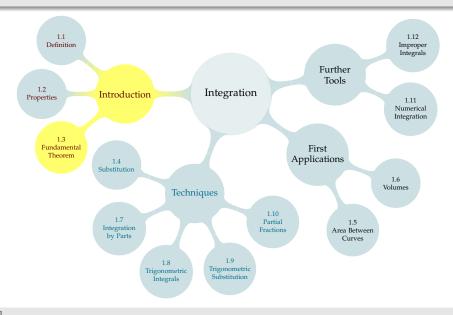
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Methods for finding the area under a curve.

► Limit of a Riemann Sum



- ► Limit of a Riemann Sum
 - ► Conceptually easy cut into rectangles





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Methods for finding the area under a curve.

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► Use Geometry



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$$\lim_{n \to \infty} \sum_{i=1}^{n} f(x_i^*) \Delta x; \quad \sum_{i=1}^{n} i = \frac{n(n+1)}{2}$$

- ▶ Use Geometry
 - Computationally nice when it's available! (Circles, triangles, symmetry, etc.)



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Methods for finding the area under a curve.

- ► Limit of a Riemann Sum
 - Conceptually easy cut into rectangles
 - ► Computationally rough



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► Up next: Fundamental Theorem of Calculus

- ▶ Limit of a Riemann Sum
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- ► Use Geometry
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- ► Up next: Fundamental Theorem of Calculus
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- ► Up next: Fundamental Theorem of Calculus
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 - ► Computationally generally nicer than Riemann sums
 - ► Doesn't work for every function

Fundamental Theorem of Calculus, Part 1

Let a < b and let f(x) be a function which is defined and continuous on [a,b]. Let

$$A(x) = \int_{a}^{x} f(t) \, \mathrm{d}t$$

for any x in [a, b]. Then the function A(x) is differentiable and

$$A'(x) = f(x) .$$

Fundamental Theorem of Calculus, Part 1

Let a < b and let f(x) be a function which is defined and continuous on [a,b]. Let

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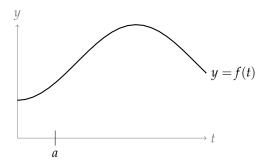
for any x in [a, b]. Then the function A(x) is differentiable and

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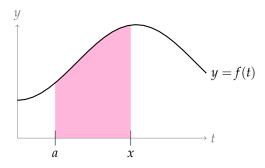
FTC(I) gives us the derivative of a very specific function (subject to some fine print).

It shows a close relationship between integrals and derivatives.

Area Function: $A(x) = \int_a^x f(t) dt$ for $a \le x \le b$

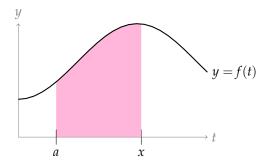


Area Function: $A(x) = \int_a^x f(t) dt$ for $a \le x \le b$

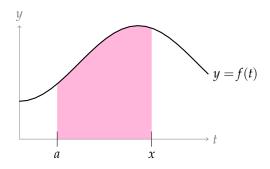




Area Function: $A(x) = \int_a^x f(t) dt$ for $a \le x \le b$

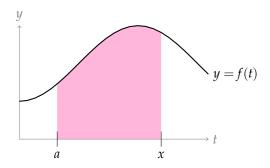






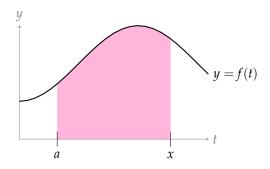
Notation: the function A depends on the variable x.





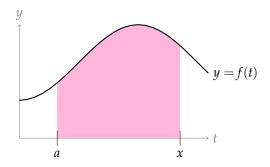
Notation: the function *A* depends on the variable *x*.





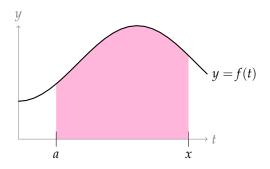
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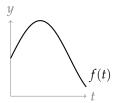
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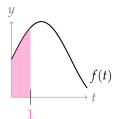
Notation: the function *A* depends on the variable *x*.

$$A(x) = \int_0^x f(t) dt \qquad B(x) = \int_0^x f(x) dt \qquad C(x) = \int_0^x f(x) dx$$

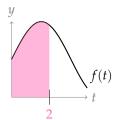




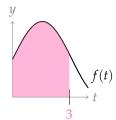
$$A(x) = \int_0^x f(t) dt \qquad B(x) = \int_0^x f(x) dt \qquad C(x) = \int_0^x f(x) dx$$
$$A(1) = \int_0^1 f(t) dt$$



$$A(x) = \int_0^x f(t) dt \qquad B(x) = \int_0^x f(x) dt \qquad C(x) = \int_0^x f(x) dx$$
$$A(2) = \int_0^2 f(t) dt$$



$$A(x) = \int_0^x f(t) dt \qquad B(x) = \int_0^x f(x) dt \qquad C(x) = \int_0^x f(x) dx$$
$$A(3) = \int_0^3 f(t) dt$$



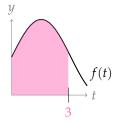


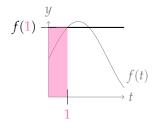
$$A(x) = \int_0^x f(t) dt \qquad B(x) = \int_0^x f(x) dt \qquad C(x) = \int_0^x f(x) dx$$

$$A(3) = \int_0^3 f(t) \, \mathrm{d}t$$

$$B(\mathbf{x}) = \int_{0}^{x} f(\mathbf{x}) \, \mathrm{d}t$$

$$A(3) = \int_0^3 f(t) dt$$
 $B(1) = \int_0^1 f(1) dt$





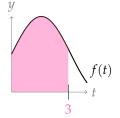


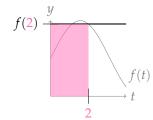
$$A(x) = \int_0^x f(t) \, \mathrm{d}t$$

$$A(3) = \int_{0}^{3} f(t) dt$$

$$A(x) = \int_0^x f(t) dt \qquad B(x) = \int_0^x f(x) dt \qquad C(x) = \int_0^x f(x) dx$$

$$A(3) = \int_0^3 f(t) dt$$
 $B(2) = \int_0^2 f(2) dt$





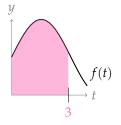


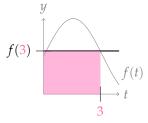
$$A(x) = \int_0^x f(t) dt \qquad B(x) = \int_0^x f(x) dt \qquad C(x) = \int_0^x f(x) dx$$

$$A(3) = \int_0^3 f(t) \, \mathrm{d}t$$

$$B(x) = \int_0^x f(x) \, \mathrm{d}t$$

$$A(3) = \int_0^3 f(t) dt$$
 $B(3) = \int_0^3 f(3) dt$







$$A(x) = \int_0^x f(t) \, \mathrm{d}t$$

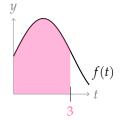
$$A(3) = \int_{0}^{3} f(t) \, \mathrm{d}t$$

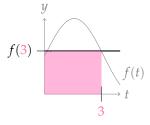
$$B(x) = \int_0^x f(x) \, \mathrm{d}t$$

$$B(3) = \int_0^3 f(3) \, \mathrm{d}t$$

$$A(x) = \int_0^x f(t) dt \qquad B(x) = \int_0^x f(x) dt \qquad C(x) = \int_0^x f(x) dx$$

$$A(3) = \int_0^3 f(t) dt$$
 $B(3) = \int_0^3 f(3) dt$ $C(1) = \int_0^1 f(1) \underbrace{d1}_{22}$





Fundamental Theorem of Calculus, Part 1

Let a < b and let f(x) be a function which is defined and continuous on [a,b]. Let

$$A(x) = \int_{a}^{x} f(t) \, \mathrm{d}t$$

for any x in [a, b]. Then the function A(x) is differentiable and

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Fundamental Theorem of Calculus, Part 1

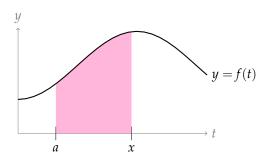
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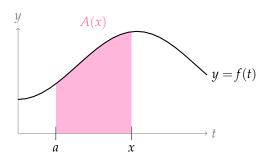
$$A'(x) = f(x) .$$

Question: Why is it true?



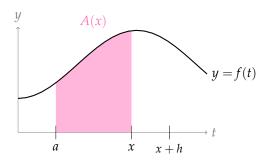
$$A'(x) = \lim_{\Delta x \to 0} \frac{\Delta A}{\Delta x} = \lim_{h \to 0} \frac{A(x+h) - A(x)}{h}$$





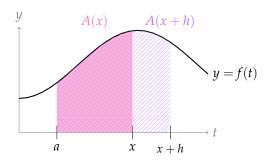
$$A'(x) = \lim_{\Delta x \to 0} \frac{\Delta A}{\Delta x} = \lim_{h \to 0} \frac{A(x+h) - A(x)}{h}$$





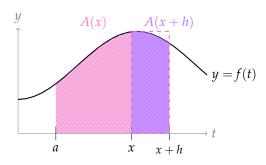
$$A'(x) = \lim_{\Delta x \to 0} \frac{\Delta A}{\Delta x} = \lim_{h \to 0} \frac{A(x+h) - A(x)}{h}$$





$$A'(x) = \lim_{\Delta x \to 0} \frac{\Delta A}{\Delta x} = \lim_{h \to 0} \frac{A(x+h) - A(x)}{h}$$

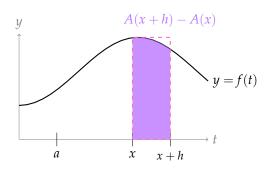




$$A'(x) = \lim_{\Delta x \to 0} \frac{\Delta A}{\Delta x} = \lim_{h \to 0} \frac{A(x+h) - A(x)}{h}$$



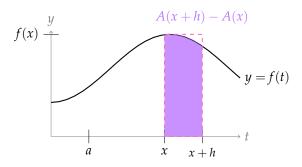
Derivative of Area Function, $A(x) = \int_a^x f(t) dt$



$$A'(x) = \lim_{\Delta x \to 0} \frac{\Delta A}{\Delta x} = \lim_{h \to 0} \frac{A(x+h) - A(x)}{h}$$



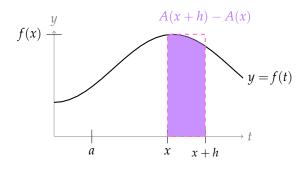
DERIVATIVE OF AREA FUNCTION, $A(x) = \int_a^x f(t) dt$



$$A'(x) = \lim_{\Delta x \to 0} \frac{\Delta A}{\Delta x} = \lim_{h \to 0} \frac{A(x+h) - A(x)}{h} = \lim_{h \to 0} \frac{hf(x)}{h}$$



DERIVATIVE OF AREA FUNCTION, $A(x) = \int_a^x f(t) dt$



$$A'(x) = \lim_{\Delta x \to 0} \frac{\Delta A}{\Delta x} = \lim_{h \to 0} \frac{A(x+h) - A(x)}{h} = \lim_{h \to 0} \frac{hf(x)}{h} = f(x)$$

When h is very small, the purple area looks like a rectangle with base h and height f(x), so $A(x+h)-A(x)\approx hf(x)$ and $\frac{A(x+h)-A(x)}{h}\approx f(x)$. As h tends to zero, the error in this approximation approaches 0.

Let a < b and let f(x) be a function which is defined and continuous on [a,b]. Let

$$A(x) = \int_{a}^{x} f(t) \, \mathrm{d}t$$

for any x in [a, b]. Then the function A(x) is differentiable and

$$A'(x) = f(x) .$$

Suppose $A(x) = \int_2^x \sin t \, dt$. What is A'(x)?

Let a < b and let f(x) be a function which is defined and continuous on [a,b]. Let

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for any x in [a, b]. Then the function A(x) is differentiable and

$$A'(x) = f(x) .$$

Suppose $A(x) = \int_2^x \sin t \, dt$. What is A'(x)?

Suppose
$$B(x) = \int_{x}^{2} \sin t \, dt$$
. What is $B'(x)$?



Let a < b and let f(x) be a function which is defined and continuous on [a,b]. Let

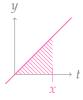
$$A(x) = \int_{a}^{x} f(t) \, \mathrm{d}t$$

for any x in [a, b]. Then the function A(x) is differentiable and

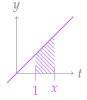
$$A'(x) = f(x) .$$

Suppose $C(x) = \int_2^{e^x} \sin t \, dt$. What is C'(x)?

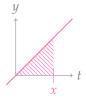
$$A(x) = \int_0^x 2t \, dt$$



$$B(x) = \int_1^x 2t \, dt$$

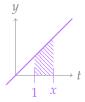


$$A(x) = \int_0^x 2t \, \mathrm{d}t$$

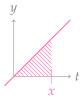


$$A'(x) = 2x$$

$$B(x) = \int_1^x 2t \, dt$$

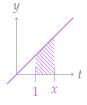


$$A(x) = \int_0^x 2t \, \mathrm{d}t$$



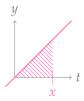
A'(x) = 2x

$$B(x) = \int_1^x 2t \, dt$$



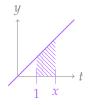
$$B'(x) = 2x$$

$$A(x) = \int_0^x 2t \, dt = x^2$$



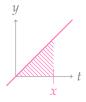
$$A'(x) = 2x$$

$$B(x) = \int_1^x 2t \, dt$$



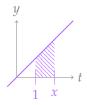
$$B'(x) = 2x$$

$$A(x) = \int_0^x 2t \, \mathrm{d}t = x^2$$



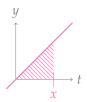
$$A'(x) = 2x$$

$$B(x) = \int_{1}^{x} 2t \, dt = x^{2} - 1$$



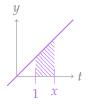
$$B'(x) = 2x$$

$$A(x) = \int_0^x 2t \, dt = x^2$$



A'(x) = 2x

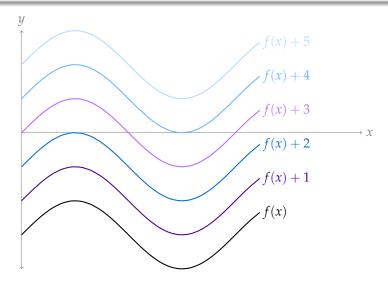
$$B(x) = \int_1^x 2t \, dt = x^2 - 1$$



$$B'(x) = 2x$$

When two functions have the same derivative, they differ only by a constant.

In this example: B(x) = A(x) - 1



If two continuous functions have the same derivative, then one is a constant plus the other.

$$If A(x) = \int_a^x f(t) dt, then^1 A'(x) = f(x)$$

 $^{^{1}}$ (as long as f(t) is continuous on [a, x])

$$If A(x) = \int_{a}^{x} f(t) dt, then^{1} A'(x) = f(x)$$

$$A(x) = \int_{a}^{x} e^{t} dt$$
. What functions could $A(x)$ be?

¹(as long as f(t) is continuous on [a, x])

$$If A(x) = \int_{a}^{x} f(t) dt, then^{1} A'(x) = f(x)$$

$$A(x) = \int_{a}^{x} \cos t \, dt$$
. What functions could $A(x)$ be?



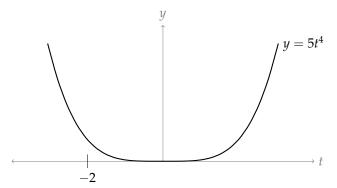
¹(as long as f(t) is continuous on [a, x])

$$If A(x) = \int_{a}^{x} f(t) dt, then^{1} A'(x) = f(x)$$

$$A(x) = \int_{-2}^{x} 5t^4 dt$$
. What functions could $A(x)$ be?

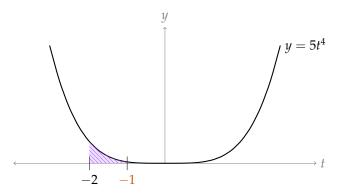
¹(as long as f(t) is continuous on [a, x])

$$A(x) = \int_{-2}^{x} 5t^4 dt = x^5 + 32$$





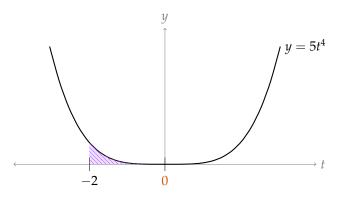
$$A(x) = \int_{-2}^{x} 5t^4 dt = x^5 + 32$$



$$A(-1) = \int_{-2}^{-1} 5t^4 dt = (-1)^5 + 32 = 31$$



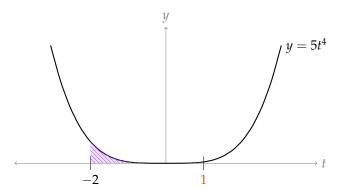
$$A(x) = \int_{-2}^{x} 5t^4 dt = x^5 + 32$$



$$A(0) = \int_{-2}^{0} 5t^4 dt = (0)^5 + 32 = 32$$



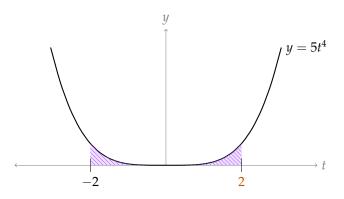
$$A(x) = \int_{-2}^{x} 5t^4 dt = x^5 + 32$$



$$A(1) = \int_{-2}^{1} 5t^4 dt = (1)^5 + 32 = 33$$



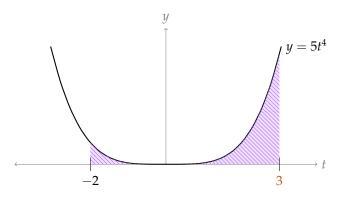
$$A(x) = \int_{-2}^{x} 5t^4 dt = x^5 + 32$$



$$A(2) = \int_{-2}^{2} 5t^4 dt = (2)^5 + 32 = 64$$



$$A(x) = \int_{-2}^{x} 5t^4 dt = x^5 + 32$$



$$A(3) = \int_{-2}^{3} 5t^4 dt = (3)^5 + 32 = 275$$

$$If A(x) = \int_{a}^{x} f(t) dt, then^{1} A'(x) = f(x)$$

$$A(x) = \int_{a}^{x} f(t) dt$$
. What functions could $A(x)$ be?



¹(as long as f(t) is continuous on [a, x])

$$If A(x) = \int_a^x f(t) dt, then^1 A'(x) = f(x)$$

$$A(x) = \int_{a}^{x} f(t) dt$$
. What functions could $A(x)$ be?

- ightharpoonup A'(x) = f(x).
- ▶ Guess a function with derivative f(x): F(x).
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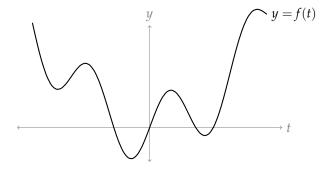
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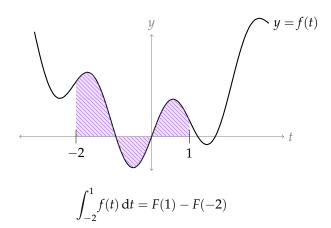
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$$\int_{a}^{b} f(t) dt = F(b) - F(a) \quad \text{where} \quad F'(x) = f(x)$$



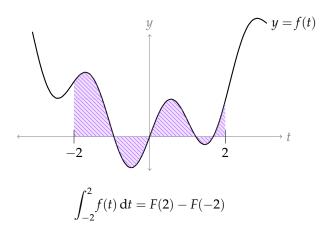


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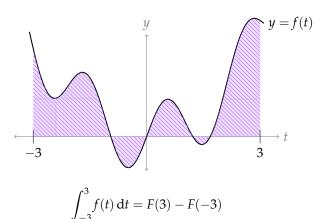




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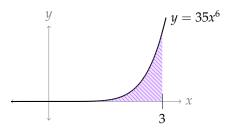
$$\int_{a}^{b} f(x) \, \mathrm{d}x = F(b) - F(a)$$

Examples:

$$\frac{d}{dx} \{5x^7\} = 35x^6$$
, so $\int_0^3 35x^6 dx =$

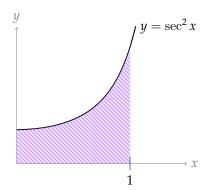
$$\frac{\mathrm{d}}{\mathrm{d}x} \left\{ \tan x \right\} = \sec^2 x, \text{ so}$$
$$\int_0^{\pi/4} \sec^2 x \, \mathrm{d}x =$$

$$\int_{0}^{3} 35x^{6} dx = F(b) - F(a) \quad \text{where} \quad F(x) = 5x^{7}$$



$$\int_0^3 35x^6 \, \mathrm{d}x = 5(3)^7 - 5(0)^7$$

$$\int_0^{\pi/4} \sec^2 x \, dx = F(b) - F(a) \quad \text{where} \quad F(x) = \tan x$$



$$\int_0^{\pi/4} \sec^2 x \, dx = \tan\left(\frac{\pi}{4}\right) - \tan 0 = 1$$

RELEVANT VOCABULARY

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An antiderivative of $\sin x$ is



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$$\left. \frac{x^2}{x+2} \right|_5^{-1} =$$



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The function f(x) evaluated from a to b

FTC Part 2, Abridged

$$\int_{a}^{b} f(x) \, \mathrm{d}x = F(x) \Big|_{a}^{b}$$

where F(x) is an antiderivative of f(x)

Definition

The **indefinite integral** of a function f(x):

$$\int f(x) \, \mathrm{d}x$$

means the *most general* antiderivative of f(x).

Examples:

$$\int 2x \, \mathrm{d}x =$$



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Examples:

$$\int 2x \, \mathrm{d}x =$$

$$\int \frac{1}{x} dx =$$

Remember: two functions with the same derivative differ by a constant, so we include the "+C" for indefinite integrals.



DEFINITE VS INDEFINITE INTEGRALS

For each pair of properties below, decide which applies to definite integrals, and which to indefinite integrals.

No limits (or bounds) of integration, $\int f(x) dx$	
Limits (or bounds) of integration, $\int_a^b f(x) dx$	
Area under a curve	
Antiderivative	
Number	
Function	

1. $\int e^x dx$

- 1. $\int e^x dx$
2. $\int \cos x dx$



- $1. \int e^x \, \mathrm{d}x$
- $2. \int \cos x \, \mathrm{d}x$
- 3. $\int -\sin x \, dx$

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- $2. \int \cos x \, \mathrm{d}x$
- 3. $\int -\sin x \, dx$
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- $2. \int \cos x \, \mathrm{d}x$
- 3. $\int -\sin x \, dx$
- 4. $\int \frac{1}{x} dx$
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- 5. $\int 1 dx$
- 6. $\int 2x \, dx$



1.
$$\int e^x dx$$

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7.
$$\int nx^{n-1} dx$$
 $(n \neq 0, \text{constant})$



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$$\int 2x \, dx$$

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 $(n \neq 0, \text{constant})$

8.
$$\int x^n dx$$
 $(n \neq -1, \text{constant})$



Power Rule for Antidifferentiation

$$\int x^n \, \mathrm{d}x = \frac{1}{n+1} x^{n+1} + C$$

if $n \neq -1$ is a constant

Example:

$$\int \left(5x^2 - 15x + 3\right) \, \mathrm{d}x =$$

ANTIDERIVATIVES TO RECOGNIZE

$$ightharpoonup \int a \, \mathrm{d}x = ax + C$$

$$\int \csc x \cot x \, dx = -\csc x + C$$

$$\int \csc^2 x \, \mathrm{d}x = -\cot x + C$$

Included Work

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