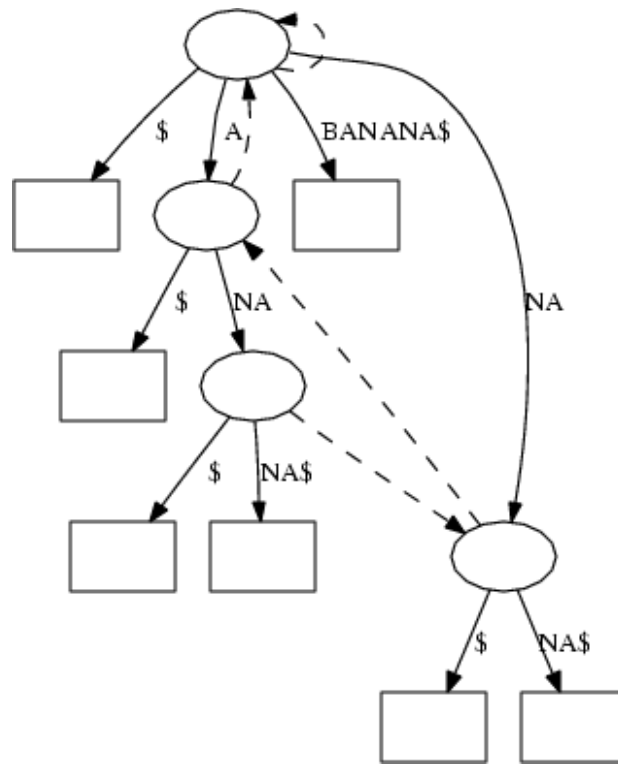


# Algorithms and Analysis

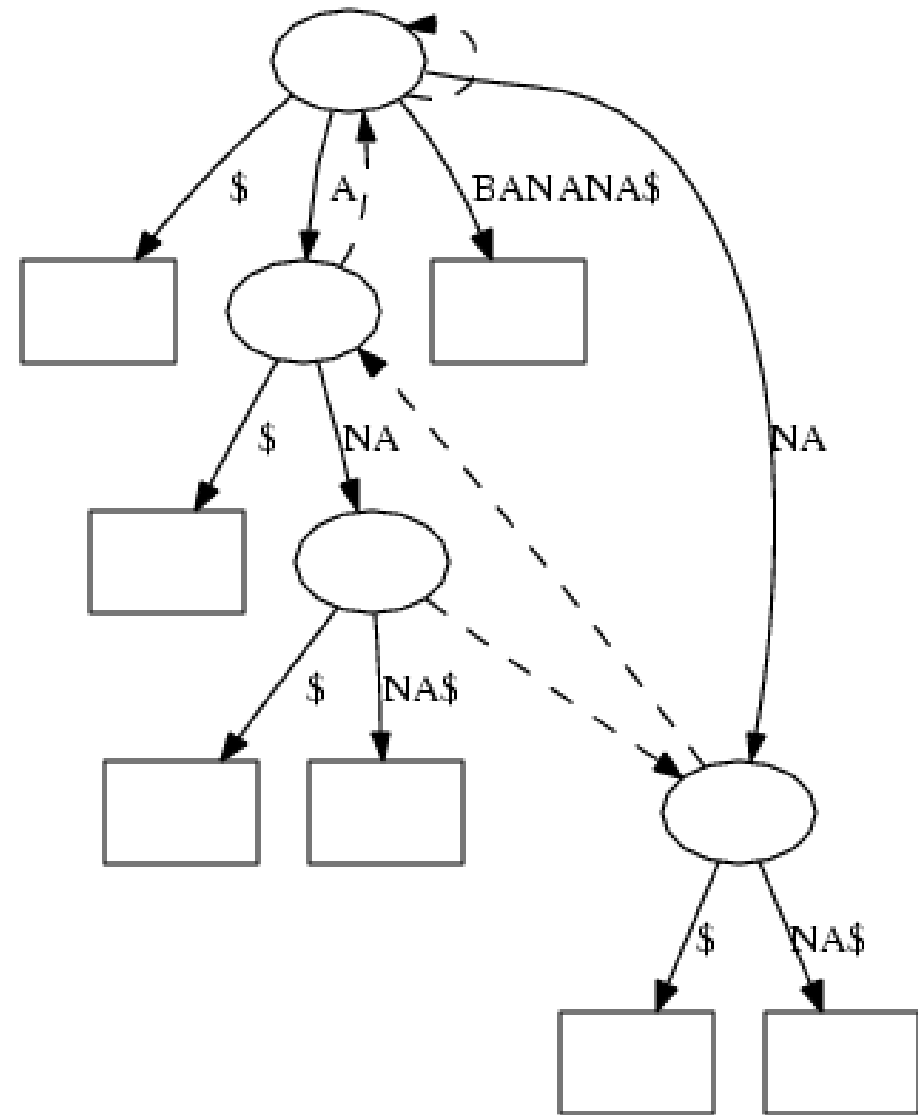
## Lesson 1: *Use Data Structures and Algorithms!*



*Course structure, examples of data structures and algorithms*

# Outline

1. **Course structure**
2. Example of Using DSA
3. Sophisticated Program
4. State-of-the-Art



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- I'm teaching you algorithms
- The analysis is an ability to reason about programming
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# Course Structure

- 30ish lectures

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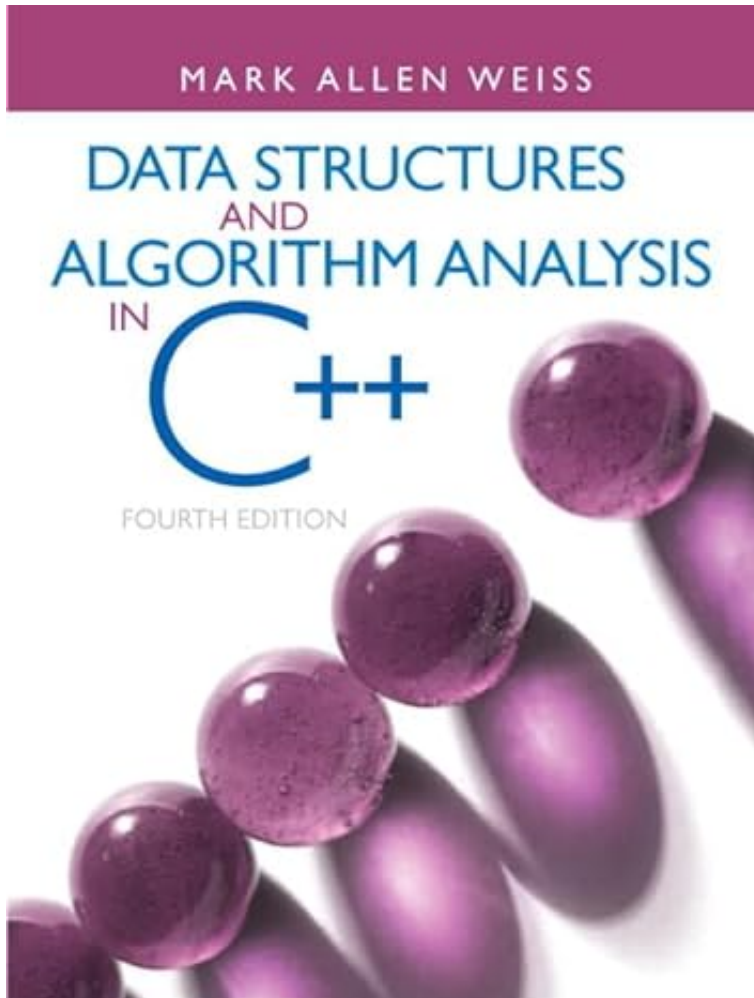
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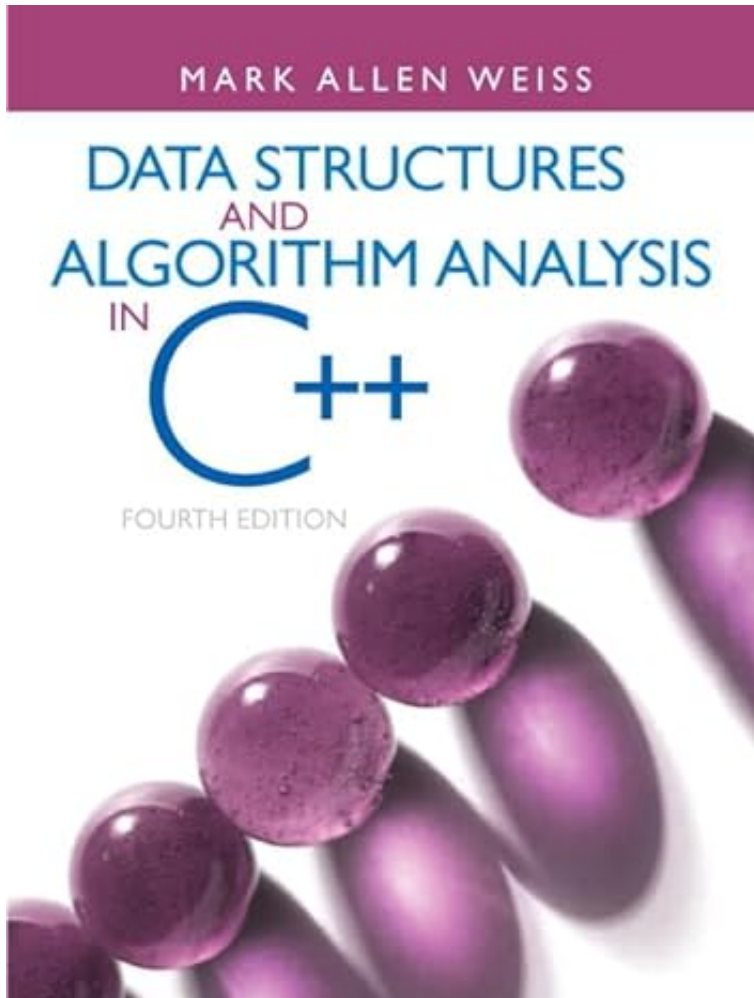


# Recommended Course Text



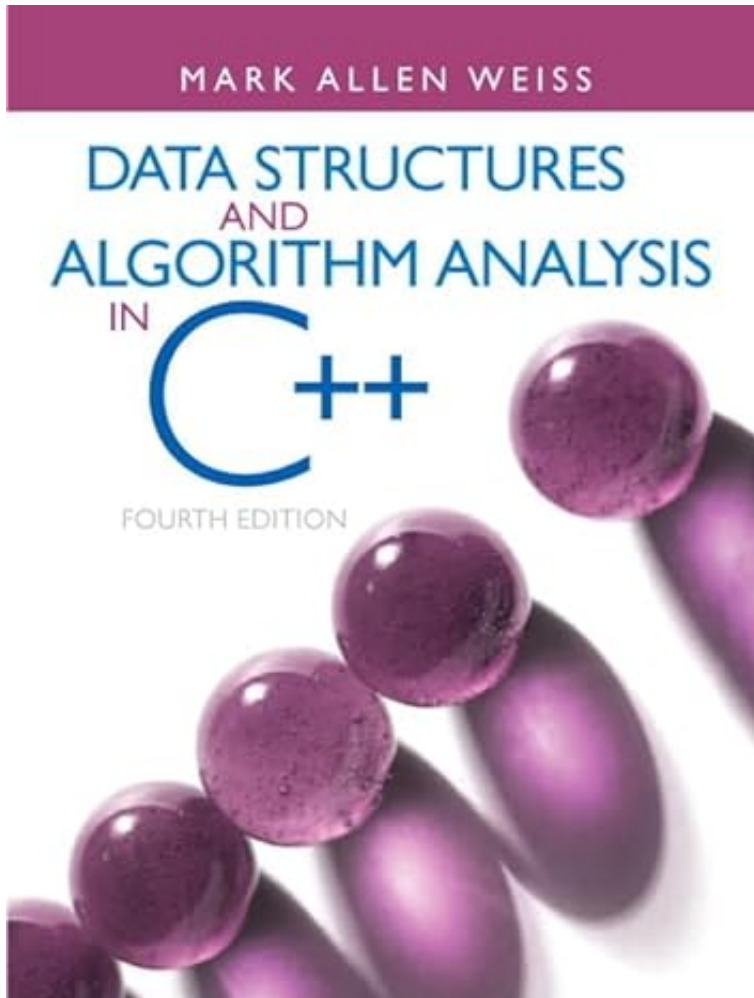
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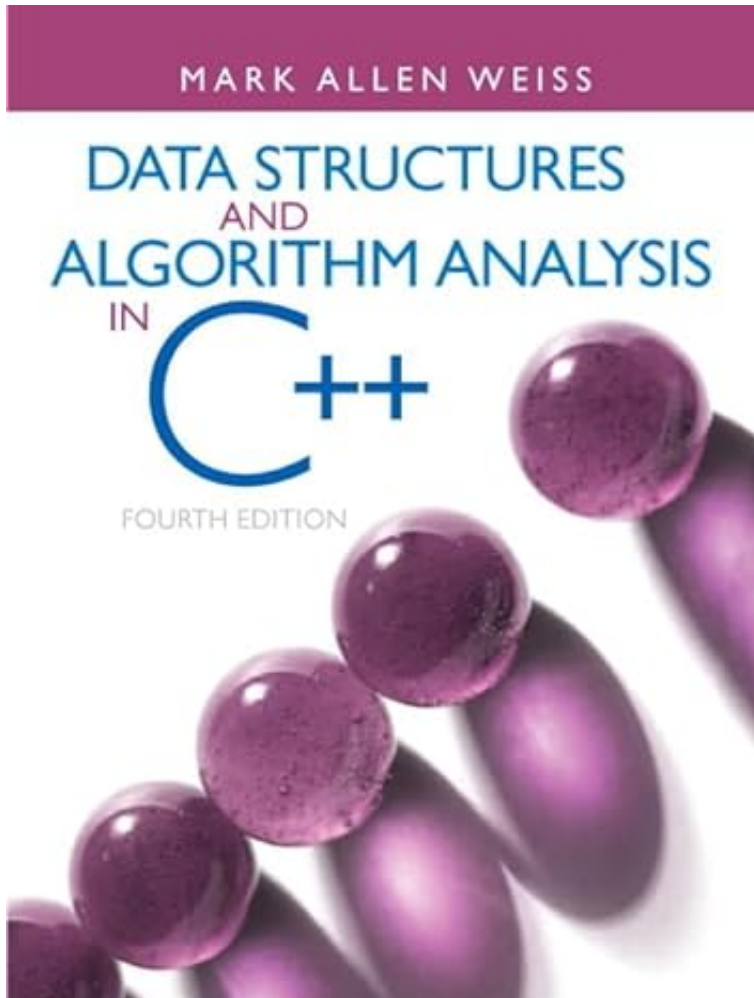
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# What is a Data Structure?

*any of various methods of organising data items (as records) in a computer*

- Container for data
- E.g. sets, stacks, lists, trees, graphs
- Clean interface, e.g. push, pop, delete
- Usually designed for fast or convenient access

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- Well defined and generic
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- Abstraction from details of problem
- Declaration of intention
- Clean interfaces
- Hidden implementations
- Makes programs readable and maintainable
- Reuse code—don't even have to write it yourself

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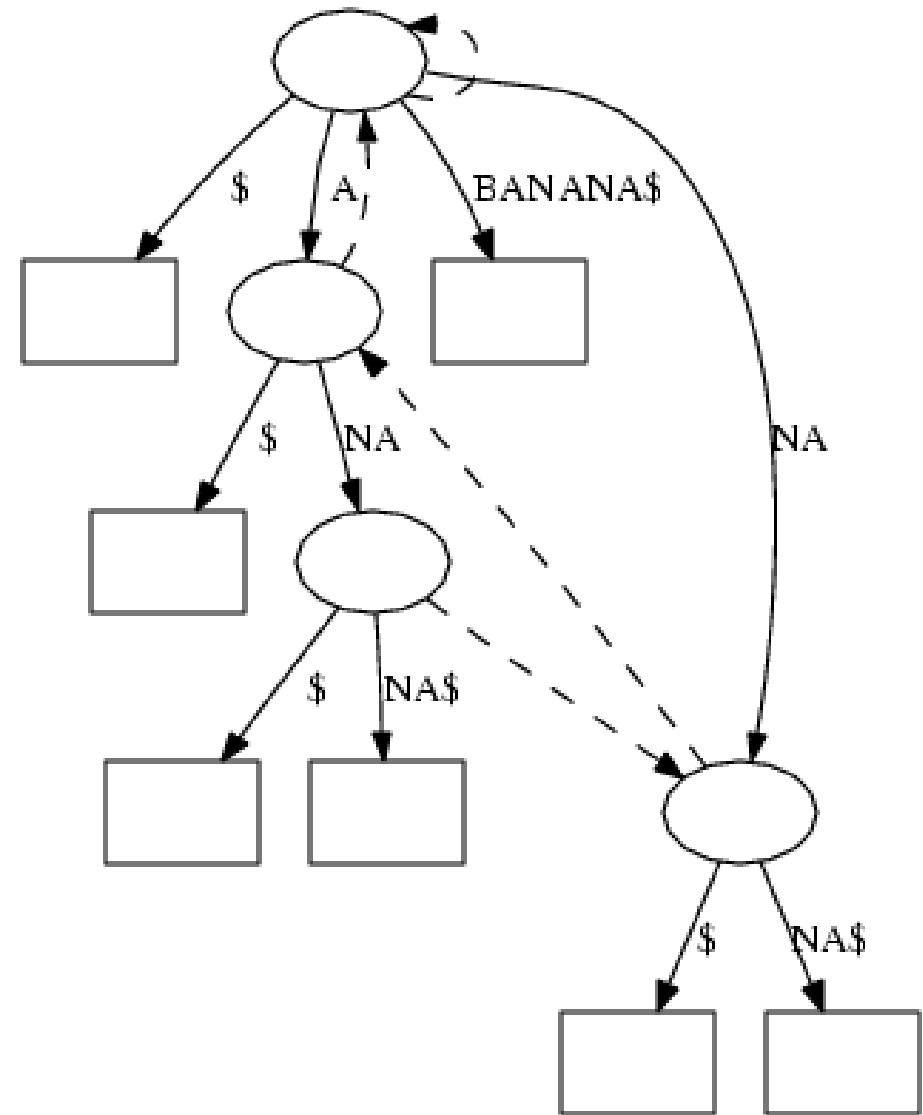
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*Thou shall not re-implement common data structures*

# Outline

1. Course structure
2. **Example of Using DSA**
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# Example: Sort program

- Suppose we want to write a program to
  - ★ read an input file of integers
  - ★ sort the integers
  - ★ write a list of integers to standard out
- In Unix there is a command called `sort` which does just this
- Note that you don't know the number of inputs

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# Code for sort

```
#include <iostream>
#include <fstream>

int main(int argc, char** argv) {
    std::ifstream myfile(argv[1]);

    int array_size = 10;
    int* array = new int[array_size];
    int cnt = 0;
    while(myfile.good()) {
        if (cnt==array_size) {
            int* new_array = new int[2*array_size];
            for(int i=0; i<array_size; ++i)
                new_array[i] = array[i];
            delete[] array;
            array = new_array;
            array_size *= 2;
        }
        myfile >> array[cnt++];
    }
}
```

```
for(int i=0; i<cnt; ++i) {  
    int index = 0;  
    for(int j=1; j<cnt-i; ++j) {  
        if (array[j]<array[index])  
            index = j;  
    }  
    std::cout << array[index] << std::endl;  
    array[index] = array[cnt-i-1];  
}  
}
```

# Notes on Code

- Details of code don't matter
- Simple program ( $\sim 20$  lines of code)
- Uses a simple array
- Difficult to see what is going on
- On 100 000 inputs it takes 10 seconds to run

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# Using Data Structures and algorithms

```
#include <iostream>
#include <fstream>
#include <iterator>
#include <vector>
#include <algorithm>
using namespace std;

int main(int argc, char *argv[])
{
    ifstream in(argv[1]);
    vector<int> data;
    copy(istream_iterator<int>(in), istream_iterator<int>(),
        back_inserter(data));
    sort(data.begin(), data.end());
    copy(data.begin(), data.end(), ostream_iterator<int>(cout, "\n"));
}
```

# Sorting Doubles

```
#include <iostream>
#include <fstream>
#include <iterator>
#include <vector>
#include <algorithm>
using namespace std;

int main(int argc, char *argv[])
{
    ifstream in(argv[1]);
    vector<double> data;
    copy(istream_iterator<double>(in), istream_iterator<double>(),
        back_inserter(data));
    sort(data.begin(), data.end());
    copy(data.begin(), data.end(), ostream_iterator<double>(cout, "\n"));
}
```

# Notes on C++

- `vector<int>` is the C++ standard resizable array
- input/output is treated as a copy
- Code is easy to read
  - ★ Declare `vector<int>` or `vector<double>`
  - ★ copy input file into vector
  - ★ sort vector
  - ★ copy sorted vector to standard output stream
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Data structure version is

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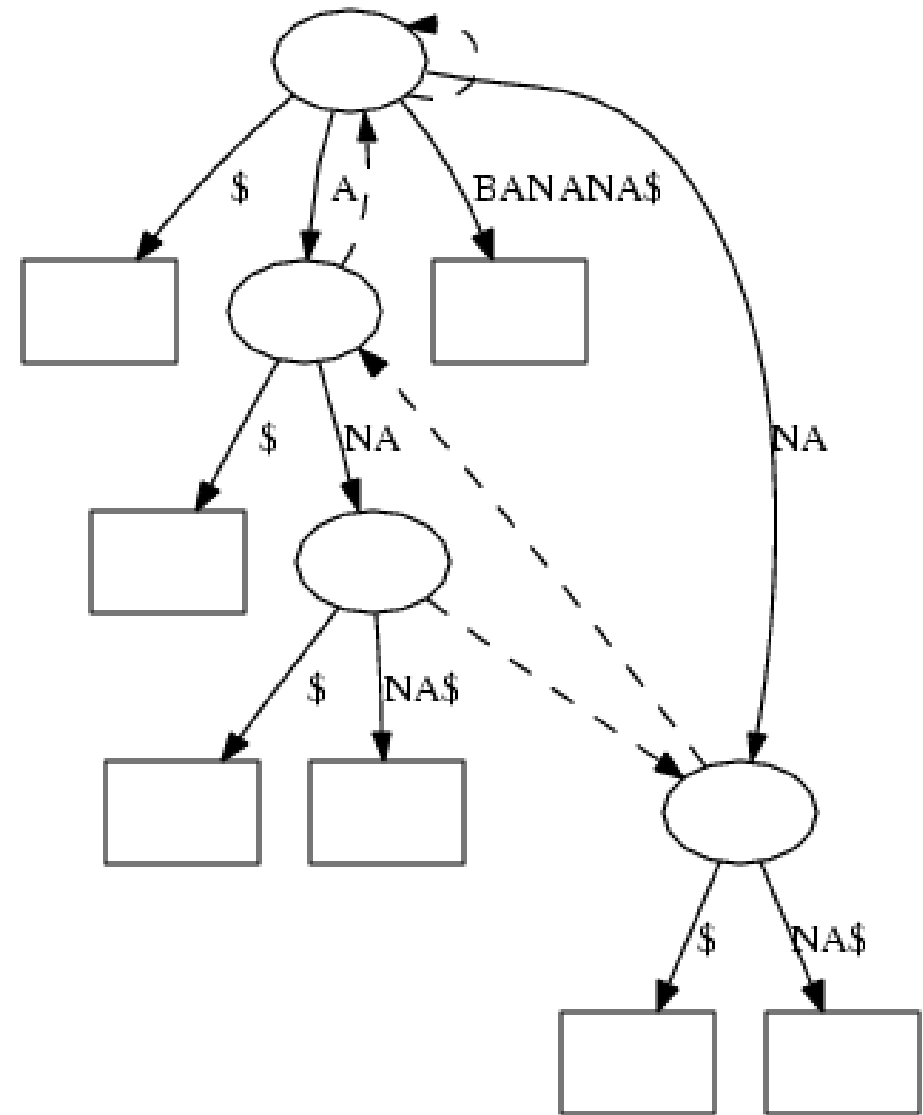
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# Sophisticated Programs

- Data structures and algorithms allow moderately competent programmers to write some very impressive programs
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# countWords

```
#include <stuff>

int main(int argc, char** argv) {
    ifstream in(argv[1]);
    map<string, int> words;

    string s;
    while(in >> s) {
        ++words[s];
    }

    vector<pair<string,int> > pairs;
    copy(words.begin(), words.end(), back_inserter(pairs));
    sort(pairs.begin(), pairs.end(),
        [](auto& a, auto&b){return a.second>b.second;});

    for(auto w=pairs.begin(); w!=pairs.end(); ++w) {
        cout << w->first << "_occurs_" << w->second << "_times\n";
    }
}
```



# Using countWords

```
> countWords text.dat | more
the occurs 97 times
of occurs 96 times
to occurs 57 times
and occurs 42 times
a occurs 36 times
be occurs 31 times
will occurs 26 times
we occurs 23 times
that occurs 23 times
is occurs 21 times
have occurs 19 times
freedom occurs 18 times
```

# Programming Challenge

- Run on “I have a dream” speech with 1550 words in 0.02 seconds
- Challenge for good programmers

*Write a program without use data structures in less than 10 times as much code that runs in less than 10 times as long*

- Probably possible, but certainly not easy

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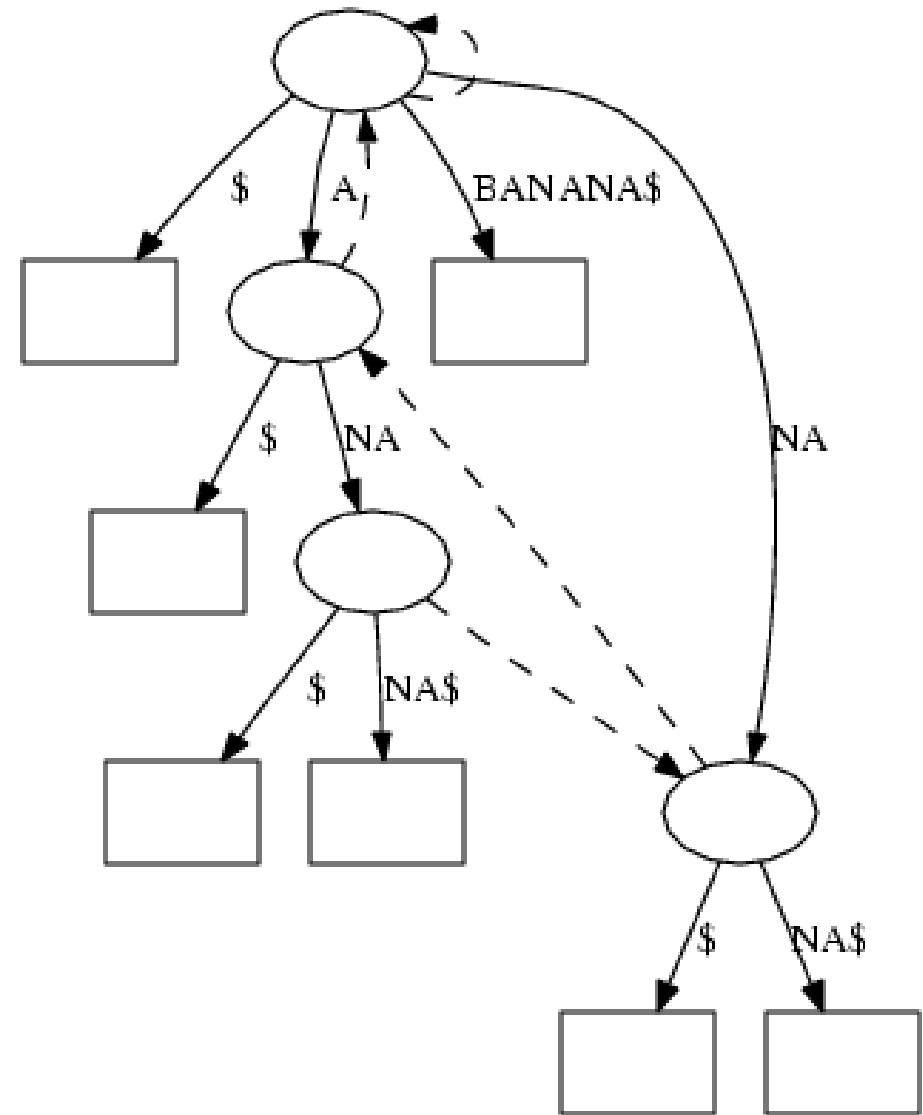
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AAAAGAGGTCATATAGTAGGTACTGTACGGATTTTAACT  
AAAAGAGGTCATATAGTAGGTACTGTACGGATTTTAACT  
AAAAGAGGTCATATAGTAGGTACTGTACGGATTTTAACT  
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AAAAGAGGTCATATAGTAGGTACTGTACGGATTTAAACAT  
AAAAGAGGTCATATAGTAGGTACTGTACGGATTTAAACAT

AGAGG	AAAGA	ACTGT	GAGGT	TTAAC	GGTGC
ATAGT	AAAGA	ACTGT	AGTAG	AGAGG	TGCAT
TGCAT	GGATT	ATATA	ACGGA	TACTG	GAGGT
TACTG	GTACG	TAGTA	GAGGT	TATAG	ATAGT
AGTAG	ATAGT	ATTTA	CGGAT	AAAGA	GATTT

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AAAGA

AGAGG	AAAGA	ACTGT	GAGGT	TTAAC	GGTGC
ATAGT	AAAGA	ACTGT	AGTAG	AGAGG	TGCAT
TGCAT	GGATT	ATATA	ACGGA	TACTG	GAGGT
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AAAGAGG

AGAGG	AAAGA	ACTGT	GAGGT	TTAAC	GGTGC
ATAGT	AAAGA	ACTGT	AGTAG	AGAGG	TGCAT
TGCAT	GGATT	ATATA	ACGGA	TACTG	GAGGT
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AAAGAGGT

AGAGG	AAAGA	ACTGT	GAGGT	TTAAC	GGTGC
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TGCAT	GGATT	ATATA	ACGGA	TACTG	GAGGT
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AAAGAGGTC

AGAGG	AAAGA	ACTGT	GAGGT	TTAAC	GGTGC
ATAGT	AAAGA	ACTGT	AGTAG	AGAGG	TGCAT
TGCAT	GGATT	ATATA	ACGGA	TACTG	GAGGT
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AAAGAGGTCAT

AGAGG	AAAGA	ACTGT	GAGGT	TTAAC	GGTGC
ATAGT	AAAGA	ACTGT	AGTAG	AGAGG	TGCAT
TGCAT	GGATT	ATATA	ACGGA	TACTG	GAGGT
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AAAGAGGTCATATA

AGAGG	AAAGA	ACTGT	GAGGT	TTAAC	GGTGC
ATAGT	AAAGA	ACTGT	AGTAG	AGAGG	TGCAT
TGCAT	GGATT	ATATA	ACGGA	TACTG	GAGGT
TACTG	GTACG	TAGTA	GAGGT	TATAG	ATAGT
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AAAAGAGGTTGCATATAGTAGGTAAGTGTACGGATTTTAAACAT  
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AAAAGAGGTTGCATATAG

AGAGG	AAAGA	ACTGT	GAGGT	TTAAC	GGTGC
ATAGT	AAAGA	ACTGT	AGTAG	AGAGG	TGCAT
TGCAT	GGATT	ATATA	ACGGA	TACTG	GAGGT
TACTG	GTACG	TAGTA	GAGGT	TATAG	ATAGT
AGTAG	ATAGT	ATTTA	CGGAT	AAAGA	GATTT

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AAAAGAGGTCATATAGTAGGTACTGTACGGATTTTAACAT  
AAAAGAGGTCATATAGTAGGTACTGTACGGATTTTAACAT  
AAAAGAGGTCATATAGTAGGTACTGTACGGATTTTAACAT  
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AGAGG	AAAGA	ACTGT	GAGGT	TTAAC	GGTGC
ATAGT	AAAGA	ACTGT	AGTAG	AGAGG	TGCAT
TGCAT	GGATT	ATATA	ACGGA	TACTG	GAGGT
TACTG	GTACG	TAGTA	GAGGT	TATAG	ATAGT
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AAAAGAGGTCATATAGTAGGTA CTGTACGGATTTTAA CAT  
AAAAGAGGTCATATAGTAGGTA CTGTACGGATTTTAA CAT

AAAGAGGTCATATAGTA

AGAGG	AAAGA	ACTGT	GAGGT	TTAAC	GGTGC
ATAGT	AAAGA	ACTGT	AGTAG	AGAGG	TGCAT
TGCAT	GGATT	ATATA	ACGGA	TACTG	GAGGT
TACTG	GTACG	TAGTA	GAGGT	TATAG	ATAGT
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AGAGG	AAAGA	ACTGT	GAGGT	TTAAC	GGTGC
ATAGT	AAAGA	ACTGT	AGTAG	AGAGG	TGCAT
TGCAT	GGATT	ATATA	ACGGA	TACTG	GAGGT
TACTG	GTACG	TAGTA	GAGGT	TATAG	ATAGT
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AAAGAGGTTGCATATAGTAG TACTG

AGAGG	AAAGA	ACTGT	GAGGT	TTAAC	GGTGC
ATAGT	AAAGA	ACTGT	AGTAG	AGAGG	TGCAT
TGCAT	GGATT	ATATA	ACGGA	TACTG	GAGGT
TACTG	GTACG	TAGTA	GAGGT	TATAG	ATAGT
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AAAAGAGGTCATATAGTAG TACTGT

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AAAAGAGGTTGCATATAGTAG TACTGTACG

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ATAGT	AAAGA	ACTGT	AGTAG	AGAGG	TGCAT
TGCAT	GGATT	ATATA	ACGGA	TACTG	GAGGT
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AAAAGAGGTCATATAGTAG TACTGTACGGAA

AGAGG	AAAGA	ACTGT	GAGGT	TTAAC	GGTGC
ATAGT	AAAGA	ACTGT	AGTAG	AGAGG	TGCAT
TGCAT	GGATT	ATATA	ACGGA	TACTG	GAGGT
TACTG	GTACG	TAGTA	GAGGT	TATAG	ATAGT
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AAAGAGGTCATATAGTAG TACTGTACGGATT

AGAGG	AAAGA	ACTGT	GAGGT	TTAAC	GGTGC
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TGCAT	GGATT	ATATA	ACGGA	TACTG	GAGGT
TACTG	GTACG	TAGTA	GAGGT	TATAG	ATAGT
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AAAAGAGGTCATATAGTAGGTACTGTACGGATTTTAAACAT

AAAGAGGTCATATAGTAG TACTGTACGGATT

AGAGG	AAAGA	ACTGT	GAGGT	TTAAC	GGTGC
ATAGT	AAAGA	ACTGT	AGTAG	AGAGG	TGCAT
TGCAT	GGATT	ATATA	ACGGA	TACTG	GAGGT
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AAAGAGGTCATATAGTAG TACTGTACGGATT

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ATAGT	AAAGA	ACTGT	AGTAG	AGAGG	TGCAT
TGCAT	GGATT	ATATA	ACGGA	TACTG	GAGGT
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AAAAGAGGTCATATAGTAGGTA CTGTACGGATTTTAA CAT  
AAAAGAGGTCATATAGTAGGTA CTGTACGGATTTTAA CAT

AAAGAGGTCATATAGTAG TACTGTACGGATTTTA

AGAGG	AAAGA	ACTGT	GAGGT	TTAAC	GGTGC
ATAGT	AAAGA	ACTGT	AGTAG	AGAGG	TGCAT
TGCAT	GGATT	ATATA	ACGGA	TACTG	GAGGT
TACTG	GTACG	TAGTA	GAGGT	TATAG	ATAGT
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AAAAGAGGTCATATAGTAGGTA~~CTGTAC~~GGATTTTAA~~CA~~T  
AAAAGAGGTCATATAGTAGGTA~~CTGTAC~~GGATTTTAA~~CA~~T  
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AAAAGAGGTCATATAGTAG TACTGTACGGATTTTAA~~CA~~

AGAGG	AAAGA	ACTGT	GAGGT	TTAAC	GGTGC
ATAGT	AAAGA	ACTGT	AGTAG	AGAGG	TGCAT
TGCAT	GGATT	ATATA	ACGGA	TACTG	GAGGT
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AGTAG	ATAGT	ATTTA	CGGAT	AAAGA	GATTT

# New Generation Sequencers

- The estimated cost of sequencing the human genome in 2005 was \$10 000 000
- To reduce the cost there was and is a drive to produce new sequencing machines
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- Can these be assembled?

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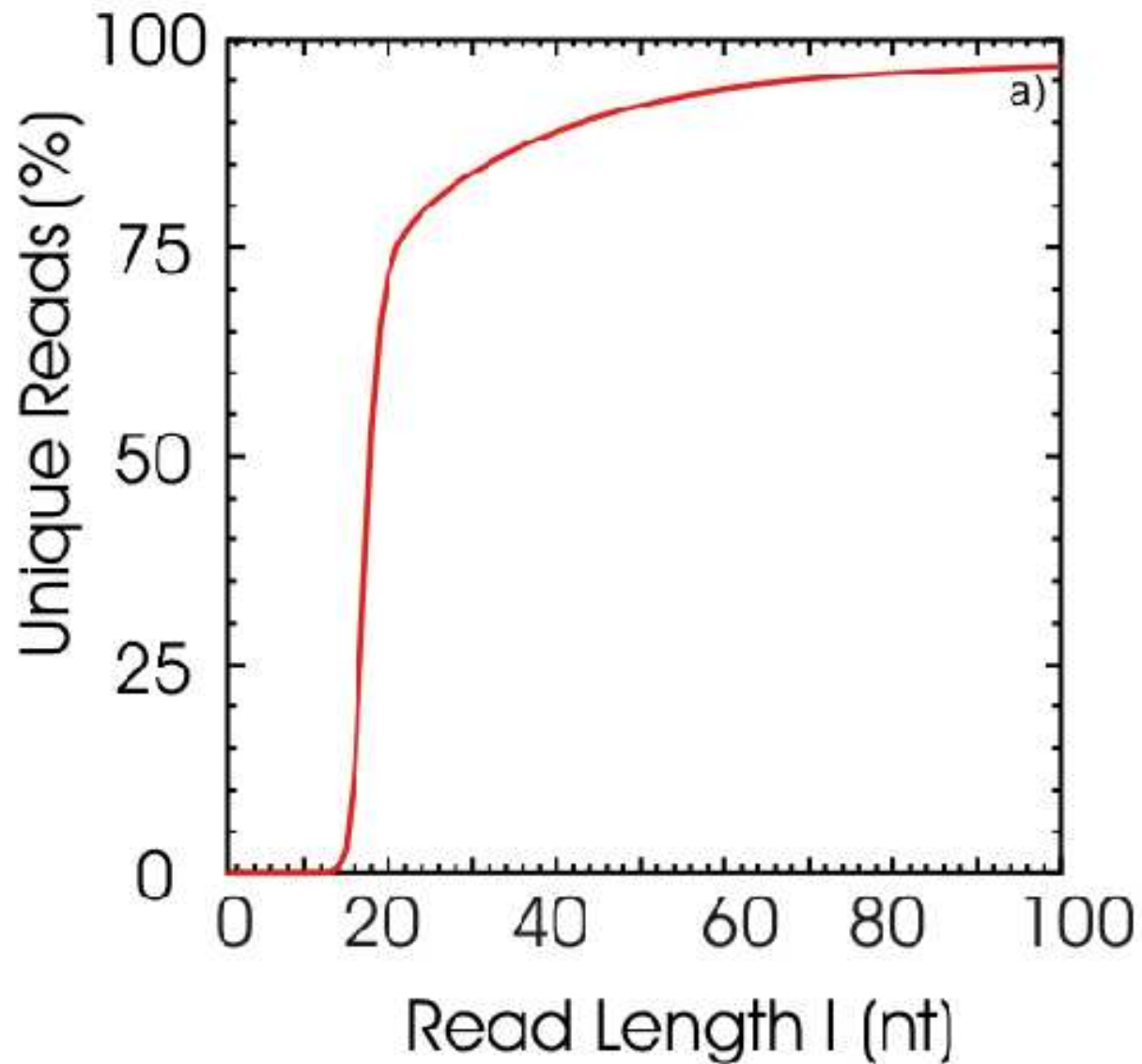
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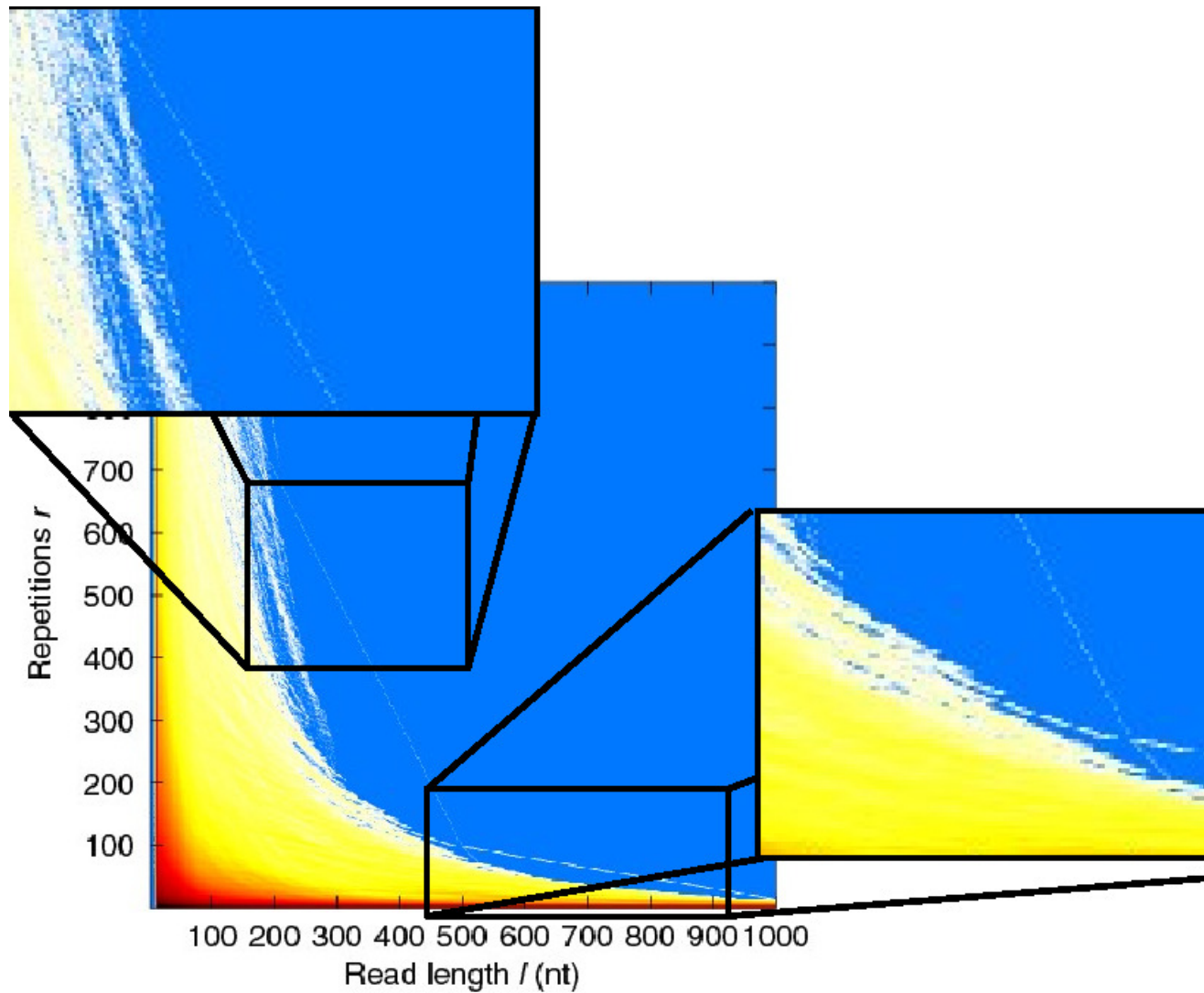
A A A A G A G G T G C A T A T A G T A G G T A C T G A G A G G T T T T A A C A T

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# Repeats in Human Genome



# Repeats Structure



# Computing Repeats

- A naive program would take  $n^2$  operations where  $n = 6.4 \times 10^9$
- If we used this we would still be waiting for the program to finish
- Could not answer this question a few years ago
- Used state-of-the-art suffix arrays
- Smart algorithms allow you to do things which you cannot do otherwise

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# To Use DSA You Need To

- Know what common data structures and algorithm do
- Understand the implementations enough to modify existing data structures to be fit for purpose
- Understand time/space complexity to select the right data structure or algorithm
- Understand software interfaces for DSA
- Be able to combine data structures
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