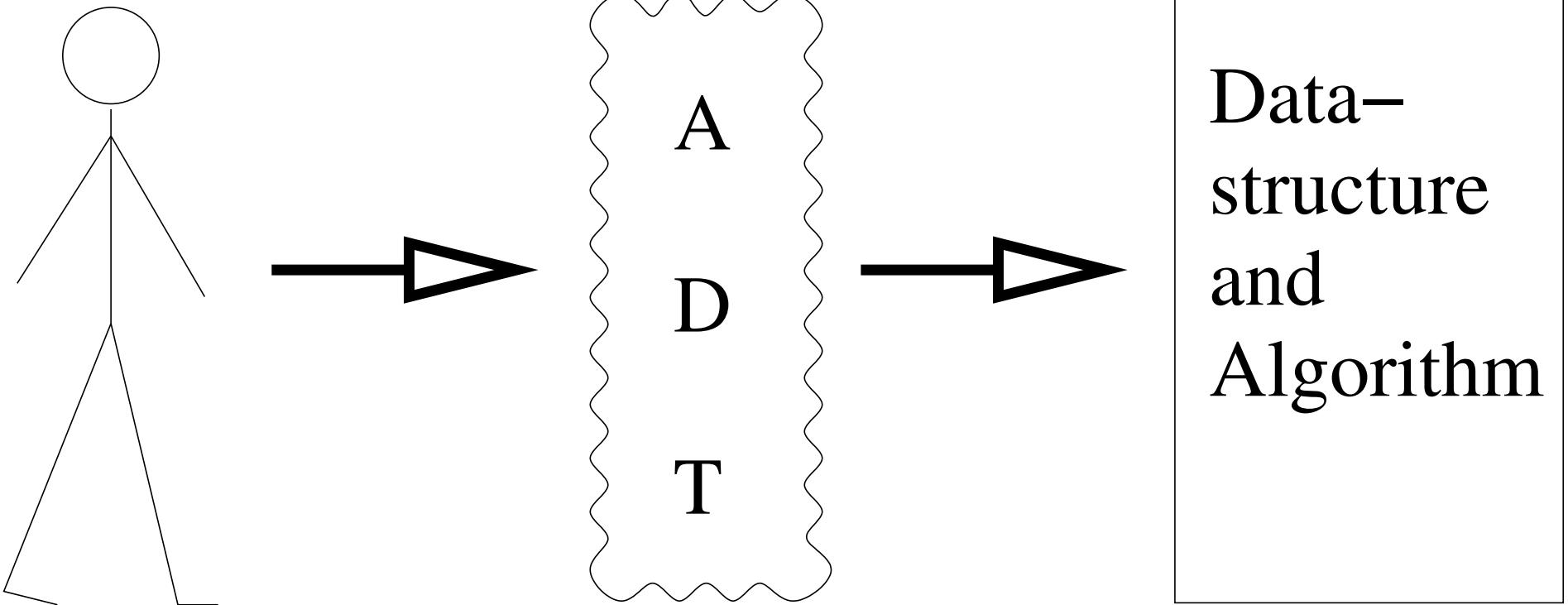
# Object-Oriented Classes



# Abstract Data Types

- With data structures there are some traditional interfaces called **Abstract Data Types** or ADTs
- These are implementation free data structures
- They are mathematical abstractions of the data structure
- Their purpose is to allow you to declare your intentions
- You are entering into an agreement that you only intend to use the underlying data structure in the way specified by the interface

# ADTs



# Say it with an ADT

- Common ADTs include stacks, queues, priority queues, sets, multisets and maps
- There are many possible implementations of these ADTs (some far from obvious)
- Each ADT has a limited set of methods associated with it
- They are an abstraction away from the implementation
- By declaring your intentions you are making your code easier to understand and maintain

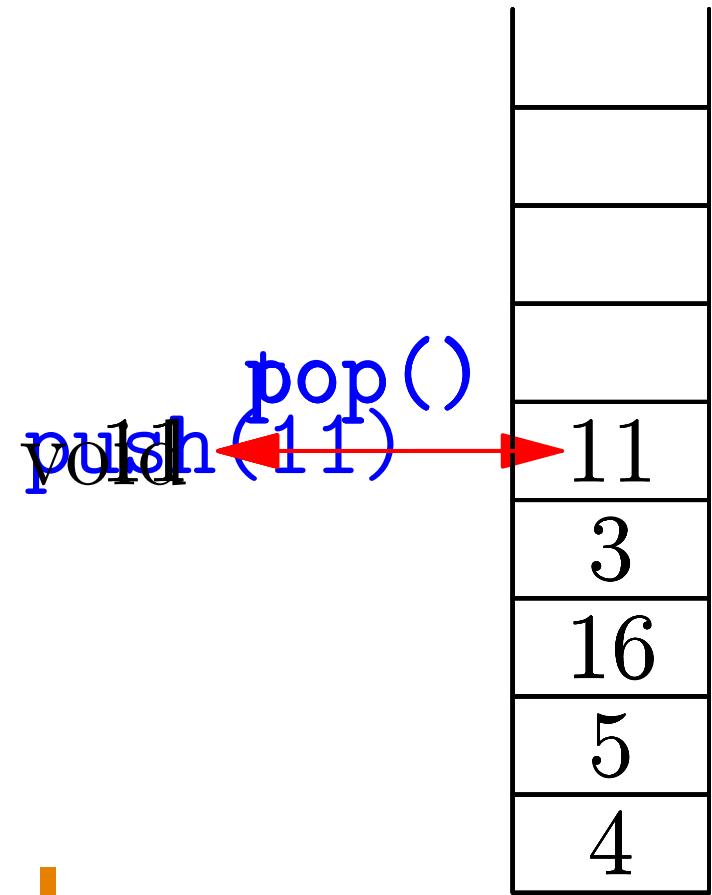
# Outline

1. Abstract Data Types (ADTs)
2. **Stacks**
3. Queues and Priority Queues
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# Stacks

- Last In First Out (LIFO) memory
- Standard functions
  - ★ `push(item)`
  - ★ `T top()`
  - ★ `T pop()` except in C++ `pop()` doesn't return the top of the stack
  - ★ `boolean empty()`
- Implemented using an array (or a linked-list)



# Why Use a Stack?

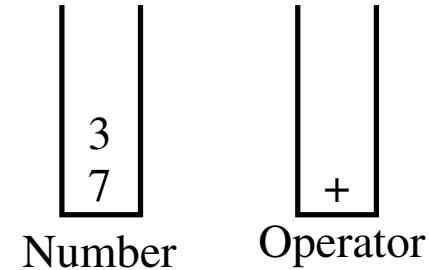
- Stacks reduces the access to memory—no longer random access
- Seems counter intuitive to reduce what you can do
- Gives you a very simple interface
- Prevents another programmer from using memory in a way that will break existing code
- Sufficient for large number of algorithms

# Uses of Stacks

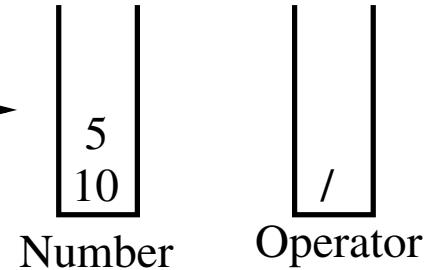
- Reversing an array
- Parsing expression for compilers
  - ★ balancing parentheses
  - ★ matching XML tags
  - ★ evaluating arithmetic expression
- Clustering algorithm

# Evaluating Arithmetic Expressions

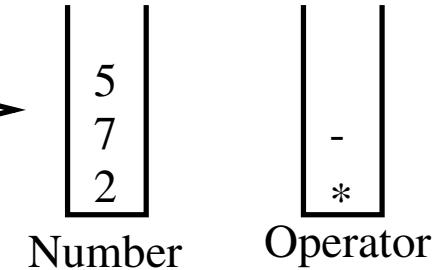
$((7+3)/5)*(7-5))$



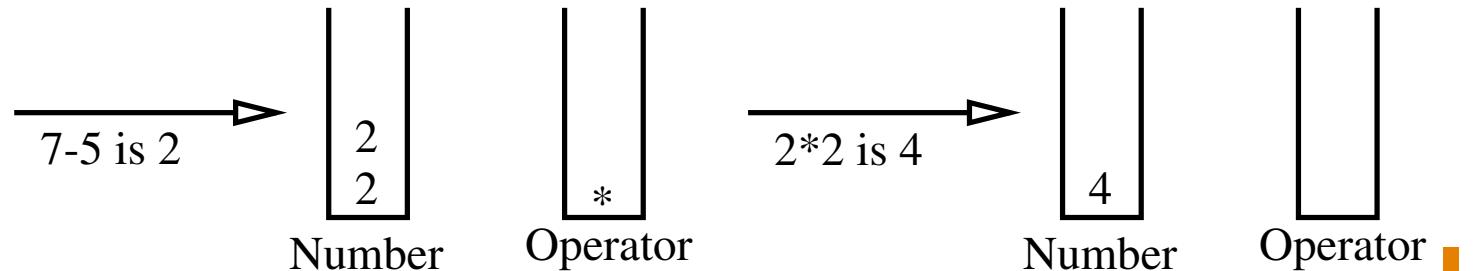
$X/5)*(7-5))$



$X*(7-5))$



)



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# Queues

- First-in-first-out (FIFO) memory model
- enqueue (elem)
- peek ()
- dequeue ()
- C++ has a double ended queue (`deque`) with `push_front()`,  
`push_back()`, etc.

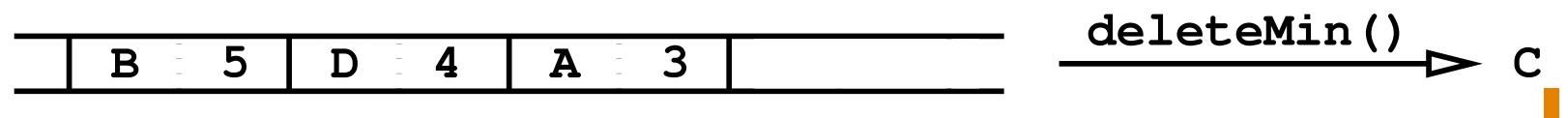


# Uses of Queues

- Queues are heavily used in multi-threaded applications (e.g. operating systems)■
- Multi-threaded applications need to minimise waiting and ensure the integrity of the data structure (for instance when an exception is thrown)■
- Because of this they are more complicated than most data structures■
- They can be implemented using linked-lists or circular arrays■

# Priority Queues

- Queue with priorities
- `insert(elem, priority)` (in C++ `push()`)
- `findMin()` (in C++ `top()`)
- `deleteMin()` (in C++ `pop()`)



# Uses of Priority Queues

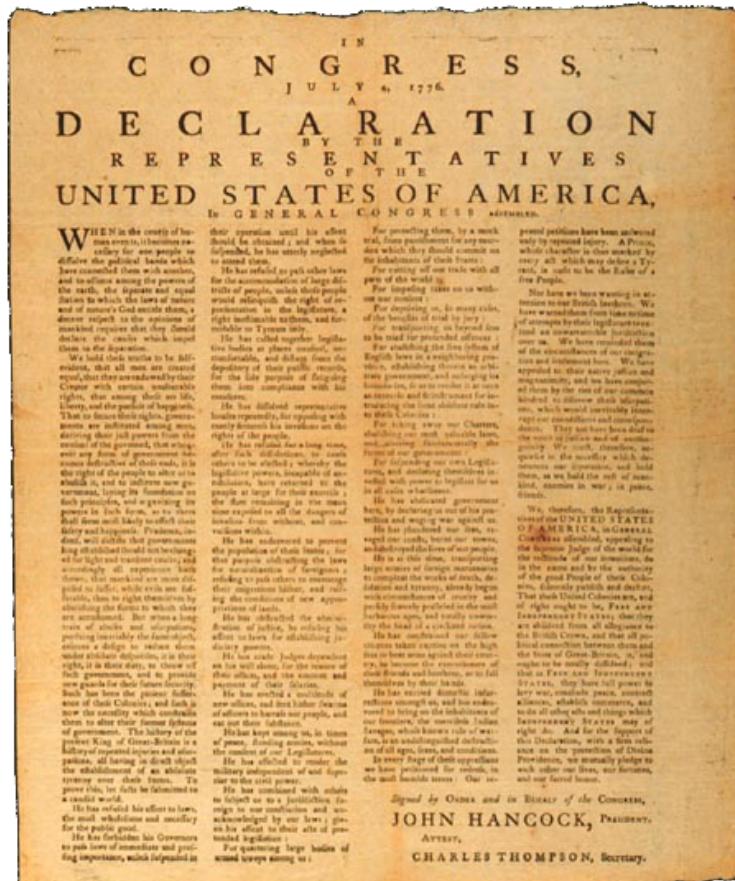
- Queues with priorities (e.g. which threads should run)
- Real time simulation
- Often used in “greedy algorithms”
  - ★ Huffman encoding
  - ★ Prim’s minimum spanning tree algorithm

# Implementation of Priority Queue

- Could be implemented using a binary tree or linked list
- Most efficient implementation uses a heap
- A heap is a binary tree implemented using an array

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# Lists

- In C++ the standard list is known as `vector<T>`
- That is, it is a collection where the order in which you put items into the list matters
- You can have repetitions of elements
- It has random access, e.g. `v[i]`
- You can `push_back(i)`, `insert`, `erase`, etc.
- C++ has a linked list class `list<T>`

# Sets

- Models mathematical sets
- Container with no ordering or repetitions
- Methods include `insert`, `find`, `size`, `erase`
- Provides fast search (`find`)
- This is the class to use when you have to rapidly find whether an object is in the set or not—don't use a list like `vector<T>`!

# Iterators

- Wish to act on all members of the set
- Performed using an iterator
- Iterators are used by many collections
- In C++ iterators follow the pointer convention

```
set<string> words;  
  
words.insert("hello");  
words.insert("world");  
  
for(auto iter = words.begin(); iter != words.end(); ++iter) {  
    cout << *iter << endl;  
}
```

# Implementation of Sets

- Sets are very important and there are many implementations depending on their usage
- Two common implementations of sets are
  - ★ hash tables: `unordered_set<T>`
  - ★ binary trees: `set<T>`
- Which is most efficient depends on the application
- Binary trees allow you to iterate in order (iterating over a hash table will give you outputs in random order)
- `multiset<T>` are sets with repetition

# Maps

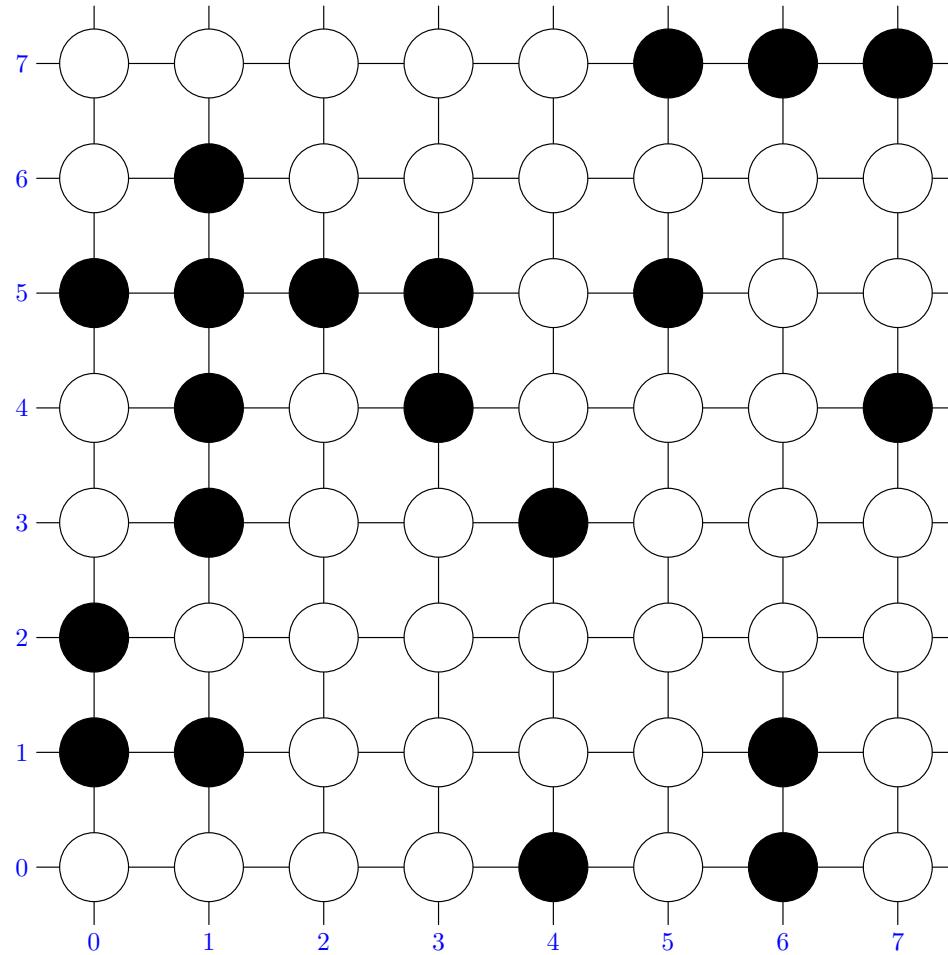
- A map provides a content addressable memory for pairs *key*:  
*value*
- It provides fast access to the *value* through the *key*
- Implement as tree or hash table
- Multimaps allows different data to be stored with the same keyword

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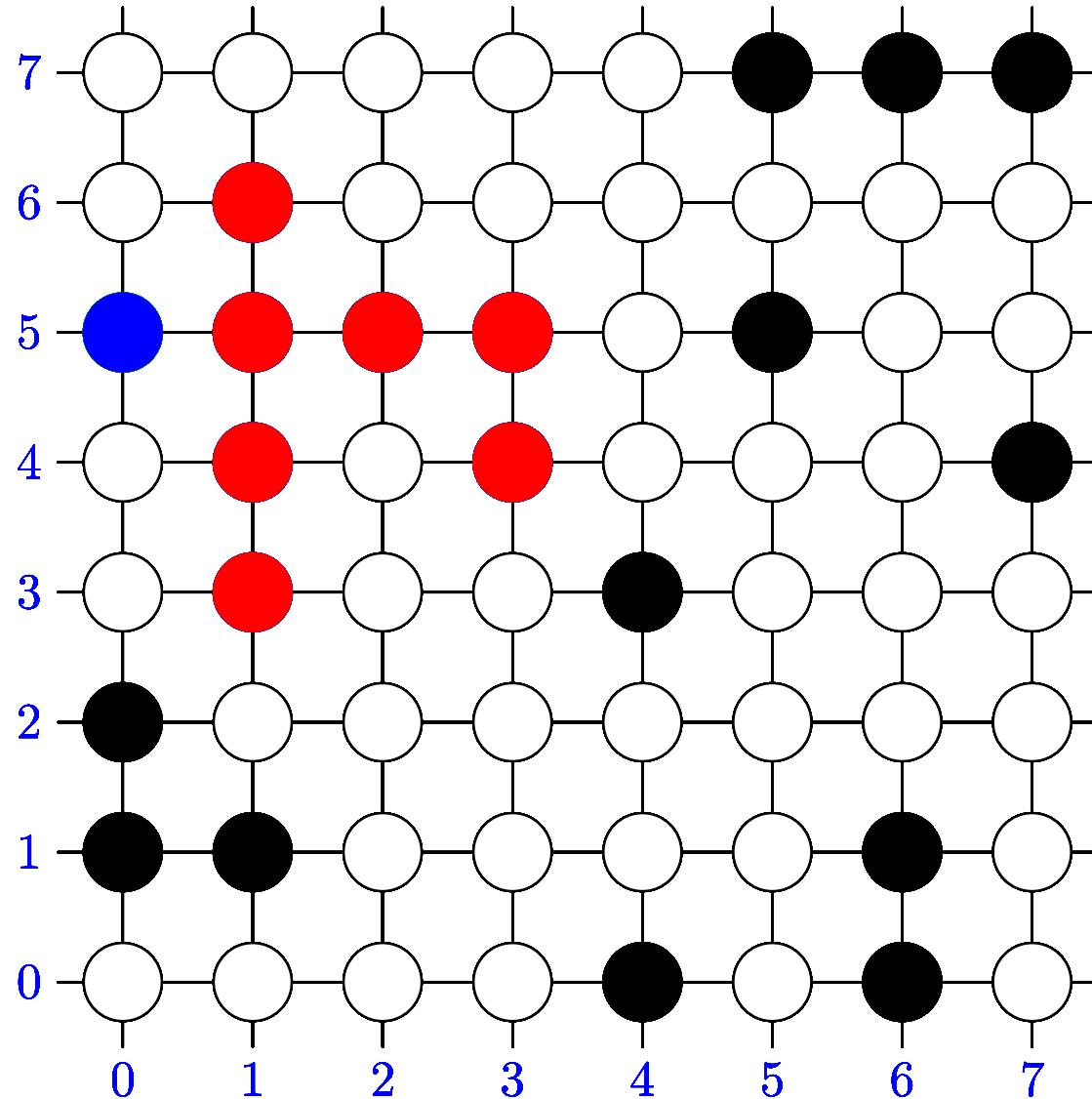


# Connected Nodes



- A frequent problem is to find clusters of connected cells ■
- Applications in computer vision, computer go, graph connectedness, . . . ■

# Connected Nodes



nextNode = (0, 5) (2,5)

uncheckedNodes =

```
(1, 6)  
(3, 4)  
(0, 5)
```

clusterNodes =  
 $\{(2, 5), \{1, 5\}, (3, 5), \}$   
 $\{3, 4\}, \{0, 5\}, (1, 4),$   
 $(1, 6), \{1, 3\} \}$

# Connected Node Algorithm

```
set<Node> findCluster(Node startNode, Graph graph) {
    stack<Node> uncheckedNodes;
    set<Node> clusterNodes;

    uncheckedNodes.push(startNode);
    clusterNodes.insert(startNode);

    while (!uncheckedNodes.empty()) {
        Node next = uncheckedNodes.top();    uncheckedNodes.pop();
        vector<Node> neighbours = graph.getNeighbours(next);
        for (Node neigh: neighbours) {
            if (graph.isOccupied(neigh) && !clusterNodes.contains(neigh)) {
                uncheckedNodes.push(neigh);
                clusterNodes.insert(neigh);
            }
        }
    }

    return clusterNodes;
}
```

# Lessons

- Abstract Data Types (ADT) are interfaces to data
- Their purpose is to allow the programmer to declare their intentions
- They often have different implementations with different properties
- The most efficient implementation is not always obvious—we will see many of these implementations as we go through this course
- You need to know the common ADTs (e.g. Stack, Queue, List, Set, Map) and how and when to use them