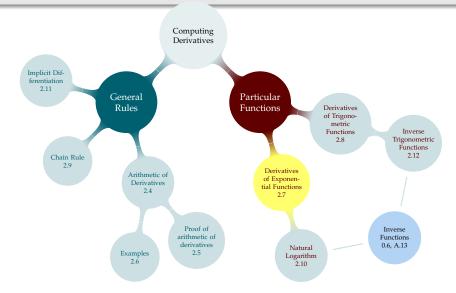
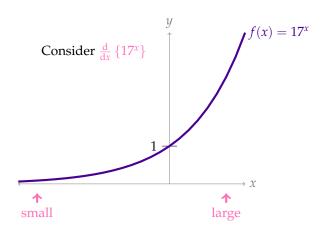
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f(x) is always increasing, so f'(x) is always positive. f'(x) might look similar to f(x).

$$\frac{\mathrm{d}}{\mathrm{d}x}\{17^x\} =$$

$$\frac{\mathrm{d}}{\mathrm{d}x}\{17^x\} = 17^x \cdot \underbrace{\lim_{h \to 0} \frac{(17^h - 1)}{h}}_{\text{constant}}$$

Given what you know about $\frac{d}{dx}\{17^x\}$, is it possible that

$$\lim_{h \to 0} \frac{17^h - 1}{h} = 0?$$

- A. Sure, there's no reason we've seen that would make it impossible.
- B. No, it couldn't be 0, that wouldn't make sense.
- C. I do not feel equipped to answer this question.

Given what you know about $\frac{d}{dr}\{17^a\}$, is it possible that $\lim_{h\to 0} \frac{17^h - 1}{h} = 0$?

- A. Sure, there's no reason we've seen that would make it
- B. No, it couldn't be 0, that wouldn't make sense.
 C. I do not feel equipped to answer this question.

The second question is there as a second chance for students who missed the first one

$$\frac{\mathrm{d}}{\mathrm{d}x}\{17^x\} = 17^x \cdot \underbrace{\lim_{h \to 0} \frac{(17^h - 1)}{h}}_{\text{constant}}$$

Given what you know about $\frac{d}{dx}\{17^x\}$, is it possible that

$$\lim_{h \to 0} \frac{17^h - 1}{h} = \infty?$$

- A. Sure, there's no reason we've seen that would make it impossible.
- B. No, it couldn't be ∞ , that wouldn't make sense.
- C. I do not feel equipped to answer this question.

2.7: Derivs of Exponential Functions

 $\frac{d}{dv}\{17^a\} = 17^a \cdot \underbrace{\lim_{k \to 0} \frac{(17^k - 1)}{k}}_{constant}$

Given what you know about $\frac{d}{ds}\{17^a\}$, is it possible that $\lim_{k\to 0} \frac{12^k-1}{k} = \infty$?

- A. Sure, there's no reason we've seen that would make it
- B. No, it couldn't be ∞, that wouldn't make sense
 C. I do not feel equipped to answer this question.

The second question is there as a second chance for students who missed the first one

$$\frac{\mathrm{d}}{\mathrm{d}x}\{17^x\} = 17^x \cdot \underbrace{\lim_{h \to 0} \frac{(17^h - 1)}{h}}_{\text{constant}}$$

h	$\left \begin{array}{c} 17^h - 1 \\ h \end{array} \right $
0.001	2.83723068608
0.00001	2.83325347992
0.0000001	2.83321374583
0.000000001	2.83321344163

2.7: Derivs of Exponential Functions

	$\frac{d}{dx}\{17^a\} = 17^a \cdot \underline{b}$
h	$\frac{17^{6}-1}{h}$
0.001	2.83723068608
0.00001	2.83325347992
0.0000001	2.83321374583
0.0000000001	2.83321344163

"It's not clear what constant this is, but it is a constant."

$$\frac{d}{dx} \{17^x\} = \lim_{h \to 0} \frac{17^{x+h} - 17^x}{h}$$

$$= \lim_{h \to 0} \frac{17^x 17^h - 17^x}{h}$$

$$= \lim_{h \to 0} \frac{17^x (17^h - 1)}{h}$$

$$= 17^x \lim_{h \to 0} \frac{(17^h - 1)}{h}$$

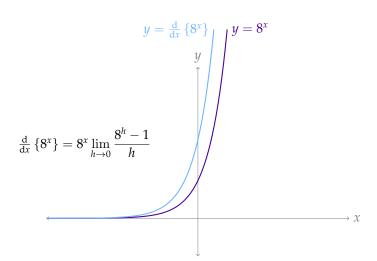
In general, for any positive number *a*,

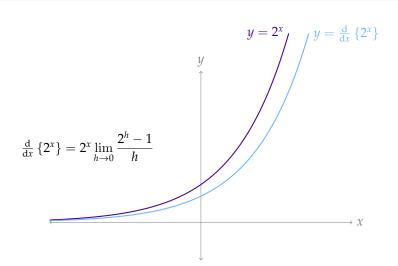
$$\frac{\mathrm{d}}{\mathrm{d}x}\{a^x\} = a^x \lim_{h \to 0} \frac{a^h - 1}{h}$$

2.7: Derivs of Exponential Functions

$$\begin{split} \frac{\mathrm{d}}{\mathrm{d}t}\{17^2\} &= \lim_{t \to \infty} \frac{12^{-tk} - 17^t}{12^t} \\ &= \lim_{t \to \infty} \frac{12^{-12^t} - 17^t}{12^t} \\ &= \lim_{t \to \infty} \frac{12^{-12^t} - 17^t}{12^t} \\ &= 17^t \lim_{t \to \infty} \frac{12^t (17^t - 1)}{12^t} \\ &= 17^t \lim_{t \to \infty} \frac{12^t (17^t - 1)}{12^t} \\ &\leq \frac{\mathrm{d}}{\mathrm{d}t}\{d^2\} = d^t \lim_{t \to \infty} \frac{d^2 - 1}{h} \end{split}$$

Point out that 17 could have been replaced with any other number. Go through and cross out 17, write in a.





In general, for any positive number a, $\frac{d}{dx}\{a^x\} = a^x \lim_{h \to 0} \frac{a^h - 1}{h}$

Euler's Number – Theorem 2.7.4

We define *e* to be the unique number satisfying

$$\lim_{h \to 0} \frac{e^h - 1}{h} = 1$$

 $e \approx 2.7182818284590452353602874713526624...$ (Wikipedia)

Theorem 2.7.4 and Corollary 2.10.6

Using this definition of *e*,

$$\frac{\mathrm{d}}{\mathrm{d}x}\left\{e^x\right\} = e^x \underbrace{\lim_{h \to 0} \frac{e^h - 1}{h}}_{1} = e^x$$

In general, $\lim_{h\to 0} \frac{a^h-1}{h} = \log_e(a)$, so $\frac{d}{dx}\{a^x\} = a^x \log_e(a)$

That
$$\lim_{h\to 0} \frac{a^h-1}{h} = \log_e(a)$$
 and $\frac{d}{dx}\{a^x\} = a^x \log_e(a)$ are consequences of $a^x = \left(e^{\log_e(a)}\right)^x = e^{x \log_e(a)}$

For the details, see the end of Section 2.7.

Things to Have Memorized

$$\frac{\mathrm{d}}{\mathrm{d}x}\left\{e^x\right\} = e^x$$

When *a* is any constant,

$$\frac{\mathrm{d}}{\mathrm{d}x}\left\{a^{x}\right\} = a^{x}\log_{e}(a)$$

Let $f(x) = \frac{e^x}{3x^5}$. When is the tangent line to f(x) horizontal?

Evaluate $\frac{d}{dx} \left\{ e^{3x} \right\}$

2 ways: product rule with $e^x \cdot e^x \cdot e^x$, or previous rule with $(e^3)^x$

Suppose the deficit, in millions, of a fictitious country is given by

$$f(x) = e^x (4x^3 - 12x^2 + 14x - 4)$$

where *x* is the number of years since the current leader took office. Suppose the leader has been in power for exactly two years.

1. Is the deficit increasing or decreasing?

2. Is the rate at which the deficit is growing increasing or decreasing?