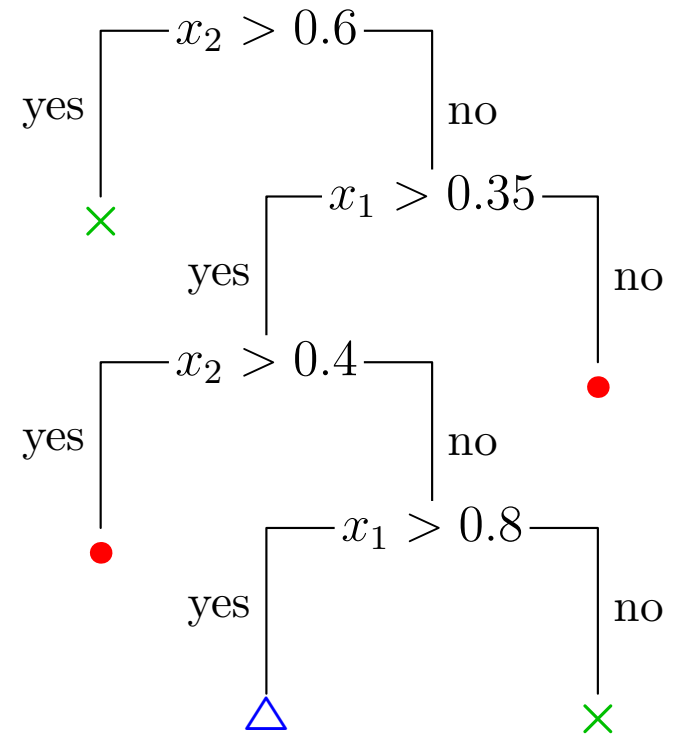
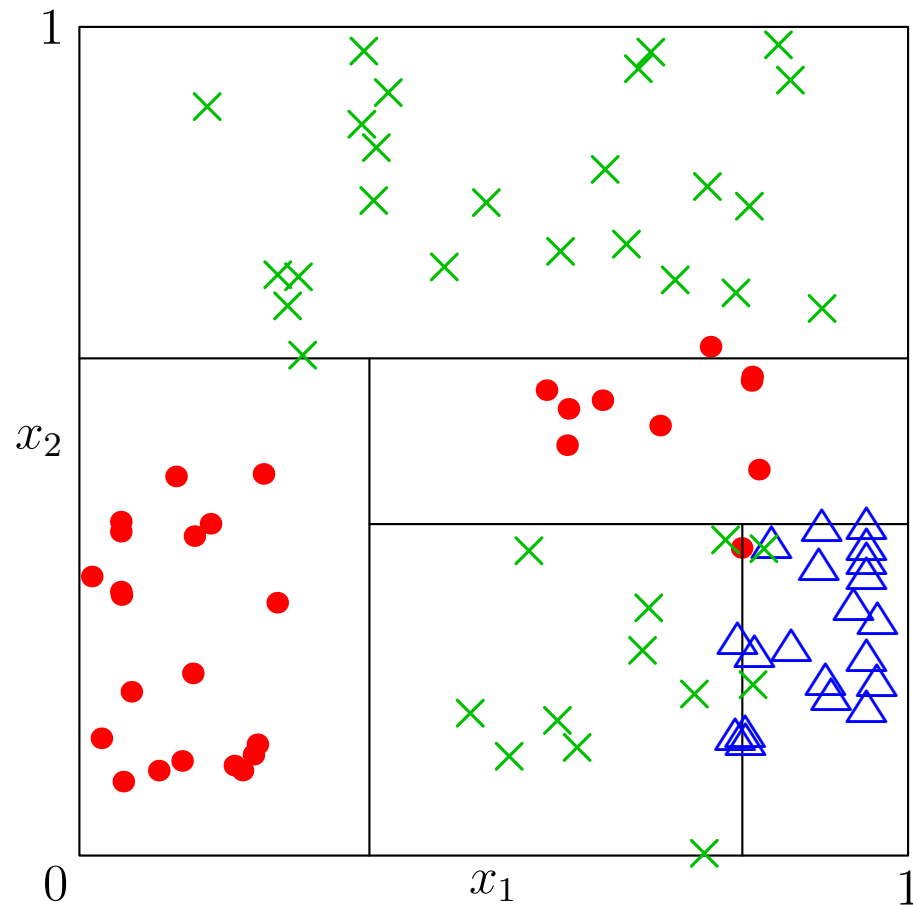


Advanced Machine Learning

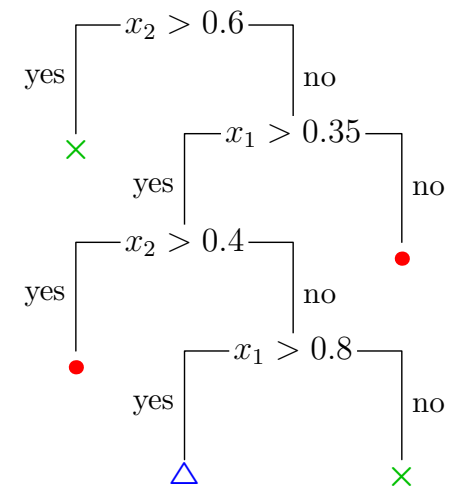
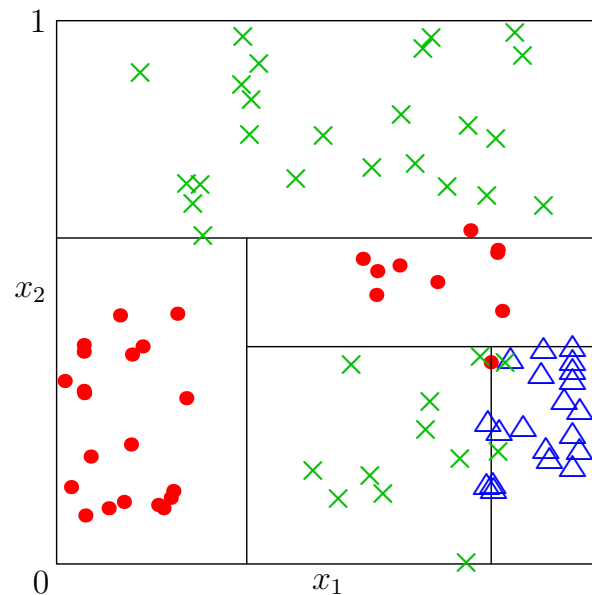
Boosting



Boosting, AdaBoost, Gradient Boosting

Outline

1. **Boosting**
2. AdaBoost
3. Gradient Boosting



Boosting

- In boosting we make a **strong learner** by using a weighted sum of **weak learners**

$$C_n(\mathbf{x}) = \sum_{i=1}^n \alpha_i \hat{h}_i(\mathbf{x})$$

- Weak learners, $\hat{h}_i(\mathbf{x})$, are learning machine that do a little better than chance
- The trick is to choose the weights, α_i
- Because the weak learners do little better than chance we (miraculously) **don't** overfit

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Shallow Trees

- One of the most effective type of weak learner are very shallow trees
- Sometimes we just use one variable (the stump)
- There are different algorithms for choosing the weights
 - ★ adaboost
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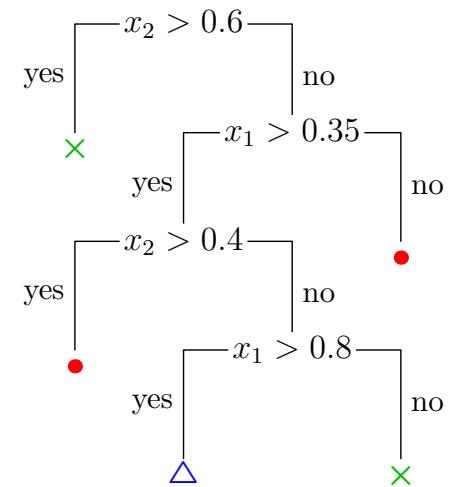
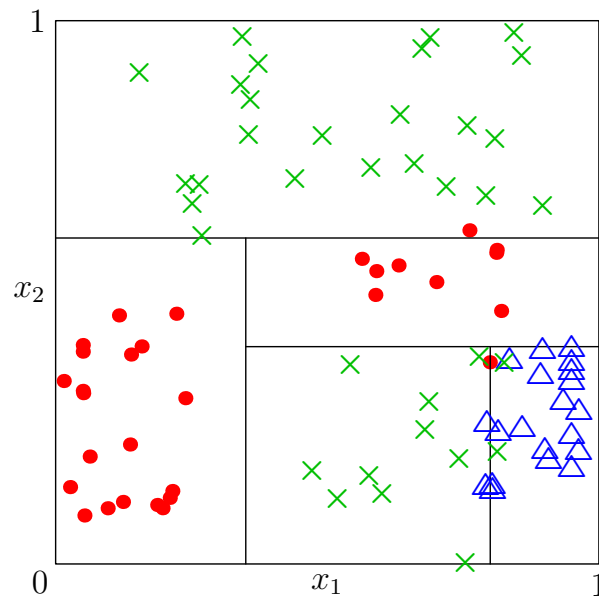
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 - ★ gradient boosting—used for regression, trains a weak learner on the residual errors

Outline

1. Boosting
2. **AdaBoost**
3. Gradient Boosting



Boosting a Binary Classifier

- Suppose we have a binary classification task with data $\mathcal{D} = \{(\mathbf{x}^\mu, y^\mu) | \mu = 1, 2, \dots, m\}$ with $y^\mu \in \{-1, 1\}$
- Our i^{th} weak learner provides a prediction $\hat{h}_i(\mathbf{x}^\mu) \in \{-1, 1\}$
- We ask, can we find a linear combination

$$C_n(\mathbf{x}) = \alpha_1 \hat{h}_1(\mathbf{x}) + \alpha_2 \hat{h}_2(\mathbf{x}) + \dots + \alpha_n \hat{h}_n(\mathbf{x})$$

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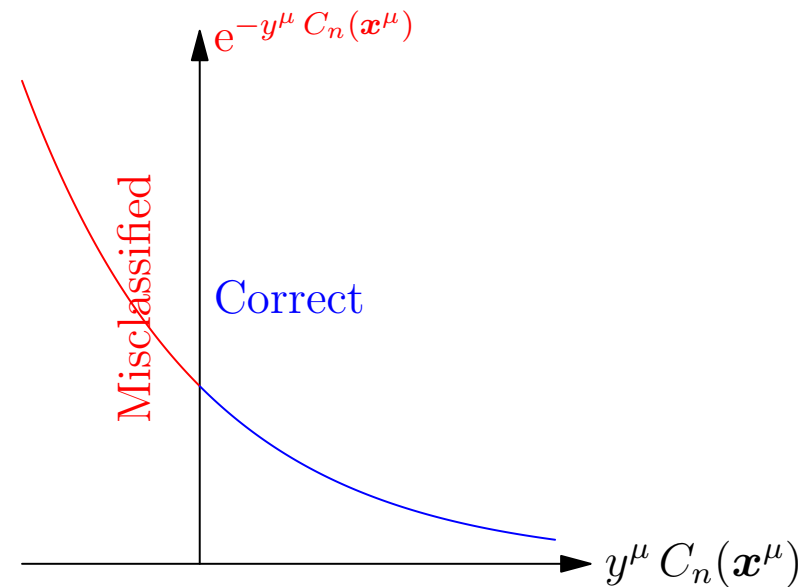
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- Note we want $y^\mu C_n(\mathbf{x}^\mu) > 0$

AdaBoost

- AdaBoost is a classic solution to this problem
- It assigns an “loss function”

$$L_n = \sum_{\mu=1}^m e^{-y^\mu C_n(\mathbf{x}^\mu)}$$

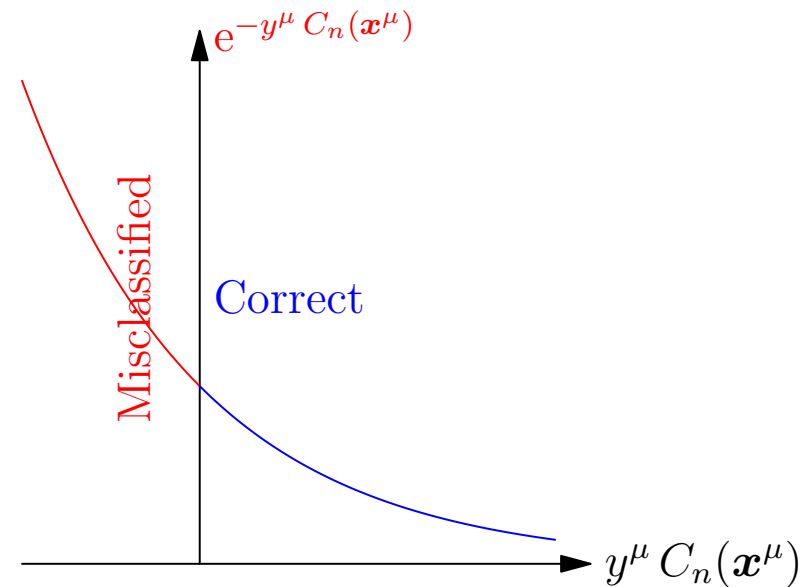


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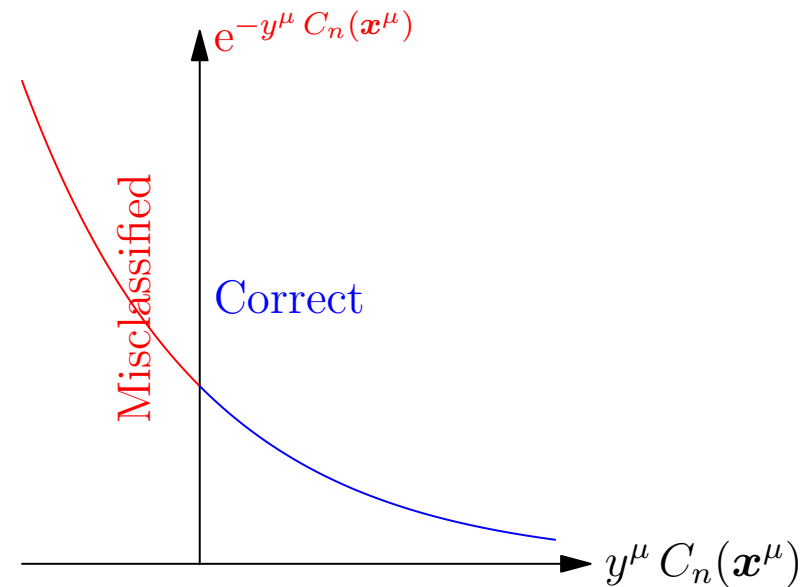


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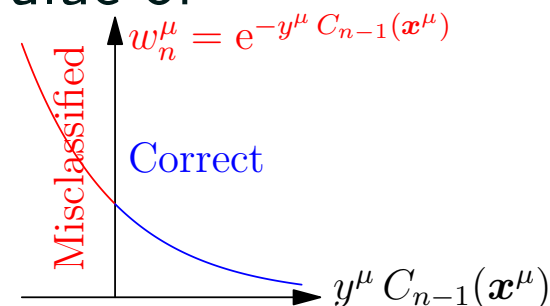
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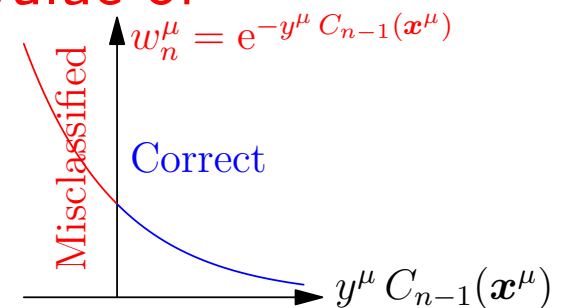
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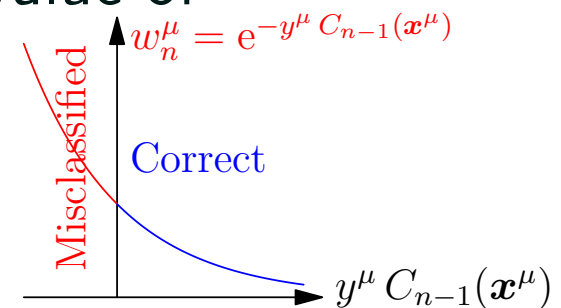
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Algorithm

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2. Associate a weight, w_n^μ , with every data point (\mathbf{x}^μ, y^μ) , $\mu = 1, 2, \dots, m$
3. Initially $w_1^\mu = 1$
4. Choose the weak learning, $\hat{h}_n(\mathbf{x}) \in \mathcal{W}$, that minimises
$$\sum_{\mu: y^\mu \neq \hat{h}_n(\mathbf{x}^\mu)} w_n^\mu$$
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2. Associate a weight, w_n^μ , with every data point (\mathbf{x}^μ, y^μ) , $\mu = 1, 2, \dots, m$
3. Initially $w_1^\mu = 1$ (large weight, w_n^μ , means (\mathbf{x}^μ, y^μ) is poorly classified)
4. Choose the weak learning, $\hat{h}_n(\mathbf{x}) \in \mathcal{W}$, that minimises
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Performance

- Adaboost works well with weak learners, usually out-performing bagging
- It doesn't work well with strong learners (tends to over-fit)
- It is limited to binary classification (there are generalisation, but they are difficult to get to work)
- It has fallen from fashion
- In contrast **gradient boosting** used for regression is very popular

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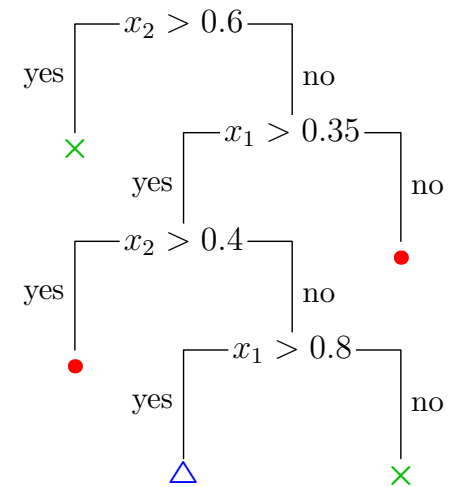
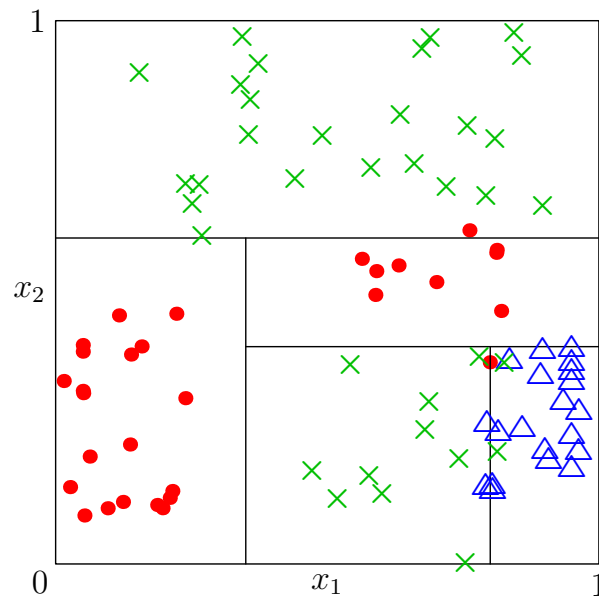
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Outline

1. Boosting
2. AdaBoost
3. **Gradient Boosting**



Gradient Boosting

- In gradient boosting we again build a strong learner as a linear combination of weak learners

$$C_n(\mathbf{x}) = C_{n-1}(\mathbf{x}) + \hat{h}_n(\mathbf{x})$$

- Gradient boosting used on regression (again using decision trees)
- At each step $\hat{h}_n(\mathbf{x})$ is trained to predict the residual error, $\Delta_{n-1} = y - C_{n-1}(\mathbf{x})$, (i.e. the target minus the current prediction)
- (This difference looks a bit like a gradient hence the rather confusing name)

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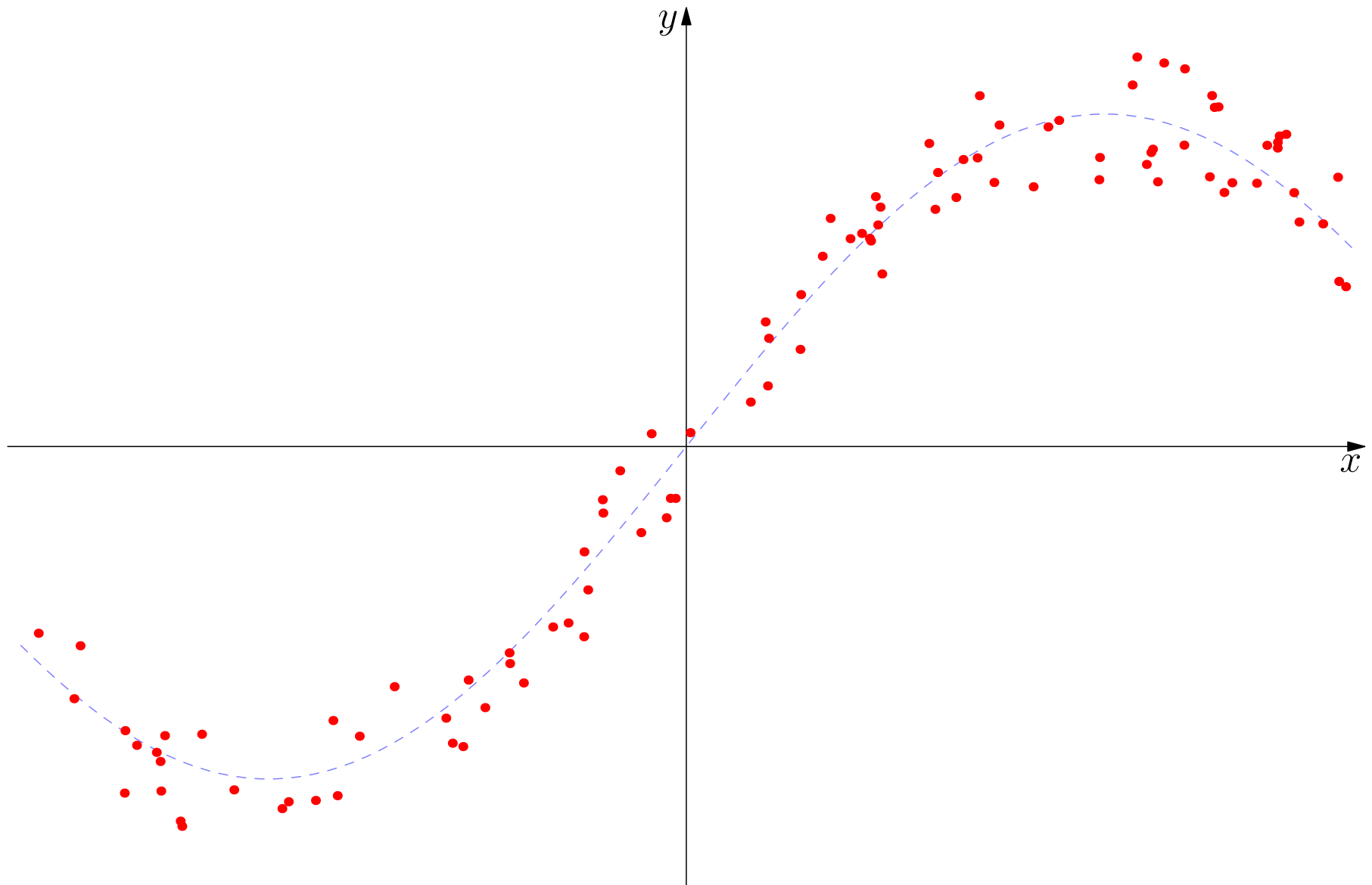
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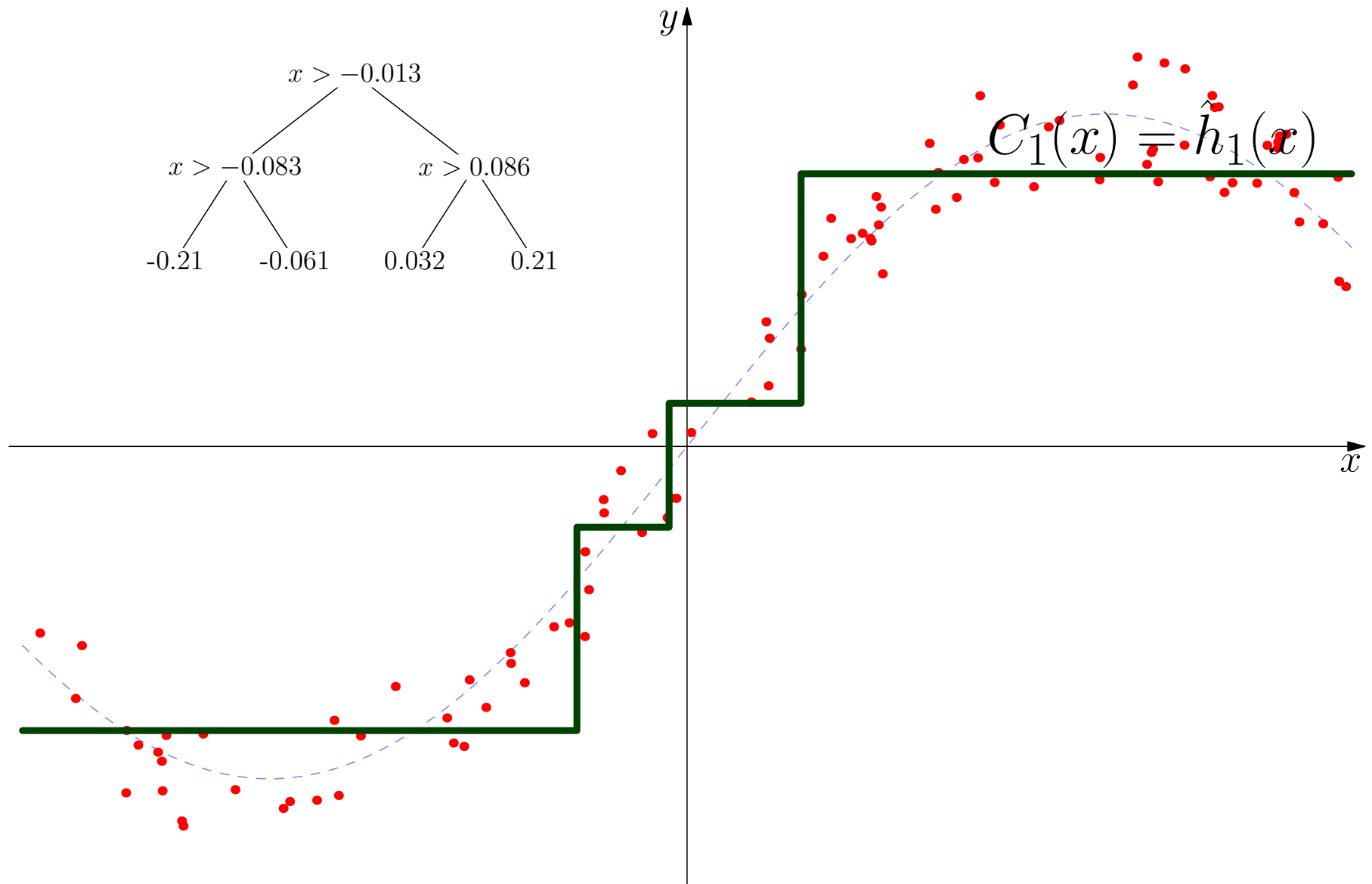
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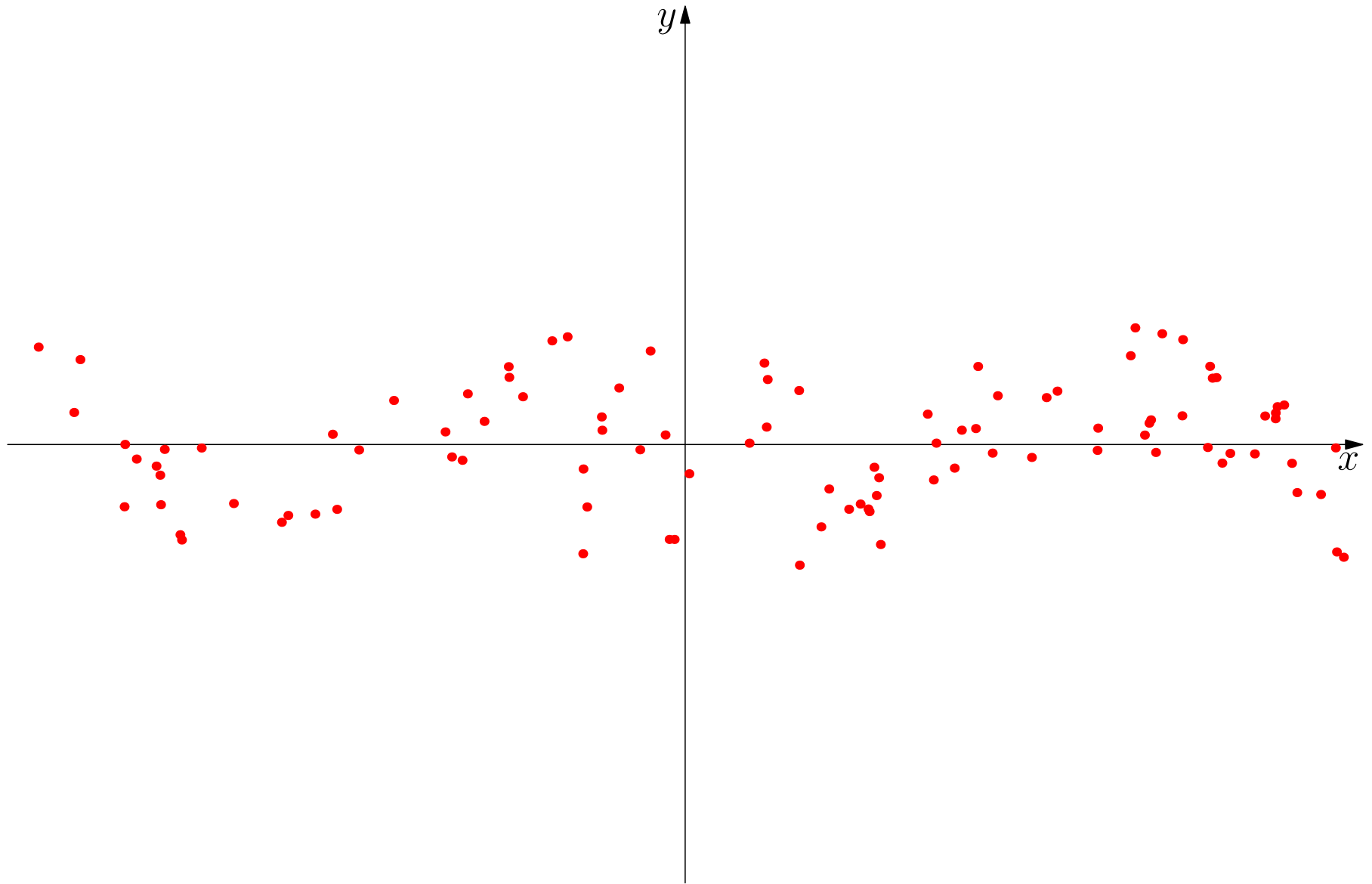
Fitting a Sin Wave



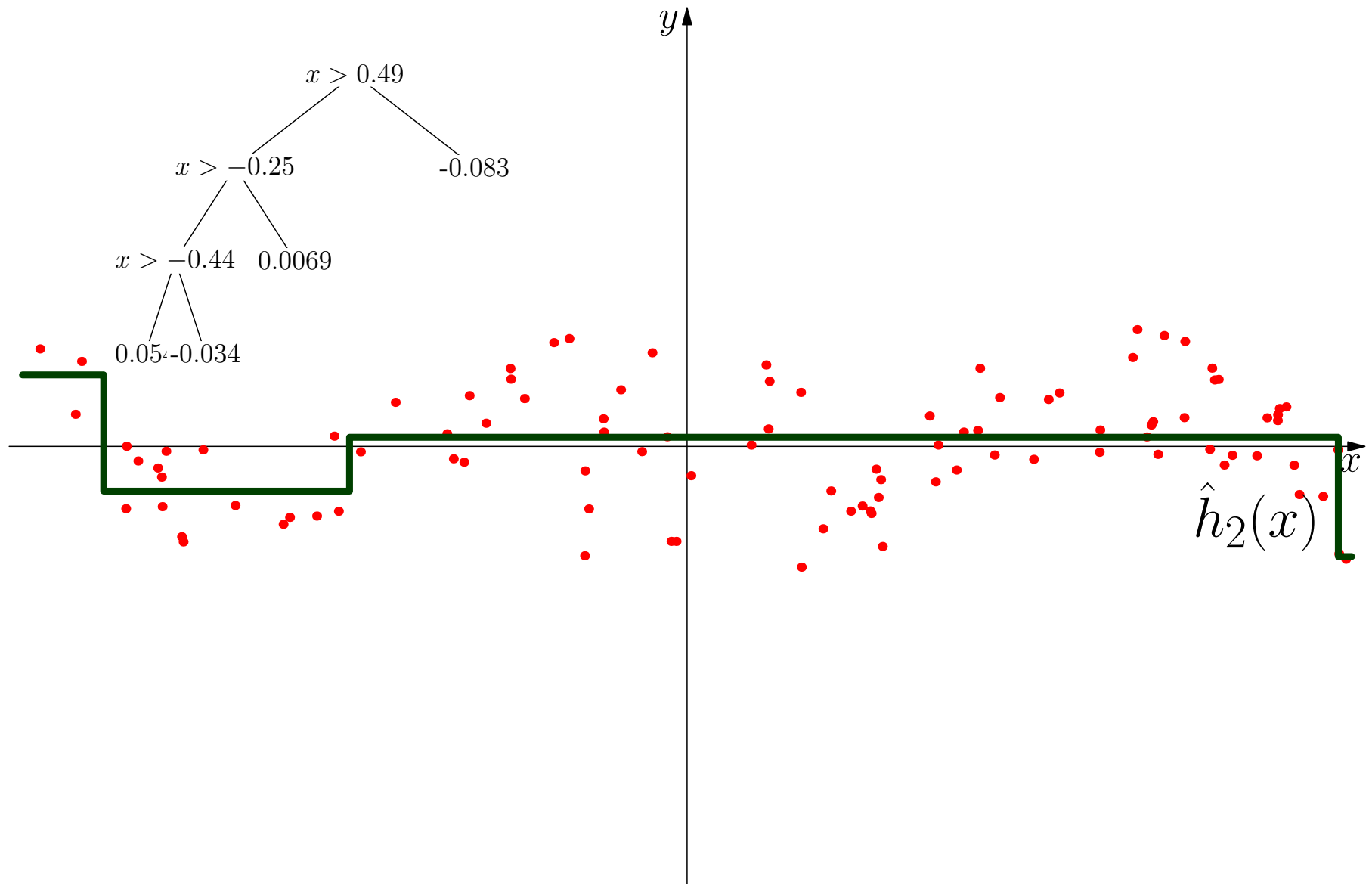
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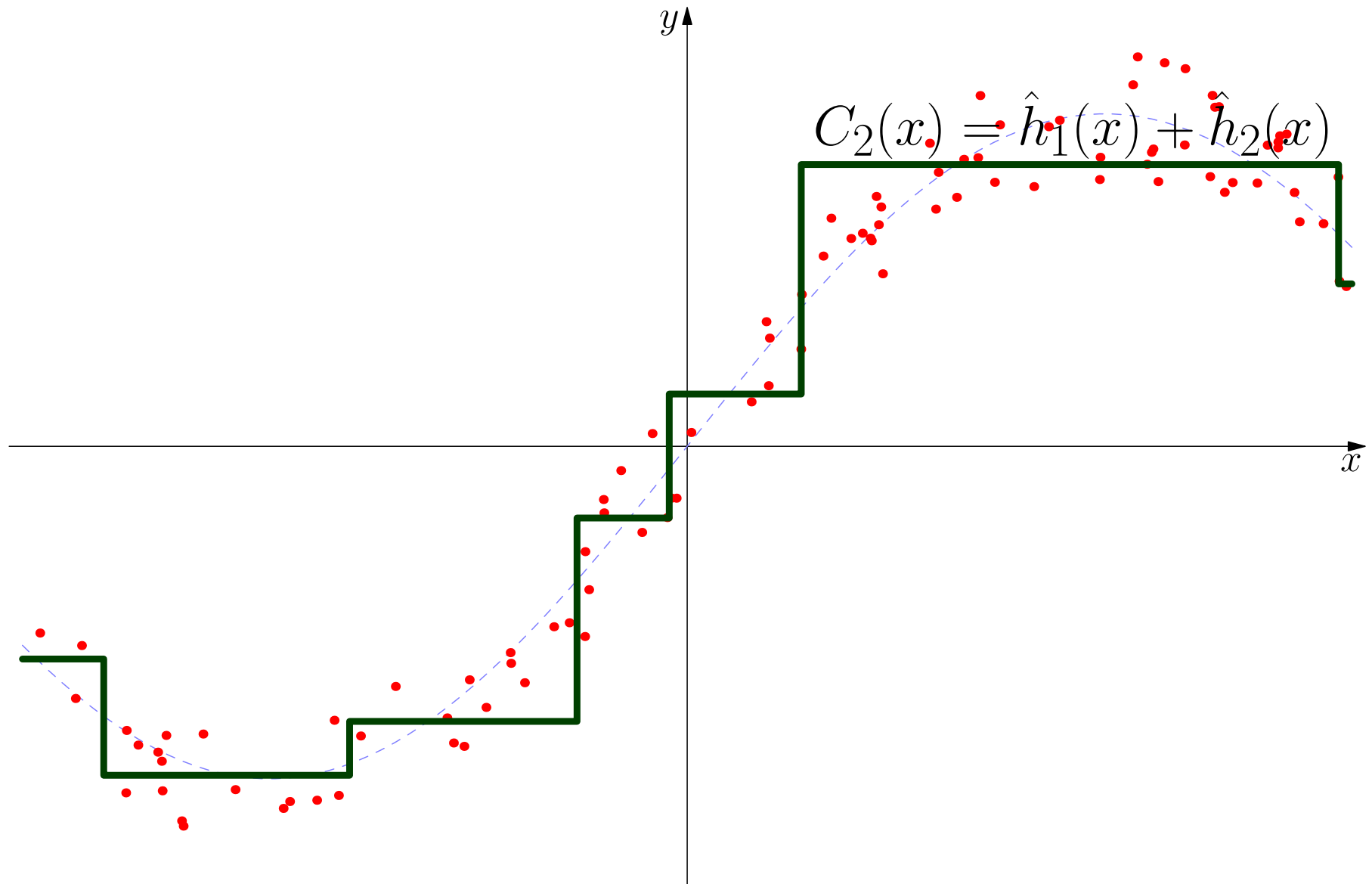
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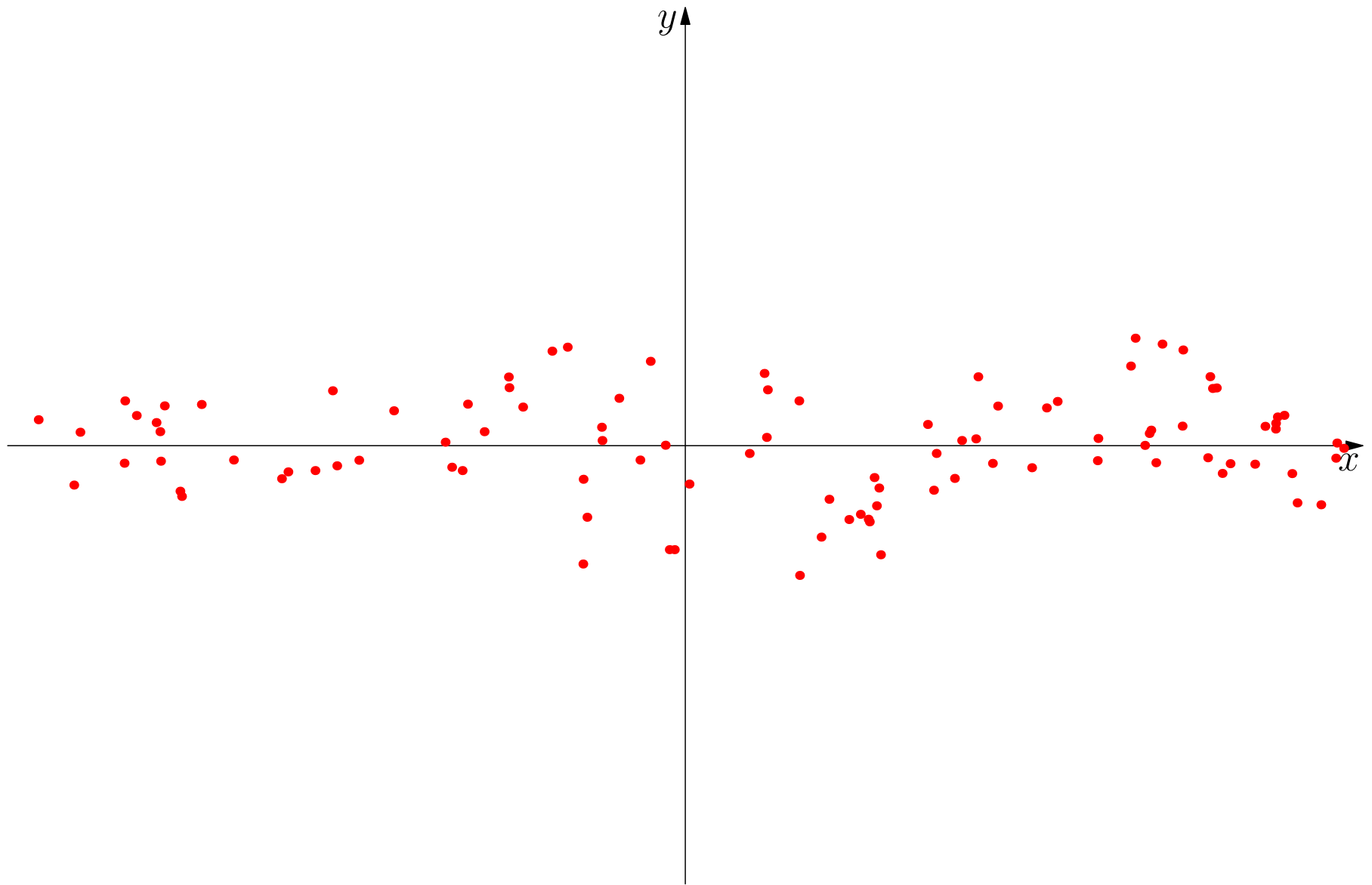
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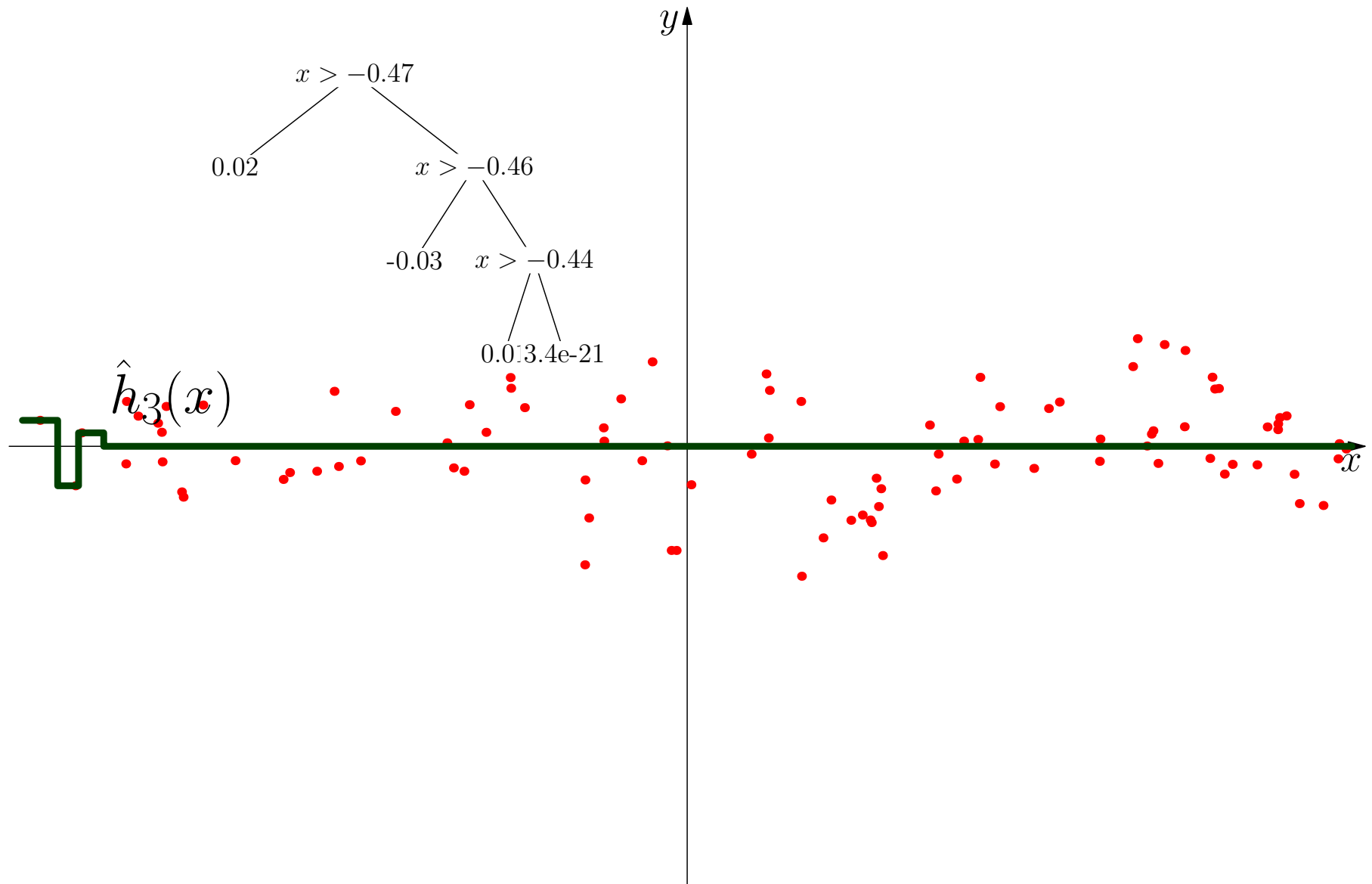
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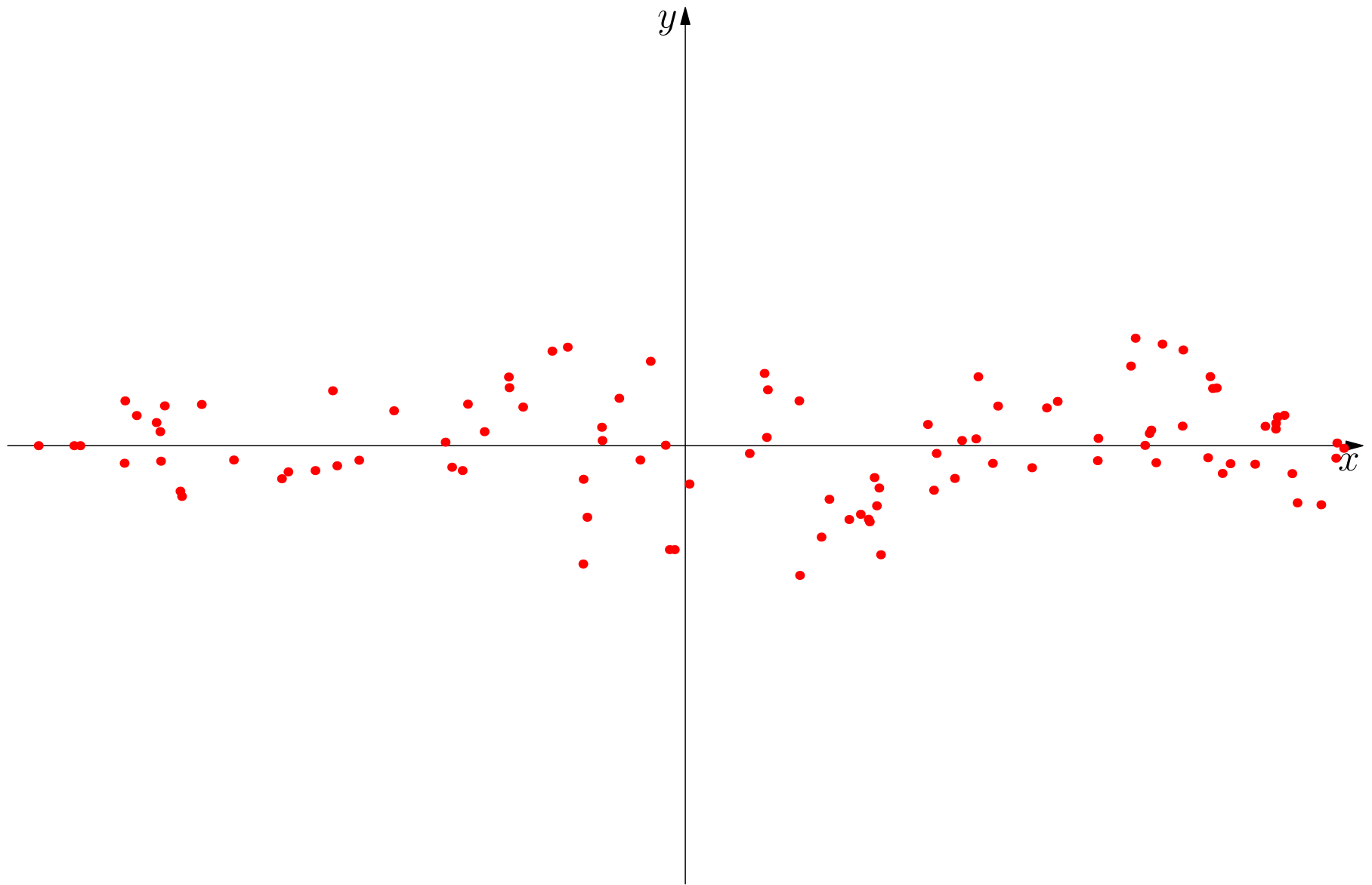
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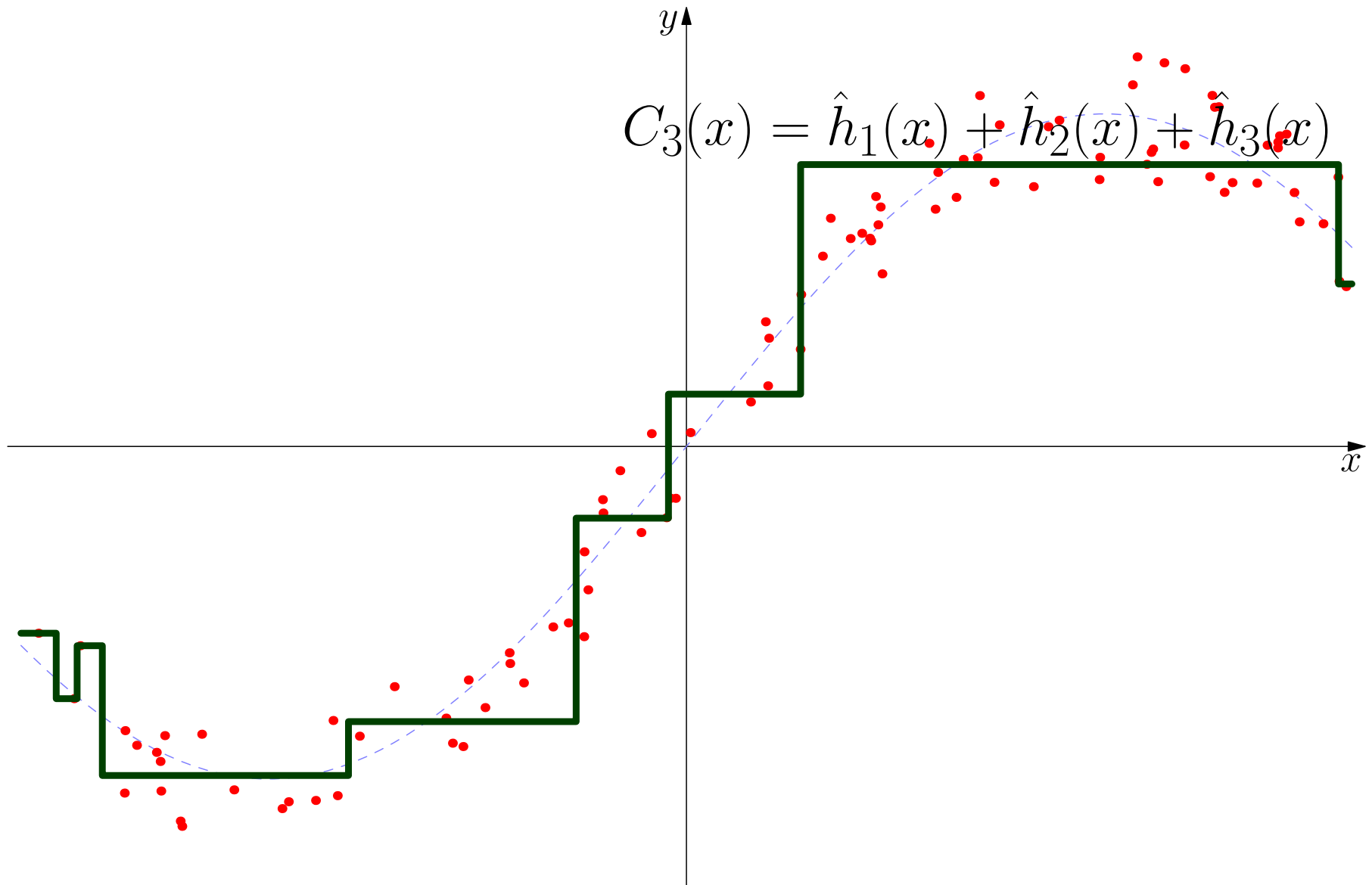
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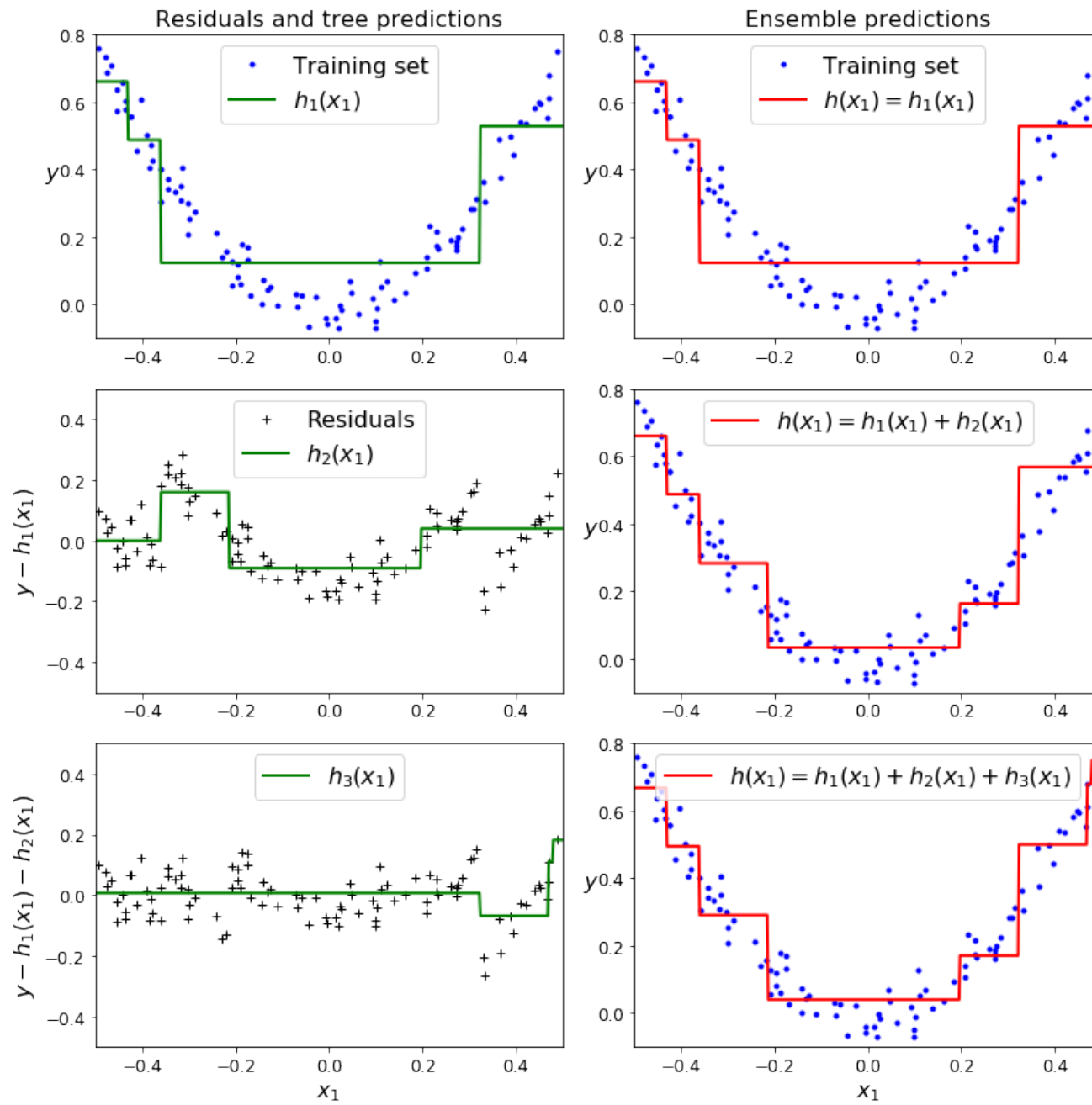


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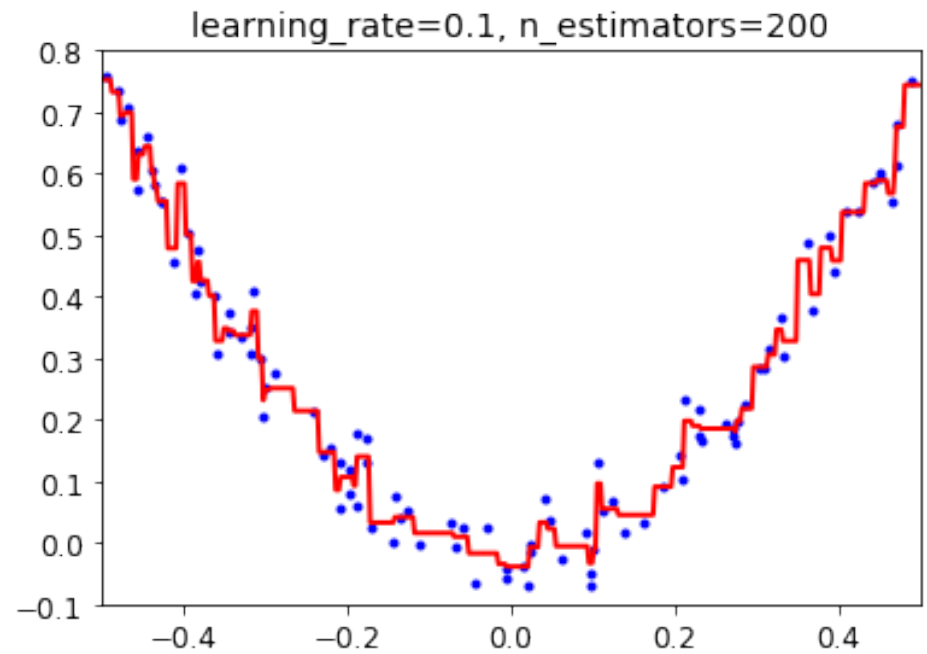
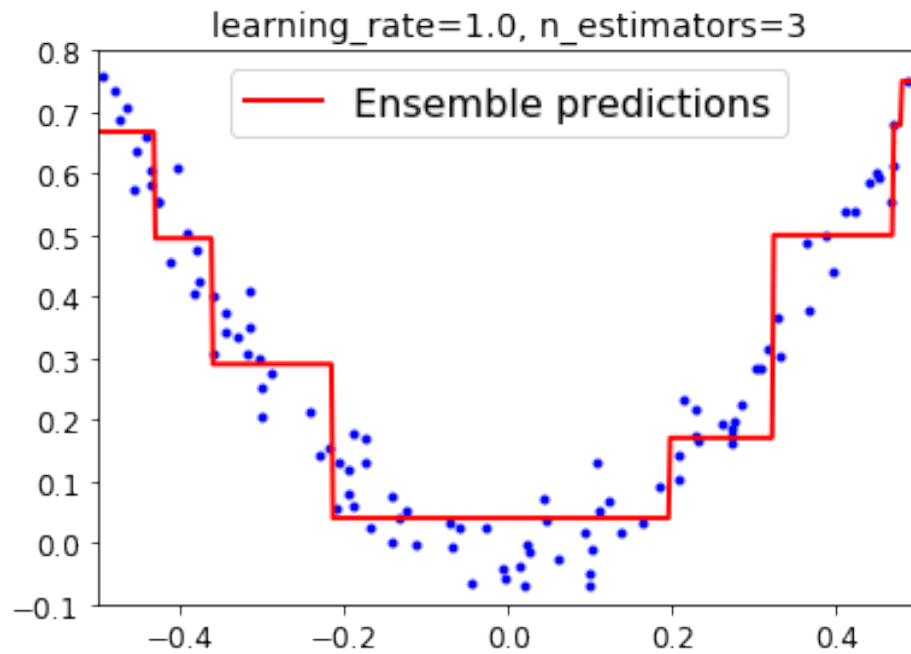
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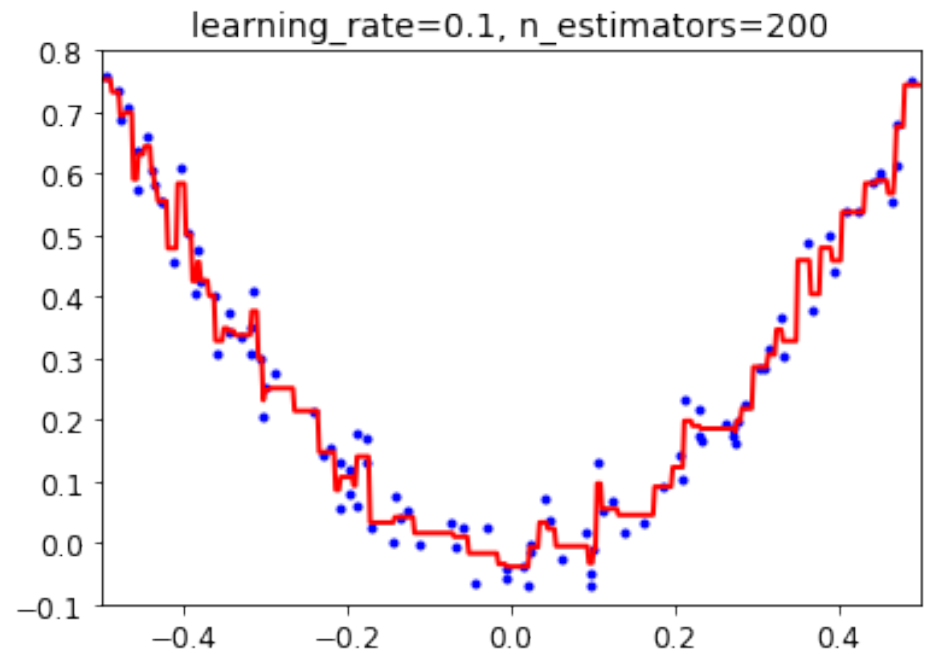
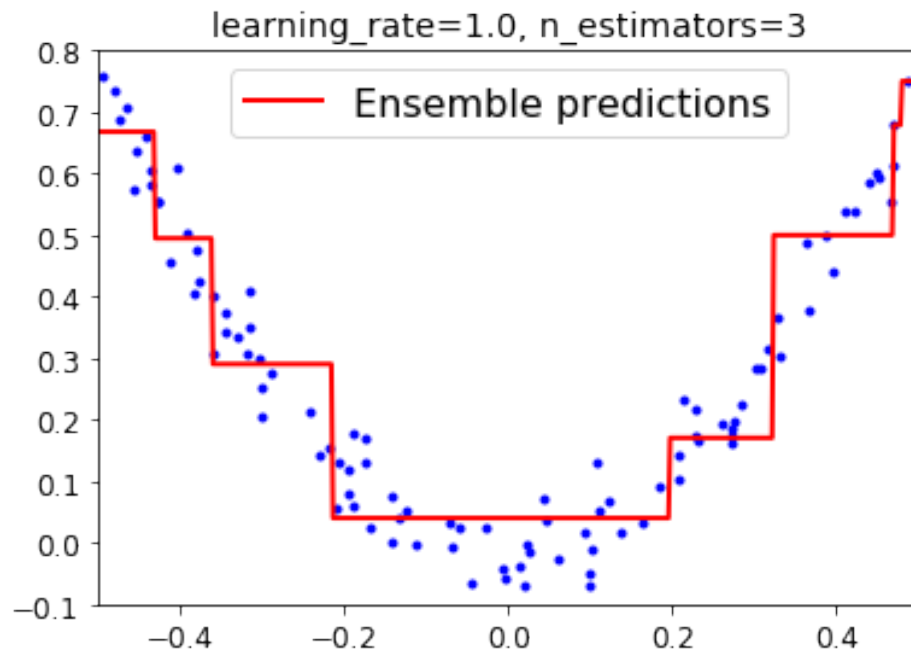
Keep On Going

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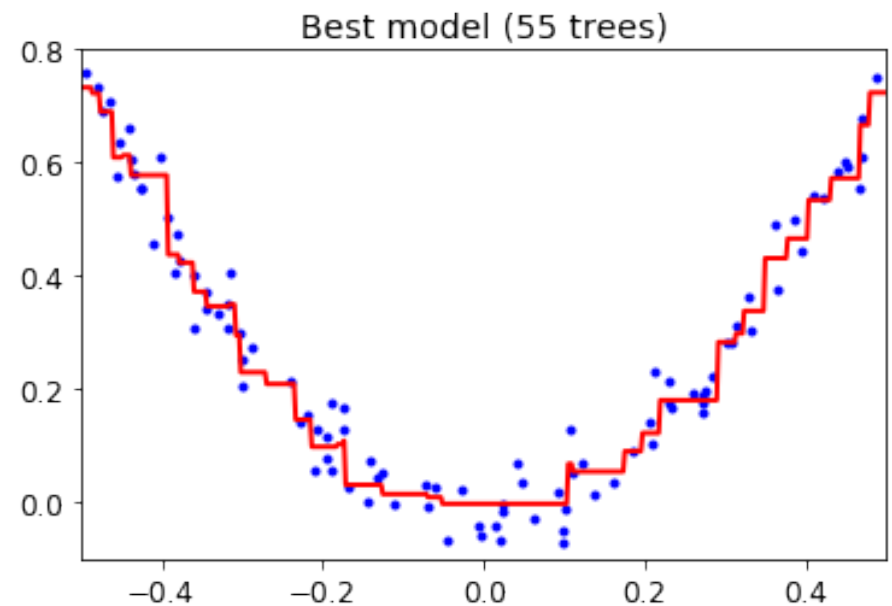
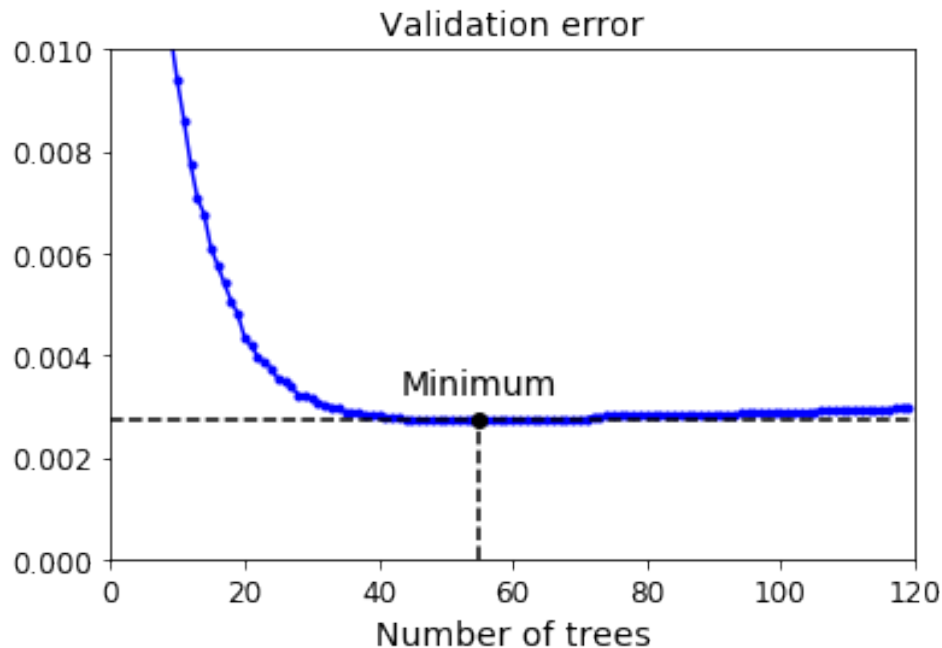
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- But we will over-fit eventually

Early Stopping

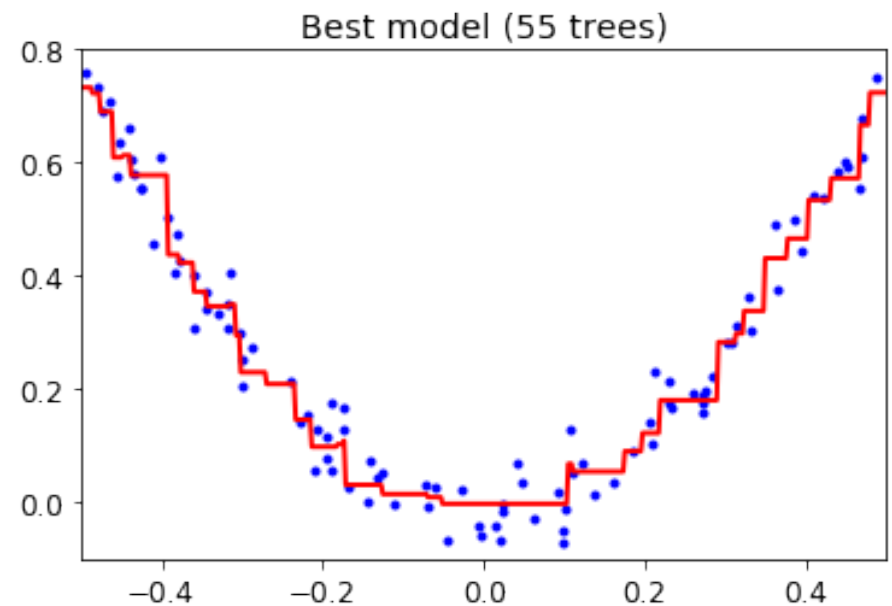
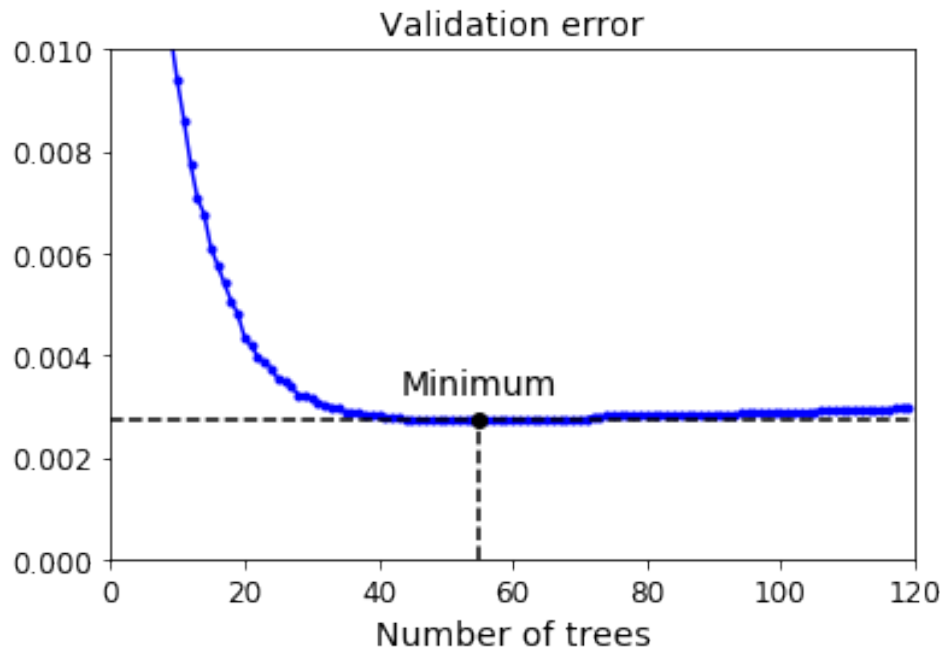
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- XGBoost stands for eXtreme Gradient Boosting
- It was much faster than most gradient boosting algorithms and scales to billions of training data points—although GBM is often better
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- Ensemble methods have proved themselves to be very powerful
- Tend to work best with very simple models (true of random forest and boosting)
- XGBoost or GBM are currently the best methods for tabular data (particular for large training sets)
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