# Design Automation Renegades

# GLOBETROTTING DIVISION

# Boilerplate Code: Data Structures and Algorithms for Design Automation

Zhiyang Ong <sup>1</sup>

REPORT ON
Common Data Structures and Algorithms
Found in Bolierplate Code for
Design Automation Software

November 25, 2018

<sup>&</sup>lt;sup>1</sup>Email correspondence to: ♥ ongz@acm.org

#### Abstract

This report describes the design and implementation of common data structures and algorithms, as well as "computational engines" that are found in electronic design automation (EDA) software.

Data structures and algorithms for digital VLSI and cyber-physical system design include: binary decision diagrams (BDDs), AND-inverter graphs (AIGs), and their associated algorithms for optimization, traversal, and other operations (such as graph matching). Common computational engines for digital systems would include: optimization and verification engines for deterministic and nondeterministic finite state machines; decision procedures for the boolean satisfiability problem (SAT solvers) and satisfiability modulo theories (SMT solvers); quantified boolean formula (QBF) solvers; and SAT and SMT solvers for maximum satisfiability (i.e., Max-SAT and Max-SMT solvers).

Regarding EDA problems that require numerical computation (in digital, analog, or mixed-signal VLSI design), the data structures and algorithms for circuit simulation based on sparse graph would be required. In addition, techniques for model order reduction shall be implemented.

Computational engines for statistical and probabilistic analyses or stochastic modeling can include data structures and algorithms for partially observable Markov decision processes (POMDPs) and Markov chains. Tools for analyses of queueing systems (based on queueing theory) should be included.

Regarding cyber-physical systems and mixed-signal circuits, hybrid automata can be used to represent these circuits and systems.

Optimization engines for EDA include: solvers for different types of mathematical programming, such as linear programming (LP), integer linear programming (ILP), mixed-integer linear programming (MILP), quadratic programming (QP), convex programming (CP), geometric programming (GP), and second-order conic programming (SOCP); solvers for pseudo-boolean optimization (PBO solvers) and weighted-boolean optimization (WBO); and meta-heuristics (e.g., evolutionary algorithms, simulated annealing, and ant colony optimization).

Algorithms shall be implemented using parallel programming, in a scalable style. In addition, considerations shall be given to the use of constraint programming.

More stuff to be included...

# **Revision History**

### Revision History:

- 1. Version 0.1, December 23, 2014. Initial copy of the report.
- 2. Version 0.1.1, September 16, 2015. Added sections for mathematics and statistics, and the abstract.
- 3. Version 0.1.2, November 10, 2018. Added sections for graphs, including directed graphs (digraphs), directed acyclic graphs (DAGs), and undirected graphs.

# Contents

Re	evision History	j
1	Algorithms 1.1 Resources for Algorithms	<b>1</b>
2	Data Structures2.1 Basic Data Structures2.2 Graphs2.2.1 Graph Representations2.2.2 Functions that need to be implemented2.2.3 Directed Graphs, and Directed Acyclic Graphs2.2.4 Undirected Graphs2.2.5 Resources for Graphs	$\begin{array}{c} 3 \\ 7 \\ 7 \\ 1 \\ 2 \end{array}$
3	Optimization3.1Benchmarks for Optimization13.2Notes on Using Optimization Tools13.3Robust Linear Programming13.4Discrete Optimization13.5Optimization Solvers13.5.1Accessible Optimization Solvers13.5.2Not Accessible Optimization Solvers1	3 3 4 4
4	Mathematics 1	7
5	Statistics 1	9
6	C++ Resources26.1 Resources for C++ and Notes About C++26.2 Computational Complexity of C++ Containers36.3 Additional Notes About C++36.3.1 Alternate Computer Number System for Representing Fractions in C++36.4 Software Development in C++36.4.1 Using "Design By Contract"36.4.2 Debugging C++ Software46.4.3 Parser Development46.5 Parallel Programming in C++4	2 3 5 6 6 9 1

7	Questions	42
	7.1 Unresolved C++ Questions	
8	Miscellaneous  8.1 Setting Up Software Development Environment	 <b>46</b>
A	cknowledgments	47
В	ibliography	61

Zhiyang Ong iii

# Chapter 1

# Algorithms

This section documents algorithms that I have implemented for my C++ -based boilerplate code repository.

A template for typesetting algorithms is shown in Procedure 1.

```
NAME OF THE ALGORITHM(ARGUMENTS)
    # Input ARGUMENT #1: Definition1
    # Input ARGUMENT #2: Definition2
   BODY OF THE PROCEDURE
    # A while loop.
    while [condition]
 3
         [Something]
    # A for loop.
    for Var = [initial value] to [final value]
5
         [Something]
    # An if-elseif-else block.
    if [Condition1]
7
        Blah...
    elseif [Condition2]
8
9
        Blah...
10
    elseif [Condition3]
        Blah...
11
12
    else
13
        Blah...
    # A variable assignment.
    blah = A[j]
        # This is indented with a tab.
    # What is the output of this procedure?
15
   return
```

### 1.1 Resources for Algorithms

Resources for algorithms:

```
1. Collected Algorithms (CALGO): http://calgo.acm.org/
```

<sup>2.</sup> Netlib Repository at UTK and ORNL [47]: http://www.netlib.org/

- 3. "The Stony Brook Algorithm Repository" by Steven Skiena [158]: http://algorist.com/algorist.html
- 4. Cosmos (from OpenGenus Foundation): https://github.com/OpenGenus/cosmos
- 5. Wikipedia:
  - (a) https://en.wikipedia.org/wiki/List\_of\_algorithm\_general\_topics
  - (b) https://en.wikipedia.org/wiki/List\_of\_algorithms#Graph\_algorithms

# Chapter 2

# **Data Structures**

### 2.1 Basic Data Structures

"[A list is a] container of variable length, and [a tuple is a] container [of] fixed length" [169, §4.3 pp. 111].

A list (in *Prolog*) can be deconstructed into [*Head* | *Tail*], where *Head* refers to the first element of the list and *Tail* refers to the rest of the list; on the other hand, tuples cannot be similarly deconstructed [169, §4.3 pp. 113].

# 2.2 Graphs

A **graph** G is an ordered pair, G = (V, E), of a vertex/node set and an edge set [180]. Types of **finite graphs** [180]:

- 1. undirected graph [180]:
  - (a) simple graph, or undirected simple finite graph [180]:
    - i. Does not allow **multiple edges** (or, **parallel edges**, or **multi-edges**) between any pair of vertices/nodes in the graph, nor (**self-)loops**.
    - ii. A symmetric loopless directed graph is a graph that has an edge  $(v_2, v_1)$  for each edge  $(v_1, v_2)$ , and it does not contain any self-loops (i.e., edges  $v_i, v_i, \forall i \in V$ ).
    - iii. Therefore, the edges of a simple graph form a set, as opposed to multigraphs that have multisets of edges.
    - iv. An edge is a two-element subset of V; other graphs (i.e., hypergraphs) can have edges with more than two nodes.
  - (b) multigraph [182]:
    - i. A multigraph allows multiple edges (or, parallel edges, or multi-edges) to exist between any pair of vertices (or, nodes) in the graph. Alternatively, for any pair of vertices (or, nodes) in the multigraph, they allow multiple edges to be incident to them [182].
    - ii. pseudograph [182]:
      - Some authors/people use pseudographs and multigraphs interchangeably/synonymously.
      - Other people use pseudographs to refer to multigraphs that allow self-loops (or loops).
    - iii. A planar graph remains planar, or preserves its planarity, when its edges become multiple edges by the addition of edges to edges in the original graph Reference this!!!!

- iv. Representations for different types of multigraphs [182]:
  - A multidigraph is also known as quiver [184].
  - undirected multigraph, which edges have no identity, is an ordered pair (or 2-tuple) G = (V, E), where V is a set of vertices (or, nodes), E is a multi-set of undirected edges (or unordered pairs of vertices).
  - undirected multigraph, which edges have an identity each (or, where each edge has an identity), is an ordered triple (or 3-tuple) G = (V, E, r), such that  $r: E \to \{\{x,y\}: x,y \in V\}$  is a function that assigns each edge to an unordered pair of vertices (i.e., endpoint nodes).
  - directed multigraph (or multidigraph or quiver), which edges have no identity, is an ordered pair (or 2-tuple) G = (V, E). Here, V is a set of vertices (or, nodes), and E is a multi-set of ordered pairs of vertices (i.e., directed edges, directed arcs, or arrows)
  - A mixed multigraph is a(n) (ordered) 3-tuple G = (V, E, A), where V is a set of vertices (or, nodes), E is a set of undirected edges, and A is a multi-set of directed edges/arcs.
  - A directed multigraph (or multidigraph or quiver), which edges have an identity each (or, where each edge has an identity), is a 4-tuple G = (V, E, s, t). Here, V is a set of vertices (or nodes), E is a multi-set of ordered pairs of vertices (i.e., directed edges, directed arcs, or arrows),  $s: E \to V$  so that each edge is assigned to its source node, and  $t: E \to V$  so that each edge is assigned to its destination/target node.
- v. A **labeled multigraph** is a 6-tuple  $G = (\sum_{V}, \sum_{E}, V, E, l_{V}, l_{E})$ . Here, V is a set of vertices (or, nodes), and E is a multi-set of ordered pairs of vertices (i.e., directed edges, directed arcs, or arrows),  $\sum_{V}$  is the finite alphabet of available vertex labels,  $\sum_{E}$  is the finite alphabet of available edge labels,  $l_{V}: V \to \sum_{V}$  is a map describing the labeling of the vertices, and  $l_{E}: E \to \sum_{E}$  is a map describing the labeling of the vertices.
- vi. A labeled multidigraph is also known as a labeled, directed multigraph. It is a 8-tuple  $G = (\sum_V, \sum_E, V, E, s, t, l_V, l_E)$ . Here, V is a set of vertices (or, nodes), and E is a multi-set of ordered pairs of vertices (i.e., directed edges, directed arcs, or arrows),  $\sum_V$  is the finite alphabet of available vertex labels,  $\sum_E$  is the finite alphabet of available edge labels,  $s: E \to V$  so that each edge is assigned to its source node (or, is a map that assigns each edge to its source node),  $t: E \to V$  so that each edge is assigned to its destination/target node),  $l_V: V \to \sum_V$  is a map describing the labeling of the vertices, and  $l_E: E \to \sum_E$  is a map describing the labeling of the vertices.

#### vii. References:

- Multiple edges: https://en.wikipedia.org/wiki/Multiple edges
- Multigraph [182]: https://en.wikipedia.org/wiki/Multigraph
- Graph labeling [177]:
  - https://en.wikipedia.org/wiki/Graph labeling
  - "Graph labeling is the assignment of labels," which can be represented by numbers and/or strings, to edges and/or vertices of a graph.
  - Vertex labeling is a function of V that assigns a set of labels to V; or, it is a function of V that assigns a label to each vertex.
  - A vertex-labeled graph is a graph with a defined vertex labeling function.
  - Edge labeling is a function of E that assigns a set of labels to E; or, it is a function of Ethat assigns a label to each edge.

- An edge-labeled graph is a graph with a defined edge labeling function.
- A weighted graph is an edge-labeled graph, such that the edge labels are members of an ordered set (e.g., the set of real numbers  $\mathbb{R}$ ).
- The term labeled graph generally refers to a vertex-labeled graphs with unique labels (e.g.,  $\{1, \ldots, |V|\}$ , where |V| is the number of vertices in the graph or the cardinality of V), unless otherwise specified.
- (c) hypergraph:

i.

- (d) multidimensional networks:
  - i. One of the distinguishing features of multi-dimensional edges is multiple edges.
- (e) mixed graph:

i.

(f) planar graph:

i.

- (g) dipole graph:
  - i. A dipole graph (or bond graph not that kind of bond graph) has a set of only two vertices, and a set of (parallel) edges between these vertices.:
    - A bond graph is a graphical representation of a physical dynamic system, and represents exchanges of physical energy; see <a href="https://en.wikipedia.org/wiki/Bond\_graph">https://en.wikipedia.org/wiki/Bond\_graph</a>.
  - ii. An order-n dipole graph Dn is a dipole graph with n edges, and is a dual to the cycle graph  $C_n$ .
  - iii. References:
    - Multiple edges: https://en.wikipedia.org/wiki/Multiple\_edges
    - Dipole graph: https://en.wikipedia.org/wiki/Dipole\_graph

#### 2. directed graph:

- (a) directed multigraphs: see aforementioned notes on "directed multigraph (or multidigraph), which edges have no identity" and "directed multigraph (or multidigraph), which edges have an identity each (or, where each edge has an identity)"
- (b) directed acyclic graphs (DAGs)

#### Additional resources about graphs:

- 1. Graph property, or graph invariant:
  - (a) https://en.wikipedia.org/wiki/Graph\_property
  - (b) Notes about vertices/nodes:
    - i. If the graph contains an edge connecting vertices u and v, e = (u, v), the vertices u and v are **adjacent** to each other [178].
    - ii. The **degree** (or valency) of vertex v, which is denoted by  $\delta(v)$  (or,  $\deg(v)$  or  $\deg(v)$ , is the number of edges that are incident to v [178].
    - iii. An **isolated vertex** is a vertex with degree zero,  $\delta(v) = 0$ . It does not an endpoint of any edge; or, no edge in a (or, any) graph is defined with an isolated vertex [178].
    - iv. A **leaf vertex**, or **pendent vertex**, is a vertex of degree one, and is an endpoint of only one edge in the graph [178].
    - v. For a vertex v of a directed graph, the **outdegree** of v (denoted by  $\delta^+(v)$ ) is its number of outgoing edges, and the **indegree** of v (denoted by  $\delta^-(v)$ ) is its number of incoming edges. A source vertex is a vertex with a zero indegree ( $\delta^-(v) = 0$ ), and a sink vertex is a vertex with a zero outdegree ( $\delta^+(v) = 0$ ) [178].

- vi. A vertex v, which has no incident edges apart from a(n) (undirected) loop from v to itself, has a degree of two; i.e., deg(v) = 0 [179].
- vii. For a graph G, its maximum degree  $\Delta(G)$  and its minimum degree  $\delta(G)$  are the maximum and minimum degree of its vertices [179].

#### 2. Multi-dimensional networks:

- (a) Multi-dimensional networks belong to type of multi-layer networks that have multiple type-s/kinds of relations [181].
- (b) A multi-dimensional network can be modeled with a multipartite edge-labeled multigraph [181, 183].
- (c) An unweighted multi-layer network can be represented as a triple G = (V, E, D), where (or, in which) V is a set of vertices, E is a dimension-specific set of edges connecting the vertices and each edge is represented by the triple (u, v, d) such that  $u, v \in V$  and  $d \in D$  (or,  $E = \{(u, v, d); u, v \in V, d \in D)$ , and D is a set of dimensions or layers [181].
  - i. For an unweighted, undirected multi-layer network, the edges/links (u, v, d) and (v, u, d) are equivalent.
  - ii. For an unweighted, directed multi-layer network, the edges/links (u, v, d) and (v, u, d) are different/distinct.
  - iii. By convention, unweighted multi-layer network are not multigraphs in a given dimension; hence, "the number of [edges/]links between two nodes in a given dimension is either zero or one". "However, the total number of [edges/]links between two nodes across all dimensions is less than or equal to |D|."
- (d) An edge of a weighted multi-layer network can be represented as a 4-tuple (or, quadruplet) e = (u, v, d, w), "where w is the weight of the [edge/]link between [vertex] u and [vertex] v in the dimension d" [181]
  - i. Weighted multi-layer networks, like unweighted multi-layer networks, can also be represented as a triple G = (V, E, D), where V is the set of vertices, E is the set of edges (each edge is represented by e = (u, v, d, w)), or  $E = \{(u, v, d, w); u, v \in V, d \in D, w \in W\}$ , W is a set of weights, and D is a set of dimensions or layers.
  - ii. A weighted multi-layer networks, where an edge is defined as  $e = (u, v, d_1, \dots, d_n, w)$ , such that  $d_1, \dots, d_n \in D$ , can model multidimensional temporal networks, or multidimensional time-varying networks [181].
- (e) Multidimensional network [181]: https://en.wikipedia.org/wiki/Multidimensional\_network.
- $(f) \ \ Multipartite \ graph \ [183]: \ https://en.wikipedia.org/wiki/Multipartite_graph$
- (g) Temporal network, or time-varying network: https://en.wikipedia.org/wiki/Temporal\_network
- (h) A 1-dimensional (1-D) network has a 2-dimensional (2-D) adjacency matrix with the size  $V \times V$ ;  $A_j^i$  is an adjacency matrix that encodes edges/links/connections between vertices i and j.
- (i) For a multi-dimensional network with |D| dimensions, it has a multi-layer adjacency tensor (or, 4-dimensional matrix, or 4-D matrix) with the size  $(V \times D) \times (V \times D)$ ;  $M_{j\beta}^{i\alpha}$  is an multi-layer adjacency tensor that encodes edges/links/connections between vertices i in layer  $\alpha$  and j in layer  $\beta$  [181].

### 3. infinite graph:

- (a) An infinite graph is a graph that is not finite. This can be worded better.
- 4. extremal graphs:
  - (a) "Extremal graph theory studies extremal (maximal or minimal) graphs which satisfy a certain property. Extremality can be taken with respect to different graph invariants, such as order, size or girth."

(b) https://en.wikipedia.org/wiki/Extremal graph theory

### 2.2.1 Graph Representations

Focus on sparse graph representations, which are common in modeling digital integrated circuits and neural networks (certain types), and dense graphs (e.g., neural networks).

For sparse graphs, use list or map -based graph representations for better memory efficiency.

For dense graphs, use matrix-based graph representation for faster access time at the expense of worse member efficiency; see https://en.wikipedia.org/wiki/Dense\_graph. Also, see https://en.wikipedia.org/wiki/Dense\_subgraph regarding dense subgraphs.

Hence, there exists a trade-off between access time and member efficiency in graph representations.

The ways to represent graphs are listed as follows:

- 1. adjacency matrix:
  - (a)
- 2. adjacency list:
  - (a)
- 3. adjacency map:
  - (a)
- 4. edge list:
  - (a) Is this equivalent to the "incidence list" graph representation? Cite this!!!
  - (b)

Alternate graph representations that I am not exploring:

- 1. distance matrix: https://en.wikipedia.org/wiki/Distance matrix
- 2. incidence matrix

### 2.2.2 Functions that need to be implemented

Solvers for the following problems (or to perform the following functions) regarding:

- 1. graph traversal:
  - (a) breadth-first search:
    - i. https://en.wikipedia.org/wiki/Breadth-first\_search
    - ii. Also, see BFS ordering: https://en.wikipedia.org/wiki/Breadth-first search
  - (b) depth-first search:
    - i. https://en.wikipedia.org/wiki/Depth-first\_search
    - ii. iterative deepening search, or more specifically iterative deepening depth-first search (IDS or IDDFS: https://en.wikipedia.org/wiki/Iterative deepening depth-first search
  - (c) graph factorization:
  - (d) References:
    - i. https://en.wikipedia.org/wiki/Graph theory
- 2. graph coloring:
  - (a) vertex coloring

- (b) edge coloring: https://en.wikipedia.org/wiki/Edge\_coloring
- (c) four color theorem, or the four color map theorem: https://en.wikipedia.org/wiki/Four\_color theorem
- (d) References:
  - i. https://en.wikipedia.org/wiki/Graph coloring
- 3. routing problems:
  - (a) shortest path problem:
    - i. Dijkstra's algorithm: https://en.wikipedia.org/wiki/Dijkstra%27s algorithm
    - ii. Bellman-Ford algorithm (or, Bellman-Ford-Moore algorithm): https://en.wikipedia.org/wiki/Bellman%E2%80%93Ford algorithm
    - iii. Ford-Fulkerson algorithm (FFA), or Ford-Fulkerson method: https://en.wikipedia.org/wiki/Ford%E2%80%93Fulkerson algorithm
    - iv. Categorize solutions into those for directed graphs and undirected graphs. Also, determine solutions for common variants of the problem.
    - v. https://en.wikipedia.org/wiki/Shortest path problem
  - (b) longest path problem:
    - i. Note that the difficulty of the problem (in terms of computational time complexity) is different for different types of graphs:
      - E.g., for undirected graphs, it is NP-hard, while linear time solutions exist for directed acyclic graphs (DAGs).
    - ii. https://en.wikipedia.org/wiki/Longest\_path\_problem
  - (c) minimum spanning tree:
    - Prim-Jarník algorithm:
      - Also, known as:
        - \* Prim's algorithm
        - \* Jarník's algorithm
        - \* Prim-Dijkstra algorithm
        - \* DJP algorithm
      - https://en.wikipedia.org/wiki/Prim%27s algorithm
    - Kruskal's algorithm: https://en.wikipedia.org/wiki/Kruskal%27s algorithm
    - https://en.wikipedia.org/wiki/Minimum\_spanning\_tree
  - (d) Steiner tree:
    - i. rectilinear minimum Steiner tree (RMST) problem: https://en.wikipedia.org/wiki/ Rectilinear Steiner tree
    - ii. https://en.wikipedia.org/wiki/Steiner tree problem
  - (e) traveling salesperson problem (NP-hard):
    - i. nearest neighbor algorithm:
      - https://en.wikipedia.org/wiki/Nearest\_neighbour\_algorithm
      - This is different from the k-nearest neighbors algorithm (k-NN); see https://en.wikipedia.org/wiki/K-nearest\_neighbors\_algorithm.
    - ii. https://en.wikipedia.org/wiki/Travelling salesman problem
  - (f) strongly connected components:
    - i. https://en.wikipedia.org/wiki/Strongly\_connected\_component
- 4. network flow:
  - (a) max-flow min-cut theorem: https://en.wikipedia.org/wiki/Max-flow\_min-cut\_theorem
  - (b) minimum-cost flow problem (MCFP): https://en.wikipedia.org/wiki/Minimum-cost\_flow\_problem

- (c) maximum flow problems: https://en.wikipedia.org/wiki/Maximum flow problem
- (d) circulation problem: https://en.wikipedia.org/wiki/Circulation problem
- (e) References:
  - i. Flow network (or transportation network): <a href="https://en.wikipedia.org/wiki/Flow\_network">https://en.wikipedia.org/wiki/Flow\_network</a>

ii.

- 5. graph partitioning:
  - (a) force-directed graph partitioning
  - (b) min-cut graph partitioning
  - (c) References:
    - i. https://en.wikipedia.org/wiki/Connectivity (graph theory)
- 6. graph-based floorplanning/placement:
  - (a) use constraint graphs for graph-based floorplanning/placement
  - (b) References:
    - i. https://en.wikipedia.org/wiki/Constraint\_graph\_(layout)
- 7. covering problems:
  - (a) In graph theory, "covering problems are specific instances of subgraph-finding problems"; see https://en.wikipedia.org/wiki/Graph\_theory
  - (b) Set cover problem:
    - i. https://en.wikipedia.org/wiki/Set cover problem
    - ii. hitting set problem
  - (c) Vertex cover problem: https://en.wikipedia.org/wiki/Vertex\_cover
  - (d) edge cover problem: https://en.wikipedia.org/wiki/Edge\_cover
  - (e) Related problems:
    - i. clique problem: https://en.wikipedia.org/wiki/Clique problem
    - ii. independent set problem, and maximum independent set: https://en.wikipedia.org/wiki/Independent\_set\_(graph\_theory)
    - iii. Covering/packing-problem pairs, or covering/packing dualities: https://en.wikipedia.org/wiki/Linear\_programming#Covering/packing\_dualities
    - iv. Packing problems: https://en.wikipedia.org/wiki/Packing problems
    - v. Reconstruction conjecture:
      - "Informally, the reconstruction conjecture in graph theory says that graphs are determined uniquely by their subgraphs."
      - https://en.wikipedia.org/wiki/Reconstruction conjecture
  - (f) References:
    - i. https://en.wikipedia.org/wiki/Covering problems
- 8. graph decomposition problems:
  - (a) arboricity: https://en.wikipedia.org/wiki/Arboricity
  - (b) cycle double cover: https://en.wikipedia.org/wiki/Cycle double cover
  - (c) graph factorization: https://en.wikipedia.org/wiki/Graph\_factorization
  - (d):

i.

- (e) References:
  - i. https://en.wikipedia.org/wiki/Graph\_theory
- 9. closure problem:
  - (a) https://en.wikipedia.org/wiki/Closure\_problem

- 10. spectral graph theory:
  - (a) "In mathematics, spectral graph theory is the study of the properties of a graph in relationship to the characteristic polynomial, eigenvalues, and eigenvectors of matrices associated with the graph, such as its adjacency matrix or Laplacian matrix."
  - (b) References:
    - i. https://en.wikipedia.org/wiki/Spectral graph theory
- 11. probabilistic graphical model (PGM):
  - (a) Also known as:
    - i. graphical model
    - ii. structured probabilistic model
  - (b) References:
    - i. https://en.wikipedia.org/wiki/Graphical\_model
    - ii. [10]
    - iii. [17]
    - iv. Cowell, Robert G.; Dawid, A. Philip; Lauritzen, Steffen L.; Spiegelhalter, David J. (1999). Probabilistic networks and expert systems. Berlin: Springer. A more advanced and statistically oriented book
    - v. Jensen, Finn (1996). An introduction to Bayesian networks. Berlin: Springer.
    - vi. Pearl, Judea (1988). Probabilistic Reasoning in Intelligent Systems (2nd revised ed.). San Mateo, CA: Morgan Kaufmann.
- 12. quantum graph:
  - (a) "In mathematics and physics, a quantum graph is a linear, network-shaped structure of vertices connected by bonds (or edges) with a differential or pseudo-differential operator acting on functions defined on the bonds."
  - (b) References:
    - i. https://en.wikipedia.org/wiki/Quantum\_graph
    - ii. [99]

Solvers for the following problems (or to perform the following functions) regarding subgraphs, induced subgraphs, and minors:

- 1. subgraph isomorphism problem:
  - (a) Find a fixed graph as a subgraph in a given graph:
    - i. "graph properties are hereditary for subgraphs"... "A graph has a property if and only if all its subgraphs also have it"; see <a href="https://en.wikipedia.org/wiki/Graph\_theory">https://en.wikipedia.org/wiki/Graph\_theory</a>.
    - ii. Finding a specific type/kind of maximal subgraph is an NP-complete problem, such as the largest complete subgraph.
  - (b) Also, see subgraph matching.
  - (c) Graph isomorphism: https://en.wikipedia.org/wiki/Graph isomorphism
  - (d) https://en.wikipedia.org/wiki/Subgraph\_isomorphism\_problem
- 2. Finding induced subgraphs in a given graph:
  - (a) "graph properties are hereditary" for induced subgraphs... "A graph has a property if and only if all its induced subgraphs also have it"; see https://en.wikipedia.org/wiki/Graph\_theory.
  - (b) Finding a specific type/kind of maximal induced subgraph is an NP-complete problem:
    - i. Independent set problem: Finding the largest edgeless induced subgraph (or independent set); see the following references:
      - https://en.wikipedia.org/wiki/Graph\_theory

- (c) Induced subgraph: https://en.wikipedia.org/wiki/Induced subgraph
- 3. minor containment problem:
  - (a) Find a fixed graph as a minor of a given graph.
  - (b) "A minor or subcontraction of a graph is any graph obtained by taking a subgraph and contracting some (or no) edges"... "A graph has a property if and only if all its minors [also] have it"
  - (c) "[Minor containment] is related to graph properties such as planarity." See Wagner's Theorem about planar graphs.
  - (d) References:
    - i. https://en.wikipedia.org/wiki/Graph theory
    - ii. Graph minor: https://en.wikipedia.org/wiki/Graph minor
- 4. subdivision containment problems:
  - (a) "Find a fixed graph as a subdivision of a given graph":
    - i. "A subdivision or homeomorphism of a graph is any graph obtained by subdividing some (or no) edges."
    - ii. "Subdivision containment is related to graph properties such as planarity." See Kuratowski's Theorem and the Kelmans-Seymour conjecture about planar graphs.
  - (b) References:
    - i. https://en.wikipedia.org/wiki/Graph theory
    - ii. Homeomorphism: https://en.wikipedia.org/wiki/Homeomorphism\_(graph\_theory) #Subdivision\_and\_smoothing
- 5. common topics:
  - (a) Planar graph: https://en.wikipedia.org/wiki/Planar graph
  - (b) network science:
    - https://en.wikipedia.org/wiki/Network science
    - Interdependent networks: https://en.wikipedia.org/wiki/Interdependent networks
    - Modularity (networks): https://en.wikipedia.org/wiki/Modularity (networks)
    - Community structure: https://en.wikipedia.org/wiki/Community structure
    - Distance (graph theory): https://en.wikipedia.org/wiki/Distance (graph theory)
    - Assortativity: https://en.wikipedia.org/wiki/Assortativity
    - Degree distribution: https://en.wikipedia.org/wiki/Degree distribution
    - Centrality: https://en.wikipedia.org/wiki/Centrality#Closeness centrality
    - Betweenness centrality: https://en.wikipedia.org/wiki/Betweenness centrality

Other problems and types of graphs, not of comparable importance:

1. nearest neighbor graph (NNG): https://en.wikipedia.org/wiki/Nearest neighbor graph

### 2.2.3 Directed Graphs, and Directed Acyclic Graphs

Notes on directed graphs (digraphs), and directed acyclic graphs (DAGs):

- 1. Functions to implement, and solves to solve the following problems:
  - (a) For DAGs:
    - i. topological sort:
      - Also known as: topological sorting, or topological ordering
      - https://en.wikipedia.org/wiki/Topological sorting
    - ii. algorithms, heuristics, and meta-heuristics to optimize:
      - BDDs; see §2.2.3.1.
      - AIGs; see §2.2.3.2
      - MIGs; see §2.2.3.3

### 2.2.3.1 Binary Decision Diagrams (BDDs)

```
Resources for BDDs:
```

```
1. https://en.wikipedia.org/wiki/Binary_decision_diagram
```

### 2.2.3.2 AND-Inverter Graphs (AIGs)

```
Resources for AIGs:
```

```
1. https://en.wikipedia.org/wiki/And-inverter_graph
```

### 2.2.3.3 Majority-Inverter Graphs (MIGs)

Resources for MIGs:

1.

### 2.2.4 Undirected Graphs

### 2.2.5 Resources for Graphs

Resources for graphs:

- 1. "The Stanford GraphBase: A Platform for Combinatorial Computing":
  - (a) [90]
  - (b) https://www-cs-staff.stanford.edu/~knuth/sgb.html
- 2. Wikipedia:
  - (a) https://en.wikipedia.org/wiki/List of algorithms#Graph algorithms
  - (b) Gallery of named graphs: https://en.wikipedia.org/wiki/Gallery of named graphs
  - (c) List of graph theory topics: https://en.wikipedia.org/wiki/List\_of\_graph\_theory\_topics
  - (d) Glossary of graph theory terms: https://en.wikipedia.org/wiki/Glossary\_of\_graph\_theory\_terms
  - (e):
  - (f):
  - (g):
  - (h):
  - (i):
  - (j):
  - (k):
  - (1):
  - (m):
  - (n) Graph algebra: https://en.wikipedia.org/wiki/Graph algebra

# Chapter 3

# Optimization

# 3.1 Benchmarks for Optimization

A collection of "optimization solvers" and benchmarks are available at [47].

Benchmarks for optimization problems:

1. MIPLIB 2010 – Mixed Integer Programming Library version 5 [91]. See [2] for publications associated with this set of benchmarks (or benchmark set).

2.

# 3.2 Notes on Using Optimization Tools

Optimization problems in EDA can be solved via optimization engines that I implement or external (i.e., third-party) optimization solvers.

Regarding external optimization solvers, some of them use Algebraic Modeling Languages (AML) [175] to model the optimization problem computationally. These optimization solvers can solve optimization problems that are formulated as computational models in a specific AML representation.

I am avoiding the use of external optimization solvers that require paid licenses. Hence, any external optimization solvers that I would use are either open-source software (or rather, free/libre/open-source software, FLOSS) or software that have free academic licenses.

Solvers that use an AML, or several AMLs, in their software interface are: 1.

For a list of optimization solvers/tools, see §3.5.

### 3.3 Robust Linear Programming

During the "lab meeting" on Friday, December 4, 2015, Prof. Jiang Hu told me that I can transform a robust linear programming into a standard/"standard" linear programming problem. He told me to look at [16] and its references.

# 3.4 Discrete Optimization

Discrete optimization is classified into the following categories [69, 96, 176]:

- 1. combinatorial optimization
- 2. integer programming

# 3.5 Optimization Solvers

A (brief) description of optimization solvers (not restricted to solvers for mathematical programming), including linear programming solvers, is provided as follows in §3.5.1 and §3.5.2.

### 3.5.1 Accessible Optimization Solvers

External optimization solvers that are open-source software or provide free academic licenses:

- 1. *LocalSolver* [77]:
  - (a) Hybrid solver for optimization problems
  - (b) Properties of the solver [77, Product: Overview]:
    - i. "next-generation, hybrid mathematical programming solver"
    - ii. solve "ultra-large real-life nonlinear problems"
    - iii. solve problems in a "model-and-run fashion without any tuning"
    - iv. reliable and robust solver: **Define reliability and robustness for solvers of optimization problems.**
    - v. dynamically combines solutions from various optimization approaches and resolves them via a hybrid neighborhood search approach
    - vi. solver engines:
      - A. "local search techniques"
      - B. "constraint propagation techniques"
      - C. "inference techniques"
      - D. linear programming solver/techniques
      - E. mixed-integer programming solver/techniques, including mixed-integer linear programming (MILP) solver/techniques; check performance comparisons on MIPLIB benchmarks (http://www.localsolver.com/news.html?id=32)
      - F. nonlinear programming solver/techniques
      - G. combined pure and direct local search techniques
    - vii. is based on the *LocalSolver Programming language* (LSP) for mathematical modeling viii. has lightweight object-oriented APIs
  - (c) From [77, Support Center: Example tour], LocalSolver can solve continuous and discrete/combinatorial optimization problems:
    - i. continuous optimization problems:
      - A. minimization of the Branin function: find the minimal point of the Branin function, within a specified domain
      - B. optimal bucket design: minimization of a bucket encapsulating/covering the rod/-cvlinder
      - C. Steel mill slab design: mathematical programming
    - ii. discrete optimization problems:
      - A. car sequencing: scheduling problem, or assignment problem.
      - B. Flowshop: scheduling problem
      - C. knapsack problem

- D. max-cut problem
- E. Quadratic Assignment Problem (QAP)
- F. Steel mill slab design: integer programming
- G. Travelling salesman problem
- H. Vehicule routing problem
- (d) Its technical documentation can be found at: http://www.localsolver.com/documentation/index.html [76].

#### 2. Stanford University:

- (a) Systems Optimization Laboratory researchers, "SOL Optimization Software," from Stanford University: School of Engineering: Department of Management Science and Engineering: Systems Optimization Laboratory, Stanford, CA, 2015. Available online at: http://web.stanford.edu/group/SOL/download.html; last accessed on December 14, 2015.
  - i. "Iterative solvers for sparse Ax = b: SYMMLQ, MINRES, MINRES-QLP, cgLanczos, CRAIG"
  - ii. "Iterative solvers for sparse least-squares problems: LSQR, LSMR, CGLS, covLSQR, LSRN"
  - iii. "Sparse and dense LU factorization (direct methods): LUSOL, LUMOD"
  - iv. "Sparse optimization: ASP"
  - v. "Optimization with convex objective and linear constraints: PDCO (including sparse optimization)"
  - vi. "Convex optimization in composite form: PNOPT"
  - vii. "Fortran 90 quad-precision dotproduct of double-precision vectors: qdotdd"

3. 4.

5.

6. 7.

8.

9.

10.

11.

12.

13.

14.15.

16.

### 3.5.2 Not Accessible Optimization Solvers

External optimization solvers that require paid licenses:

- 1. Stanford University:
  - (a) Systems Optimization Laboratory researchers, "SOL Optimization Software," from Stanford University: School of Engineering: Department of Management Science and Engineering: Systems Optimization Laboratory, Stanford, CA, 2015. Available online at: http://web.stanford.edu/group/SOL/download.html; last accessed on December 14, 2015.
    - i. LSSOL
    - ii. MINOS

- iii. NPSOL iv. QPOPT v. SNOPT vi. SQOPT
- 2.
- 3.
- 4.
- 5.
- 6.
- 7.
- 8.
- 9.
- 10.
- 11.
- 12.
- 13.
- 14.
- 15.

# Chapter 4

# Mathematics

Math symbols that I use frequently:

1. 
$$\mathbb{N}$$
2.  $\sum_{i=1}^{i=1}$ 
3.  $f(x) = \lim_{n \to \infty} \frac{f(x)}{g(x)}$ 

- 5. q

A 
$$3 \times 3$$
 matrix:  $\begin{pmatrix} 11 & 12 & 13 \\ 21 & 22 & 23 \\ 31 & 32 & 33 \end{pmatrix}$ 

Here is an equation:

$$\iint_{\Sigma} \nabla \times \mathbf{F} \cdot d\mathbf{\Sigma} = \oint_{\partial \Sigma} \mathbf{F} \cdot d\mathbf{r}.$$
 (4.1)

Here is an equation that is not numbered.

$$\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t}$$

Here is the set of Maxwell's equations that is numbered.

$$\nabla \cdot \mathbf{E} = \frac{\rho}{\varepsilon_0} \tag{4.2}$$

$$\nabla \cdot \mathbf{B} = 0 \tag{4.3}$$

$$\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t} \tag{4.4}$$

$$\nabla \times \mathbf{B} = \mu_0 \left( \mathbf{J} + \varepsilon_0 \frac{\partial \mathbf{E}}{\partial t} \right) \tag{4.5}$$

minimize 
$$\sum_{i=1}^{c} c_i \cdot x_i$$

$$\underline{x} \in S$$
subject to:
$$x_1 + x_4 = 0$$

$$x_3 + 7 \cdot x_4 + 2 \cdot x_9 = 0$$

$$f(n) = \begin{cases} case - 1 & : \text{n is odd} \\ case - 2 & : \text{n is even} \end{cases}$$
 (4.6)

*Proof.* This is a proof for BLAH . . .

**Theorem 4.1.** TITLE of theorem. My theorem is...

**Axiom 4.1.** TITLE of axiom. Blah...

Cases of putting a bracket/parenthesis on the right side of the equation.

$$B' = -\partial \times E,$$
  
 $E' = \partial \times B - 4\pi j,$  Maxwell's equations

Labeling an arrow:  $\xrightarrow{ewq}$ 

Chapter 5

**Statistics** 

# Chapter 6

# C++ Resources

Quick advice: Learn how to use C++1y features, including those of C++11, C++14, and C++17. Older C++ versions include C++98 and C++03.

Reference: Free Software Foundation contributors, "C++1y/C++14 Support in GCC," from GCC, the GNU Compiler Collection: GCC Projects, Free Software Foundation, Boston, MA, November 14, 2015. Available online at: https://gcc.gnu.org/projects/cxx1y.html; last accessed on January 25, 2016.

# Add references for this chapter!

Books/references that cover the following modern C++ standards:

- 1. C++11:
  - [174]
  - [164]
  - [165]
  - [20]
  - [22]
  - [94]
  - [97]
  - [98]
  - [105]
  - [104]
  - [123]
  - [126]
  - [148]
  - [156]
  - [163]
  - [188]
  - [78]
  - [5]
  - [19]
  - [38]
  - [60]

- [64]
- [67]
- [73]
- [84]
- [110]
- [135]
- [147]
- [172]
- [13]
- [66]
- 2. C++14:
  - [63]•
  - [68]
  - [79]
  - [109]
  - [116]
  - [44]
  - [106]
  - [107]
  - [114] Important.
  - [168]
  - [34]
  - [39]
  - [57]
  - [65]
  - [74]
  - [167]
  - [166]

  - [50]
- 3. *C++17*:
  - [108]
  - [40]
  - [80]
  - [117]
  - [137]
  - [143]
  - [159]
- 4. Other books/references that may over modern C++:
  - [11]
  - [122]
  - [36]
  - [128]
  - [161]
  - [173]
  - [12]

```
• [33]
```

- [49]
- [136]
- [48]
- [113]
- [130]
- [157]
- [185]
- [35]
- [43]
- [54]
- [61]
- [101]
- [102]
- [103]
- [125]
- 5. Other helpful resources for C++:
  - [53] used with R
  - [93]
  - [115]

### 6.1 Resources for C++ and Notes About C++

Some C++ resources are:

- 1. Online C++ tutorial reference: [26, 27, 29, 160]: http://www.cplusplus.com/reference/stl/
- 2. Pointers to functions [27]: http://www.cplusplus.com/doc/tutorial/pointers/
- 3. An online C++ reference: [30].
- 4. From an online Marshall Cline resource: [23–25]
- 5. Books on C++: [92,133]; processed for C++ templates
- 6. Embedded C++: [87]
- 7. GUI and other graphics with C++: [133]
- 8. Summaries of C++: [83]

Some C++ STL resources are:

- 1. Online C++ STL reference: [28]: http://www.cplusplus.com/reference/stl/
- 2. [30]: http://en.cppreference.com/w/cpp/container
- 3. From an online C++ STL resource from SGI (formerly, Silicon Graphics, Inc.): [71,72].
- 4. Another online C++ STL reference: [118]: http://www.tutorialspoint.com/cplusplus/cpp\_stl\_tutorial.htm
- 5. Other online C++ STL references: [139, 140].
- 6. http://www.cs.wustl.edu/~schmidt/PDF/stl4.pdf

Books to classify:

1. C++ programming: [73, 134, 142, 146, 151, 152]

References for C++ libraries of interest:

1. Boost C++: [85, 121, 131, 149]

- 2. Other libraries that can be considered include: cpp-netlib: The C++ Network Library; nana; FLTK; gtkmm; Qt; evince; glibmm; cairomm; opencv; Ogre3D; OpenGL; CGAL; QuantLib; Google Test; and cppunit.
- 3. E.g., see http://en.cppreference.com/w/cpp/links/libs [30, Useful resources: List of C++ libraries A list of open source C++ libraries].

#### C++ topics:

- 1. Function objects:
  - (a) https://en.wikipedia.org/wiki/Functional\_(C%2B%2B)
  - (b) http://stackoverflow.com/questions/356950/c-functors-and-their-uses
  - (c) http://www.cprogramming.com/tutorial/functors-function-objects-in-c++.html
  - (d) [84, pp. 233–243]
  - (e) [134, pp. 327–332, 885, 922–931, 947]
  - (f) [151, pp. 126–129]. Function pointers are pointers to functions; note that these functions are not variables.

### 2. Strings:

- (a) [164], Chp 23
- (b) [162], Chp 23
- (c) [65], Chp 18
- (d) [5], Chp 19
- (e) [73, pp. 56–60, string data types, variable vs. literal; strings and string class, 13, 82–87, 320–324, 363–365, 496]
- (f) [84, 655–716]
- (g) [146, pp. 64–67, 320–325, 465–482]
- (h) [150, §14.2]
- (i) [134, pp. 114–131]
- (j) [52], Chp 1
- (k) [70]:
  - i. The put pointer points "to the next free byte in the stringstream." That is, it "holds the address of the next byte in the output area of the" stringstream. When the stringstream is empty, the put pointer points to the beginning of the stringstream buffer. [70, §9.8].
  - ii. "The type of the put pointer" does not matter to the software developer(s), since they "cannot access it directly" [70, §9.8].
  - iii. "The get pointer holds the address of the next byte in the input area of the stream, or the next byte we get if we use >> to read data from the stringstream" [70, §9.9].
  - iv. "The end pointer indicates the end of the stringstream. Attempting to read anything at or after this position will cause the read to fail because there is nothing else to read" [70, §9.9].
  - v. Developers only have to know about how put, get, and end pointers work. They do not have to know the actual representation of these pointers [70, §9.9].
  - vi. The stringstream object acts as a buffer, and is "an area of allocated memory" ("by the stringstream member functions") [70, §9.9].
- (1) [111]:
  - i. C strings (or C-strings, or C-style strings) are null-terminated strings (arrays of characters that each end with a terminating "null character" with ASCII value 0) and are arrays of characters; the "null character" is usually represented by the literal character '\0'. "However, an array of char is NOT by itself a C string."

- ii. "Since char is a built-in data type, no header file is required to create a C string. The C library header file <cstring> contains a number of utility functions that operate on C strings."
- iii. "It is also possible to declare a C string as a pointer to a char: char\* s3 = "hello"; " It creates a character array with just enough memory space (in the heap) to store the null-terminated string. The address of the string's first character is placed in the char pointer s3. When this improperly used, it can corrupt program memory or cause run-time errors.
- iv. "[Use] the C library function strlen()" to determine "the length of a C string." It returns an unsigned integer representing the number of characters in the string, excluding the terminating null character.
- v. Relational operators (such as ==,!=,>,<,>=,<=) compare the addresses of the first characters in the two string operands (as the array names are treated as pointers), instead of the contents of these strings.
- vi. "Use the C library function strcmp()" "to compare the contents of two C strings." The input arguments of this function are two pointers to C strings.
- vii. "Use the C library function strcpy()" to assign a string to a C string or change its contents. The strcpy() function accepts a pointer to the C string as the first input argument, and a pointer to the contents of a valid C string or string literal (i.e., a character) as the second input argument. The C library function strcat() has the same input arguments as strcpy(), and is used for concatenating two strings.
- viii. C strings can be used as input parameters or the return type. They are specified as char[] or char\*.
- ix. "A C++ string is an object of the class string, which is defined in the header file <string> and which is in the standard namespace." The variable name of a C++ string is a pointer to the first character of the string; the variable name contains the address of the string's first character. The C++ string is a dynamically-allocated array of characters.
- x. "[Use] the string class methods length() or size()" to determine "the length of the C++ strings."
- xi. To improve memory efficiency and reduce memory usage, explicitly *pass a string object*. Else, the C++ string objects are pass and returned by value, which involves making a copy of the string object.
- xii. Concatenate C++ strings, C strings, and string literals in any order using the "+" operator.
- xiii. Convert a C++ string into a C string via the c\_str() function of the string class. The c\_str() function returns a pointer to the array of characters representing the string. If the C++ string is not null-terminated, a null character is appended to the new C string. The returned C string "can be used, printed, copied, etc." but not be modified.
- xiv. Since programming with arrays can enbug the code more easily, the use of C++ string is (strongly) recommended for use. This is because the properties of a2
- xv. When a C string is required by a function, convert the C++ string into a C string (as aforementioned). Instances in which a C string have to be converted into a C++ string are:
  - A. Strings passed into main() as C strings from the command line argument.
  - B. Functions for file input/output operations require filenames to be specified as C strings.
  - C. The C++ string class does not have the equivalent functions of certain C string library functions.
  - D. Unlike C++ strings, C strings can be serialized in binary format without requiring a bunch of extra code to be written.
- xvi. The function atoi converts a string to an integer. Similar functions for converting

strings into numbers are: atol and atof. The C++ STL does not have a itoa function to convert a number to an integer. However, some compilers supports this function in the C Standard General Utilities Library.

- (m) The function strtol converts a string into a long integer:
  - i. See http://www.cplusplus.com/reference/cstdlib/strtol/.
  - ii. [28, <cstdlib> (stdlib.h) C Standard General Utilities Library: strtol function]
- (n) Danny Kalev, "String Streams," in *InformIT: The Trusted Technology Learning Source: Articles: Programming: C/C++ Articles: InformIT C++ Reference Guide*, Pearson Education, Indianapolis, IN, January 1, 2003. Available online at: http://www.informit.com/guides/content.aspx?g=cplusplus&seqNum=72; last accessed on November 13, 2015.
  - i. Static buffers (via atoi(), sprintf(), or sscanf() from the  $\langle stdio.h \rangle$ ) for type conversions can cause buffer overflow and do not provide adequate type safety (i.e., adequate type checking mechanism). This can be mitigated via stringstreams.

#### 3. IO Streams:

- (a) [65], Chp 12
- (b) [164], Chp 10-11
- (c) [97], Chp 8
- (d) [5], Chp 28
- (e) [60, chp. 12].
- (f) [73, Chp. 8, pp. 351–388; pp. 4, 12–15, 49–51, 150–154, 352, 361–365, 497–498]
- (g) [84, pp. 743–847]
- (h) [135], Chp 17q
- (i) [61, Chp. 13].
- (j) [59], Chp 12.
- (k) [146, §2.2; Chp. 6]
- (l) [162], Chp 10-11
- (m) [150, §14.3-14.8]
- (n) [134, pp. 262–273]
- (o) [52], Chp 2
- (p) [124], Chp 16
- (q) [153], Chp 21
- (r) [152, Chp. 18, pp. 417–450; Appendix A, pp. 563–580]
- (s) [171], Chp 10
- (t) [151, Chp. 8–9, pp. 187–235; Chp. 20–21, pp. 511–568]

#### 4. Templates:

- (a) [65], Chp 11,21
- (b) [164], Chp 19
- (c) [97], Chp 16
- (d) [5], Chp 29
- (e) [60, §16.2–§16.4]
- (f) [84, pp. 13, 26–27, 33–34, 36, 62, 68, 1024]
- (g) [61, §16.2–§16.4]
- (h) [146, Chp. 17]
- (i) [162], Chp 19
- (j) [133, §6.16, pp. 193–195]
- (k) [1], book

- (l) [134, pp. –]
- (m) [52], Chp 3
- (n) [124], Chp 24
- (o) [153], Chp 18
- (p) [152, Chp. 16, pp. 375–394]
- (q) [170], book
- (r) [4], book; typelist Chp 3
- (s) [171], Chp 6
- (t) [51], Chp 16
- (u) [151, Chp. 18, pp. 461–487]
- (v) References:
  - i. [120] recommends including the implementation file (.cpp), instead of the header file (.hpp) in any C++ file that uses the C++ template.
  - ii. [14] argues for separating the C++ template definitions in the header file (.hpp) from the C++ template implementations in the implementation file (.cpp).
  - iii. "Although standard C++ has no such requirement, some compilers require that all function and class templates need to be made available in every translation unit they are used. In effect, for those compilers, the bodies of template functions must be made available in a header file. To repeat: that means those compilers won't allow them to be defined in non-header files such as .cpp files.... There is an export keyword which is supposed to mitigate this problem, but it's nowhere close to being portable." [62]
  - iv. [15] argues that you can merge the definition and implementation in a single file, which ends with the .hpp file extension.
  - v. [41,45] argue that both the definition and the implementation of C++ templates should be placed together in the C++ header file, with white space
  - vi. This is a list of different implementations of a C++ template:
    - A. Implemented with C++ template definition and implementation in one file, where the definition and implementation are clearly separated/distinguished/demarcated. The implementation is appended to the end of the definition, with some white space to separate them [41, 45, 62].
    - B. Implemented with merged C++ template definition and implementation in one file [15].
    - C. Implemented with C++ template definition and implementation separately in different files: a C++ header file and a C++ implementation file. Any file that uses this C++ template will have to import the C++ implementation file, instead of the C++ header file [14,120]. I shall use this method. This clearly decouples the C++ template definition and implementation separately into different files, and keeps things modular in my software architecture. It prevents templates from being huge monoliths.
- 5. Debugging:
  - (a) [52], Chp 11 (especially memory management problems, pp. 533)
- 6. STL, books on C++ STL:
  - (a) [60, §16.5, 983–996]
  - (b) [84]
  - (c) [146, Chp. 18, pp. 943–998]
  - (d) [138]
  - (e) [134, Chp. 16, pp. 877–922, 930–940]

```
(f) [152, Chp. 21, 499–545]
    (g) [141]
    (h) [82]
 7. STL containers:
    (a) [65], Chp 15-16
    (b) [97], Chp 9,11
     (c) [5], Chp 18
    (d) [135], Chp 16
     (e) [55]:
          i. vector<int> v(10); // Create an int vector of size 10.
         ii. v[5] = 10; // Target of this assignment is the return value of operator/.
         iii. Determine how to operate with a pointer to a vector of pointers:
             A. vector < object^* > *connections;
             B. object* oneObject = new object;
             C. connections—>push_back(oneObject);
             D. (*connections)[0]->Initialize(index);
     (f) [146, §18.2, pp. 960–977]
    (g) [138], book
    (h) [150, Chp. 8]
     (i) [154], Chp 8
     (j) [52], Chp 4
    (k) [124], Chp 25
     (l) [171], Chp 7
    (m) [151, Chp. 24, pp. 625–691; Chp. 25–38, pp. 695–927]
8. STL algorithms:
    (a) [65], Chp 15,17
    (b) [97], Chp 10
     (c) [5], Chp 18
    (d) [135], Chp 16
     (e) [146, §18.3, pp. 977-991]
     (f) [138], book
    (g) [52], Chp 5
    (h) [124], Chp 25
     (i) [171], Chp 7
9. Function addresses:
    (a) [164], Chp 8
    (b) [162], Chp 8
    (c) [134, pp. 330–331]
    (d) [51], Chp 3, pp. 213
10. Dynamic memory management problems:
    (a) [65], Chp 10,22
    (b) [97], Chp 12,13
```

(c) [5], Chp 14

(d) [60, §13.9, 750–754].

(e) [135], Chp 9,12

(f) [59], Chp 13.

- (g) [112], Chp 2-4
- (h) [134, Chp. 9, pp. 393–423; Chp. 12, pp. 562–606; Chp. 13, pp. 677–685]
- (i) [142, §3.1; §8.1]
- (j) [153], Chp 29
- (k) [51], Chp 6,13
- (l) [151, pp. 349–359]

### 11. Function overloading:

- (a) [164], Chp 8
- (b) [60, §6.14, pp. 356–360].
- (c) [61, §6.14, pp. 359–363].
- (d) [59], Chp 6.
- (e) [146, §4.4, pp. 230–243]
- (f) [162], Chp 8
- (g) [134, pp. 216–217, 365–370]. Function overloading is also known as function polymorphism [134, pp. 388].
- (h) [153], Chp 14
- (i) [51], Chp 7
- (j) [151, Chp. 14, pp. 361–384]

### 12. Operator overloading:

- (a) [97], Chp 14
- (b) [146, §11.2, pp. 633–651]
- (c) [134, pp. 502–515, 524–537]
- (d) [124], Chp 18
- (e) [153], Chp 15
- (f) [152, Chp. 13, pp. 299–330]
- (g) [51], Chp 12
- (h) [151, Chp. 15, pp. 385–418]

#### 13. Constants:

- (a) [51], Chp 8
- 14. Functions and pointers:
  - (a) See [132, §7.2-7.4] regarding passing arguments by value, reference, and by address.
  - (b) [164], Chp 8:
    - i. Pass-by-reference:
      - A. e.g., void init(vector<double> &v)
      - B. "It is not possible to refer directly to a reference variable after it is defined; any occurrence of its name refers directly to the variable it references."
      - C. "Once a reference is created, it cannot be later made to reference another variable.

        This is something that is often done with pointers."
      - D. "References cannot be null, whereas pointers can; every reference refers to some variable, although it may or may not be valid."
      - E. "References cannot be uninitialized. Because it is impossible to reinitialize a reference, they must be initialized as soon as they are created. In particular, local and global variables must be initialized where they are defined, and references which are data members of a class must be initialized in the initializer list of the class's constructor."

- F. Avoid mixing references and pointers in a block of code to avoid confusion, and make it easier for the C++ code to be read and debug.
- G. The required syntax for pointers make them prominent in comparison to that of references.
- H. The number of operations on references is less than that on pointers. Hence, usage of references is easier to understand than that of pointers. Consequently, it is easier to use references than pointers without enbugging the code.
- I. Pointers can be invalidated as follows:
  - "Carrying a null value"
  - "Out-of-bounds [pointer] arithmetic"
  - Illegal casts on pointers
  - Produce pointers from random integers
- J. References can be invalidated as follows:
  - "[Refer] to a variable with automatic allocation which goes out of scope"
  - "[Refer] to an object inside a block of dynamic memory which has been freed"
- K. "Arrays are always passed by address. This includes C strings."
- L. "Dynamic storage is allocated using pointers."
- M. Reference: Kurt McMahon, "Passing Variables by Address," in Northern Illinois University: College of Engineering and Engineering Technology: Department of Computer Science: CSCI 241 Intermediate Programming in C++ (Fall 2015): Notes, Northern Illinois University, DeKalb, IL, October 28, 2015. Available online at: http://faculty.cs.niu.edu/~mcmahon/CS241/Notes/pass\_by\_address.html; last accessed on November 3, 2015.
- ii. Pass-by-const-reference: e.g., void print(const vector<double> &v)
- iii. Pass-by-value: e.g., void fn(int x)
- iv. Pass-by-address: e.g., void print(int \* ptr)
  - A. Reference: Kurt McMahon, "Passing Variables by Address," in Northern Illinois University: College of Engineering and Engineering Technology: Department of Computer Science: CSCI 241 Intermediate Programming in C++ (Fall 2015): Notes, Northern Illinois University, DeKalb, IL, October 28, 2015. Available online at: http://faculty.cs.niu.edu/~mcmahon/CS241/Notes/pass\_by\_address.html; last accessed on November 3, 2015.
- (c) [97], Chp 6
- (d) [5], Chp 12-13
- (e) [73, Chp. 5, pp. 193–248; Chp. 7, pp. 307–349]
- (f) [135], Chp 7-8
- (g) [146, Chp. 4–5; §11.1; and Chp. 14]
- (h) [162], Chp 8
- (i) [134, Chp. 7–8, pp. 279–391].:
  - i. [134, pp. 382–383] provides information on which function version (from function overloading, function templates, and function template overloading) is chosen by the compiler, during compilation.
  - ii. const member functions (put the const after the function parentheses) guarantees that the invoking object would not be modified.
- (j) [124], Chp 15,20
- (k) [152, Chp. 6–8, pp. 105–179]
- (l) [51], Chp 11:
  - i. use const at the end of accessor functions

- ii. Do not use pointers as instance variables
- (m) [151, Chp. 5–6; pp. 113–160]
- (n) Elsewhere:
  - i. http://stackoverflow.com/questions/1143262/what-is-the-difference-between-const-[119]:
    - A. Read it backwards; the first *const* can be on either side of the type.
    - B. "Read pointer declarations right-to-left."
    - C. From the answer of Ted Dennison, July 17, 2009. Rule: The "const" goes after the thing it applies to. Putting const at the very front (e.g., const int \*) is an exception to the rule.
    - D.  $int^*$  pointer to int
    - E. int const \* == const int \* pointer to const int
    - F. int \* const const pointer to int
    - G. int const \* const == const int \* const const pointer to const int
    - H. int \*\* pointer to pointer to int
    - I. int \*\* const A const pointer to a pointer to an int
    - J. int \* const \* A pointer to a const pointer to an int
    - K. int const \*\* A pointer to a pointer to a const int
    - L. int \* const \* const A const pointer to a const pointer to an int
  - ii. For the following [119], let:  $int \ var\theta = 0$ ;
    - A.  $const\ int\ \&ptr1 = var0;$  // Constant reference
    - B. int \* const ptr2 = &var0; // Constant pointer
    - C. int const \* ptr3 = &var0; // Pointer to const
    - D. const int \* const ptr4 = &var0; // Const pointer to a const
  - iii. [127]:
    - A. "A reference is a variable that refers to something else and can be used as an alias for that something else. A pointer is a variable that stores a memory address, for the purpose of acting as an alias to what is stored at that address. So, a pointer is a reference, but a reference is not necessarily a pointer. Pointers are a particular implementation of the concept of a reference, and the term tends to be used only for languages that give you direct access to the memory address. References can be implemented internally in a language using pointers, or using some other mechanism." Answer from dan1111.
    - B. "Passing an object by value means making a copy of it. You can modify that copy without affecting the original. Making that copy can cost a lot of memory access though. Passing an object by reference means passing a handle to that object. This is cheaper because you don't need to make a copy. It also means that any changes you make will affect the original." Answer from Steve Rowe.
    - C. "There is no such thing as a null reference. A reference must always refer to some object. As a result, if you have a variable whose purpose is to refer to another object, but it is possible that there might not be an object to refer to, you should make the variable a pointer, because then you can set it to null. On the other hand, if the variable must always refer to an object, i.e., if your design does not allow for the possibility that the variable is null, you should probably make the variable a reference." Answer from Harssh S. Shrivastava.
  - iv. A pointer is dereferenced via the explicit \* operator. The \* operator should not be used to dereference a reference (variable) [144].
  - v. [144]:

- A. int \*pi = &i; // Indirect expression to dereference pi to i. "Declare pi as an object of type 'pointer to int' whose initial value is the address of object i" [145].
- B. int &ri = i; // ri is dereferenced to refer to i. "Declares ri as an object of type 'reference to int' referring to i" [145].
- C. The C++ standard does not dictate how compilers shall implement references. However, popular compilers tend to implement references as pointers. Therefore, there are no significant advantages of using references or pointers.
- vi. [145]:
  - A. "A valid reference must refer to an object; a pointer need not. A pointer, even a const pointer, can have a null value. A null pointer doesn't point to anything."
  - B. I can bind a reference to a null pointer, but I cannot dereference a null pointer since it can "produce undefined behavior".
- vii. You cannot call a non-const method from a const method. That would 'discard' the const qualifier.:
  - A. http://stackoverflow.com/questions/2382834/discards-qualifiers-error
- viii. Pointer to constant data: const type\* variable; and type const \* variable;
  - A. http://www.cprogramming.com/reference/pointers/const pointers.html
- ix. Pointer with constant memory address:  $type * const \ variable = some-memory-address;$ A. http://www.cprogramming.com/reference/pointers/const\_pointers.html
- x. Constant data with a constant pointer:  $const\ type\ ^*\ const\ variable = some-memory-address;$  and  $type\ const\ ^*\ const\ variable = some-memory-address;$ 
  - A. http://www.cprogramming.com/reference/pointers/const pointers.html
- (o) With shallow copying, I would only copy the memory references or pointers. The copy and the original reference the same object. On the other hand, with deep copying, I would copy the values; this is also known as cloning. The copy and the original reference do not share objects; each of them references its own object. The default copy constructor carries out shallow copy.

#### 15. Extern function:

- (a) : i.
- (b):
- (b) . i.
- (c) : i.
- (d) : i.
- (e) : i.
- (f):
- i.
- (g) : i.

### 16. typename:

(a) Evan Driscoll, "A Description of the C++ typename keyword," from the Department of Computer Sciences, University of Wisconsin-Madison College of Engineering, University of Wisconsin-Madison, Madison, WI. Available online at: http://pages.cs.wisc.edu/~driscoll/typename.html; last accessed on February 15, 2016.

- (b) From [7, API documentation for Eigen3: The template and typename keywords in C++], or http://eigen.tuxfamily.org/dox/TopicTemplateKeyword.html.
- (c) Wikipedia contributors, "typename," in *Wikipedia, The Free Encyclopedia: C++*, Wikimedia Foundation, San Francisco, CA, April 13, 2015. Available online at: https://en.wikipedia.org/wiki/Typename; last accessed on February 15, 2016.:
  - i. Usage #1: "A synonym for 'class' in template parameters"
  - ii. Usage #2: "A method for indicating that a dependent name is a type"
- (d) [146, pp. 916]
- (e)
- (f)
- (g)
- (h)
- (i)
- (j)
- (k)
- 17. OOD and inheritance:
  - (a) [65], Chp 4-9
  - (b) [164], Chp 9
  - (c) [97], Chp 7,15,18,19
  - (d) [5], Chp 24-26
  - (e) [60, Chp. 13–15; Appendices E and J].
  - (f) [73, Chp. 9–10, 389–479]
  - (g) [135], Chp 10-11,13,14,15
  - (h) [61, Chp. 7, 11, 15; Appendices A, D, J, and K].
  - (i) [59], Chp 13,14,15.
  - (j) [146, Chp. 10; §12.1, 696–711; Chp. 15; Chp. 17]
  - (k) [162], Chp 9
  - (l) [134, Chp. 10–14, pp. 445–786]
  - (m) [124], Chp 13-14,21
  - (n) [152, pp. 6–8; Chp. 11–12, pp. 245–298; Chp. 14–15, pp. 331–373]
  - (o) [171], Chp 3-4,8
  - (p) [51], Chp 14,15
  - (q) [151, Chp. 11–12, pp. 255–325; Chp. 16–17, pp. 419–460]
- 18. SW engineering issues:
  - (a) [65], Chp 24-26
  - (b) [5], Chp 21
  - (c) [142, Chp. 4 and 7]
  - (d) Debugging:
    - i. [150, §14.2]
- 19. multi-threading:
  - (a) [154], Chp 3
  - (b) [142, §5.1]
- 20. graphs:
  - (a) [154], Chp 7
- 21. typedef:

- (a) In the sandbox, use the *Make* target make typedef to study an example of how typedef can be used. When the header file defines/specifies the typedef, and is included in the C++ implementation file and other C++ implementation files that instantiates those objects, it can be used subsequently without additional definition/specification. October 6, 2015.
- (b) [146, pp. 510-512]

I am skipping topics, such as: run-time type ID and casting operators [152, Chp. 19, pp. 451–470]; namespaces [152, pp. 472–480]; #error C++ preprocessor [152, pp. 552]; #line C++ preprocessor [152, pp. 558]; #pragma C++ preprocessor [152, pp. 559]; ## C++ preprocessor operator [152, pp. 559–560]; and C++ predefined macro names [152, pp. 560–561].

# 6.2 Computational Complexity of C++ Containers

Table 6.1 shows a tabulated summary of containers in the C++ Standard Template Library (STL) and the computational complexity for each of their common operations: add(element e), remove(element e), search(element e), size(), empty(), begin(), and end().

Container \ Complexity	add	remove	search	size	empty	begin	end
vector	O(1)	O(n)	O(n)	O(1)	O(1)	O(1)	O(1)
list	O(1)	O(n)	O(n)	O(1)	O(1)	O(1)	O(1)
queue	O(1) amortized	O(1)	O(n)	O(1)	O(1)	O(1)	O(1)
priority queue	O(log n)	O(log n)	$O(\log n)$ ???, or $O(n)$	O(1)	O(1)	O(1)	???
set	O(log n)	O(log n)	O(log n)	O(1)	O(1)	O(1)	O(1)
multi-set	O(log n)	???	O(log n)	O(1)	O(1)	O(1)	O(1)
map	O(log n)	O(log n)	O(log n)	O(1)	O(1)	O(1)	O(1)
multi-map	O(log n)	???	O(log n)	O(1)	O(1)	O(1)	O(1)
stack	O(1)	O(1)	O(n)	O(1)	O(1)	O(1)	O(1)

Table 6.1: Computational Complexity of Basic Operations of Containers from the C++ STL.

To conclude, we can get some facts about each data structure:

- 1. std::list is very very slow to iterate through the collection due to its very poor spatial locality.
- 2. std::vector and std::deque perform always faster than std::list with very small data
- 3. std::list handles very well large elements
- 4. std::deque performs better than a std::vector for inserting at random positions (especially at the front, which is constant time)
- 5. std::deque and std::vector do not support very well data types with high cost of copy/assignment

This draws simple conclusions on the usage of each data structure [21,82]:

- 1. Number crunching: use std::vector or std::deque
- 2. Linear search: use std::vector or std::deque
- 3. Random Insert/Remove:
- 4. Small data size: use std::vector
- 5. Large element size: use std::list (unless if intended principally for searching)

- 6. Non-trivial data type: use std::list unless you need the container especially for searching. But for multiple modifications of the container, it will be very slow.
- 7. Push to front: use std::deque or std::list

#### Notes about asymptotic notations:

- 1. Comparison of big O notations, and other asymptotic notations, in general based on "running time (T(n))" [Wikipedia 2015a][Wikipedia 2015]:
  - (a) O(1): constant time
  - (b)  $O(\log^* n)$ , log star: iterated logarithmic time.

Log star n is a recursive function;  $\log^* n := \begin{cases} 0 & \text{: if } n \leq 1 \\ 1 + \log^*(\log n) & \text{: if } n > 1 \end{cases}$  [Wikipedia 2015b]

- (c)  $O(\log \log n)$ : log-logarithmic, double logarithmic
- (d)  $O(\log n)$ : logarithmic time, computational time complexity class DLOGTIME. E.g.,  $\log n^2$ .
- (e) poly(log n) or  $O((\log n)^c)$ , c > 1: polylogarithmic time. E.g.,  $(\log n)^2$ .
- (f)  $O(n^c)$ , where 0 < c < 1: fractional power. E.g.,  $n^{\frac{2}{3}}$ .
- (g) o(n): sub-linear time (or sublinear time)
- (h) O(n): linear time
- (i)  $O(n \log^* n)$ : "n log star n" time, or "n log-star n"
- (j)  $O(n \log n) = O(\log n!)$ : linearithmic time, including  $\log n!$ . Or, loglinear, or quasilinear.
- (k)  $O(n^2)$ : quadratic time
- (l)  $O(n^3)$ : cubic time
- (m) poly(n), or  $2^{O(\log n)}$ . Or,  $O(n^c)$ , c > 1: polynomial time, including  $n, n \log n, n^{10}$ . Computational time complexity class P. Or, algebraic.
- (n)  $2^{\text{poly}(\log n)}$ : quasi-polynomial time, including  $n^{\log \log n}$ ,  $n^{\log n}$ . Computational time complexity class QP.
- (o)  $O(2^{n^{\varepsilon}})$ ,  $\forall \varepsilon > 0$ : sub-exponential time, including  $O(2^{\log n^{\log \log n}})$ . Computational time complexity class SUBEXP.
- (p)  $2^{o(n)}$ : sub-exponential time, including  $2^{n^{\frac{1}{3}}}$ . Computational time complexity class SUBEXP. Or, L-notation.
- (q)  $2^{O(n)}$ : exponential time (with linear exponent), including  $1.1^n, 10^n$ . Computational time complexity class E.
- (r)  $2^{\text{poly}(n)}$ . Or,  $O(c^n)$ , c > 1: exponential time, including  $2^n$ ,  $2^{n^2}$ . Computational time complexity class EXPTIME.
- (s) O(n!): factorial time, including n!.
- (t)  $2^{2^{\text{poly}(n)}}$ : double exponential time, including  $2^{2^n}$ . Computational time complexity class 2-EXPTIME.
- (u)  $n! > n^n$
- 2. Types of asymptotic notations [Wikipedia 2015]:
  - (a) f(n) = O(g(n)): Big O notation, or Big Oh notation
  - (b)  $f(n) = \Omega(g(n))$ : Big Omega notation
  - (c)  $f(n) = \Theta(g(n))$ : Big Theta notation
  - (d) f(n) = o(g(n)): Small O notation, or Small Oh notation
  - (e)  $f(n) = \omega(g(n))$ : Small Omega notation
  - (f)  $f(n) \sim g(n)$ : "On the order of"
- 3. References:

- (a) [Wikipedia 2015] Wikipedia contributors, "Big O notation," sections Orders of common functions and Related asymptotic notations: Family of Bachmann?Landau notations, in Wikipedia, The Free Encyclopedia: Analysis of algorithms, or Asymptotic analysis, Wikimedia Foundation, San Francisco, CA, November 29, 2015. Available online at: https://en.wikipedia.org/wiki/Big\_0\_notation#Orders\_of\_common\_functions; last accessed on December 1, 2015.
- (b) [Wikipedia 2015a] Wikipedia contributors, "Time complexity," section *Table of common time complexities*, in *Wikipedia, The Free Encyclopedia: Computational complexity theory*, Wikimedia Foundation, San Francisco, CA, November 16, 2015. Available online at: https://en.wikipedia.org/wiki/Time\_complexity#Table\_of\_common\_time\_complexities; last accessed on December 1, 2015.
- (c) [Wikipedia 2015b] Wikipedia contributors, "Iterated logarithm," in *Wikipedia, The Free Encyclopedia: Asymptotic analysis*, Wikimedia Foundation, San Francisco, CA, November 6, 2015. Available online at: https://en.wikipedia.org/wiki/Iterated\_logarithm; last accessed on December 1, 2015.
- 4. Note that I denote "is defined as" as:  $\equiv$ ,  $\stackrel{\triangle}{=}$ ,  $\stackrel{\text{def}}{=}$ , :=
- 5. Note that  $\log n$  is faster than  $(\log n)^2$ , although initially the latter is slightly faster than the former (for negligibly small n).

Books on computational complexity:

1. [84, pp.10–11]

### 6.3 Additional Notes About C++

Static variables:

1. K. Hong, "Static Variables and Static Class Members - 2015," San Francisco, CA. Available online from Open Source . . . : Java/C++/Python/Android/Design Patterns: C++ Tutorial Home - 2015 at: http://www.bogotobogo.com/cplusplus/statics.php; last accessed on October 23, 2015.

#### Formatting data:

- 1. Synesis Software Pty Ltd staff, "Synesis Software Training Courses: FastFormat, Beginner's (part 1 of 2)," Synesis Software Pty Ltd, Sydney, Australia, 2015. Available online at: http://www.synesis.com.au/training-beginners-fastformat.html; December 1, 2015 was the last accessed date.
  - (a) "Formatting APIs":
    - i. "Replacement-based APIs":
      - A. "Streams (printf()-family)"
      - B. "Boost.Format"
      - C. "FastFormat.Format"
    - ii. "Concatenation-based APIs":
      - A. "IOStreams"
      - B. "Loki.SafeFormat"
      - C. "FastFormat.Write"
  - (b) "struct tm"
  - (c) "struct in\_addr"
  - (d) "ATL types"
  - (e) "ACE types"

- 2. Synesis Software Pty Ltd staff, "Synesis Software Training Courses: FastFormat, Advanced (part 2 of 2)," Synesis Software Pty Ltd, Sydney, Australia, 2015. Available online at: http://www.synesis.com.au/training-advanced-fastformat.html; December 1, 2015 was the last accessed date.
  - (a) "Format-specification Defect Handling": "Scoping" and "Disgnostic Logging"

# 6.3.1 Alternate Computer Number System for Representing Fractions in C++

An alternate computer number system for representing fractions in C++ is the fixed-point number system. For a detailed classification of computer number systems, see [100].

In C++, the numerical data types are based on cardinal numbers (e.g., one, two, three, ...), instead of ordinal numbers/integers (e.g., first, second, third, ...); see [46,129,187] for the definitions of "cardinal number" and "ordinal number." From [129], "a Nominal Number is a number used only as a name, or to identify something (not as an actual value or position)." E.g., "the number on the back of a footballer ("8")," "a postal code ("91210")," and "a model number ("380")."

Resources to help me implement the fixed-point "data type" as a class in C++, and fixed-point arithmetic:

1.

## 6.4 Software Development in C++

Notes about software development in C++:

- 1. Notes from Synesis Software Pty Ltd:
  - (a) Synesis Software Pty Ltd staff, "Synesis Software Training Courses," Synesis Software Pty Ltd, Sydney, Australia, 2015. Available online at: http://www.synesis.com.au/training.html; December 1, 2015 was the last accessed date.
    - i. Use FastFormat as a "C++ diagnostic logging API library"
    - ii. STLSoft libraries. "Apply the concepts, principles and techniques of Extended STL to enhance the expressiveness, flexibility, and performance of your C++ software." See [186] for more details.
    - iii. "Building Bullet-Proof Software in C++ no system built by Synesis Software has ever failed in production. This course takes you through the principles and practices of how we develop software, providing you with practical, applicable strategies and tactics for achieving the same outcome in your software developments."
    - iv. "Guerilla Testing C++ or, 'How to discover the Gold Nuggets in your Big Ball of Mud'. No matter how badly a C++ codebase is enmeshed, you can get it under test if you know how to master its coupling."
  - (b) Synesis Software Pty Ltd staff, "Resources," Synesis Software Pty Ltd, Sydney, Australia. Available online at: http://www.synesis.com.au/resources.html; December 1, 2015 was the last accessed date.
    - i. 100% type-safe C++ API
    - ii. C++ diagnostic logging API library (or, diagnostic logging libraries):
      - A. Pantheios: http://pantheios.org/
      - B. ACE

- C. log4cxx
- iii. C++ formatting library: FastFormat http://fastformat.org/
- iv. "The STLSoft libraries provide STL extensions and facades over operating-system and third-party-library APIs. The libraries are 100% header-only." See http://stlsoft.org/.
- v. "UNIXem is a simple library that emulates a useful subset of the UNIX system APIs on Windows... UNIXem is the only library provided by Synesis Software that is not production-quality. It is appropriate for research, such as when developing tests for cross-platform software." See http://synesis.com.au/software/unixem.html.
- (c) Synesis Software Pty Ltd staff, "Guerilla Testing C++ or, 'How to discover the Gold Nuggets in your Big Ball of Mud'," Synesis Software Pty Ltd, Sydney, Australia. Available online at: http://www.synesis.com.au/training-guerilla-testing-cplusplus.html; December 1, 2015 was the last accessed date.:
  - i. "Change is the most expensive part of the cost of a software project. The biggest impediments to change are lack of clarity on what to alter to effect the change, and uncertainty about unintended side-effects of the change."
  - ii. "No matter how badly a C++ codebase is enmeshed, you can get it under test if you know how to master its coupling."
  - iii. "Many long-lived codebases have evolved to a point where some, perhaps most, aspects of its functionality are no longer precisely known / codified / automatically tested. This course will teach you, using practical examples, how to wrest control from any codebase, no matter how badly enmeshed, isolate known pieces of good functionality, get them under test, and eventually to isolate and separate them into a new context, while, where required, maintaining compatibility with their original context."
  - iv. "This course will teach you how to refactor any codebase with confidence, rather than poking at the edges of its functionality in fear."
  - v. "Release costs" serve as an indicator to the existence of "a Big Ball of Mud."
  - vi. "Factors that inhibit testing":
    - A. "Coupling, coupling, coupling"
    - B. "The inconstant environment"
    - C. "Trust"
    - D. "Defensive code"
    - E. "Fuzzy (or no!) abstraction borders"
  - vii. "Key characteristics" identified in situ: "diagnostics, contracts, code coverage, and testing."
  - viii. Remember the following "when testing mud-balls": "automation; minimalism, incrementality, unit testing vs component testing; coverage (in realistic time); only change what you can test (and are testing!) [there are] exceptions to this rule; beyond salvation sometimes it's just mud."
    - ix. Islands of "known Functionality" are created as follows:
      - A. "Decomposition Identifying Units, Identifying Components, and Identifying Modules"
      - B. "Triage"
      - C. "Isolation"
      - D. "Striding two worlds"
      - E. "Transplantation"
      - F. "Separation"
      - G. "Versioning Static and Dynamic"
      - H. "When to 'throw it out'."
    - x. "Inconstant Environment" handling:

- A. "File system"
- B. "Memory"
- C. "User-interface"
- D. "Time"
- E. "Data storage"
- xi. Techniques to address/mitigate coupling:
  - A. "Pre-processor":
    - #ifdef
    - #define
    - #include
    - "I would recommend putting your include guards above your includes. That way the includes don't get parsed twice for the same file." That is, the preprocessors #ifdef and #define should be placed above the #include statements. This would avoid repetitive parsing of (header) files that are included. Reference: sdsmith, comment to the question "Why is the discrepancy in these two cases of using C++ templates?," Stack Exchange Inc., New York, NY, March 30, 2016. Available online from Stack Exchange Inc.: Stack Overflow: Questions at: http://stackoverflow.com/q/36319028/1531728; March 30, 2016 was the last accessed date [155].
  - B. "linkage":
    - "interpositioning"
    - "dynamic library redirection"
  - C. "object-oriented techniques":
    - "overloading"
    - "overriding"
    - "inheritance"
    - "interfaces"
  - D. "patterns":
    - "class adaptor"
    - "instance adaptor"
    - "decorator"
    - "visitor"
  - E. "generic programming":
    - "policies"
    - "shims"
    - "traits"
  - F. "Testing":
    - "Stubbing"
    - "Mocking"
    - "Versioned testing"

xii. xiv. xv. xv. xvi. xvii. xviii.

2. To obtain the x86 assembly output to a C++ program:

- (a) Reference: Andrew Edgecombe, answer to "How do you get assembler output from C/C++ source in gcc?," Stack Exchange Inc., New York, NY, September 26, 2008 (edited by Prashant Kumar on May 1, 2012). Available online from *Stack Exchange Inc.: Stack Overflow: Questions* at: http://stackoverflow.com/a/137074; March 15, 2016 was the last accessed date.:
  - i. To view the source file: cat /source\_file/
  - ii. To remove all symbol table and relocation information from the executable, the executable for that source file becomes: gcc -s /source\_file.c/:
    - A. Or, try: gcc -S /source\_file.c/
    - B. Alternatively, try: strip [source\_file]
    - C. gcc -g [source\_file.c] adds debugging information to the executable.
  - iii. If access to source files is unavailable, but access to the object file is available, use: objdump -S -disassemble [object\_file] > [object\_file.dump]. Use file [object\_file] to determine if I can get enough information from the object file.:
    - A. gcc -S -o [unassembled\_file.s] [source\_file.c]
    - B. To view the output file from gcc -S: cat |source\_file|
- (b) References: [6, pp. 3, or pp. 15 in the PDF] and Kenneth Finnegan, answer to "How do you get assembler output from C/C++ source in gcc?," Stack Exchange Inc., New York, NY, September 26, 2008. Available online from Stack Exchange Inc.: Stack Overflow: Questions at: http://stackoverflow.com/a/137479; March 16, 2016 was the last accessed date. Also, includes information from comments to this answer by Sundaram Ramaswamy (May 6, 2013) and Luu Vĩnh Phúc (June 7, 2014):
  - i. Create assembly code: c++-S-fverbose-asm-g-02 [ $source\_code.cpp$ ] -o [ $unassem-bled\_file.s$ ]
  - ii. Create assembled code interfaced with source lines: as -alhnd [unassembled\_file.s] > [listing\_file.lst]
  - iii. Alternatively, the on line version on Mac OS X, try:
    - A. g++-g-00-c-fverbose-asm-Wa,-adhln-test.cpp > test.lst
    - B. gcc -c -g -Wa, -ahl=test.s test.c
    - C. gcc -c -g -Wa,-a,-ad [other GCC options] test.c > test.txt
- (c) Reference: Cr McDonough, answer to "How do you get assembler output from C/C++ source in gcc?," Stack Exchange Inc., New York, NY, September 29, 2013. Available online from *Stack Exchange Inc.: Stack Overflow: Questions* at: http://stackoverflow.com/a/19083877; March 16, 2016 was the last accessed date.
  - i. g++ -g -0 -Wa,-aslh horton\_ex2\_05.cpp > list.txt
- (d) Reference: Andrew Pennebaker, answer to "How do you get assembler output from C/C++ source in gcc?," Stack Exchange Inc., New York, NY, February 6, 2013. Available online from Stack Exchange Inc.: Stack Overflow: Questions at: http://stackoverflow.com/a/7871911; March 16, 2016 was the last accessed date. Also, comment from Grady Player (February 6, 2013) is helpful.
  - i. To get the LLVM assembly code, try: 11vm-gcc -emit-11vm -S hello.c
  - ii. I can also use the same command for clang.

### 6.4.1 Using "Design By Contract"

The "Design By Contract" approach shall be used in software development. This approach is also known as: "contract programming, programming by contract, and design-by-contract programming." Adhere strongly to Hoare logic.

#### References:

Wikipedia contributors, "Design by contract," in *Wikipedia, The Free Encyclopedia: Software design*, Wikimedia Foundation, San Francisco, CA, January 20, 2016. Available online at: https://en.wikipedia.org/wiki/Design\_by\_contract; last accessed on February 9, 2016.

Wikipedia contributors, "Hoare logic," in *Wikipedia, The Free Encyclopedia: Static program analysis*, Wikimedia Foundation, San Francisco, CA, November 8, 2015. Available online at: https://en.wikipedia.org/wiki/Hoare\_logic; last accessed on February 10, 2016.

That is, at the start of an implementation of a (C++) function, check that its precondition(s) is (/are) met; preconditions shall be chosen to be as weak as possible. Within the implementation of the function, check if the assertions (properties that must be true during execution of the function) hold. Lastly, at the end of the implementation, check that its postcondition(s) is (/are) met; postconditions shall be chosen to be as strong as possible.

#### Reference:

Wikipedia contributors, "Predicate transformer semantics," in *Wikipedia, The Free Encyclopedia: Formal methods*, Wikimedia Foundation, San Francisco, CA, November 25, 2015. Available online at: https://en.wikipedia.org/wiki/Predicate\_transformer\_semantics; last accessed on February 10, 2016.

#### 6.4.1.1 Hoare Logic for Computer Arithmetic

Check if arithmetic and logical operations cause overflows or underflows [31, 32]. When faced with a constrained range for representing real numbers with bits in computer hardware, a constrained resolution such that a representation smaller than single-precision floating-point numbers is required, or low-cost and/or low-power electronic/computer systems that do not have floating-point arithmetic circuits, use a circuit-based implementation of fixed-point arithmetic.

### 6.4.2 Debugging C++ Software

This section covers debugging syntax errors (in  $\S6.4.2.1$ ) that are reported by C++ compilers. It also covers semantic errors that can be discovered via software testing and formal verification tools; see [42,  $\S4.4$ , pp. 119]. In addition, it includes performance debugging [42,  $\S4.5$ , pp. 119–120], using software profilers [56, Figure 7.1, pp. 292; and  $\S7.2.10$ , pp. 302] [88, pp. 148] [95, pp. 35-9 – 35-10] [57,  $\S3.2$ , pp. 16–18] [8,  $\S3.3.2$ , pp. 21–22; pp. 23; Figure 40, pp. 102; Appendix C,  $\SC.1.7$ , pp. 104] and static analysis software [8,  $\S5.4$ , 65-66; and Figure 40, pp. 102] [3] [9,  $\S7.1$ , 176–183] [37,  $\S5.2.4$ , pp. 82–83; and  $\S5.4.2$ , pp. 90–92] [58, Chapter 7, pp. 109–117] [95,  $\S35.5$ , pp. 35-10 – 35-14] [18]. These phases cannot be highly overlapped consider by more than a significant amount.

To functionally debug software with success, these four steps should be carried out: "test input generation, error detection, error diagnosis, and error correction" [89].

#### 6.4.2.1 Interpreting C++ Compilation Errors

A missing semiconlon ";", or lack of matching curly braces "}" (or parentheses ")", square brackets "]", or angle brackets ">"), can cause a lot of compilation errors [75].

### 6.4.3 Parser Development

Parser development via Lex/Yacc, Flex/Bison, ANTLR, Parsec, Ragel, Spirit Parser Framework, Jet-PAG (Jet Parser Auto-Generator), Monkey, MyParser, SableCC, . . .

Reference: Wikipedia contributors, "Comparison of parser generators," in *Wikipedia, The Free Encyclopedia: Parser generators*, Wikimedia Foundation, San Francisco, CA, February 18, 2016. Available online at: https://en.wikipedia.org/wiki/Comparison\_of\_parser\_generators; last accessed on February 18, 2016.

```
Determine if LLVM can be used for parser development. An example of a C++ parser is shown in [151, Chp. 40, pp. 959–993].
```

# 6.5 Parallel Programming in C++

Resources for parallel programming in C++:

1. C++ -based MPI programming: [86]

## 6.6 Numerical Computing in C++

Numerical computing resources for C++:

1. Scientific computing: [130]

2.

# Chapter 7

# Questions

# 7.1 Unresolved C++ Questions

Questions about C++:

1.

### 7.2 Resolved C++ Questions

Difference between pointers and references:

- 1. Yusuf Kemal Özcan ("BFaceCoder"), "Is there any difference between pointers and references? [duplicate]," Stack Exchange Inc., New York, NY, April 18, 2013. Available online from Stack Exchange Inc.: Programmers Stack Exchange: Questions at: http://programmers.stackexchange.com/questions/195337/is-there-any-difference-between-pointers-and-references; October 6, 2015 was the last accessed date.
  - (a) Answer from dan1111, April 18, 2013: http://programmers.stackexchange.com/a/195343 and http://programmers.stackexchange.com/questions/195337/is-there-any-difference-be 195343#195343.

(b)

- 2. Macneil Shonle and Programmers Stack Exchange contributors, "What's a nice explanation for pointers? [closed]," Stack Exchange Inc., New York, NY, July 30, 2015. Available online from Stack Exchange Inc.: Programmers Stack Exchange: Questions at: http://programmers.stackexchange.com/questions/17898/whats-a-nice-explanation-for-pointers; October 6, 2015 was the last accessed date.
  - (a) Answer from Kevin, November 10, 2010: http://programmers.stackexchange.com/a/17919 and http://programmers.stackexchange.com/questions/17898/whats-a-nice-explanation-fo 17919#17919. "A pointer is a variable that contains an address to a variable. A pointer is both defined and dereferenced (yielding the value stored at the memory location that it points to) with the '\*' operator; the expression is mnemonic." ... char (\*(x())[])()
  - (b) Answer from Barfield, November 10, 2010: http://programmers.stackexchange.com/a/ 18087 and http://programmers.stackexchange.com/questions/17898/whats-a-nice-explanations/18087#18087. "Pointer[s] are a bit like the application shortcuts on your desktop."
  - (c) Answer from Gulshan, November 10, 2010: http://programmers.stackexchange.com/a/17915 and http://programmers.stackexchange.com/questions/17898/whats-a-nice-explanate 17915#17915. Pointers point to instance and static variables. A pointer can point to different variables during the execution of the program, but must point to one variable at

any instance (i.e., point in time) during execution. Also, the pointer must point to variables of the same type. Associate a pointer with a variable via the reference to the variable; e.g., int \*pointer; pointer = & variable; ... According to Ptolemy, December 2, 2010: http://programmers.stackexchange.com/a/23016. int \*pointer = & variable; creates a pointer to the variable. ... Dereference the pointer (add \* as a prefix) to store the value of an expression (based on variables, strings, or constants). According to Ptolemy, & variable is the "address of the variable" and it "represents the literal value for" the pointer. "The pointer" refers to the data that the pointer points to, or something "pointed to by" the pointer.

- (d) Answer from Sridhar Iyer, November 11, 2010: http://programmers.stackexchange.com/a/18529 and http://programmers.stackexchange.com/questions/17898/whats-a-nice-explana 18529#18529. A "pointer is a variable that store[s] the address of another variable (or just any variable). \* is used to get the value at the memory location that is stored in the pointer variable. & operator gives the address of a memory location."
- (e) Answer from rwong, November 2, 2010: http://programmers.stackexchange.com/a/18054 and http://programmers.stackexchange.com/questions/17898/whats-a-nice-explanation-fo 18054#18054. Each pointer, which is a special type of variable, must point to only one variable. Variables that are not pointers must not point to anything; however, such variables can be pointed to by any number of pointers.
- (f) Answer from back2dos, November 10, 2010: http://programmers.stackexchange.com/a/18092 and http://programmers.stackexchange.com/questions/17898/whats-a-nice-explanations/18092#18092. The pointer [variable] interprets the value of the pointer [variable] as the address of another variable that it points to. Hence, the value of the pointer [variable] refers to a specific location in memory (specified by the address), and is called the reference. Dereferencing is the process of accessing the value of the memory location that it points/refers to. That is, \*v dereferences the value of v, and provides the value at the memory location referred to by the address in v. &v provides a reference (or the address of the memory location for v) to the variable v.
- (g) Answer from *Ptolemy*, December 2, 2010: http://programmers.stackexchange.com/a/23016 and http://programmers.stackexchange.com/questions/17898/whats-a-nice-explanations/16#23016. At a low level, the concept of memory can be viewed as a massive array. "Any position in the array" can be accessed "by its index location." "Passing the index location rather than copying the entire memory" is more efficient in terms of performance and memory usage. Hence, "pointers are useful." "For [a] method to store the index location [of] where all the data [in the array] is stored," "a memory index location" can be passed in as a parameter. Pointers can be chained indefinitely; "keep track of how many times [I] need to look at the addresses to find the actual data object." While pointers to heap memory are safe, "pointers to stack memory are dangerous when passed outside the method."
- (h) Also, see http://www.udel.edu/CIS/105/pconrad/03F/2003.fall.doc by "P. Conrad."
- 3. [81, pp. 15, second last paragraph]
  - (a) "The value of a pointer is the address to which it points"; or, the "the value of a pointer is the address."
- 4. [55]
  - (a) "pointers use the \* $\dot{I}$  and  $->\dot{I}$  operators, references use ."
  - (b) "Both pointers and references let you refer to other objects indirectly."
  - (c) "there is no such thing as a null reference"
  - (d) "A reference must always refer to some object."

- (e) "As a result, if you have a variable whose purpose is to refer to another object, but it is possible that there might not be an object to refer to, you should make the variable a pointer, because then you can set it to null."
- (f) "On the other hand, if the variable must always refer to an object, i.e., if your design does not allow for the possibility that the variable is null, you should probably make the variable a reference."
- (g) "Because a reference must refer to an object, C++ requires that references be initialized." . . . Pointers do not have to be initialized; i.e., pointers can be uninitialized. However, "uninitialized pointers" are "valid but risky."
- (h) Since null references do not exist, references can be used more efficiently than pointers. This is because the validity of a reference does not have to be tested prior to usage.
- (i) Before using pointers, they should be tested against null (i.e., check the validity of a reference prior to usage).
- (j) "Pointers may be reassigned to refer to different objects." "A reference ... always refer to the object with which it is initialized."
- (k) "You should use a pointer whenever you need to take into account the possibility that there's nothing to refer to (in which case you can set the pointer to null) or whenever you need to be able to refer to different things at different times (in which case you can change where the pointer points)."
- (l) "You should use a reference whenever you know there will always be an object to refer to and you also know that once you're referring to that object, you'll never want to refer to anything else."
- (m) "There is one other situation in which you should use a reference, and that's when you're implementing certain operators. The most common example is operator[]. This operator typically needs to return something that can be used as the target of an assignment."
- (n) "References, then, are the feature of choice when you know you have something to refer to, when you'll never want to refer to anything else, and when implementing operators whose syntactic requirements make the use of pointers undesirable. In all other cases, stick with pointers."
- 5. Prakash Rajendran, Theodore Logan (Commodore Jaeger), Josh Lee, sbi, Rob<sub>φ</sub>, Sudhanshu Aggarwal, lpapp, Alf, Deduplicator, Sam, and Siddhant Saraf, "What are the differences between a pointer variable and a reference variable in C++?," Stack Exchange Inc., New York, NY, March 2, 2015. Available online from Stack Exchange Inc.: Stack Overflow: Questions at: http://stackoverflow.com/questions/57483/what-are-the-differences-between-a-pointer-variable-at October 8, 2015 was the last accessed date.
  - (a) A pointer can be re-assigned any number of times while a reference can not be re-seated after binding.
  - (b) Pointers can point nowhere (NULL), whereas reference always refer to an object.
  - (c) You can't take the address of a reference like you can with pointers.
  - (d) There's no "reference arithmetics" (but you can take the address of an object pointed by a reference and do pointer arithmetics on it as in &obj + 5).
  - (e) Use references in function parameters and return types to define useful and self-documenting interfaces.
  - (f) Use pointers to implement algorithms and data structures.

6. (a) 8. (a) 8. (a) 10. (a) 11. (a)



# Chapter 8

# Miscellaneous

List of interesting resources:

- 1. List of important publications in theoretical computer science: https://en.wikipedia.org/wiki/List\_of\_important\_publications\_in\_theoretical\_computer\_science
- 2. List of important publications in computer science: https://en.wikipedia.org/wiki/List\_of\_important\_publications\_in\_computer\_science
- 3. List of important publications in mathematics: https://en.wikipedia.org/wiki/List\_of\_important\_publications\_in\_mathematics#Graph\_theory

# 8.1 Setting Up Software Development Environment

Setting up software development environment for C++:

- 1. Platform-independent environments and software:
  - (a) Linux, Mac OS X, and Microsoft Windows:
  - (b) Truly platform independent:
- 2. *Mac OS X*:
  - (a) Integrated development environments (IDEs):
    - i. Xcode:
      - A.  $Preferences \Longrightarrow Text \ Editing \Longrightarrow Editing \Longrightarrow Code \ folding \ ribbon$
      - B. Preferences  $\implies$  Text Editing  $\implies$  Indentation  $\implies$  Syntax-aware indenting: Automatically indent based on syntax + Indent "//" comments one level deeper + Align consecutive "//" comments
- 3. Linux:
  - (a) Text editors:
    - i. *gedit*:
      - Α.
    - ii. *NEdit*:
      - Α.
  - (b)

### 8.2 Software Dependencies of The Boilerplate Code Project

The software dependencies of the "Boilerplate Code" project are found in the following *Markdown* file: .../lamiera-per-caldaie/notes/miscellaneo/software-dependencies.md.

# Acknowledgments

I would like to thank Ms. Deepika Panchalingam for motivating me to revise basic data structures and algorithms for internship and job interviews.

I would also like to thank the following users on Stack Overflow for their help: sdsmith2016 [155].

# **Bibliography**

- [1] David Abrahams and Aleksey Gurtovoy. C++ Template Metaprogramming: Concepts, Tools, and Techniques from Boost and Beyond. The C++ In-Depth Series. Pearson Education, Boston, MA, 2005.
- [2] Tobias Achterberg, Erling Andersen, Oliver Bastert, Timo Berthold, Robert E. Bixby, E. A. Boyd, Sebastian Ceria, Emilie Danna, Gerald Gamrath, Ambros M. Gleixner, Stefan Heinz, R. R. Indovina, Thorsten Koch, Andrea Lodi, Alexander Martin, Cassandra M. McZeal, Hans Mittelmann, Ted Ralphs, Daniel Rehfeldt, Domenico Salvagnin, Martin W. P. Savelsbergh, Daniel E. Steffy, and Kati Wolter. MIPLIB 2010 bibliography. Available online from Konrad-Zuse-Zentrum für Informationstechnik Berlin: MIPLIB Mixed Integer Problem Library at: http://miplib.zib.de/biblio.html; December 9, 2015 was the last accessed date, December 1 2015.
- [3] Sarita V. Adve, Doug Burger, Rudolf Eigenmann, Alasdair Rawsthorne, Michael D. Smith, Catherine H. Gebotys, Mahmut T. Kandemir, David J. Lilja, Alok N. Choudbary, Jesse Z. Fang, and Pen-Chung Yew. Changing interaction of compiler and architecture. <u>IEEE Computer</u>, 30(12):51–58, December 1997.
- [4] Andrei Alexandrescu. Modern C++ Design: Generic Programming and Design Patterns Applied. The C++ In-Depth Series. Addison-Wesley, Indianapolis, IN, 2001.
- [5] Alex Allain. Jumping into C++. Cprogramming.com, San Francisco, CA, 2012.
- [6] Jörg Arndt. Matters computational: Ideas, algorithms, source code. Available online at: http://www.jjj.de/fxt/ and http://www.jjj.de/fxt/fxtbook.pdf; self-published; October 9, 2014 was the last accessed date, September 7 2010.
- [7] Philip Avery, Abraham Bachrach, Sebastien Barthelemy, Carlos Becker, David Benjamin, Cyrille Berger, Armin Berres, Jose Luis Blanco, Mark Borgerding, Romain Bossart, Kolja Brix, Gauthier Brun, Philipp Büttgenbach, Thomas Capricelli, Nicolas Carre, Jean Ceccato, Vladimir Chalupecky, Benjamin Chrétien, Andrew Coles, Jeff "complexzeros", Marton Danoczy, Jeff Dean, Georg Drenkhahn, Christian Ehrlicher, Martinho Fernandes, Daniel Gomez Ferro, Rohit Garg, Mathieu Gautier, Anton Gladky, Stuart Glaser, Marc Glisse, Frederic Gosselin, Gaël Guennebaud, Philippe Hamelin, Marcus D. Hanwell, David Harmon, Chen-Pang He, Hauke Heibel, Christoph Hertzberg, Pavel Holoborodko, Tim Holy, Intel staff, Trevor Irons, Benoît Jacob, Bram de Jong, Kibeom Kim, Moritz Klammler, Claas Köhler, Alexey Korepanov, Igor Krivenko, Marijn Kruisselbrink, Abhijit Kundu, Moritz Lenz, Bo Li, Sebastian Lipponer, Daniel Lowenberg, David J. Luitz, Naumov Maks, Angelos Mantzaflaris, D. J. Marcin, Konstantinos A. Margaritis, Roger Martin, Ricard Marxer, Vincenzo Di Massa, Christian Mayer, Frank Meier-Dörnberg, Keir Mierle, Laurent Montel, Eamon Nerbonne, Alexander Neundorf, Jason Newton, Jitse Niesen, Desire Nuentsa, Jan Oberländer, Jos van den Oever, Michael Olbrich, Simon Pilgrim, Bjorn Piltz, Benjamin

Piwowarski, Zach Ploskey, Giacomo Po, Sergey Popov, Manoj Rajagopalan, Stjepan Rajko, Jure Repinc, Kenneth Frank Riddile, Richard Roberts, Adolfo Rodriguez, Peter Román, Oliver Ruepp, Radu Bogdan Rusu, Guillaume Saupin, Olivier Saut, Benjamin Schindler, Michael Schmidt, Dennis Schridde, Jakob Schwendner, Christian Seiler, Martin Senst, Sameer Sheorey, Andy Somerville, Alex Stapleton, Benoit Steiner, Sven Strothoff, Leszek Swirski, Adam Szalkowski, Silvio Traversaro, Piotr Trojanek, Anthony Truchet, Adolfo Rodriguez Tsourouksdissian, James Richard Tyrer, Rhys Ulerich, Henry de Valence, Ingmar Vanhassel, Michiel Van Dyck, Scott Wheeler, Freddie Witherden, Urs Wolfer, Manuel Yguel, and Pierre Zoppitelli. Eigen. Available online at: http://eigen.tuxfamily.org/index.php?title=Main\_Page; February 15, 2016 was the last accessed date, February 12 2016.

- [8] Hyunki Baik, François Bodin, Ross Dickson, Max Domeika, Scott A. Hissam, Skip Hovsmith, James Ivers, Ian Lintault, Stephen Olsen, and David Stewart. Multicore programming practices guide. Technical report, The Multicore Association, El Dorado Hills, CA, 2013.
- [9] Brian Bailey, Grant Martin, and Andrew Piziali. <u>ESL Design and Verification: A Prescription for Electronic System-Level Methodology</u>. The Morgan Kaufmann Series in Systems on Silicon. Morgan Kaufmann, San Francisco, CA, 2007.
- [10] David Barber. <u>Bayesian Reasoning and Machine Learning</u>. Cambridge University Press, New York, NY, 2012.
- [11] Gerassimos Barlas. Multicore and GPU Programming: An Integrated Approach. Morgan Kaufmann, Waltham, MA, 2015.
- [12] Wojciech Basalaj and Richard Corden. High integrity C++ coding standard V4.0: An overview. Technical report, Programming Research Ltd., Hersham, Surrey, England, U.K., November 2013.
- [13] Pete Becker. Working draft, standard for programming language C++. Technical Report N3242, International Organization for Standardization and International Electrotechnical Commission, Genève, Switzerland, February 28 2011.
- [14] Ben. answer to the question 'why can templates only be implemented in the header file?'. Available online from Stack Exchange Inc.: Stack Overflow: Questions at: http://stackoverflow.com/a/16493574/1531728; March 30, 2016 was the last accessed date, May 11 2013.
- [15] Benoît. answer to the question 'why can templates only be implemented in the header file?'. Available online from Stack Exchange Inc.: Stack Overflow: Questions at: http://stackoverflow.com/a/495128/1531728; edited by Evan Teran, February 10, 2009; March 31, 2016 was the last accessed date, January 30 2009.
- [16] Dimitris Bertsimas and Melvyn Sim. The price of robustness. Operations Research, 52(1):35–53, January–February 2004.
- [17] Christopher M. Bishop. <u>Pattern Recognition and Machine Learning</u>. Information Science and Statistics. Springer Science+Business Media, LCC, New York, NY, 2006.
- [18] Jean-Louis Boulanger. <u>Static Analysis of Software: The Abstract Interpretation</u>. John Wiley & Sons, Hoboken, NJ, 2013.
- [19] Gary Bronson. A First Book of C++. Course Technology, Boston, MA, fourth edition, 2012.

- [20] Gary J. Bronson. <u>C++ for Engineers and Scientists</u>. Cengage Learning, Boston, MA, fourth edition, 2013.
- [21] Dov Bulka and David Mayhew. <u>Efficient C++: Performance Programming Techniques</u>. Addison Wesley Longman, Inc., Indianapolis, IN, 2000.
- [22] Frank M. Carrano and Timothy Henry. <u>Data Abstraction & Problem Solving with C++: Walls</u> and Mirrors. Prentice Hall, Upper Saddle River, NJ, sixth edition, 2013.
- [23] Marshall Cline. C++ FAQ Lite: Frequently asked questions. Available online from the course web page of CS210 Data Structures and Abstractions Lab(Spring 2015), Department of Computer Science, Faculty of Science, University of Regina at: http://www.cs.uregina.ca/Links/class-info/210/C++FAQ/; self-published; July 10, 2015 was the last accessed date, July 10 2000.
- [24] Marshall Cline. C++ FAQ Lite: Frequently asked questions. Available online from the Computer Science Department, B. Thomas Golisano College of Computing and Information Sciences, Rochester Institute of Technology at: http://www.cs.rit.edu/~mjh/docs/c++-faq/; self-published; July 10, 2015 was the last accessed date, May 2 2003.
- [25] Marshall Cline. C++ FAQ Lite: Frequently asked questions. Available online from the web page of Laura Mensi and Paolo Copello, *Tiscali Italia S.p.A.: Tiscali Webspace: Fanelia Italy Computer Programming, Psychiatry, Escaflowne, and much more* at: http://web.tiscali.it/fanelia/cpp-faq-en/; self-published; July 10, 2015 was the last accessed date, July 28 2011.
- [26] cplusplus.com. The C++ resources network. Available online at: http://www.cplusplus.com/; April 2, 2014 was the last accessed date, 2014.
- [27] cplusplus.com. C++ language. Available online from *The C++ Resources Network: Tutorials* at: http://www.cplusplus.com/doc/tutorial/; February 5, 2016 was the last accessed date, 2015.
- [28] cplusplus.com. Reference: C++ reference. Available online at: http://www.cplusplus.com/reference/; November 2, 2015 was the last accessed date, 2015.
- [29] cplusplus.com. Tutorials. Available online from *The C++ Resources Network* at: http://www.cplusplus.com/doc/; February 5, 2016 was the last accessed date, 2015.
- [30] cppreference.com contributors. C++ reference. Available online at: http://en.cppreference.com/w/cpp; September 17, 2015 was the last accessed date, June 16 2015.
- [31] Lawrence Crowl. C++ binary Fixed-Point arithmetic. Technical Report N3352, International Organization for Standardization and International Electrotechnical Commission, Genève, Switzerland, January 15 2012.
- [32] Lawrence Crowl. C++ binary Fixed-Point arithmetic. Technical Report P0106R0, International Organization for Standardization and International Electrotechnical Commission, Genève, Switzerland, September 27 2015.
- [33] Nell Dale. <u>C++ Plus Data Structures</u>. Jones and Bartlett Learning, Burlington, MA, fifth edition, 2013.
- [34] Nell Dale and Chip Weems. <u>Programming and Problem Solving with C++</u>. Jones and Bartlett Learning, Burlington, MA, sixth (comprehensive) edition, 2014.

- [35] Michael Dawson. <u>Beginning C++ Through Game Programming</u>. Course Technology, Boston, MA, third edition, 2011.
- [36] Michael Dawson. <u>Beginning C++ Through Game Programming</u>. Course Technology, Boston, MA, fourth edition, 2014.
- [37] Mourad Debbabi, Fawzi Hassaïne, Yosr Jarraya, Andrei Soeanu, and Luay Alawneh. <u>Verification and Validation in Systems Engineering: Assessing UML/SysML Design Models.</u> Springer-Verlag Berlin Heidelberg, Heidelberg, Germany, 2010.
- [38] Paul Deitel and Harvey Deitel. C++ How to Program. Deitel<sup>6</sup> How to Program. Prentice Hall, Boston, MA, eighth edition, 2012.
- [39] Paul Deitel and Harvey Deitel. C++ How to Program. Deitel<sup>8</sup> How to Program. Prentice Hall, Upper Saddle River, NJ, ninth edition, 2014.
- [40] Paul Deitel and Harvey Deitel. <u>C++ How to Program</u>. Deitel<sup>8</sup> How to Program. Pearson Education, Hoboken, NJ, tenth edition, 2017.
- [41] DevSolar. answer to the question 'why can templates only be implemented in the header file?'. Available online from *Stack Exchange Inc.: Stack Overflow: Questions* at: http://stackoverflow.com/a/495511/1531728; March 30, 2016 was the last accessed date, January 30 2009.
- [42] Ian G. Harris Dhiraj K. Pradhan. <u>Practical Design Verification</u>. Cambridge University Press, New York, NY, 2009.
- [43] Davide Di Gennaro. Advanced C++ metaprogramming. Self-published, 2011.
- [44] Davide Di Gennaro. <u>Advanced Metaprogramming in Classic C++</u>. The Expert's Voice<sup>ö</sup> in C++. Apress Media, LLC, Berkeley, CA, 2015.
- [45] Germán Diago. answer to the question 'why can templates only be implemented in the header file?'. Available online from *Stack Exchange Inc.: Stack Overflow: Questions* at: http://stackoverflow.com/a/16509701/1531728; March 31, 2016 was the last accessed date, May 12 2013.
- [46] Dictionary.com staff. Dictionary.com: Find the meanings and definitions of words at dictionary.com. Available online at: http://dictionary.reference.com/; February 5, 2016 was the last accessed date, 2016.
- [47] Jack Dongarra and Eric Grosse. Netlib repository. Available online at: http://www.netlib.org/; February 3, 2016 was the last accessed date, 2016.
- [48] Allen B. Downey. <u>How to Think Like A Computer Scientist</u>. Green Tea Press, Needham, MA, C++ version edition, November 2012.
- [49] Adam Drozdek. <u>Data Structures and Algorithms in C++</u>. Cengage Learning, Boston, MA, fourth edition, 2013.
- [50] Stefanus Du Toit. Working draft, standard for programming language C++. Technical Report N3797, International Organization for Standardization and International Electrotechnical Commission, Genève, Switzerland, October 13 2013.

- [51] Bruce Eckel. Thinking in C++: Introduction to Standard C++, volume 1. Prentice Hall, Upper Saddle River, NJ, second edition, 2000.
- [52] Bruce Eckel and Chuck Allison. <u>Thinking in C++: Practical Programming</u>, volume 2. Prentice Hall, Upper Saddle River, NJ, 2003.
- [53] Dirk Eddelbuettel. Seamless R and C++ Integration with Rcpp, volume 64 of Use R! Springer Science+Business Media, New York, NY, 2013.
- [54] Edison Design Group staff. C++ front end: Internal documentation. Technical report, Edison Design Group, Inc., West Orange, NJ, December 21 2011.
- [55] EliteHussar. Distinguish between pointers and references in C++. Available online from *cplus-plus.com The C++ Resources Network* at: http://www.cplusplus.com/articles/ENywvCM9/; October 8, 2015 was the last accessed date, August 20 2010.
- [56] Joseph A. Fisher, Paolo Faraboschi, and Cliff Young. <u>Embedded Computing: A VLIW Approach</u> to Architecture, Compilers, and Tools. Morgan Kaufmann, San Francisco, CA, 2005.
- [57] Agner Fog. Optimizing software in C++: An optimization guide for Windows, Linux and Mac platforms. Available online at: http://www.agner.org/optimize/optimizing\_cpp.pdf; July 1, 2015 was the last accessed date, August 7 2014.
- [58] Neal Ford. The Productive Programmer: Theory in Practice. O'Reilly Media, Sebastopol, CA, 2008.
- [59] Tony Gaddis. Starting Out With C++: From Control Structures Through Objects. Pearson Education, Boston, MA, sixth (brief) edition, 2010.
- [60] Tony Gaddis. Starting Out With C++: From Control Structures Through Objects. Addison-Wesley, Boston, MA, seventh edition, 2012.
- [61] Tony Gaddis, Judy Walters, and Godfrey Muganda. Starting Out With C++: Early Objects. Addison-Wesley, Boston, MA, seventh edition, 2011.
- [62] Anton Gogolev. answer to the question 'why can templates only be implemented in the header file?'. Available online from *Stack Exchange Inc.: Stack Overflow: Questions* at: http://stackoverflow.com/a/495032/1531728; edited by Jonathan Henly, September 19, 2013; March 30, 2016 was the last accessed date, January 30 2009.
- [63] Peter Gottschling. <u>Discovering Modern C++: An Intensive Course for Scientists, Engineers, and Programmers.</u> The C++ In-Depth Series. Addison-Wesley, Boston, MA, 2016.
- [64] Brad Green. Programming problems: A primer for the technical interview fundamentals in c++11. Self-published, 2012.
- [65] Marc Gregoire. Professional C++. John Wiley & Sons, Indianapolis, IN, third edition, 2014.
- [66] Marc Gregoire, Nicholas A. Solter, and Scott J. Kleper. <u>Professional C++</u>. John Wiley & Sons, Indianapolis, IN, second edition, 2011.
- [67] Richard Groff. C++ Tutorial. Wiffletree World, LLC, Arlington, TX, 2012.

- [68] Kurt Guntheroth. Optimized C++: Proven Techniques for Heightened Performance. O'Reilly Media, Sebastopol, CA, 2016.
- [69] P. L. Hammer, E. L. Johnson, and B. H. Korte. Conclusive remarks. In <u>Discrete Optimization II</u>, Proceedings of the Advanced Research Institute on Discrete Optimization and Systems Applications of the Systems Science Panel of NATO and of the Discrete Optimization Symposium, volume 5 of <u>Annals of Discrete Mathematics</u>, pages 427–453. North-Holland, Banff, Alberta, Canada and Vancouver, British Columbia, Canada, August 1979.
- [70] Steve Heller. C++: A Dialog: Programming with the C++ Standard Library. Pearson Education, Upper Saddle River, NJ, 2003.
- [71] Hewlett-Packard Company staff. Standard template library programmer's guide. Available online in SGI The Trusted Leader in High Performance Computing: Tech Archive: Standard xTemplate Library Programmer's Guide at: http://www.sgi.com/tech/stl/; September 30, 2015 was the last accessed date, 1994.
- [72] Hewlett-Packard Company staff. STL complexity specifications. Available online in SGI

   The Trusted Leader in High Performance Computing: Tech Archive: Standard Template
  Library Programmer's Guide: Design documents: STL Complexity Specifications at: http:
  //www.sgi.com/tech/stl/complexity.html; September 30, 2015 was the last accessed date,
  http://www.sgi.com/tech/stl/complexity.html 2014.
- [73] Cay S. Horstmann. C++ for Everyone. John Wiley & Sons, Hoboken, NJ, second edition, 2012.
- [74] Ivor Horton. Beginning C++. Apress, New York, NY, 2014.
- [75] Justin Husted. Fixing some common compiler problems. Available online from the *UW ACM's* (University of Washington's chapter of the Association for Computing Machinery) web page: Tutorials: [Development] in UNIX at: http://www.cs.washington.edu/acm/tutorials/dev-in-unix/compiler-problems.html; February 17, 2016 was the last accessed date, May 19 2000.
- [76] Innovation 24 staff. LocalSolver 5.5 documentation: Overview. Innovation 24, Paris, France, 2015.
- [77] Innovation 24 staff. Localsolver: Mathematical optimization solver. Available online at: http://www.localsolver.com/; December 7, 2015 was the last accessed date, 2015.
- [78] ISO/IEC JTC1/SC22/WG21 members. Information technology programming languages C++. Technical Report INCITS/ISO/IEC 14882-2011[2012], American National Standards Institute, New York, NY, February 14 2012.
- [79] ISO/IEC JTC1/SC22/WG21 members. Information technology programming languages C++. Technical Report CAN/CSA-ISO/IEC 14882:16, Canadian Standards Association, Toronto, Canada, December 2016.
- [80] ISO/IEC JTC1/SC22/WG21 members. Programming languages C++. Technical Report ISO/IEC STANDARD 14882, International Organization for Standardization and International Electrotechnical Commission, Vernier, Genève, Switzerland, December 2017.

- [81] Ted Jensen. A tutorial on pointers and arrays in C. Available online as Version 1.2 at: http://pweb.netcom.com/~tjensen/ptr/cpoint.htm, http://pweb.netcom.com/~tjensen/ptr/pointers.htm, and http://home.earthlink.net/~momotuk/pointers.pdf; self-published; October 8, 2015 was the last accessed date, September 2003.
- [82] Nicolai M. Josuttis. <u>The C++ Standard Library: A Tutorial and Reference</u>. Addison-Wesley, Reading, MA, 1999.
- [83] Nicolai M. Josuttis. Josuttis' summary of STL algorithms. Available online at: http://www.josuttis.com/libbook/algolist.pdf; self-published; July 1, 2015 was the last accessed date, 1999.
- [84] Nicolai M. Josuttis. <u>The C++ Standard Library: A Tutorial and Reference</u>. Pearson Education, Upper Saddle River, NJ, second edition, 2012.
- [85] Björn Karlsson. Beyond the C++ Standard Library: An Introduction to Boost. Pearson Education, Boston, MA, 2006.
- [86] George Em Karniadakis and Robert M. Kirby II. <u>Parallel Scientific Computing in C++ and MPI:</u>
  <u>A Seamless Approach to Parallel Algorithms and Their Implementation</u>. Cambridge University Press, Cambridge, U.K., 2003.
- [87] Jayantha Katupitiya and Kim Bentley. <u>Interfacing with C++: Programming Real-World Applications</u>. Springer-Verlag Berlin Heidelberg, Heidelberg, Germany, 2006.
- [88] Brian W. Kernighan and Rob Pike. <u>The Practice of Programming</u>. Addison-Wesley Professional Computing Series. Addison-Wesley, Reading, MA, 1999.
- [89] Darko Kirovski and Miodrag Potkonjak. A quantitative approach to functional debugging. In Proceedings of the IEEE/ACM International Conference on Computer-Aided Design (ICCAD 1997), pages 170–173, San Jose, CA, November 9–13 1997. IEEE Computer Society, IEEE Press.
- [90] Donald E. Knuth. <u>The Stanford GraphBase: A Platform for Combinatorial Computing</u>. ACM Press and Addison-Wesley, New York, NY and Reading, MA, 1993.
- [91] Thorsten Koch, Tobias Achterberg, Erling Andersen, Oliver Bastert, Timo Berthold, Robert E. Bixby, Emilie Danna, Gerald Gamrath, Ambros M. Gleixner, Stefan Heinz, Andrea Lodi, Hans Mittelmann, Ted Ralphs, Domenico Salvagnin, Daniel E. Steffy, and Kati Wolter. MIPLIB 2010: Mixed integer programming library version 5. Mathematical Programming Computation, 3(2):103–163, June 2011.
- [92] Andrew Koenig and Barbara Moo. <u>Accelerated C++: Practical Programming by Example</u>. The C++ In-Depth Series. Addison-Wesley, Boston, MA, 2000.
- [93] Gayle Laakmann. Cracking the technical interview: 150 technical interview questions and solutions, written by experts. Self-published, 2009.
- [94] Jeff Langr. Modern C++ Programming with Test-Driven Development: Code Better, Sleep Better. The Pragmatic Programmers, Raleigh, NC, October 2013.

- [95] Insup Lee, Joseph Y-T. Leung, and Sang H. Son. <u>Handbook of Real-Time and Embedded Systems</u>. Chapman & Hall/CRC Computer & Information Science. Chapman & Hall/CRC, Boca Raton, FL, 2008.
- [96] Jon Lee. A First Course in Combinatorial Optimization, volume 36 of Cambridge Texts in Applied Mathematics. Cambridge University Press, New York, NY, 2004.
- [97] Stanley B. Lippman, Josée Lajoie, and Barbara E. Moo. <u>C++ Primer</u>. Addison-Wesley, Upper Saddle River, NJ, fifth edition, 2013.
- [98] Ray Lischner. Exploring C++ 11: Problems and Solutions Handbook. Apress Media, LLC, Berkeley, CA, 2013.
- [99] László Lovász. <u>Large Networks and Graph Limits</u>, volume 60 of <u>Colloquium Publications</u>. American Mathematical Society, Providence, RI, 2012.
- [100] Mi Lu. Arithmetic and Logic in Computer Systems. John Wiley & Sons, Hoboken, NJ, 2004.
- [101] Michael Main and Walter Savitch. <u>Data Structures and Other Objects Using C++</u>. Addison-Wesley, Reading, MA, fourth edition, 2011. Lecture slides based on this book are available online at: <a href="http://www.cs.colorado.edu/~main/supplements/lectures.html">http://www.cs.colorado.edu/~main/supplements/lectures.html</a>; September 20, 2010 was the last accessed date.
- [102] D. S. Malik. C++ Programming: From Problem Analysis to Program Design. Course Technology, Boston, MA, fifth edition, 2011.
- [103] D. S. Malik. C++ Programming: Program Design Including Data Structures. Course Technology, Boston, MA, fifth edition, 2011.
- [104] D. S. Malik. C++ Programming: From Problem Analysis to Program Design. Cengage Learning, Boston, MA, sixth edition, 2013.
- [105] D. S. Malik. <u>C++ Programming: Program Design Including Data Structures</u>. Cengage Learning, Boston, MA, sixth edition, 2013.
- [106] D. S. Malik. <u>C++ Programming: From Problem Analysis to Program Design</u>. Cengage Learning, Stamford, CT, seventh edition, 2015.
- [107] D. S. Malik. <u>C++ Programming: Program Design Including Data Structures</u>. Cengage Learning, Stamford, CT, seventh edition, 2015.
- [108] D. S. Malik. <u>C++ Programming: From Problem Analysis to Program Design</u>. Cengage Learning, Boston, MA, eighth edition, 2018.
- [109] Norman Matloff. Parallel Computing for Data Science: With Examples in R, C++ and CUDA. Chapman & Hall/CRC The R Series. CRC Press, Boca Raton, FL, 2016.
- [110] Michael B. McLaughlin. C++ Succinctly. Succinctly. Syncfusion Inc., Morrisville, NC, 2012.
- [111] Kurt McMahon. C strings and C++ strings. Available online from Kurt McMahon's web page: Notes at: https://www.prismnet.com/~mcmahon/Notes/strings.html; self-published; November 3, 2015 was the last accessed date.

- [112] Scott Meyers. Effective C++: 55 Specific Ways to Improve Your Programs and Designs. Addison-Wesley Professional Computing Series. Pearson Education, Upper Saddle River, NJ, third edition, 2005.
- [113] Scott Meyers. <u>Effective C++ Digital Collection</u>: 140 Ways to Improve Your Programming. Addison-Wesley Professional Computing Series. Addison-Wesley, Upper Saddle River, NJ, 2012.
- [114] Scott Meyers. Effective Modern C++: 42 Specific Ways to Improve Your Use of C++11 and C++14. O'Reilly Media, Sebastopol, CA, 2015.
- [115] Mike Mintz and Robert Ekendahl. <u>Hardware Verification with C++: A Practitioner's Handbook.</u> Springer Science+Business Media, <u>LCC</u>, New York, NY, 2006.
- [116] Sandipan Mohanty. Programming in C++: Introduction to the current language standard C++14. Available online from Forschungszentrum Jülich GmbH: Institute for Advanced Simulation: Jülich Supercomputing Center at: https://www.fz-juelich.de/SharedDocs/Downloads/IAS/JSC/EN/slides/cplusplus.pdf and https://www.fz-juelich.de/SharedDocs/Downloads/IAS/JSC/EN/slides/cplusplus/cplusplus.pdf?\_\_blob=publicationFile; October 3, 2017 was the last accessed date, May 30 June 2 2016.
- [117] Sandipan Mohanty. Programming in C++: Introduction to the language standard C++14 (and a preview of C++17). Available online from Forschungszentrum Jülich GmbH: Institute for Advanced Simulation: Jülich Supercomputing Center at: https://www.fz-juelich.de/SharedDocs/Downloads/IAS/JSC/EN/slides/cplusplus/cplusplus.pdf and https://www.fz-juelich.de/SharedDocs/Downloads/IAS/JSC/EN/slides/cplusplus/cplusplus.pdf; jsessionid=F6F2721BAADDF0E098B19D576F1E0ED1?\_\_blob=publicationFile; self-published; June 22, 2018 was the last accessed date, May 29 June 1 2017.
- [118] Mohtashim. C++ STL tutorial. Available online at *Tutorials Point: C++ Tutorial: C++ STL Tutorial*: http://www.tutorialspoint.com/cplusplus/cpp\_stl\_tutorial.htm; September 17, 2015 was the last accessed date, 2015.
- What difference [119] Peter Mortensen. is the between  $int^*$ , int const const and int const Available online from Stack Exchange Inc.: Stackconst, Overflow: Questions http://stackoverflow.com/questions/1143262/ at: what-is-the-difference-between-const-int-const-int-const-and-int-const; October 1, 2015 was the last accessed date, March 13 2015.
- [120] Black Moses. answer to the question 'why is the discrepancy in these two cases of using C++ templates?'. Available online from Stack Exchange Inc.: Stack Overflow: Questions at: http://stackoverflow.com/a/36319466/1531728 and http://stackoverflow.com/questions/36319028/why-is-the-discrepancy-in-these-two-cases-of-using-c-templates/36319466#36319466; edited by Kuba Ober, on March 30, 2016; March 30, 2016 was the last accessed date, March 30 2016.
- [121] Arindam Mukherjee. <u>Learning Boost C++ Libraries: Solve Practical Programming Problems</u>
  <u>Using Powerful, Portable, and Expressive Libraries from Boost.</u> Packt Publishing, Birmingham,
  West Midlands, England, U.K., July 2015.
- [122] Carlos Oliveira. Practical C++ Financial Programming: Practical Solutions in Financial Engineering. The Expert's Voice<sup>6</sup> in Programming. Apress Media, LLC, Berkeley, CA, 2015.

- [123] Mikael Olsson. <u>C++ Quick Syntax Reference</u>. The Expert's Voice<sup>6</sup>. Apress Media, LLC, New York, NY, 2013.
- [124] Steve Oualline. <u>Practical C++ Programming</u>. Programming Style Guidelines. O'Reilly Media, Sebastopol, CA, second edition, 2003.
- [125] Brian Overland. C++ Without Fear: A Beginner's Guide That Makes You Feel Smart. Pearson Education, Boston, MA, second edition, 2011.
- [126] Brian Overland. C++ for the Impatient. Pearson Education, Upper Saddle River, NJ, 2013.
- [127] Yusuf Kemal Özcan. Is there difference referany between pointers and ences? online fromStack Exchange Inc.: Available *Programmers* StackExchange: Questions at: http://programmers.stackexchange.com/questions/195337/ is-there-any-difference-between-pointers-and-references; 2015October 28,the last accessed date, April 18 2013.
- [128] Alonso Peña. <u>Advanced Quantitative Finance with C++</u>. Community Experience Distilled. Packt Publishing, Birmingham, West Midlands, England, U.K., 2014.
- [129] Rod Pierce. Maths is fun: Maths resources. Available online at: https://www.mathsisfun.com/; February 5, 2016 was the last accessed date, 2016.
- [130] Joe Pitt-Francis and Jonathan Whiteley. <u>Guide to Scientific Computing in C++</u>. Undergraduate Topics in Computer Science. Springer-Verlag London, London, U.K., 2012.
- [131] Antony Polukhin. Boost C++ Application Development Cookbook: Over 80 practical, task-based recipes to create applications using Boost libraries. Packt Publishing, Birmingham, West Midlands, England, U.K., 2013.
- [132] Alex Pomeranz. Learn C++. Available online at: http://www.learncpp.com/; April 2, 2014 was the last accessed date, 2014.
- [133] Constantine Pozrikidis. <u>Introduction to C++ Programming and Graphics</u>. Springer Science+Business Media, LCC, New York, NY, 2007.
- [134] Stephen Prata. C++ Primer Plus. Sams Publishing, Indianapolis, IN, fifth edition, 2005.
- [135] Stephen Prata. C++ Primer Plus: Developer's Library. Pearson Education, Upper Saddle River, NJ, sixth edition, 2012.
- [136] Programming Research Ltd. staff. High integrity C++: Coding standard version 4.0. Technical report, Programming Research Ltd., Hersham, Surrey, England, U.K., October 3 2013.
- [137] Siddhartha Rao. <u>Sams Teach Yourself C++ in One Hour a Day</u>. Sams Publishing, Indianapolis, IN, eighth edition, 2017.
- [138] Greg Reese. <u>C++ Standard Library Practical Tips</u>. Charles River Media Programming Series. Charles River Media, Hingham, MA, 2006.

- [139] Chris Riesbeck. Standard C++ containers. Available online from *Prof. Chris Riesbeck's web page: Programming: Useful C++ / Unix Resources*, Computer Science Division, Department of Electrical Engineering and Computer Science, Robert R. McCormick School of Engineering and Applied Science, Northwestern University at: <a href="http://www.cs.northwestern.edu/~riesbeck/programming/c++/stl-summary.html">http://www.cs.northwestern.edu/~riesbeck/programming/c++/stl-summary.html</a>; September 30, 2015 was the last accessed date, July 3 2009.
- [140] Chris Riesbeck. Useful C++ / Unix resources. Available online from *Prof. Chris Riesbeck's web page: Programming*, Computer Science Division, Department of Electrical Engineering and Computer Science, Robert R. McCormick School of Engineering and Applied Science, Northwestern University at: http://www.cs.northwestern.edu/~riesbeck/programming/c++/; September 30, 2015 was the last accessed date, July 2 2009.
- [141] Robert Robson. <u>Using the STL: The C++ Standard Template Library</u>. Springer-Verlag Berlin Heidelberg New York, Heidelberg, Germany, second edition, 2000.
- [142] Philip Romanik and Amy Muntz. <u>Applied C++: Practical Techniques for Building Better</u> Software. The C++ In-Depth Series. <u>Addison-Wesley</u>, Boston, MA, 2003.
- [143] Stephan Roth. Clean C++: Sustainable Software Development Patterns and Best Practices with C++ 17. Apress Media, LLC, Berkeley, CA, 2017.
- [144] Dan Saks. An introduction to references. Available online from *UBM Electronics: UBM Canon Electronics Engineering Communities: Embedded Cracking the Code to Systems Development* at: http://www.embedded.com/print/4024641; October 8, 2015 was the last accessed date, February 26 2001.
- [145] Dan Saks. References vs. pointers. Available online from UBM Electronics: UBM Canon Electronics Engineering Communities: Embedded Cracking the Code to Systems Development at: http://www.embedded.com/electronics-blogs/programming-pointers/4023307/References-vs-Pointers and http://www.embedded.com/print/4023307; October 28, 2015 was the last accessed date, March 15 2001.
- [146] Walter Savitch. <u>Problem Solving with C++</u>. Pearson Education, Boston, MA, seventh edition, 2009.
- [147] Walter Savitch. Problem Solving with C++. Addison-Wesley, Reading, MA, eighth edition, 2012.
- [148] Walter Savitch and Kenrick Mock. <u>Absolute C++</u>. Addison-Wesley, Reading, MA, fifth edition, 2013.
- [149] Boris Schäling. The boost C++ libraries. Available online at: http://en.highscore.de/cpp/boost/; self-published; February 26, 2013 was the last accessed date, 2012.
- [150] Edward Scheinerman. C++ for Mathematicians: An Introduction for Students and Professionals. Chapman & Hall/CRC, Boca Raton, FL, 2006.
- [151] Herbert Schildt. C++: The Complete Reference. McGraw-Hill, Berkeley, CA, third edition, 1998.
- [152] Herbert Schildt. C++ from the Ground Up. McGraw-Hill/Osborne, Berkeley, CA, third edition, 2003.

- [153] Herbert Schildt. <u>C++: The Complete Reference</u>. Osborne Complete Reference Series. McGraw-Hill/Osborne, Berkeley, CA, fourth edition, 2003.
- [154] Herbert Schildt. The Art of C++. McGraw-Hill/Osborne, Emeryville, CA, 2004.
- [155] sdsmith. comment to the question 'why is the discrepancy in these two cases of using C++ templates?'. Available online from *Stack Exchange Inc.: Stack Overflow: Questions* at: http://stackoverflow.com/q/36319028/1531728; March 30, 2016 was the last accessed date, March 30 2016.
- [156] Robert C. Seacord. <u>Secure Coding in C and C++</u>. The SEI Series in Software Engineering. Addison-Wesley, Upper Saddle River, NJ, second edition, 2013.
- [157] Yair Shapira. Solving PDEs in C++: Numerical Methods in a Unified Object-Oriented Approach. SIAM Computational Science and Engineering. Society for Industrial and Applied Mathematics, Philadelphia, PA, second edition, 2006.
- [158] Steven S. Skiena. <u>The Algorithm Design Manual</u>. Springer-Verlag London, London, U.K., second edition, 2008.
- [159] Richard Smith. Working draft, standard for programming language C++. Technical Report N4659, International Organization for Standardization and International Electrotechnical Commission, Genève, Switzerland, March 21 2017.
- [160] Juan Soulié. C++ Language Tutorial. cplusplus.com, June 2007.
- [161] Milan Stevanovic. Advanced C and C++ Compiling: An engineering guide to compiling, linking, and libraries using C and C++. Apress, New York, NY, 2014.
- [162] Bjarne Stroustrup. <u>Programming: Principles and Practice Using C++</u>. Pearson Education, Boston, MA, 2009.
- [163] Bjarne Stroustrup. <u>The C++ Programming Language</u>. Pearson Education, Upper Saddle River, NJ, fourth edition, 2013.
- [164] Bjarne Stroustrup. <u>Programming: Principles and Practice Using C++</u>. Pearson Education, Upper Saddle River, NJ, second edition, 2014.
- [165] Bjarne Stroustrup. <u>A Tour of C++</u>. The C++ In-Depth Series. Pearson Education, Upper Saddle River, NJ, 2014.
- [166] Bruce Sutherland. C++ Game Development Primer. Apress Media, LLC, Berkeley, CA, 2014.
- [167] Bruce Sutherland. <u>Learn C++ for Game Development</u>. Apress Media, LLC, Berkeley, CA, 2014.
- [168] Bruce Sutherland. <u>C++ Recipes: A Problem-Solution Approach</u>. Apress Media, LLC, Berkeley, CA, 2015.
- [169] Bruce A. Tate. Seven Languages in Seven Weeks: A Pragmatic Guide to Learning Programming Languages. Pragmatic Bookshelf. The Pragmatic Programmers, Raleigh, NC, 2010.
- [170] David Vandevoorde and Nicolai M. Josuttis. <u>C++ Templates: The Complete Guide</u>. Pearson Education, Boston, MA, 2003.

- [171] Dirk Vermeir. Multi-Paradigm Programming using C++. Springer-Verlag London Berlin Heidelberg, London, U.K., 2001.
- [172] Vibrant Publishers. C++ Internals: Interview Questions You'll Most Likely Be Asked. Job Interview Questions Series. Vibrant Publishers, second edition, 2012.
- [173] Mark Allen Weiss. <u>Data Structures and Algorithm Analysis in C++</u>. Pearson Education, Upper Saddle River, NJ, fourth edition, 2014.
- [174] Wikibooks contributors. More C++ Idioms. Wikimedia Foundation, San Francisco, CA, June 18 2014.
- [175] Wikipedia contributors. Algebraic modeling language. Available online in Wikipedia, The Free Encyclopedia: Specification languages at: https://en.wikipedia.org/wiki/Algebraic\_modeling\_language; December 11, 2015 was the last accessed date, May 3 2015.
- [176] Wikipedia contributors. Discrete optimization. Available online in Wikipedia, The Free Encyclopedia: Mathematical optimization at: https://en.wikipedia.org/wiki/Discrete\_optimization; December 9, 2015 was the last accessed date, May 17 2015.
- [177] Wikipedia contributors. Graph labeling. Available online from Wikipedia, The Free Encyclopedia: Extensions and generalizations of graphs at: https://en.wikipedia.org/wiki/Graph\_labeling; November 25, 2018 was the last accessed date, August 30 2017.
- [178] Wikipedia contributors. Vertex (graph theory). Available online from Wikipedia, The Free Encyclopedia: Graph theory at: https://en.wikipedia.org/wiki/Vertex\_(graph\_theory); November 20, 2018 was the last accessed date, October 24 2017.
- [179] Wikipedia contributors. Degree (graph theory). Available online from Wikipedia, The Free Encyclopedia: Graph theory at: https://en.wikipedia.org/wiki/Degree\_(graph\_theory); November 20, 2018 was the last accessed date, November 12 2018.
- [180] Wikipedia contributors. Graph (discrete mathematics). Available online from Wikipedia, The Free Encyclopedia: Graph theory at: https://en.wikipedia.org/wiki/Graph\_(discrete\_mathematics); November 25, 2018 was the last accessed date, November 19 2018.
- [181] Wikipedia contributors. Multidimensional network. Available online from Wikipedia, The Free Encyclopedia: Network theory at: https://en.wikipedia.org/wiki/Multidimensional\_network; November 25, 2018 was the last accessed date, November 14 2018.
- [182] Wikipedia contributors. Multigraph. Available online from Wikipedia, The Free Encyclopedia: Extensions and generalizations of graphs at: https://en.wikipedia.org/wiki/Multigraph; November 20, 2018 was the last accessed date, May 30 2018.
- [183] Wikipedia contributors. Multipartite graph. Available online from Wikipedia, The Free Encyclopedia: Graph families at: https://en.wikipedia.org/wiki/Multipartite\_graph; November 25, 2018 was the last accessed date, May 30 2018.
- [184] Wikipedia contributors. Quiver (mathematics). Available online from Wikipedia, The Free Encyclopedia: Directed graphs at: https://en.wikipedia.org/wiki/Quiver\_(mathematics); November 25, 2018 was the last accessed date, November 10 2018.

- [185] Anthony Williams. C++ Concurrency in Action: Practical Multithreading. Manning Publications Co., Shelter Island, NY, 2012.
- [186] Matthew Wilson. Extended STL: Collections and Iterators, volume 1. Addison-Wesley, Upper Saddle River, NJ, 2007.
- [187] Wolfram Research staff. Wolfram MathWorld: The web's most extensive mathematics resource. Available online at: http://mathworld.wolfram.com/; February 5, 2016 was the last accessed date, January 29 2016.
- [188] Diane Zak. An Introduction to Programming with C++. Course Technology, Boston, MA, seventh edition, 2013.