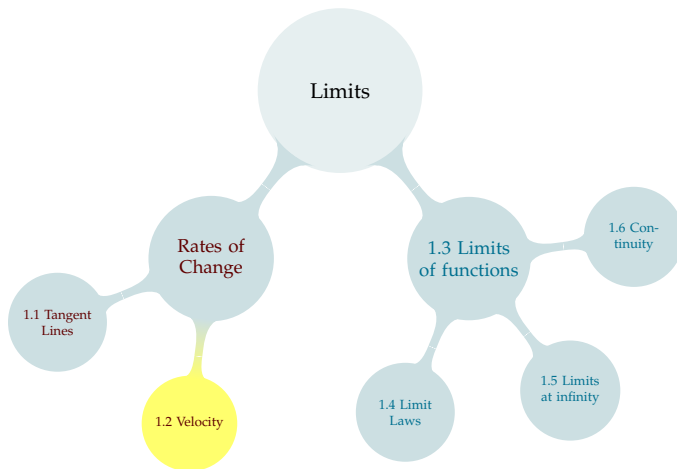
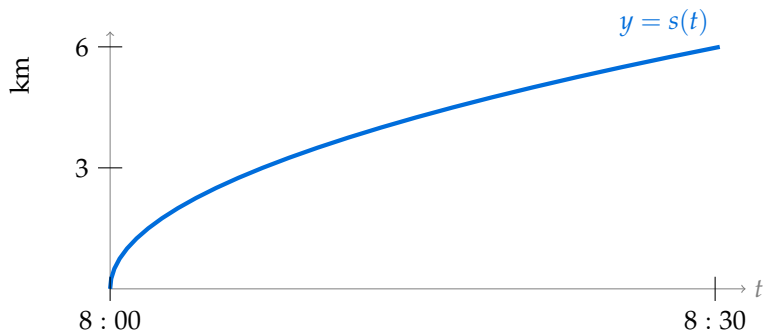
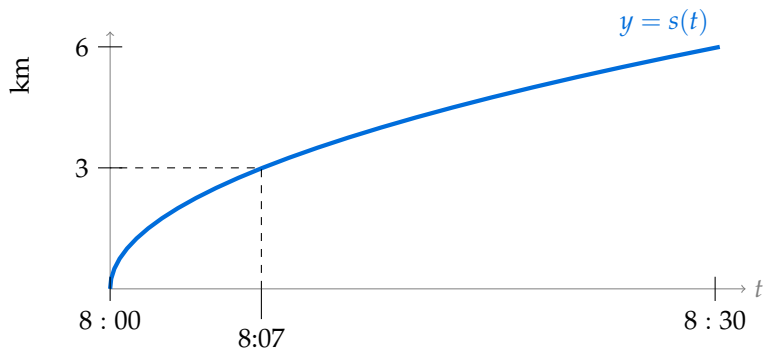
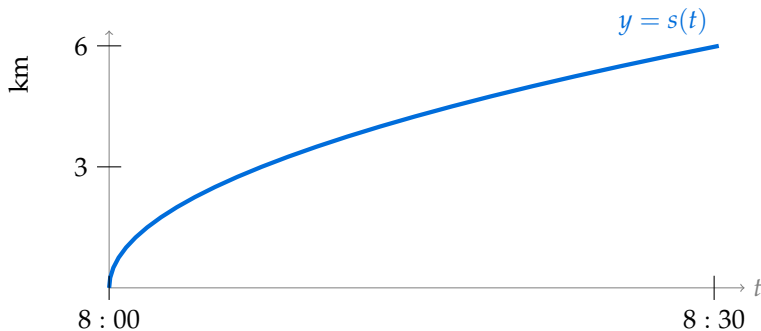


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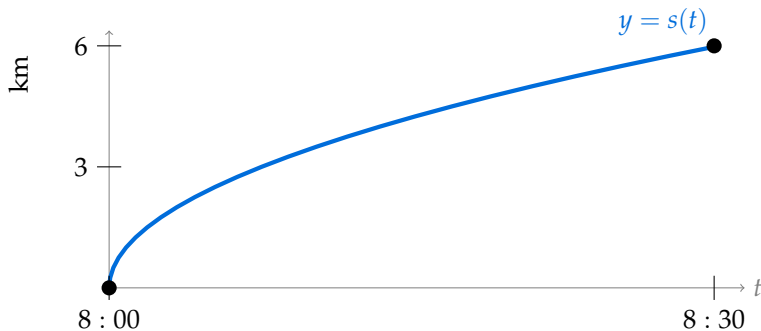






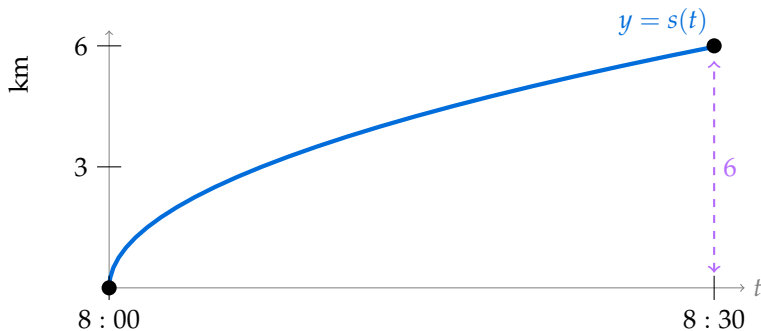
It took $\frac{1}{2}$ hour to bike 6 km. 12 kph represents the:

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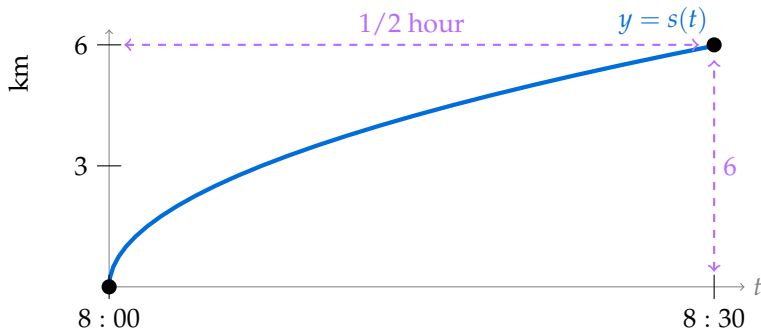
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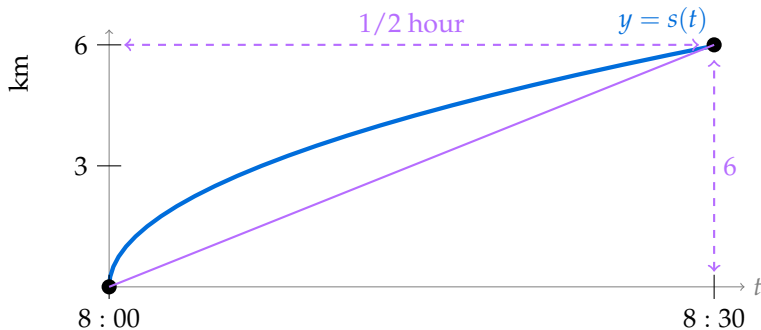
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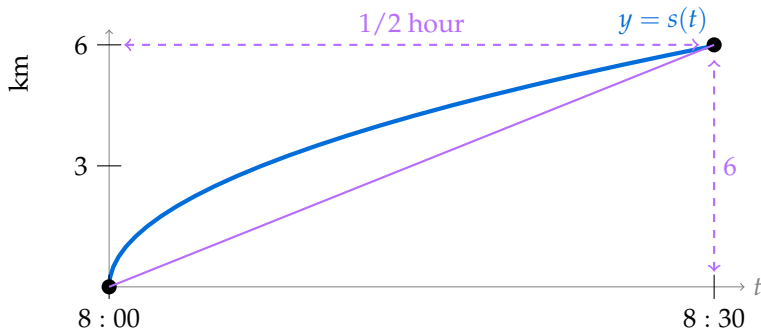
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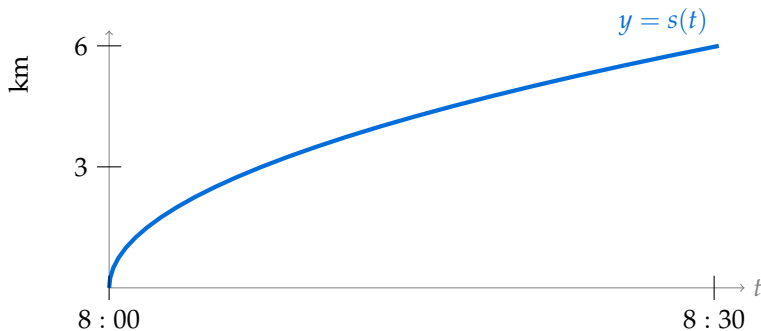
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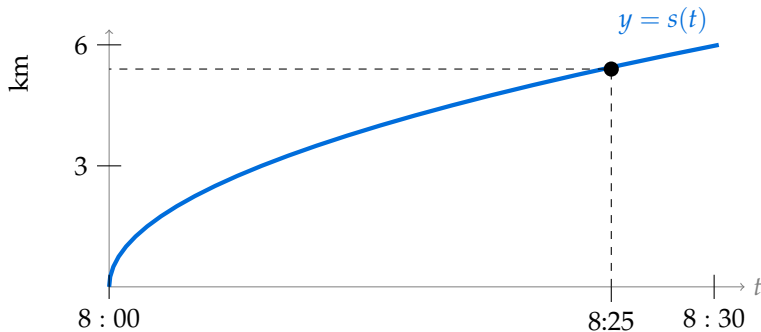
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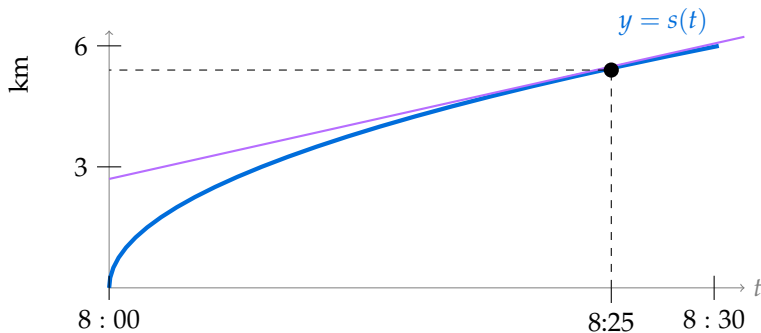
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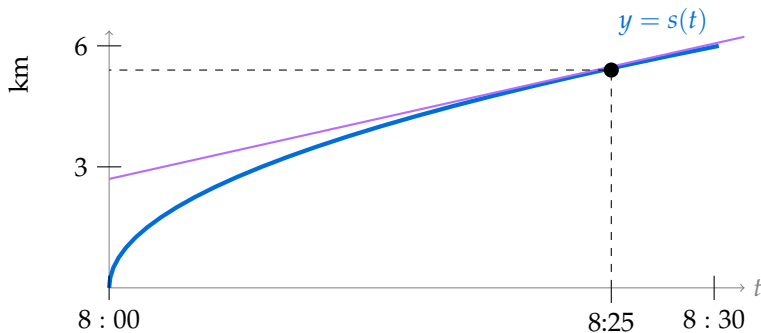
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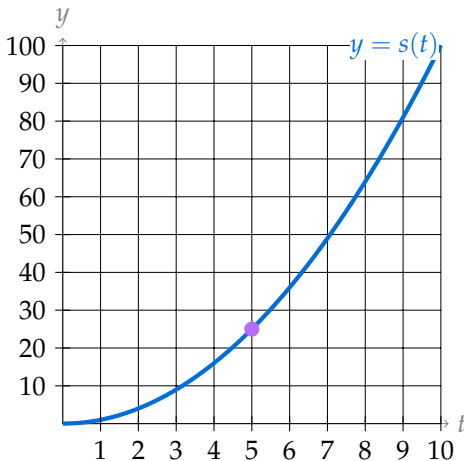


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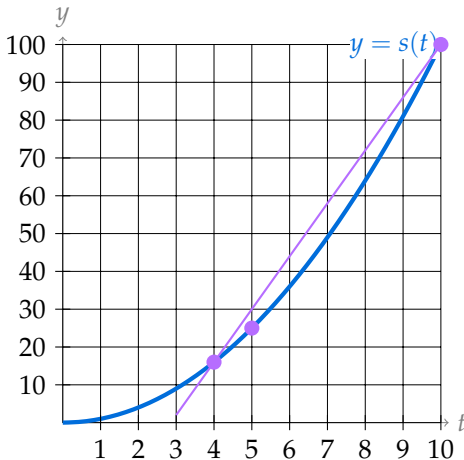
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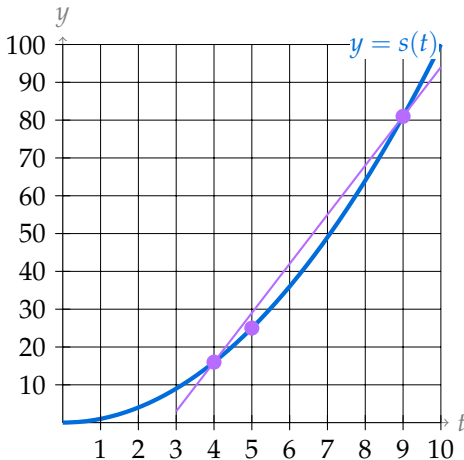
One way:
Estimate the
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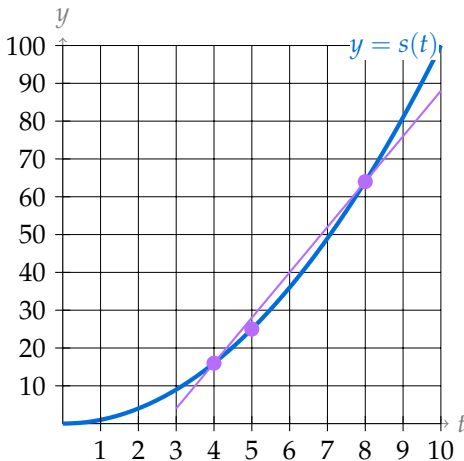
Another way:
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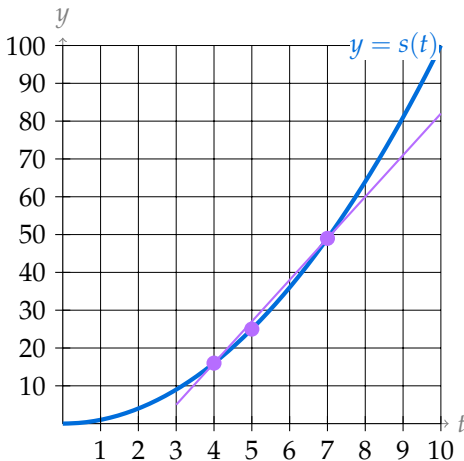
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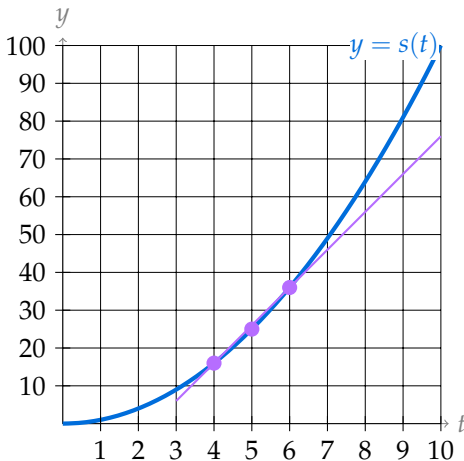
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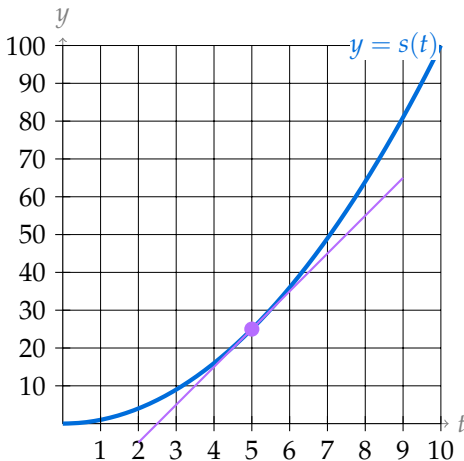
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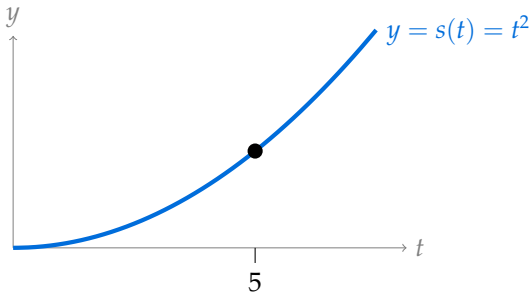
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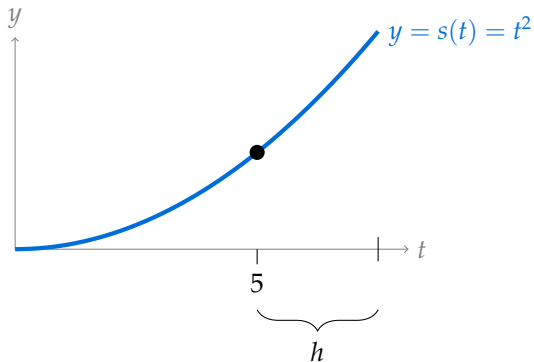


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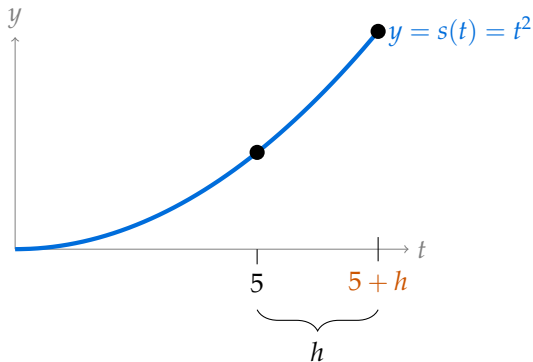
Let's look for an algebraic way of determining the velocity of the balloon when $t = 5$.



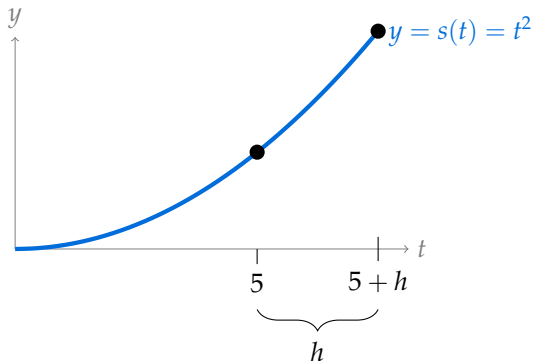
Suppose the interval $[5, \]$ has length h . What is the right endpoint of the interval?



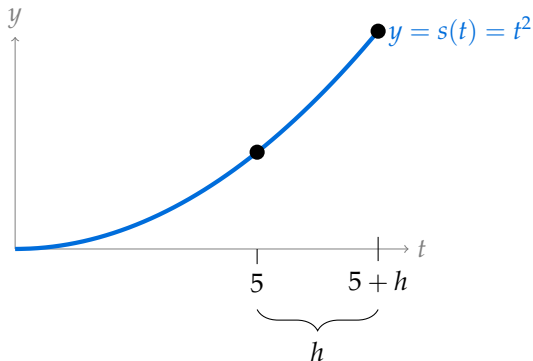
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Write the equation for the average (vertical) velocity from $t = 5$ to $t = 5 + h$.

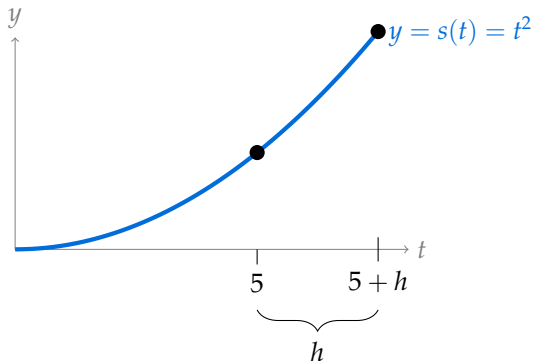


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$$\text{vel} = \frac{\Delta \text{ height}}{\Delta \text{ time}} = \frac{s(5+h) - s(5)}{(5+h) - 5} = \frac{(5+h)^2 - 5^2}{h}$$

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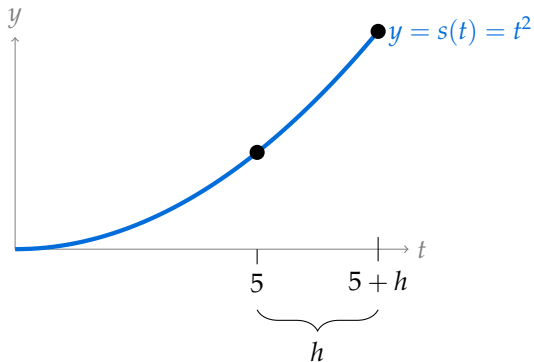
$$\begin{aligned}\text{vel} &= \frac{\Delta \text{ height}}{\Delta \text{ time}} = \frac{s(5+h) - s(5)}{(5+h) - 5} = \frac{(5+h)^2 - 5^2}{h} \\ &= 10 + h \text{ when } h \neq 0\end{aligned}$$

When h is very small,

$$\approx 10$$



What do you think is the slope of the tangent line to the graph when $t = 5$?



OUR FIRST LIMIT

Average Velocity, $t = 5$ to $t = 5 + h$:

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It means: As h gets extremely close to 0, $(10 + h)$ gets extremely close to 10.

Included Work



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