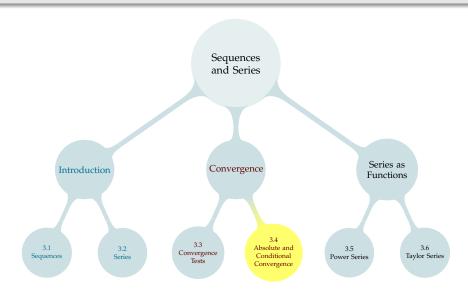
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### FOUR SERIES

Let  $a_n = \left(-\frac{2}{3}\right)^n$ . Do the following series converge or diverge?

$$\sum_{n=0}^{\infty} a_n$$

$$\sum_{n=0}^{\infty} |a_n|$$

Let  $b_n = \frac{(-1)^n}{n}$ . Do the following series converge or diverge?

$$\sum_{n=1}^{\infty} b_n$$

$$\sum_{n=1}^{\infty}|b_n|$$

#### The series

$$\sum_{n=0}^{\infty} \left( -\frac{2}{3} \right)^n$$

is called absolutely convergent, because the series converges and if we replace the terms being added by their absolute values, that series *still* converges.

#### The series

$$\sum_{n=0}^{\infty} \frac{(-1)^n}{n}$$

is called conditionally convergent, because the series converges, but if we replace the terms being added by their absolute values, that series *diverges*.

# Absolute and conditional convergence

- (a) A series  $\sum_{n=1}^{\infty} a_n$  is said to **converge absolutely** if the series
  - $\sum_{n=1}^{\infty} |a_n| \text{ converges.}$
- (b) If  $\sum_{n=1}^{\infty} a_n$  converges but  $\sum_{n=1}^{\infty} |a_n|$  diverges we say that  $\sum_{n=1}^{\infty} a_n$  is **conditionally convergent**.

### **Theorem**

If the series  $\sum_{n=1}^{\infty} |a_n|$  converges then the series  $\sum_{n=1}^{\infty} a_n$  also converges.

That is, absolute convergence implies convergence.

If $\sum a_n$	and $\sum  a_n $	then we say $\sum a_n$ is
converges	converges	
converges	diverges	
diverges	diverges	
diverges	converges	

### Does the series

$$\sum_{n=1}^{\infty} \frac{(-1)^n}{n^2}$$

converge or diverge?

### Does the series

$$\sum_{n=1}^{\infty} \frac{\sin(n)}{n^2}$$

converge or diverge?