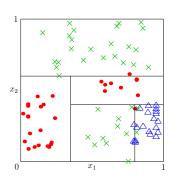
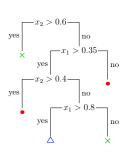
# **Advanced Machine Learning**

## Boosting





Boosting, AdaBoost, Gradient Boosting

Adam Prügel-Bennett

COMP6208 Advanced Machine Learning

## **Boosting**

 In boosting we make a strong learner by using a weighted sum of weak learners

$$C_n(\boldsymbol{x}) = \sum_{i=1}^n \alpha_i \hat{h}_i(\boldsymbol{x})$$

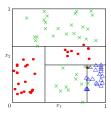
- ullet Weak learners,  $\hat{h}_i(x)$ , are learning machine that do a little better than chancel
- The trick is to choose the weights,  $\alpha_i$
- Because the weak learners do little better than chance we (miraculously) don't overfit that much

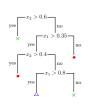
Adam Prügel-Bennett

COMP6208 Advanced Machine Learning

## Outline

- 1. Boosting
- 2. AdaBoost
- 3. Gradient Boosting





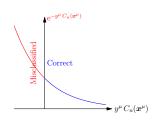
Adam Prügel-Bennett

COMP6208 Advanced Machine Learning

#### AdaBoost

- AdaBoost is a classic solution to this problem
- It assigns an "loss function"

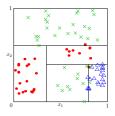


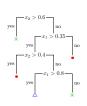


 This punishes examples where there is an errors more than correct classifications

## Outline

- 1. Boosting
- 2. AdaBoost
- 3. Gradient Boosting





Adam Prügel-Bennett

COMP6208 Advanced Machine Learning

#### **Shallow Trees**

- One of the most effective type of weak learner are very shallow trees
- Sometimes we just use one variable (the stump) although usually we would use slightly deeper trees
- There are different algorithms for choosing the weights
  - ★ adaboost—a classic algorithm for binary classification
- ★ gradient boosting —used for regression, trains a weak learner on the residual errors

Adam Prügel-Bennett

COMP6208 Advanced Machine Learning

## **Boosting a Binary Classifier**

- Suppose we have a binary classification task with data  $\mathcal{D}=\{(\boldsymbol{x}^{\mu},y^{\mu})|\mu=1,2,...,m\} \text{ with } y^{\mu}\in\{-1,1\} \text{I}$
- ullet Our  $i^{th}$  weak learner provides a prediction  $\hat{h}_i(oldsymbol{x}^\mu) \in \{-1,1\}$
- We ask, can we find a linear combination

$$C_n(\mathbf{x}) = \alpha_1 \hat{h}_1(\mathbf{x}) + \alpha_2 \hat{h}_2(\mathbf{x}) + \dots + \alpha_n \hat{h}_n(\mathbf{x})$$

- So that  $\operatorname{sgn}(C_n(x))$  is a strong learner?
- Note we want  $y^{\mu}C_n(x^{\mu})>0$

Adam Prügel-Bennett

Adam Prügel-Bennett

COMP6208 Advanced Machine Learnin

#### **Iterative Learning**

• We build up a strong learner iteratively (greedily)

$$C_n(\boldsymbol{x}) = C_{n-1}(\boldsymbol{x}) + \alpha_n \hat{h}_n(\boldsymbol{x})$$

 $\bullet$  Defining  $w_1^\mu=1$  and  $w_n^\mu=\mathrm{e}^{-y^\mu C_{n-1}(\boldsymbol{x}^\mu)}$  then

$$\begin{split} L_n(\alpha_n) &= \sum_{\mu=1}^m \mathrm{e}^{-y^\mu C_n(\boldsymbol{x}^\mu)} = \sum_{\mu=1}^m \mathrm{e}^{-y^\mu (C_{n-1}(\boldsymbol{x}^\mu) + \alpha_n \hat{h}_n(\boldsymbol{x}^\mu))} \\ &= \sum_{\mu=1}^m w_n^\mu \mathrm{e}^{-\alpha_n y^\mu \hat{h}_n(\boldsymbol{x}^\mu)} = \sum_{\mu:y^\mu \neq \hat{h}_n(\boldsymbol{x}^\mu)}^{\alpha_n} w_n^\mu \mathbf{e}^{\alpha_n} + \sum_{\mu:y^\mu = \hat{h}_n(\boldsymbol{x}^\mu)}^{\alpha_n} w_n^\mu \mathbf{e}^{-\alpha_n} \\ &= \mathrm{e}^{-\alpha_n} \sum_{\mu=1}^m w_n^\mu + (\mathrm{e}^{\alpha_n} - \mathrm{e}^{-\alpha_n}) \sum_{\mu:y^\mu \neq \hat{h}_n(\boldsymbol{x}^\mu)} w_n^\mu \end{split}$$

## **Choosing a Weak Classifier**

• To minimise the loss

$$L_n(\alpha_n) = e^{-\alpha_n} \sum_{\mu=1}^m w_n^{\mu} + (e^{\alpha_n} - e^{-\alpha_n}) \sum_{\mu: y^{\mu} \neq \hat{h}_n(\boldsymbol{x}^{\mu})} w_n^{\mu}$$

• We choose the weak learner with the lowest value of

$$\sum_{\mu:y^{\mu}\neq \hat{h}_{n}(\boldsymbol{x}^{\mu})} w_{n}^{\mu} = \sum_{\mu:y^{\mu}\neq \hat{h}_{n}(\boldsymbol{x}^{\mu})} e^{-y^{\mu}C_{n-1}(\boldsymbol{x}^{\mu})}$$
Correct

• That is, it misclassifies only where the other learners classify well

dam Priigel-Rennett COMP6208 Advanced Machine Learning

## **Algorithm**

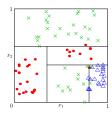
- 1. Start with a set of weak learners  $\mathcal{W}$
- 2. Associate a weight,  $w_n^{\mu}$ , with every data point  $(x^{\mu}, y^{\mu})$ ,  $\mu = 1, 2, ..., m$
- 3. Initially  $w_1^{\mu}=1$  (large weight,  $w_n^{\mu}$ , means  $(x^{\mu},y^{\mu})$  is poorly classified)
- 4. Choose the weak learning,  $\hat{h}_n(x)\in\mathcal{W}$ , that minimises  $\sum\limits_{\mu:y^\mu\neq\hat{h}_n(x^\mu)}w_n^\mu$
- 5. Update predictor  $C_n(x) = C_{n-1}(x) + \alpha_n \hat{h}_n(x)$  where  $\alpha_n = \frac{1}{2} \log \left( \frac{\sum\limits_{\mu: y^\mu = \hat{h}_n(x^\mu)} w_n^\mu}{\sum\limits_{\mu: y^\mu \neq \hat{h}_n(x^\mu)} w_n^\mu} \right)^{\blacksquare}$
- 6. Update  $w_{n+1}^\mu=w_n^\mu \mathrm{e}^{-y^\mu \alpha_n \hat{h}_n(\boldsymbol{x}^\mu)}$
- 7. Go to 4

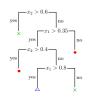
Adam Prügel-Bennett

COMP6208 Advanced Machine Learning

## Outline

- 1. Boosting
- 2. AdaBoost
- 3. Gradient Boosting

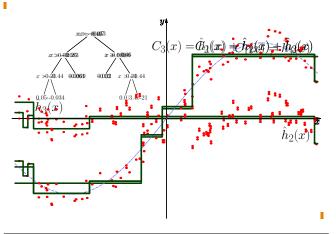




Adam Prügel-Bennett

COMP6208 Advanced Machine Learning

#### Fitting a Sin Wave



# **Choosing Weights**

• We now choose the weight  $\alpha_n$  to minimise the loss  $L_n(\alpha_n)$ 

• That is

Adam Prügel-Bennett

COMP6208 Advanced Machine Learning

#### **Performance**

- Adaboost works well with weak learners, usually out-performing bagging
- It doesn't work well with strong learners (tends to over-fit)
- It is limited to binary classification (there are generalisation, but they are difficult to get to work)
- It has fallen from fashion
- In contrast gradient boosting used for regression is very popular

Adam Prügel-Benne

COMP6208 Advanced Machine Learning

## **Gradient Boosting**

 In gradient boosting we again build a strong learner as a linear combination of weak learners

$$C_n(\boldsymbol{x}) = C_{n-1}(\boldsymbol{x}) + \hat{h}_n(\boldsymbol{x})$$

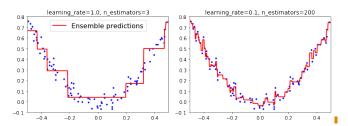
- Gradient boosting used on regression (again using decision trees)
- At each step  $\hat{h}_n(x)$  is trained to predict the residual error,  $\Delta_{n-1} = y C_{n-1}(x)$ , (i.e. the target minus the current prediction)
- (This difference looks a bit like a gradient hence the rather confusing name)

Adam Prügel-Bennett

COMP6208 Advanced Machine Learning

## Keep On Going

#### • We can keep on going



• But we will over-fit eventually

Adam Prügel-Bennett COMP6208 Advanced Machine Learning

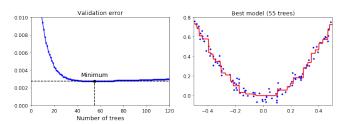
### XGBoost

- XGBoost is an implementation of gradient boosting that won the Higg's Boson challenge and regularly wins Kaggle competitions
- XGBoost stands for eXtreme Gradient Boosting
- It was much faster than most gradient boosting algorithms and scales to billions of training data points—although GBM is often better!
- It uses a cleverly chosen regularisation term to favour simple trees
- Finds a clever way to approximately minimise error plus regulariser very fast
- Rather a bodge of optimisation hacks

dam Prügel-Bennett COMP6208 Advanced Machine Learning

### **Early Stopping**

• Like many algorithms we often get better results by early stopping



 Use cross-validation against a validation set to decide when to stop!

Adam Prügel-Bennett COMP6208 Advanced Machine Learning 18

#### Conclusion

- Ensemble methods have proved themselves to be very powerful
- Tend to work best with very simple models (true of random forest and boosting)
   —seems to reduce over-fitting
- XGBoost or GBM are currently the best methods for tabular data (particular for large training sets)
   probably
- For images, signal and speech deep learning can give very significant advantage
- Probabilistic models can be better if you have a good model

Adam Prügel-Bennett COMP6208 Advanced Machine Learning 20