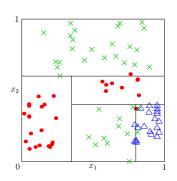
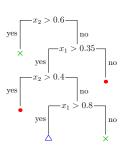
Advanced Machine Learning

Boosting





Boosting, AdaBoost, Gradient Boosting

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Boosting

 In boosting we make a strong learner by using a weighted sum of weak learners

$$C_n(\boldsymbol{x}) = \sum_{i=1}^n \alpha_i \hat{h}_i(\boldsymbol{x})$$

- ullet Weak learners, $\hat{h}_i(x)$, are learning machine that do a little better than chancel
- The trick is to choose the weights, α_i
- Because the weak learners do little better than chance we (miraculously) don't overfit that much

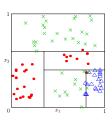
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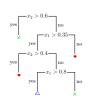
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Outline

- 1. Boosting
- 2. AdaBoost
- 3. Gradient Boosting
- 4. Dropout





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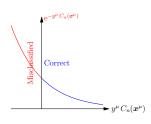
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AdaBoost

- AdaBoost is a classic solution to this problem
- It assigns an "loss function"

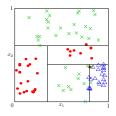


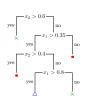


 This punishes examples where there is an errors more than correct classifications

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Shallow Trees

- One of the most effective type of weak learner are very shallow trees
- Sometimes we just use one variable (the stump) although usually we would use slightly deeper trees
- There are different algorithms for choosing the weights
 - ★ adaboost—a classic algorithm for binary classification
 - * gradient boosting—used for regression, trains a weak learner on the residual errors

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Boosting a Binary Classifier

- Suppose we have a binary classification task with data $\mathcal{D}=\{(x^\mu,y^\mu)|\mu=1,2,...,m\}$ with $y^\mu\in\{-1,1\}$
- Our i^{th} weak learner provides a prediction $\hat{h}_i({m x}^\mu) \in \{-1,1\}$
- We ask, can we find a linear combination

$$C_n(\mathbf{x}) = \alpha_1 \hat{h}_1(\mathbf{x}) + \alpha_2 \hat{h}_2(\mathbf{x}) + \dots + \alpha_n \hat{h}_n(\mathbf{x})$$

- So that $\operatorname{sgn} (C_n(x))$ is a strong learner?
- Note we want $y^{\mu}C_n(x^{\mu})>0$

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Iterative Learning

• We build up a strong learner iteratively (greedily)

$$C_n(\boldsymbol{x}) = C_{n-1}(\boldsymbol{x}) + \alpha_n \hat{h}_n(\boldsymbol{x})$$

 \bullet Defining $w_1^\mu=1$ and $w_n^\mu=\mathrm{e}^{-y^\mu C_{n-1}(\boldsymbol{x}^\mu)}$ then

$$\begin{split} L_n(\alpha_n) &= \sum_{\mu=1}^m \mathrm{e}^{-y^\mu C_n(\mathbf{x}^\mu)} \mathbf{I} = \sum_{\mu=1}^m \mathrm{e}^{-y^\mu (C_{n-1}(\mathbf{x}^\mu) + \alpha_n \hat{h}_n(\mathbf{x}^\mu))} \mathbf{I} \\ &= \sum_{\mu=1}^m w_n^\mu \mathrm{e}^{-\alpha_n y^\mu \hat{h}_n(\mathbf{x}^\mu)} \mathbf{I} = \mathbf{e}^{\alpha_n} \sum_{\mu: y^\mu \neq \hat{h}_n(\mathbf{x}^\mu)} w_n^\mu \mathbf{e}^{\alpha_n} \mathbf{I} + \mathbf{e} \mathbf{I}^{\alpha_n} \sum_{\mu: y^\mu = \hat{h}_n(\mathbf{x}^\mu)} w_n^\mu \mathbf{e}^{-\alpha_n} \mathbf{I} \\ &= \mathrm{e}^{-\alpha_n} \sum_{\mu=1}^m w_n^\mu + (\mathrm{e}^{\alpha_n} - \mathrm{e}^{-\alpha_n}) \sum_{\mu: y^\mu \neq \hat{h}_n(\mathbf{x}^\mu)} w_n^\mu \mathbf{I} \end{split}$$

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Choosing a Weak Classifier

• To minimise the loss

$$L_n(\alpha_n) = e^{-\alpha_n} \sum_{\mu=1}^m w_n^{\mu} + (e^{\alpha_n} - e^{-\alpha_n}) \sum_{\mu: y^{\mu} \neq \hat{h}_n(\boldsymbol{x}^{\mu})} w_n^{\mu}$$

• We choose the weak learner with the lowest value of

$$\sum_{\mu:y^{\mu}\neq \hat{h}_{n}(\boldsymbol{x}^{\mu})} w_{n}^{\mu} = \sum_{\mu:y^{\mu}\neq \hat{h}_{n}(\boldsymbol{x}^{\mu})} \mathrm{e}^{-y^{\mu}C_{n-1}(\boldsymbol{x}^{\mu})} \mathrm{Correct}$$

• That is, it misclassifies only where the other learners classify well

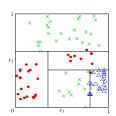
Algorithm

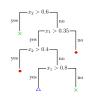
- 1. Start with a set of weak learners \mathcal{W}
- 2. Associate a weight, w_n^μ , with every data point $({m x}^\mu,y^\mu)$, $\mu=1,2,\ldots,m$
- 3. Initially $w_1^{\mu} = 1$ (large weight, w_n^{μ} , means (x^{μ}, y^{μ}) is poorly classified)
- 4. Choose the weak learning, $\hat{h}_n(x)\in\mathcal{W}$, that minimises $\sum\limits_{\mu:y^\mu\neq\hat{h}_n(x^\mu)}w_n^\mu$
- 5. Update predictor $C_n(x) = C_{n-1}(x) + \alpha_n \hat{h}_n(x)$ where $\int_{-\infty}^{\infty} \sum_{n=0}^{\infty} w_n^{\mu}$
- 6. Update $w_{n+1}^\mu=w_n^\mu \mathrm{e}^{-y^\mu \alpha_n \hat{h}_n(\boldsymbol{x}^\mu)}$
- 7. Go to 4

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Outline

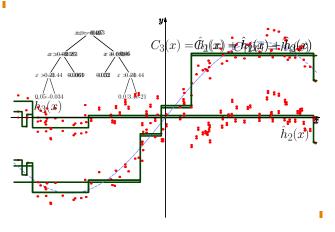
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Fitting a Sin Wave



Choosing Weights

• We now choose the weight α_n to minimise the loss $L_n(\alpha_n)$

• That is

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Performance

- · Adaboost works well with weak learners, usually out-performing bagging
- It doesn't work well with strong learners (tends to over-fit)
- It is limited to binary classification (there are generalisation, but they are difficult to get to work)
- It has fallen from fashion
- In contrast gradient boosting used for regression is very popular

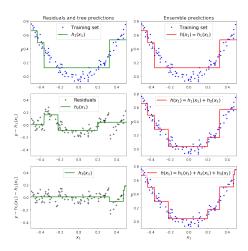
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Gradient Boosting

• In gradient boosting we again build a strong learner as a linear combination of weak learners

$$C_n(\boldsymbol{x}) = C_{n-1}(\boldsymbol{x}) + \hat{h}_n(\boldsymbol{x})$$

- Gradient boosting used on regression (again using decision trees)
- At each step $\hat{h}_n(x)$ is trained to predict the **residual error**, $\Delta_{n-1} = y - C_{n-1}(\boldsymbol{x})$, (i.e. the target minus the current prediction)
- (This difference looks a bit like a gradient hence the rather confusing name)

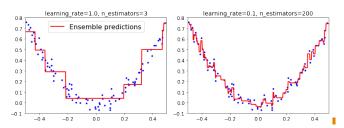


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Keep On Going

• We can keep on going



• But we will over-fit eventually

XGBoost

- XGBoost is an implementation of gradient boosting that won the Higg's Boson challenge and regularly wins Kaggle competitions
- XGBoost stands for eXtreme Gradient Boosting
- It uses a cleverly chosen regularisation term to favour simple trees
- Finds a clever way to approximately minimise error plus regulariser very fast
- Rather a bodge of optimisation hacks
- It was much faster than most gradient boosting algorithms and scales to billions of training data points—although GBM is often better

Ensembling in Deep Learning

- For most machine learning ensembling different machines usually gives a reasonable improvement in performance
- The machines should have roughly the same performance
- Of course, this comes at the price of having to train multiple machines
- One can try to train a machine to decide how to combine different machines (stacking) but beware, it is very easy to overfit
- Usually better to average predictions for regression or do majority voting for classification problems

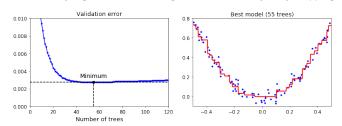
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Conclusion

- Ensemble methods have proved themselves to be very powerful
- Tend to work best with very simple models (true of random forest and boosting) - seems to reduce over-fitting
- XGBoost or GBM are currently the best methods for tabular data (particular for large training sets) probably p
- For images, signal and speech deep learning can give very significant advantage
- Probabilistic models can be better if you have a good model

Early Stopping

• Like many algorithms we often get better results by early stopping

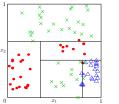


• Use cross-validation against a validation set to decide when to stop

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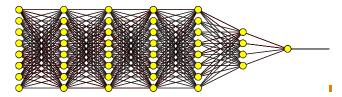




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Dropout

• For deep learning we can control for over-fitting using dropout



• This can be seen as ensembling lots of much simpler machines

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