Further Mathematics and Algorithms

Outline

Lesson 3: Declare your intentions (not your actions)



ADTs, stacks, queues, priority queues, sets, maps

(ADTs)

1. Abstract Data Types

- 2. Stacks
- 3. Queues and Priority Queues
- 4. Lists, Sets and Maps
- 5. Putting it Together



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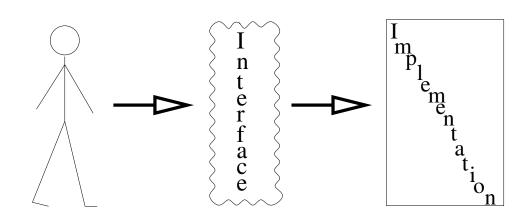
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Object Oriented Programming

- OO-programming allows you to build large systems reliably
- In the OO-methodology you separate the interface from the implementation
- The interface is the public methods (functions) of a class
- The implementation is hidden (encapsulated) and may be changed without affecting how the class is used
- There exist other ways of programming, but C++ is designed to support the OO-methodology—for building systems it is brilliant■

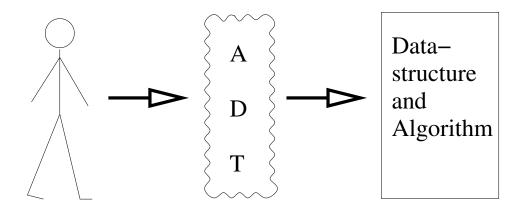
Object-Oriented Classes



Abstract Data Types

ADTs

- With data structures there are some traditional interfaces called Abstract Data Types or ADTsI
- These are implementation free data structures
- They are mathematical abstractions of the data structure
- Their purpose is to allow you to declare you intentions
- You are entering into an agreement that you only intend to use the underlying data structure in the way specified by the interface



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Say it with an ADT

- Common ADTs include stacks, queues, priority queues, sets, multisets and maps
- There are many possible implementations of these ADTs (some far from obvious)
- Each ADT has a limited set of methods associated with it
- They are an abstraction away from the implementation
- By declaring your intentions you are making your code easier to understand and maintain!

Outline

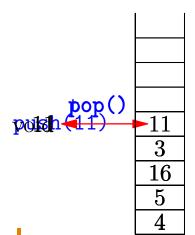
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Stacks

- Last In First Out (LIFO) memory
- Standard functions
 - push (item)
 - * T top()▮
 - ⋆ T pop() lexcept in C++ pop() doesn't return the top of the stack
 - ★ boolean empty()
- Implemented using an array! (or a linked-list)



• Stacks reduces the access to memory—no longer random access

Why Use a Stack?

- Seems counter intuitive to reduce what you can do
- Gives you a very simple interface
- Prevents another programmer from using memory in a way that will break existing code
- Sufficient for large number of algorithms

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Uses of Stacks

- Reversing an array
- Parsing expression for compilers
 - ★ balancing parentheses
 - ★ matching XML tags
 - ★ evaluating arithmetic expression
- Clustering algorithm

Evaluating Arithmetic Expressions

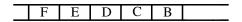
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Queues

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- First-in-first-out (FIFO) memory model
- enqueue (elem)
- peek()
- dequeue()
- C++ has a double ended queue (deque) with push_front(), push_back(), etc.



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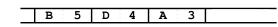
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Uses of Queues

- Queues are heavily used in multi-threaded applications (e.g. operating systems)
- Multi-threaded applications need to minimise waiting and ensure the integrity of the data structure (for instance when an exception is thrown)
- Because of this they are more complicated than most data structures
- They can be implemented using linked-lists or circular arrays

Priority Queues

- Queue with priorities
- insert (elem, priority) (in C++ push())
- findMin() (in C++ top())
- deleteMin() (in C++ pop())



deleteMin()

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Uses of Priority Queues

- Queues with priorities (e.g. which threads should run)
- Real time simulation
- Often used in "greedy algorithms"
 - ★ Huffman encoding
 - ★ Prim's minimum spanning tree algorithm

Implementation of Priority Queue

- Could be implemented using a binary tree or linked list
- Most efficient implementation uses a heap!
- A heap is a binary tree implemented using an array

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Lists

- In C++ the standard list is known as vector<T>
- That is, it is a collection where the order in which you put items into the list counts
- You can have repetitions of elements
- It has random access, e.g. v[i]
- You can push_back(i), insert, erase, etc.
- C++ has a linked list class List<T>

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Sets Iterators

- Models mathematical sets
- Container with no ordering or repetitions
- Methods include insert, find, size, erase
- Provides fast search (find)
- This is the class to use when you have to rapidly find whether an object is in the set or not—don't use a list like vector<T>!

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Implementation of Sets

- Sets are very important and there are many implementations depending on their usage!
- Two common implementations of sets are
 - ★ hash tables: unordered_set<T>
 - ★ binary trees: set<T> ■
- Which is most efficient depends on the application
- Binary trees allow you to iterate in order (iterating over a hash table will give you outputs in random order)
- multiset<T> are sets with repetition

- Wish to act on all members of the set
- Performed using an iterator
- Iterators are used by many collections
- In C++ iterators follow the pointer convention

```
set<string> words;
words.insert("hello");
words.insert("world");

for(auto iter = words.begin(); iter != words.end(); ++iter) {
  cout << *iter << endl;
}</pre>
```

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Maps

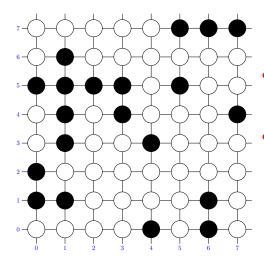
- A map provides a content addressable memory for pairs *keyword:* data
- It provides fast access to the data through the keyword
- Implement as tree or hash table
- Multimaps allows different data to be stored with the same keyword

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Connected Nodes

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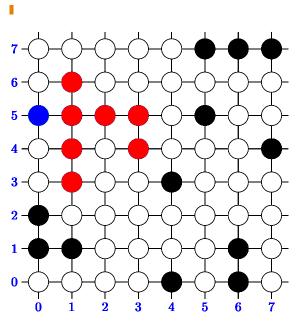
- A frequent problem is to find clusters of connected cells
- Applications in computer vision, computer go, graph connectedness, . . . I

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Connected Nodes



stewart No(0, 6) (2,5)

uncheckedNodes =

(1, 6) (3, 3) (0, 5)

clusterNodes = $\{\(2,5),\(1,5),\(3,5),\(3,4),\(0,5),\(1,4),\(1,6),\(1,3)\}$

Connected Node Algorithm

```
set<Node> findCluster(Node startNode, Graph graph)
{
  stack<Node> uncheckedNodes = new Stack<Node>();
  set<Node> clusterNodes = new HashSet<Node>();

  uncheckedNodes.push(startNode);
  clusterNodes.add(startNode);

  while (!uncheckedNodes.empty()) {
    Node next = uncheckedNodes.top(); uncheckedNodes.pop();
    vector<Node> neighbours = graph.getNeighbours(next);

    for (Node neigh: neighbours) {
        if (graph.isOccupied(neigh) && !clusterNodes.contains(neigh) ) {
            uncheckedNodes.push(neigh);
            clusterNodes.insert(neigh);
        }
    }
    return clusterNodes;
}
```

Lessons

- Abstract Data Types (ADT) are interfaces to data
- Their purpose is to allow the programmer to declare their intentions!
- They often have different implementations with different properties
- The most efficient implementation is not always obvious—we will see many of these implementations as we go through this course
- You need to know the common ADTs (e.g. Stack, Queue, List, Set, Map) and how and when to use them!

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