

FIGURE 10.4. Loss functions for two-class classification. The response is $y = \pm 1$; the prediction is f, with class prediction $\operatorname{sign}(f)$. The losses are misclassification: $I(\operatorname{sign}(f) \neq y)$; exponential: $\exp(-yf)$; binomial deviance: $\log(1 + \exp(-2yf))$; squared error: $(y - f)^2$; and support vector: $(1 - yf)_+$ (see Section 12.3). Each function has been scaled so that it passes through the point (0,1).

f(x) = 0. The goal of the classification algorithm is to produce positive margins as frequently as possible. Any loss criterion used for classification should penalize negative margins more heavily than positive ones since positive margin observations are already correctly classified.

Figure 10.4 shows both the exponential (10.8) and binomial deviance criteria as a function of the margin $y \cdot f(x)$. Also shown is misclassification loss $L(y, f(x)) = I(y \cdot f(x) < 0)$, which gives unit penalty for negative margin values, and no penalty at all for positive ones. Both the exponential and deviance loss can be viewed as monotone continuous approximations to misclassification loss. They continuously penalize increasingly negative margin values more heavily than they reward increasingly positive ones. The difference between them is in degree. The penalty associated with binomial deviance increases linearly for large increasingly negative margin, whereas the exponential criterion increases the influence of such observations exponentially.

At any point in the training process the exponential criterion concentrates much more influence on observations with large negative margins. Binomial deviance concentrates relatively less influence on such observa-