Outline

Lesson 5: Point to where you are going: links



Linked lists

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Non-Contiguous Data

- So far we have considered arrays where the data is stored in a contiguous chunk of memory!
- This has the great advantage of allowing random access
- It has the disadvantage that it is expensive to add or remove data from the middle of the list or to rearrange the data
- A different approach is to use units of data that point to other units

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Self-Referential Classes

• The building block for a linked list is a node class

```
struct Node<T>
{
   Node(U value, Node<U> *node): value(value), next(node) {}
   T element;
   Node<T> *next;
}
```

• We create new nodes

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Node<int> *node = new Node<int>(10, pt_to_next)

- Note that node is the address of this node!
- I make it a struct as this is a class where I want public access to the element and next
- I can make this class a private class of my linked list

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Singly Linked List

• We can build a linked list by stringing nodes together



We don't show the "pointer" to element

- A singly linked list has a single "pointer" to the next element
- A doubly linked list has "pointers" to the next and previous element—we will see this later
- We should be able to create a linked list, add elements, remove elements, see if an element exists, etc.

- 1. References
- 2. Singly Linked List
- 3. Stacks and Queues
- 4. Doubly Linked List
- 5. Using Linked Lists
- 6. Skip Lists



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Non-Contiguous Data Structures

- There are a lot of important data structures using non-contiguous memory
 - ⋆ Binary trees
 - ⋆ Graphs
- In this lecture we consider linked-lists
- This is a classic data structure which is almost entirely useless
- However, it serves as a good introduction to much more useful data structures

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Implementation

- We consider a lightweight implementation
- The class will have a head, a size counter and have a Node as a nested class

```
class MyList {
private:
   template <typename U>
   struct Node{
    Node(U value, Node<U> *node): value(value), next(node) {}
   U value;
   Node<U> *next;
};
Node<T> *head;
unsigned noElements;
```

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Simple Methods

```
    The constructor is simple (and not strictly necessary)
    MyList(): n(0), head(0) {}
```

• Other simple methods are unsigned size() const {return noElements;}

```
bool empty() const {
  return head == 0;
}
```

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Remove Head of List

```
void remove_head()
{
   Node<T>* dead = head;
   head = head->next
   noElements--;
   delete dead;
}
head

A B C D null
remove_head()

3
noElements
```

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Complexity of Stack

- All operations of the stack is constant time, i.e. O(1)
- This is the same time complexity as an array implementation
- Memory requirement is approximately $2 \times n$ reference and n objects—same as worst case for an array!
- However, hidden cost of creating and destroying Node objects

Adding elements

```
void add(T element)

Node<T> *newNode = new Node<E>();

newNode.element = element;
newNode.next = head;
head = newNode;
noElements++;
return true;
)

head
B
C
D
E null
add(A)
A
newNode
```

Other Methods

- We can easily implement many other methods
 - \star get(int i)—return i^{th} item in list

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- ★ remove(T obj)-remove obj from list
- ★ insert(int position, element)
- Note that get (int i) requires moving down the list so is O(n) (i.e. not random access)

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Stack

• It is easy to implement a stack using a linked list

```
template <typename T>
class Stack<E>
{
   private Mylist<T> list = new mylist<T>();

   boolean push(E obj) {list.add(obj);}

E top() {return list.get_head();} // throw exception

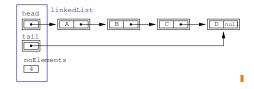
E pop() {
   T tmp = list.get_head();
   list.remove_head();
   return tmp;
}

   boolean empty() {return list.empty();}
}
```

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Point to the Back

- ullet To find the end of the queue takes n jumps
- Thus our linked list isn't the right data structure to implement a gueue
- However, we could include a pointer to the end of the queue



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Implementing a Queue

- We can then add elements to the tail in constant time
- ullet We can the implement a queue in O(1) time by
 - ★ enqueueing at the back
 - ★ dequeueing at the head
- I leave the implementation details as an exercise for you
- Note that although adding an element to the tail is constant time, removing an element from the tail is O(n) as we have to find the new tail

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Doubly linked list

- In a more powerful linked list we would like to navigate the list in either direction
- To achieve this it uses a doubly-linked lists with elements to next and previous

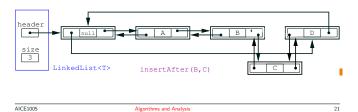
Time Complexity

- ullet add and remove from head and tail O(1)
- ullet find O(n) and slow

class Node<T>

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 \bullet insert and delete O(1) (faster than an array list) once position is found.



When To Use Linked Lists

- It is difficult to think of applications where linked lists are the best data structure
- lists—variable length arrays are usually better
- queues—linked list OK, but circular arrays are probably better
- sorted lists—binary trees much better
- linked lists have efficient insertion and deletion but it is difficult to think of an application where this matters!

Outline

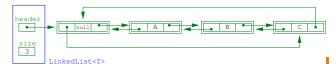
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Dummy Node

 List includes a dummy nodel—this make the implementations slicker!



Symmetric data structure so processing head and tail is equally
efficient.

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Line Editor

- One application where efficient insertion and deletion matters is a line editor
- We are usually working at a particular location in the text
- We often want to add or delete whole lines
- Storing the lines as strings in a linked list would allow a fairly efficient implementation

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Skip Lists

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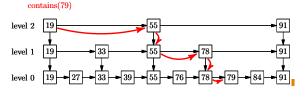


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Efficiency of Skip Lists

- \bullet Skip lists provide $\Theta(\log_2(n))$ search as opposed to $\Theta(n) {\hspace{-0.01cm}\blacksquare}$
- They have the similar time complexity to binary trees, although binary trees are slightly faster
- They have one advantage over binary trees—they allow efficient concurrent access
- The standard template library provides a doubly linked list, list<T>| as well as a slingly linked-list slist<T>|

- \bullet Linked lists have the disadvantage that to get to anywhere in the list takes on average $\Theta(n)$ steps!
- Even if you kept an ordered list you still need to traverse it
- Skip lists are hierarchies of linked lists which allow binary search



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Lessons

- Node structures that point to other Node structures are used in many important data structures
- Linked lists are the simplest examples of this kind of structure and consequently has a dominant position in most DSA books
- In practice linked lists are seldom the data structure of choice—before choosing to use a linked list consider the alternatives
- There are some important uses for linked lists, e.g. skip lists and hash tables (see lecture on hashing)

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