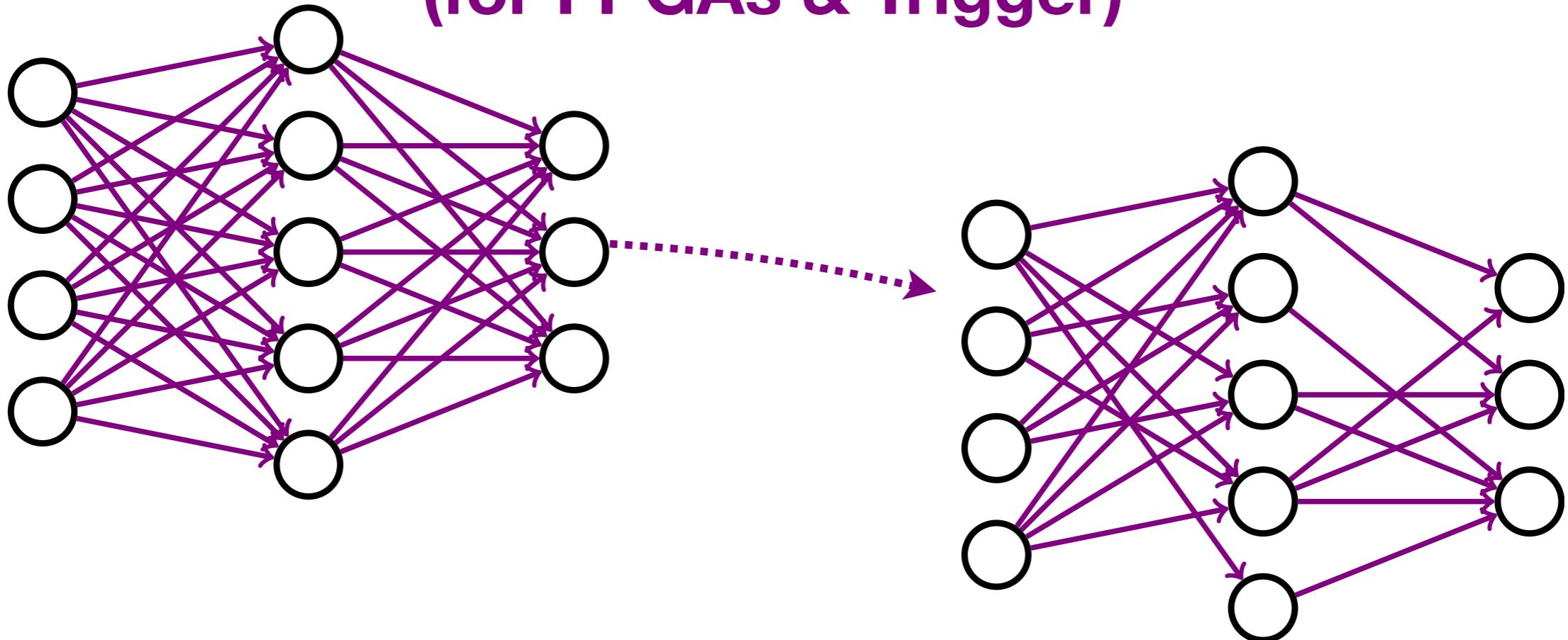
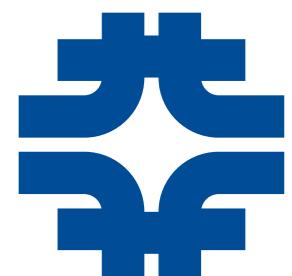


Compression of Deep Neural Networks (for FPGAs & Trigger)



Javier Duarte
Fermilab

Reconstruction, Trigger, and Machine Learning for the HL-LHC
MIT
4/27/2018



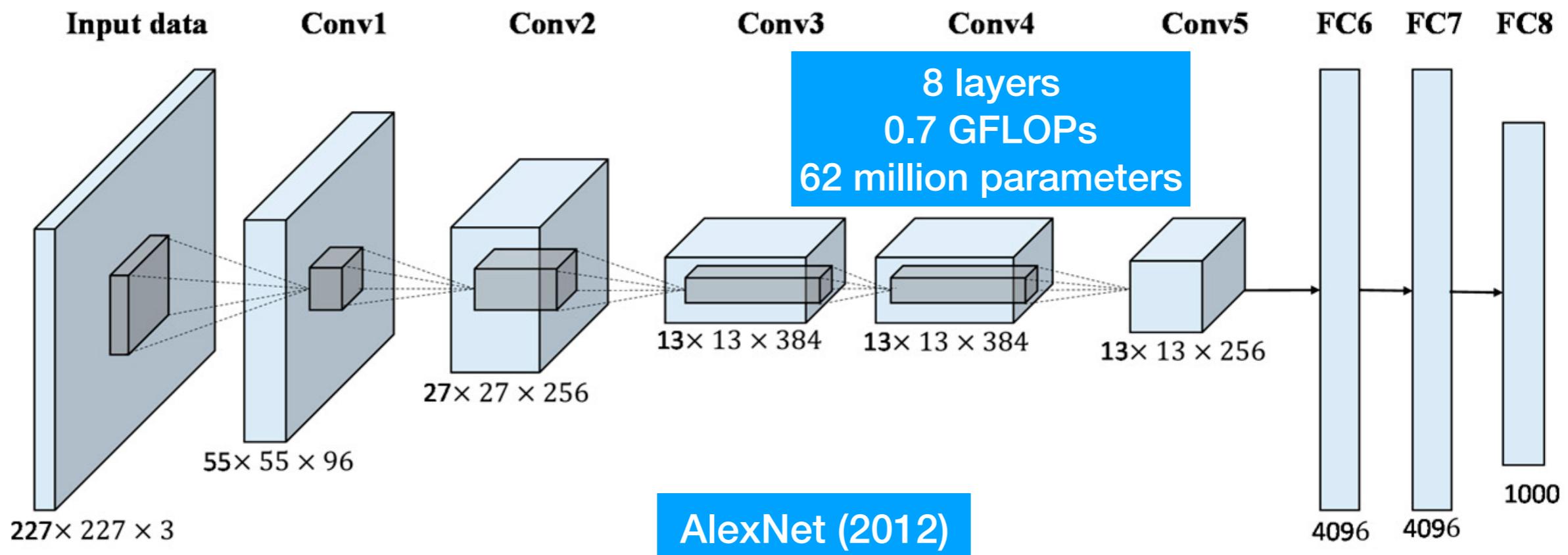
Outline

- Introduction and Motivation
 - Why compress neural networks?
- Compression of neural networks
 - Example: iterative retraining with regularization
 - Other techniques
- Examples of Compressed CNNs
 - SqueezeNet
 - Energy-Aware Pruning
 - Ternary/Binary Nets
- Summary and Outlook



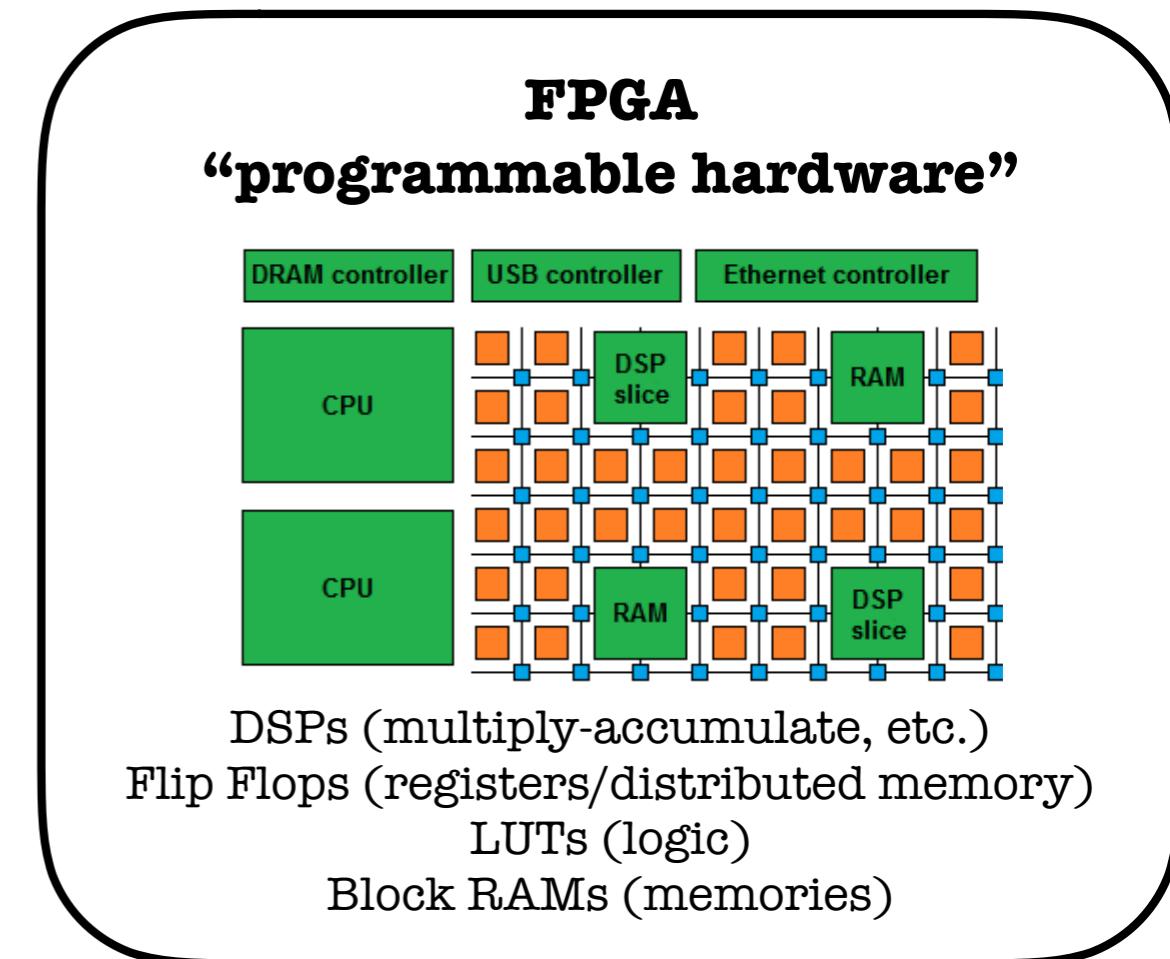
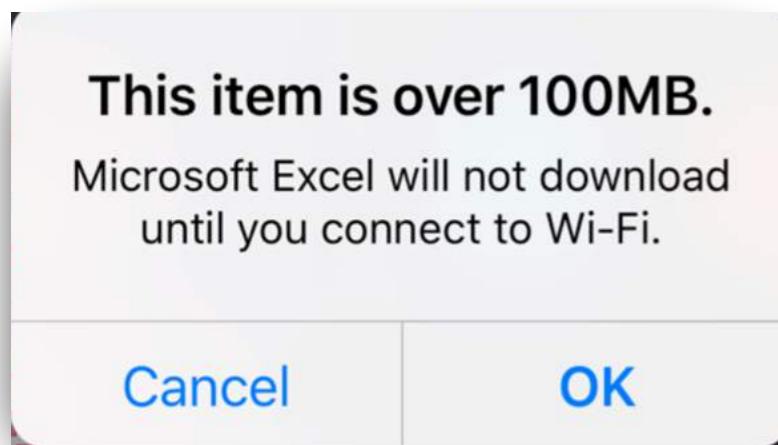
Neural Network Overparametrization

- Neural Networks are generally **overparametrized**
- You can control overfitting (dropout, regularization, large training samples, ...) but in the end you have a model with **many redundant weights**
- For applications with **limited memory, resources, or power** want to minimize network **size, complexity, and memory references**



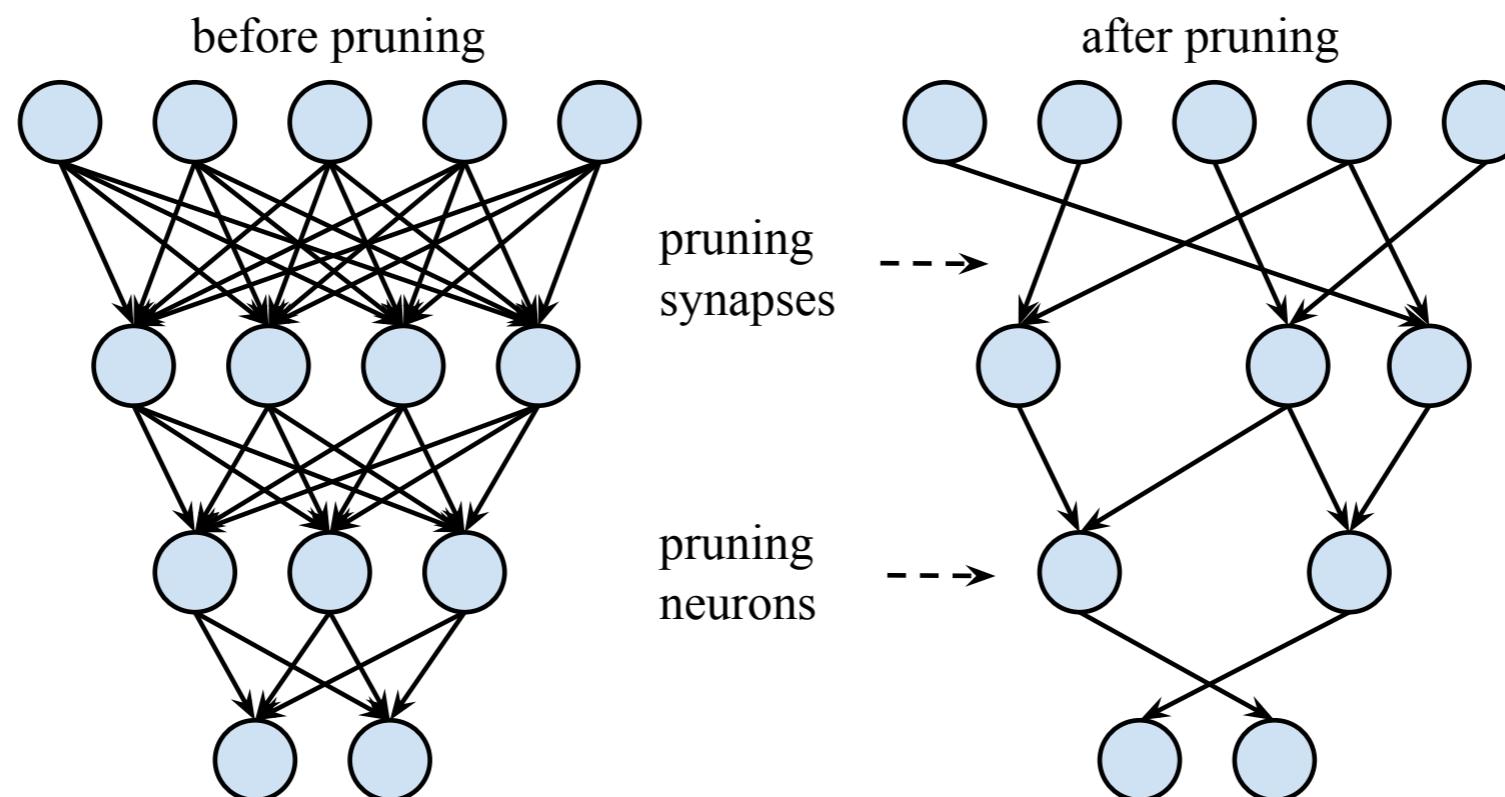
Why compress?

- If you can substitute matrix multiplication for sparse matrix multiplication, you can speed up computations especially on highly parallelized architectures like **FPGAs** (skip unnecessary computations)
- Reducing size and energy consumption is better for mobile applications



Efficient Neural Networks

- Compression/Pruning
 - Removing redundant synapses and neurons
- Quantization
 - Restrict the weights, biases, and activations to certain quantized values
 - Fixed point, integers, ternary, binary, etc.

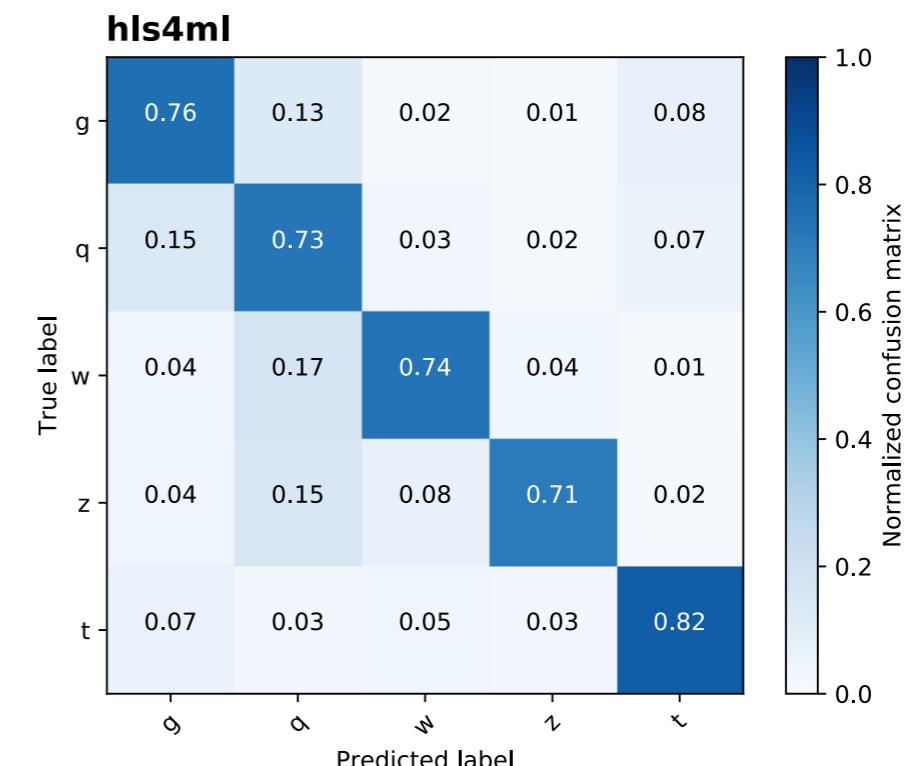
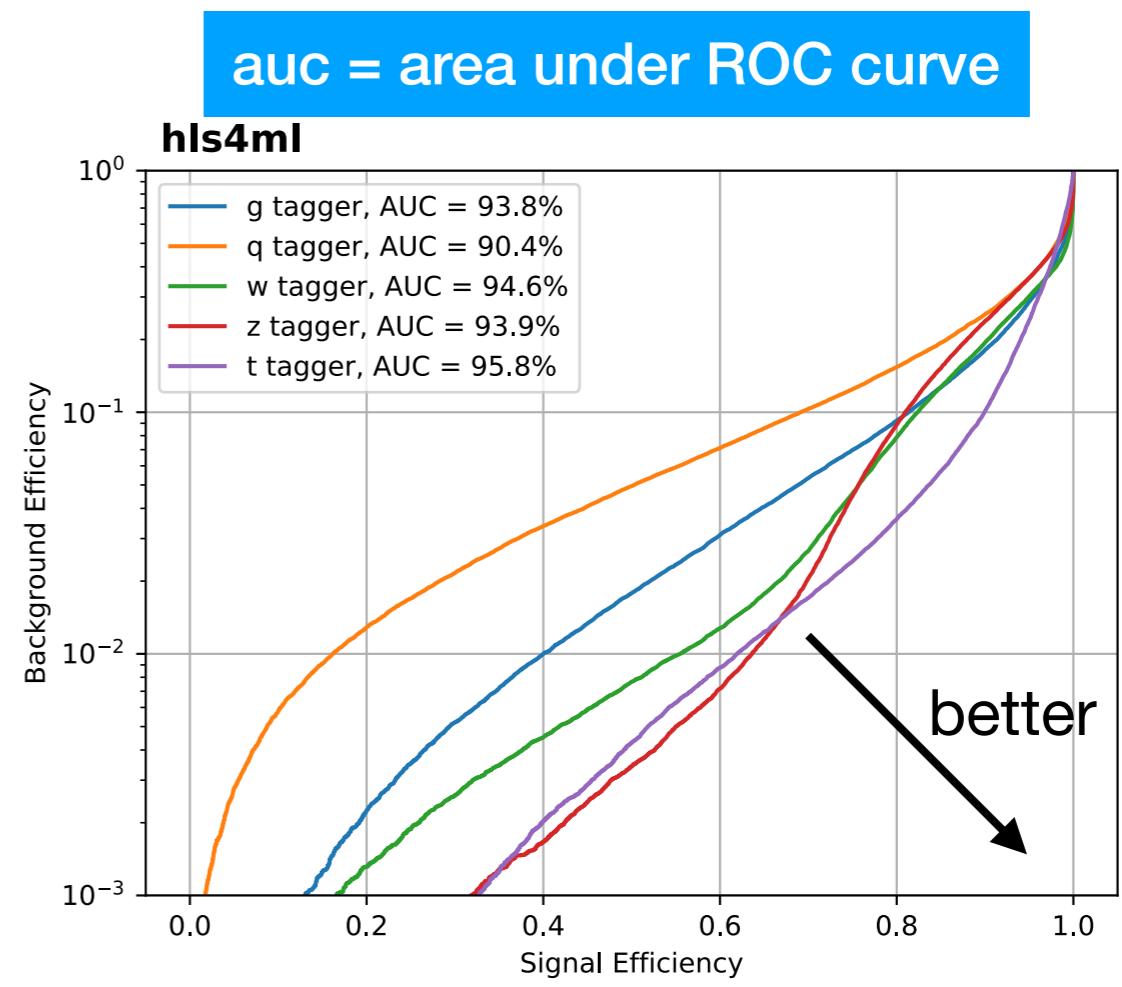
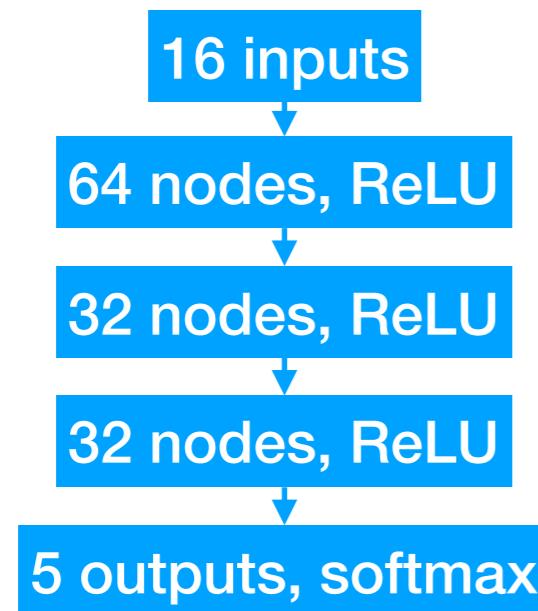


For further reading: [arXiv:1510.00149](https://arxiv.org/abs/1510.00149)



Simple Example: Jet Substructure

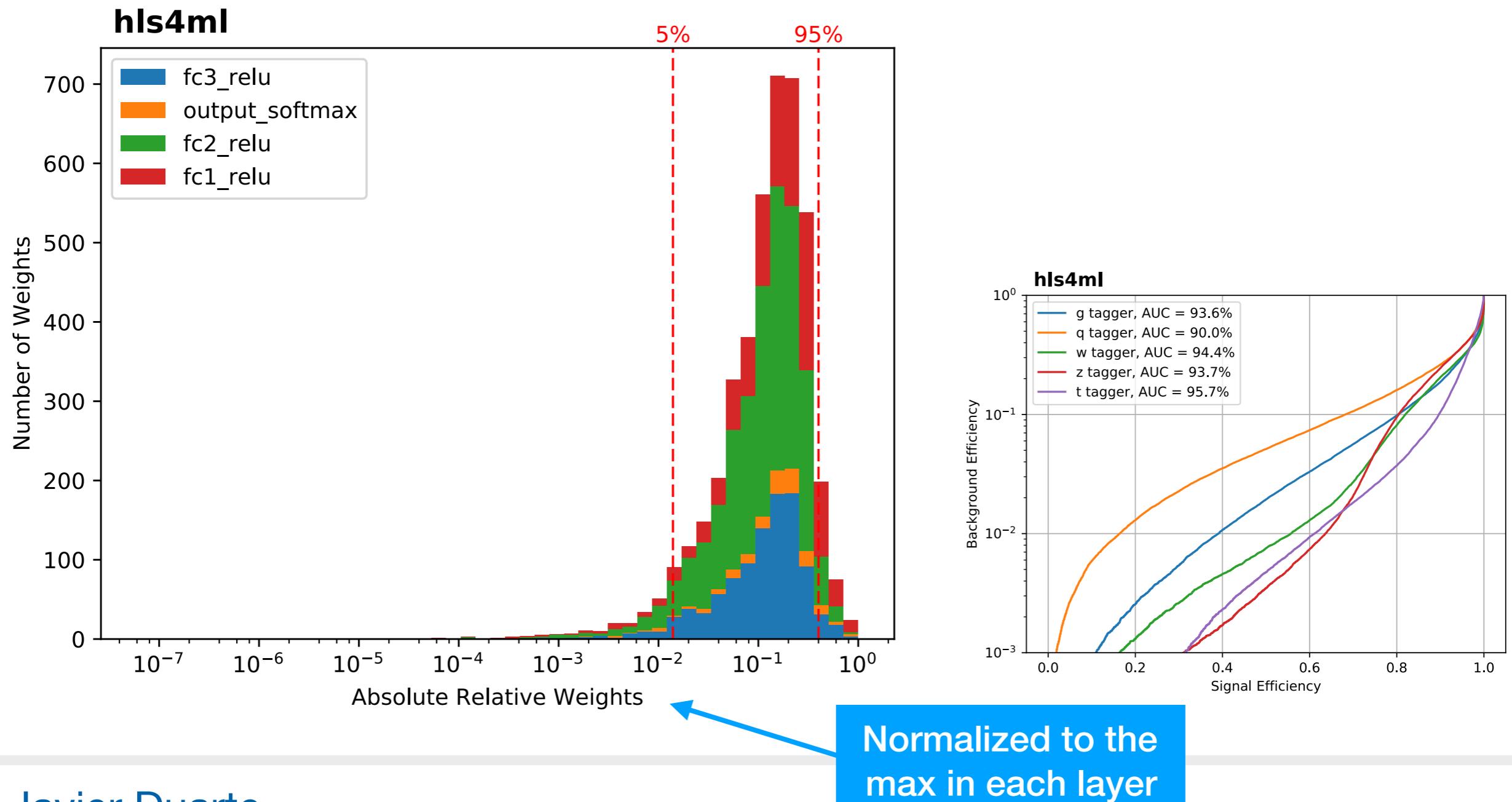
- 5 output multi-classifier
 - Does a jet originate from a quark, gluon, W/Z boson, top quark?
- Fully connected network
- 16 expert inputs
 - jet mass, multiplicity, ECFs



Distribution of Weights

<https://github.com/hls-fpga-machine-learning/keras-training>

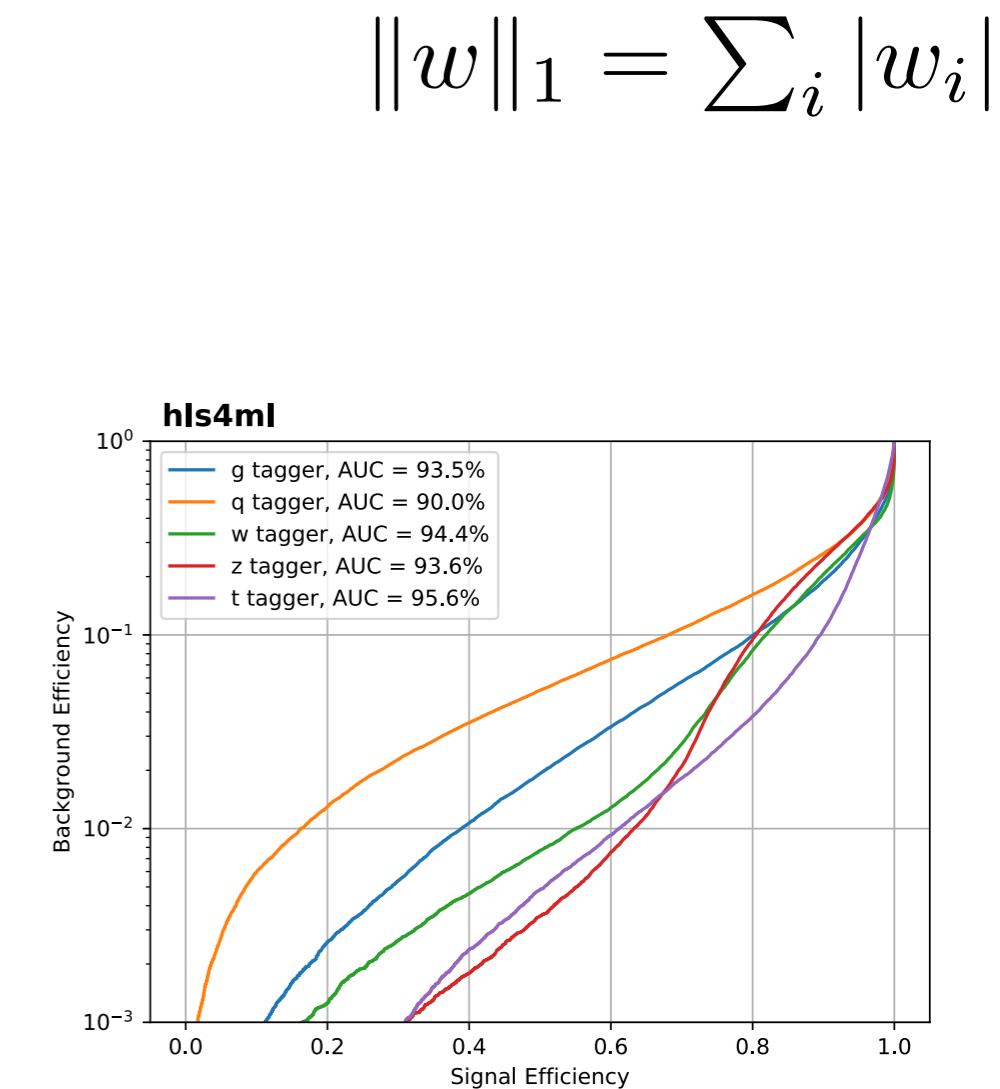
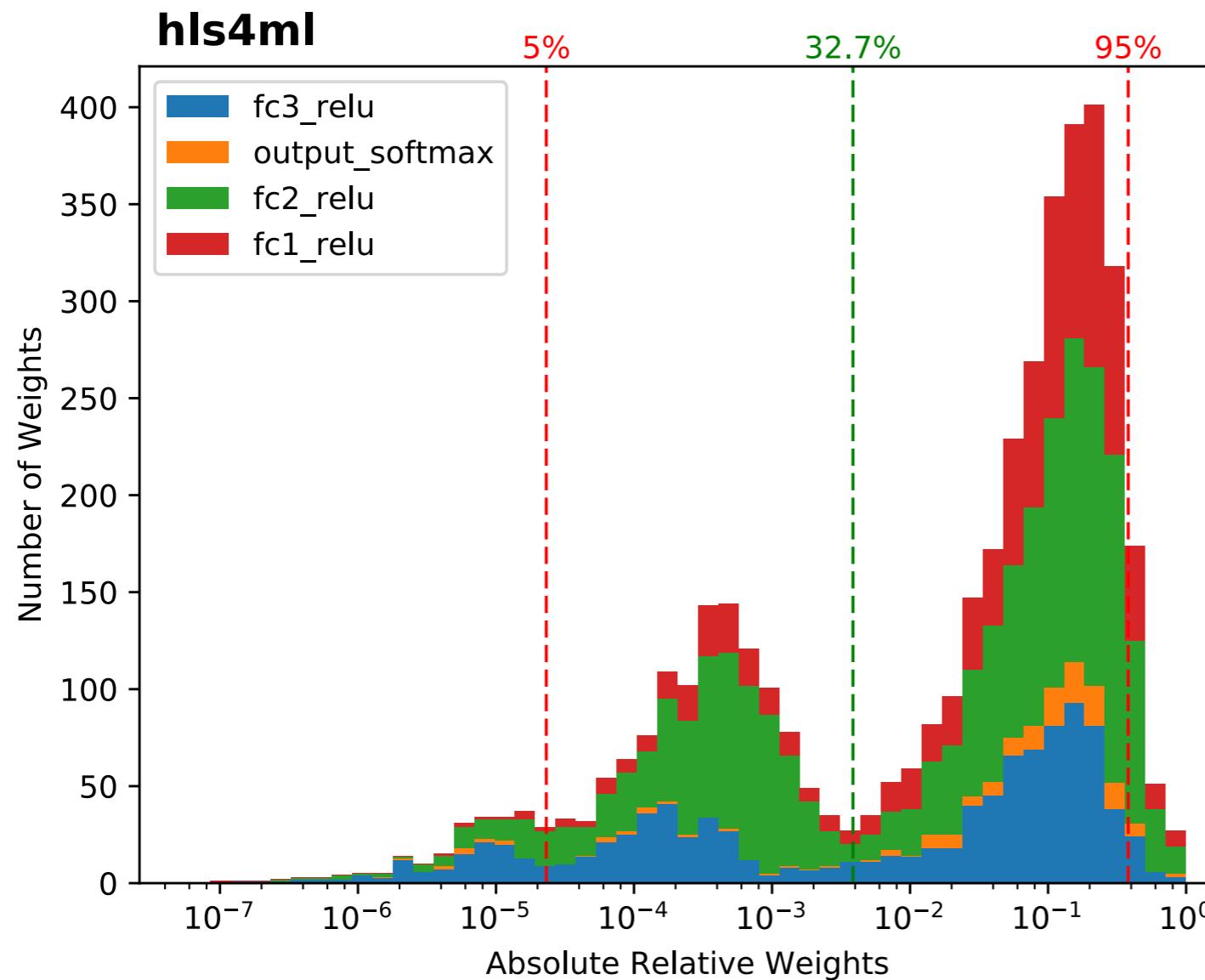
- Distribution of weights after training
- Not obvious which weights to prune



Weights after Regularization

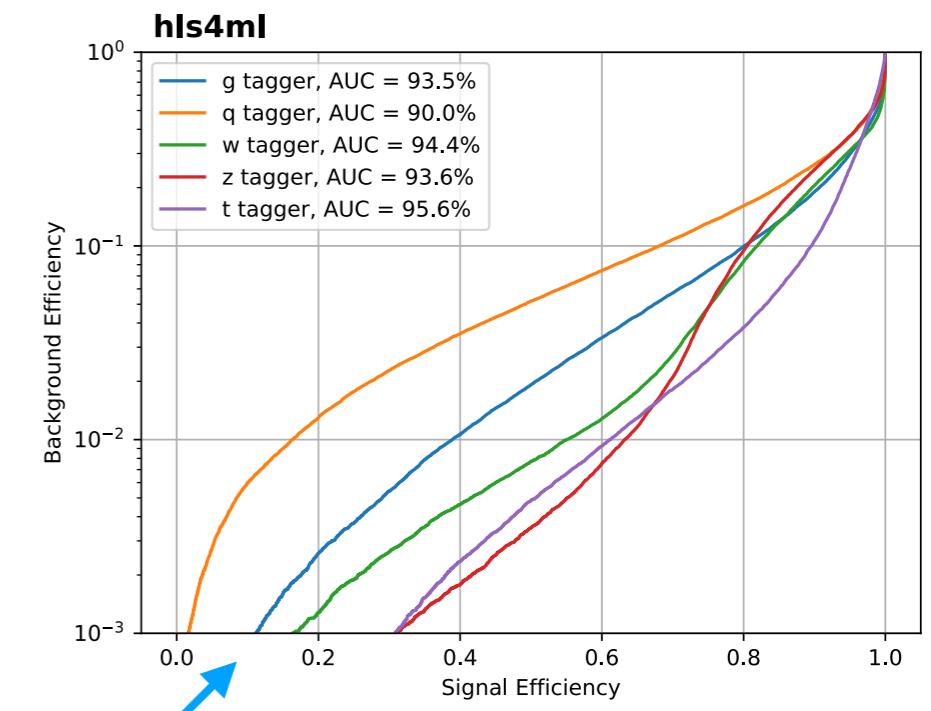
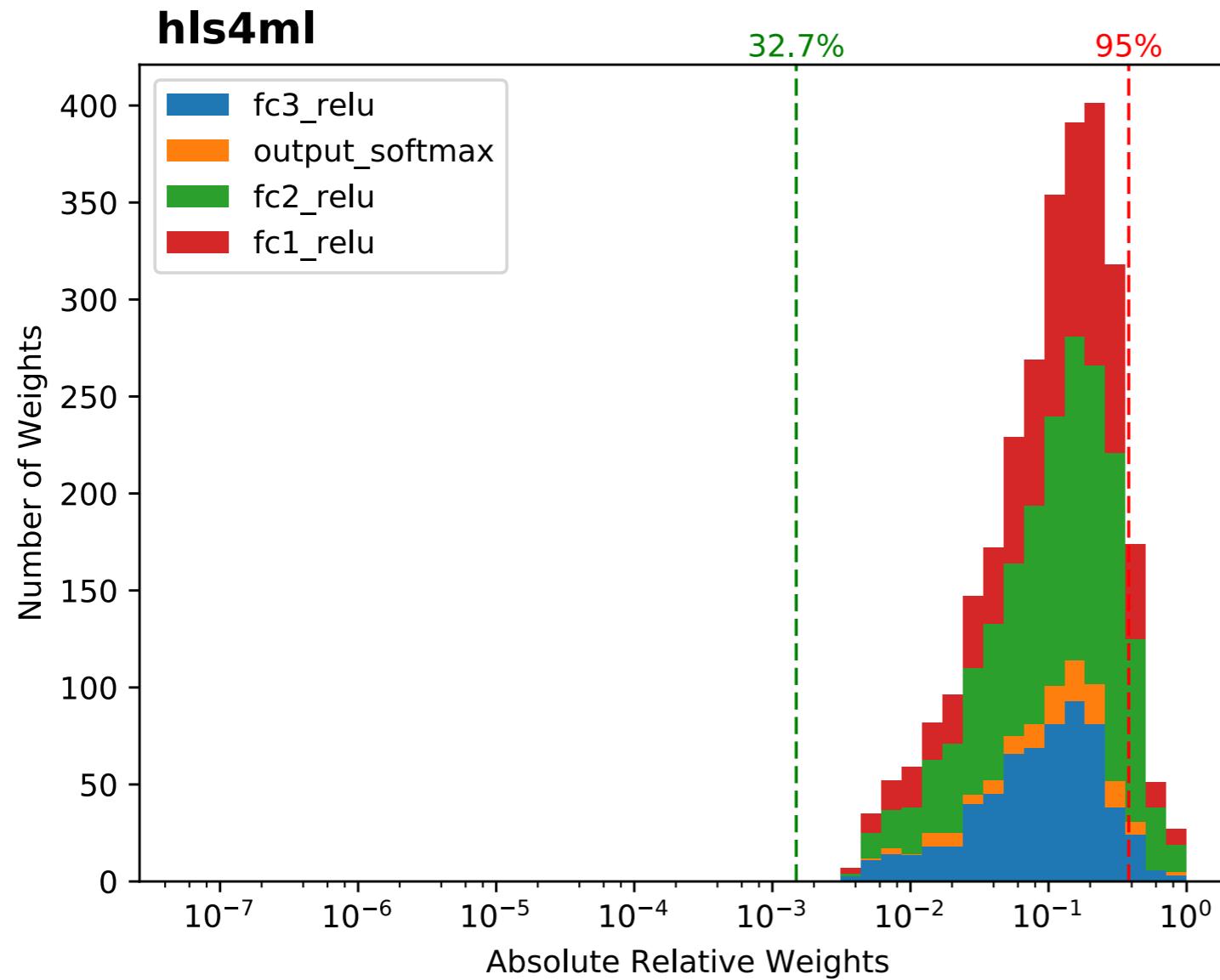
- Distribution of weights after training with L₁ regularization, lambda = 10⁻⁴
- Two populations of weights

$$L_\lambda(\mathbf{w}) = L(\mathbf{w}) + \lambda \|\mathbf{w}\|_1$$



Weights after Pruning

- Prune the bottom population
- No effect on output classifier (even before retraining!)

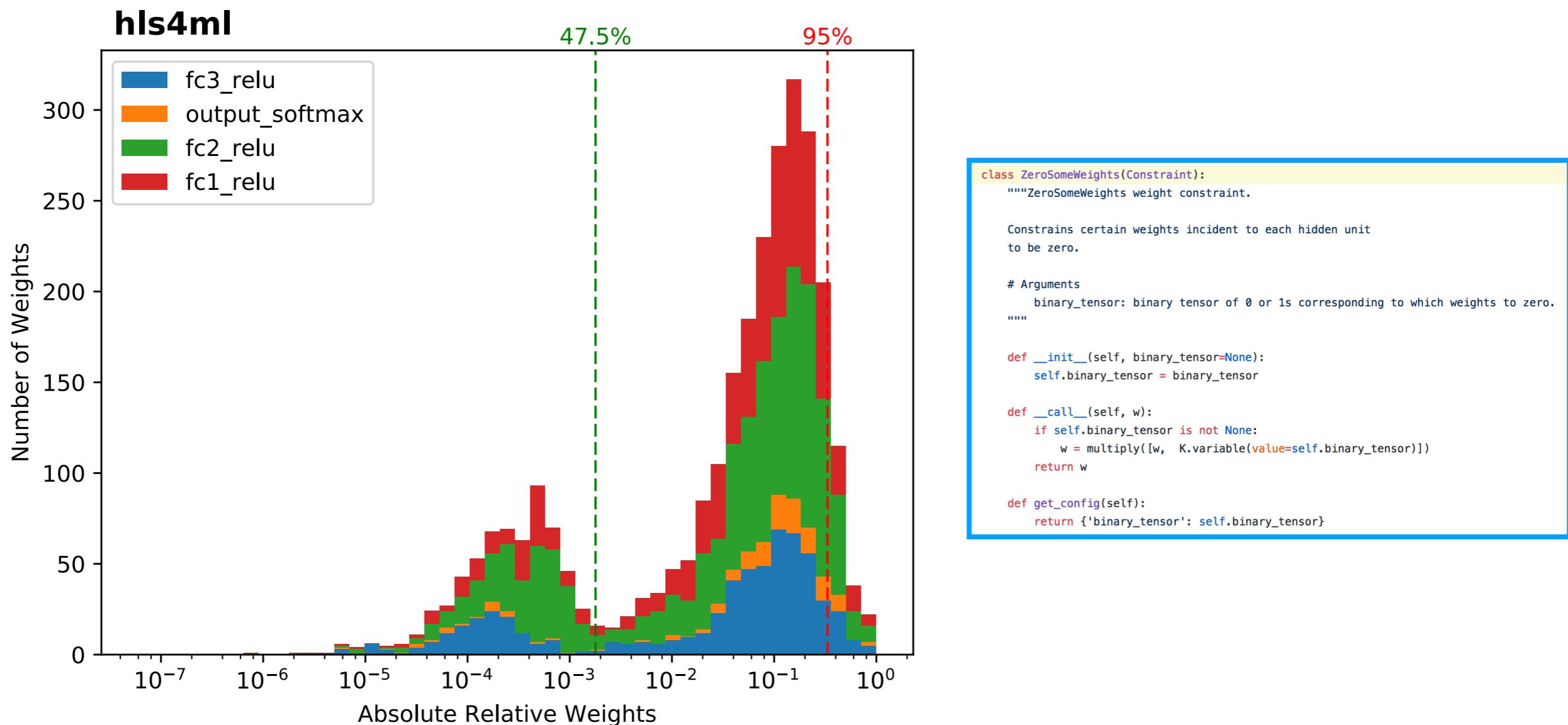


No effect



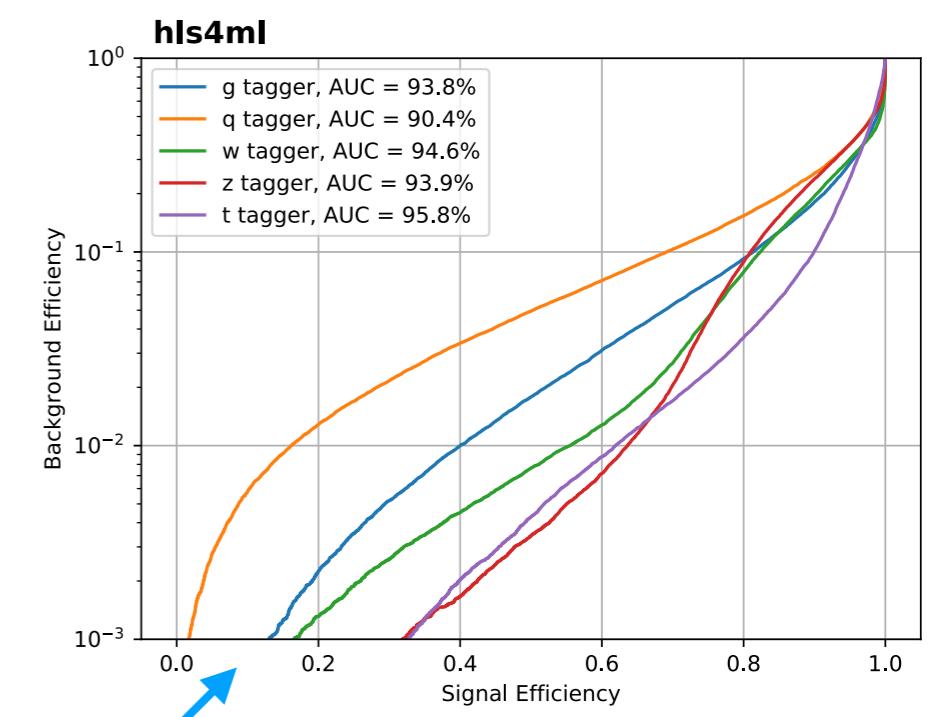
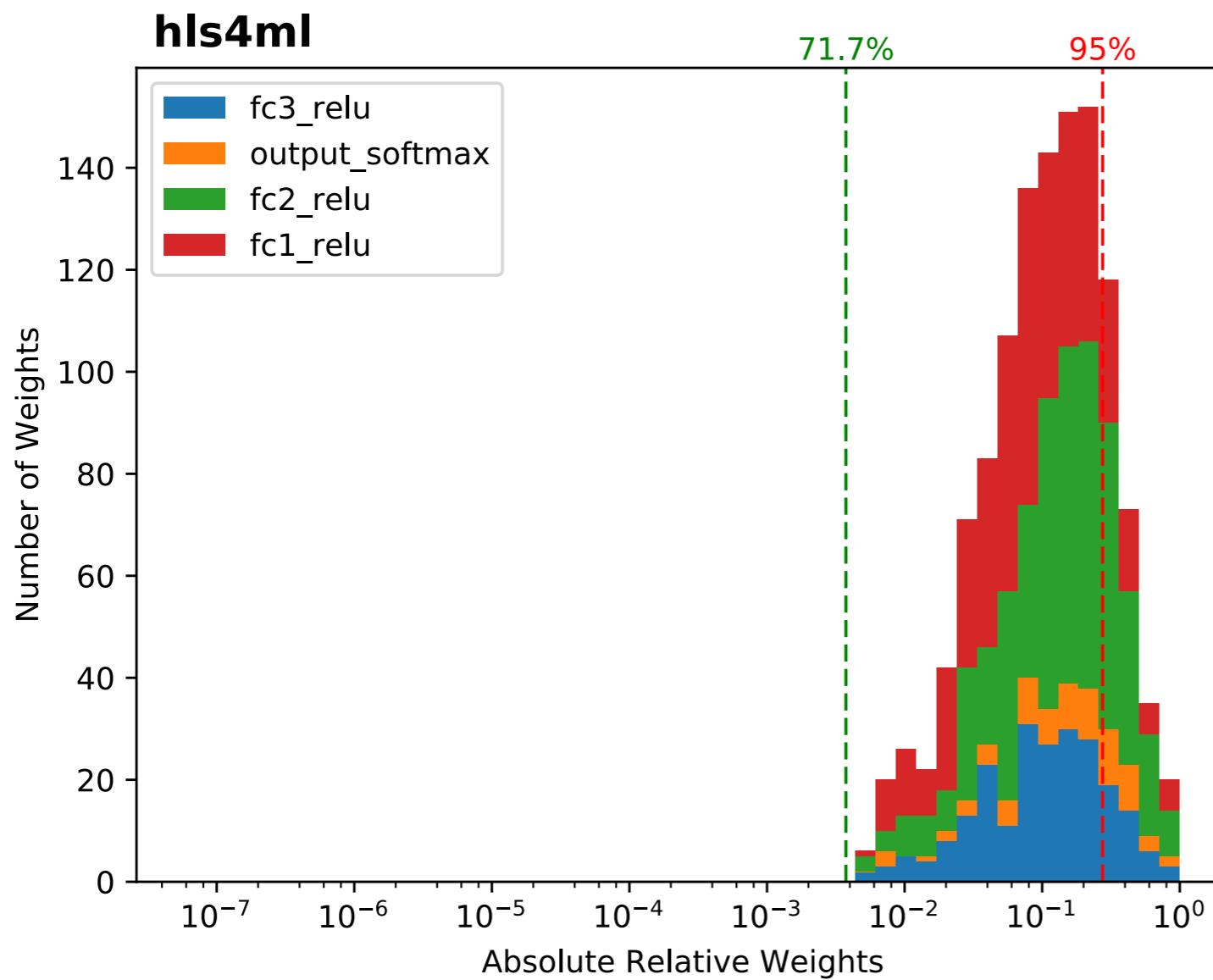
Retraining with Constraints

- Retrain with [kernel constraint](#) to keep the pruned weights fixed to zero
- Keep L₁ regularization (to find additional weights to prune)



Weights after Iterative Pruning & Retraining

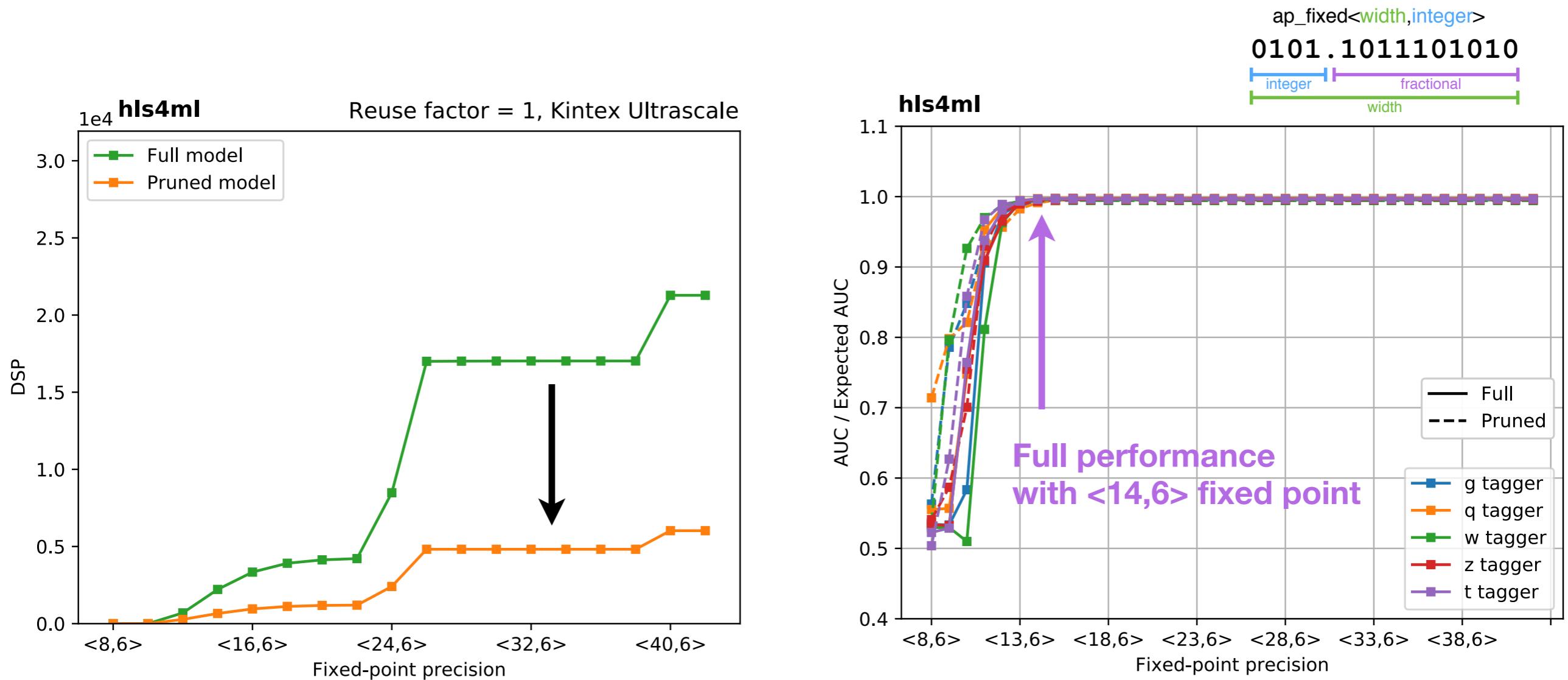
- After 7 iterations, pruned away 72% of the weights
- No effect on output classifier



No effect



Effect of Compression for FPGA Inference



- Big reduction in DSP usage with pruned model!
- Note: we didn't retrain using quantized weights (should get us down to ~8 bits instead of ~14 bits)

Other Compression Schemes

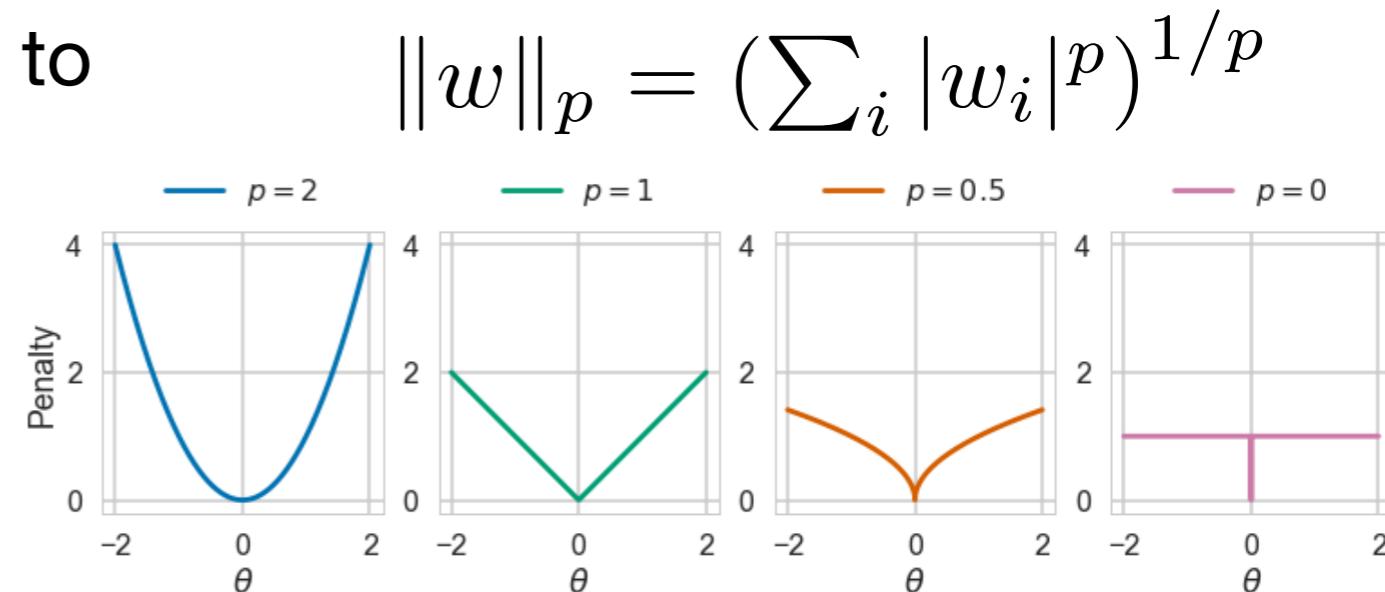
Louizos et al. 2017

[arXiv:1712.01312](https://arxiv.org/abs/1712.01312)

- Train with L_p ($0 \leq p < 1$) regularization to promote sparsity (though difficult to optimize)

- as $p \rightarrow 0$, $L_p \rightarrow L_0$

- “Optimal brain damage”: use second derivatives of loss function to rank **parameter saliency** (rather than using parameter magnitude)



LeCun et al. 1989
[NIPS 250](https://nips.cc/Conferences/1989/Paper%20Presentations/250.pdf)

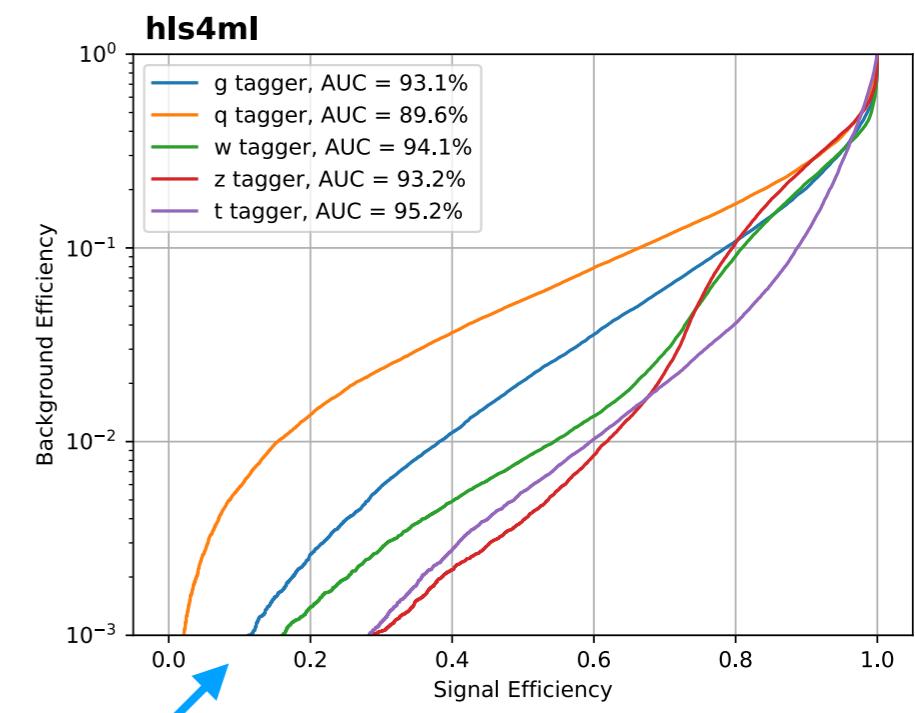
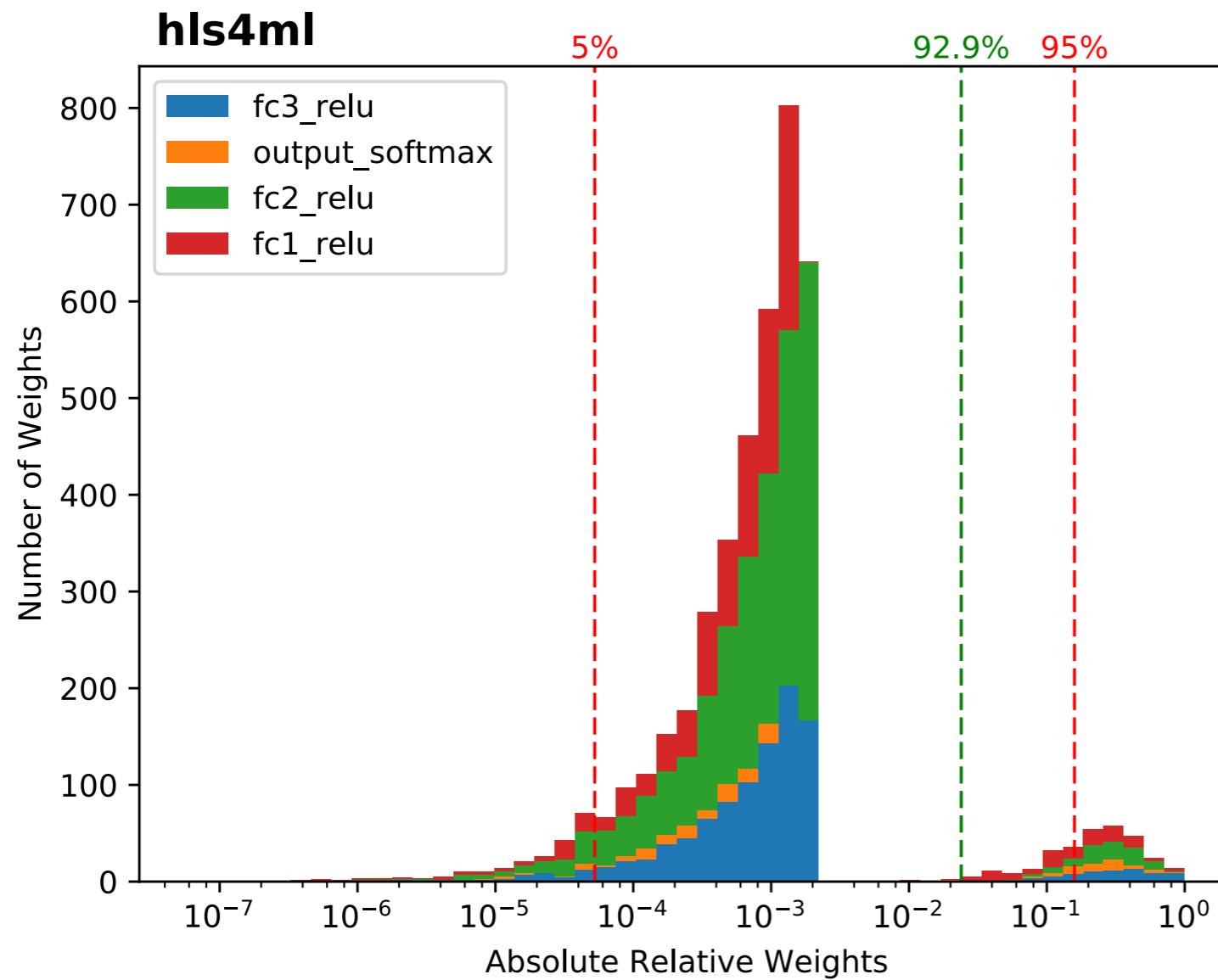
- Deep Compression
 - Trained quantization
 - Weight-sharing using k-means clustering to identify weights to share
 - Huffman coding (optimal prefix)

Han et al. 2015
[arXiv:1510.00149](https://arxiv.org/abs/1510.00149)



Aggressive L_p Regularization

- Train with L_p, p= 1/10, $\lambda = 10^{-3}$ can prune away 93% of weights
- Small effect on output classifier



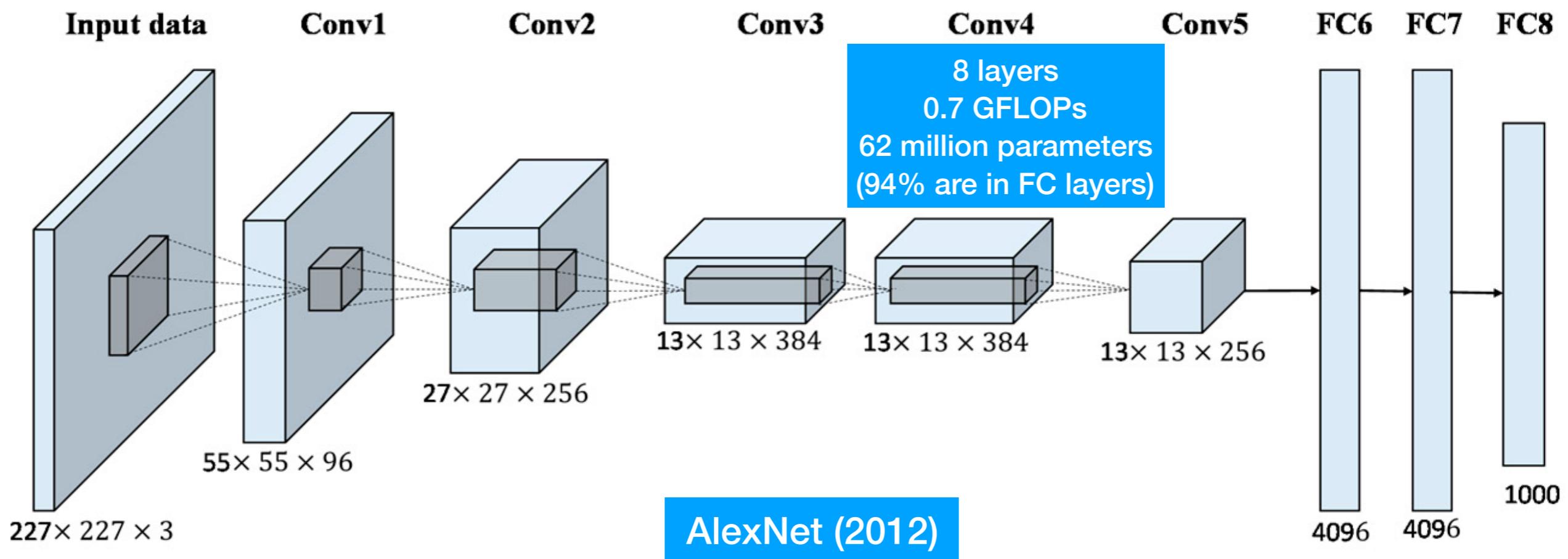
Small effect



Big Convolutional Neural Networks

- Main task is computer vision/image recognition
- Control the number of parameters by baking in assumptions like locality and translation invariance to **share weights** within a layer

Krizhevsky, et al.
[NIPS 4824](#)

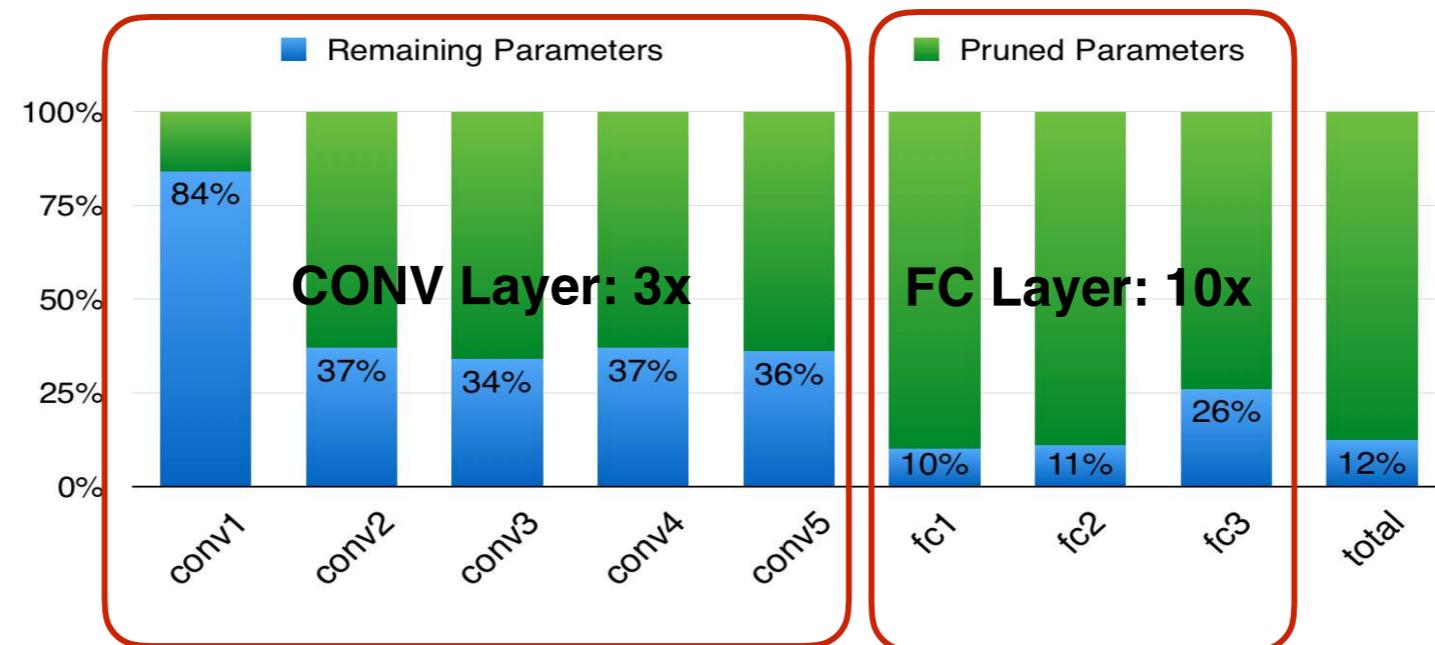


Pruned AlexNet

Han et al. 2015
[arXiv:1510.00149](https://arxiv.org/abs/1510.00149)

- Using “Deep Compression” can prune AlexNet by factor of 35x (Han et al. 2015)

| CNN architecture | Compression Approach | Data Type | Original → Compressed Model Size | Reduction in Model Size vs. AlexNet | Top-1 ImageNet Accuracy | Top-5 ImageNet Accuracy |
|------------------|--------------------------------------|-----------|----------------------------------|-------------------------------------|-------------------------|-------------------------|
| AlexNet | None (baseline) | 32 bit | 240MB | 1x | 57.2% | 80.3% |
| AlexNet | Deep Compression (Han et al., 2015a) | 5-8 bit | 240MB → 6.9MB | 35x | 57.2% | 80.3% |



SqueezeNet

Han et al. 2016
[arXiv:1602.07360](https://arxiv.org/abs/1602.07360)

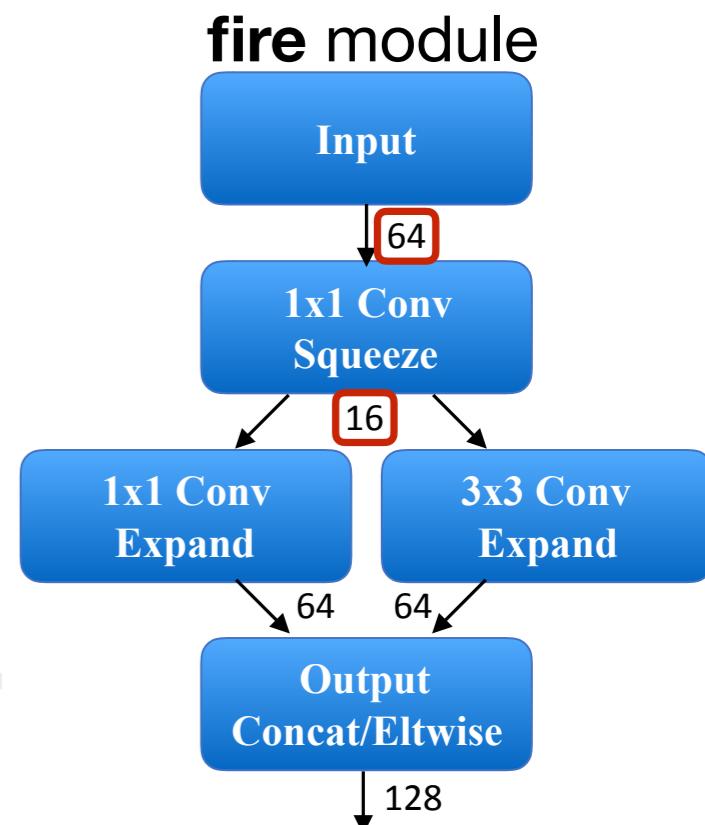
- 6-bit SqueezeNet smaller than 32-bit AlexNet by a factor of 510 and achieves the same accuracy (Han et al. 2016)
- Not just a compressed AlexNet, but re-thinking of architecture

| CNN architecture | Compression Approach | Data Type | Original → Compressed Model Size | Reduction in Model Size vs. AlexNet | Top-1 ImageNet Accuracy | Top-5 ImageNet Accuracy |
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| SqueezeNet (ours) | Deep Compression | 6 bit | 4.8MB → 0.47MB | 510x | 57.5% | 80.3% |

Strategies:

1. Replace 3x3 filters with 1x1 filters (**9x fewer parameters**)
2. Decrease the number of input channels to 3x3 filters using squeeze layers
3. Downsample late in the network so that convolution layers have large activation maps

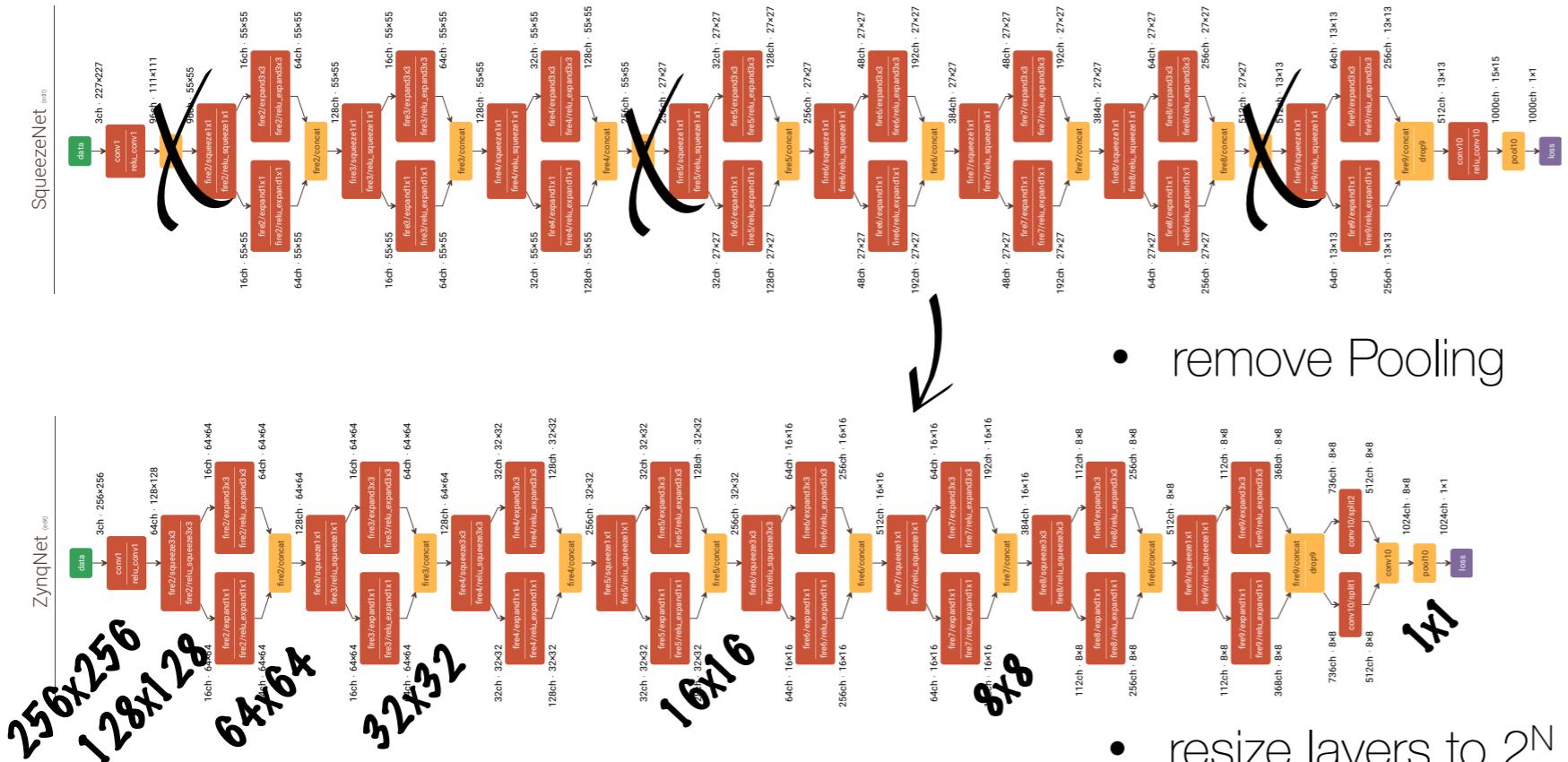
microarchitecture:



SqueezeNet on FPGA

- Fits on one FPGA with on board memory (Gschwend 2016)

Additional optimization for FPGA



Gschwend 2016
ZynqNet

- remove Pooling
- resize layers to 2^N

FPGA resources
(Kintex 7)

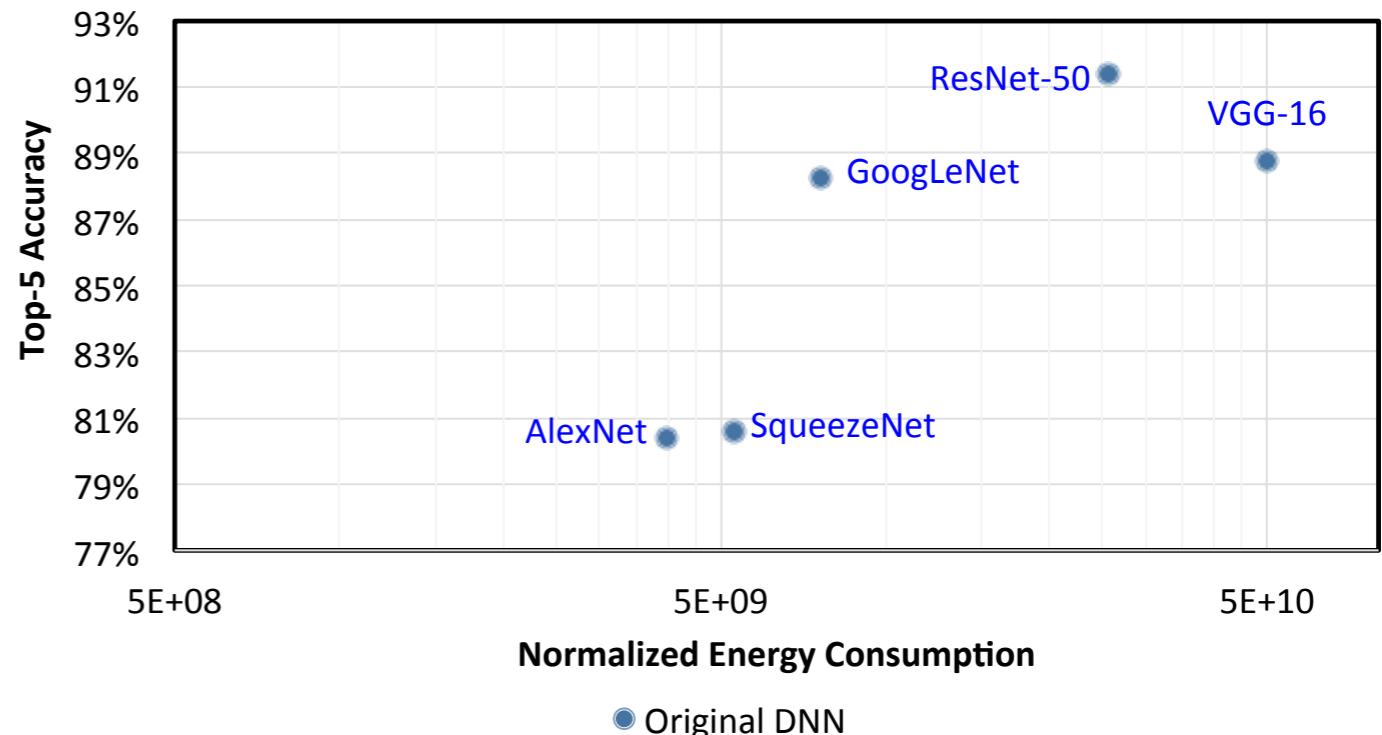
| resource | Block RAM | DSP Slices | FF | LUT |
|-------------|-----------|------------|------|------|
| used | 996 | 739 | 137k | 154k |
| available | 1090 | 900 | 437k | 218k |
| utilization | 91 % | 82 % | 31 % | 70 % |



Energy-Aware Pruning

Yang et al. 2017
[arXiv:1611.05128](https://arxiv.org/abs/1611.05128)

- Key insights:
 - Less operations do not necessarily mean less energy consumption
 - CONV layers dominate the overall energy consumption
 - Prune while directly optimizing for energy consumption



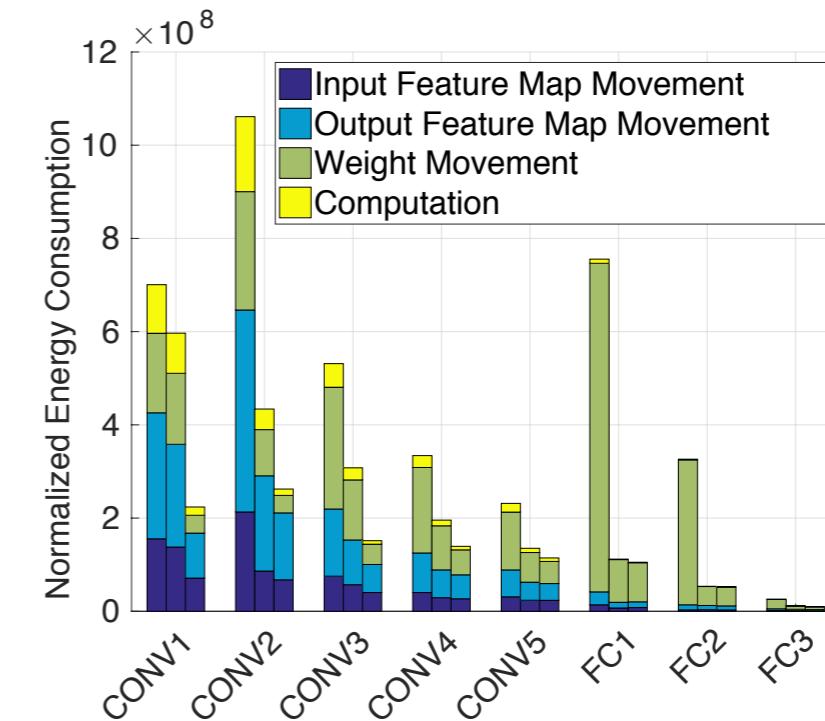
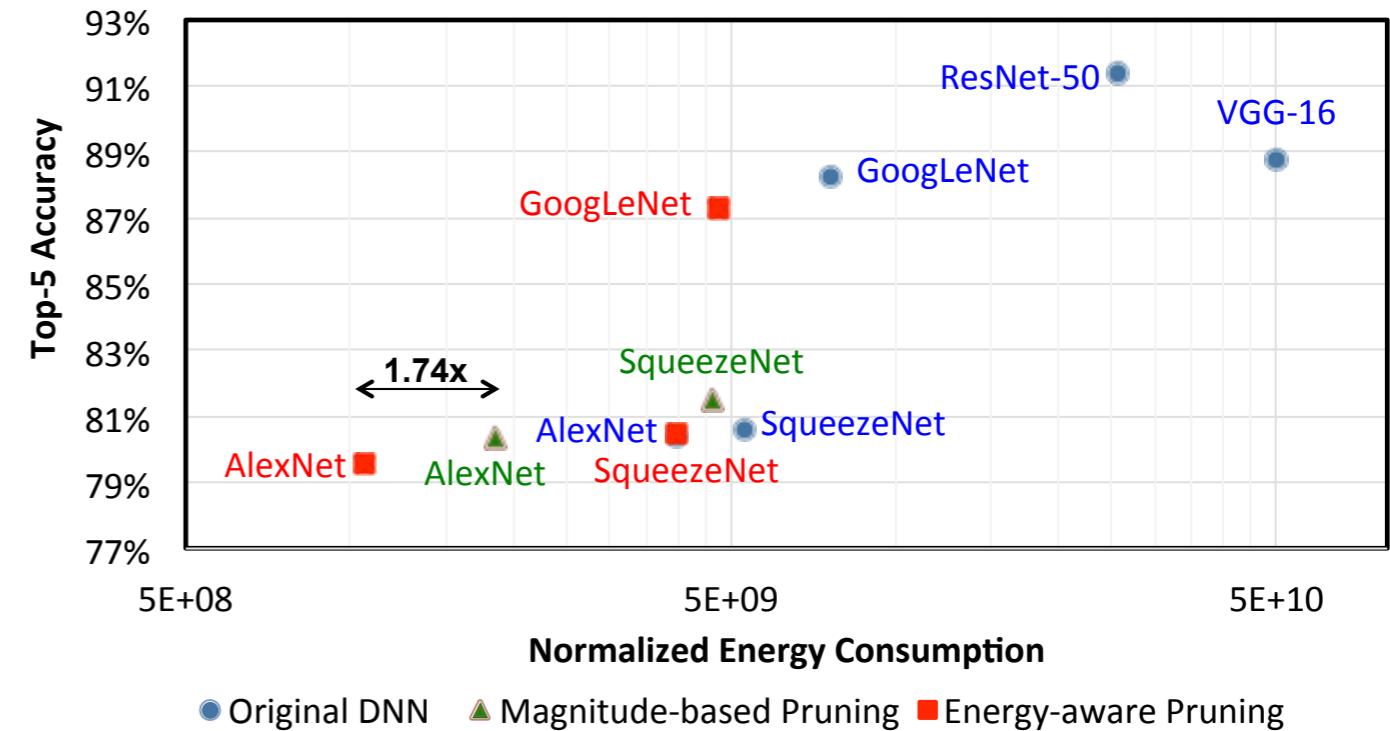
How much energy does your NN consume?
<https://energyestimation.mit.edu/>



Energy-Aware Pruning

Yang et al. 2017
[arXiv:1611.05128](https://arxiv.org/abs/1611.05128)

- Key insights:
 - Less operations do not necessarily mean less energy consumption
 - CONV layers dominate the overall energy consumption
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Left-to-right: AlexNet, pruned AlexNet, energy-aware pruned AlexNet

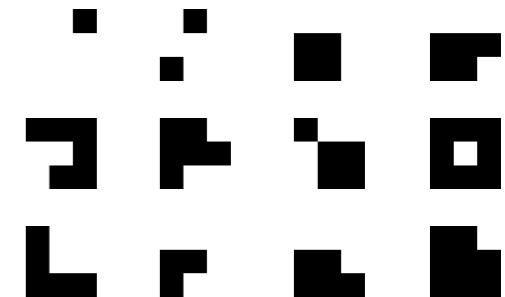


Binary/Ternary Networks

- Ultimate of quantization/compression

- BinaryConnect, BinaryNet: weights (+1, -1)
- Binary Weight Nets: weights (+w, -w),
- Ternary Weight Nets: weights (+w, 0, -w)
- Trained Ternary Quantization: (+w₁, 0, -w₂)

Binary weight filters



Sze et al. (Survey)
[arXiv:1703.09039](https://arxiv.org/abs/1703.09039)

| Reduce Precision Method | | bitwidth | | Accuracy loss vs. 32-bit float (%) |
|------------------------------|--|------------------|-------------|---------------------------------------|
| | | Weights | Activations | |
| Dynamic Fixed Point | Binary weight filters | | | |
| | w/o fine-tuning [121] | 8 | 10 | 0.4 |
| Reduce Weight | w/ fine-tuning [122] | 8 | 8 | 0.6 |
| | BinaryConnect [127] | 1 | 32 (float) | 19.2 |
| | Binary Weight Network (BWN) [129] | 1* | 32 (float) | 0.8 |
| | Ternary Weight Networks (TWN) [131] | 2* | 32 (float) | 3.7 |
| Reduce Weight and Activation | Trained Ternary Quantization (TTQ) [132] | 2* | 32 (float) | 0.6 |
| | XNOR-Net [129] | 1* | 1* | 11 |
| | Binarized Neural Networks (BNN) [128] | 1 | 1 | 29.8 |
| | DoReFa-Net [120] | 1* | 2* | 7.63 |
| | Quantized Neural Networks (QNN) [119] | 1 | 2* | 6.5 |
| Non-linear Quantization | HWGQ-Net [130] | 1* | 2* | 5.2 |
| | LogNet [135] | 5 (conv), 4 (fc) | 4 | 3.2 |
| | Incremental Network Quantization (INQ) [136] | 5 | 32 (float) | -0.2 |
| | Deep Compression [118] | 8 (conv), 4 (fc) | 16 | 0 |
| | | 4 (conv), 2 (fc) | 16 | 2.6 |

TABLE III

METHODS TO REDUCE NUMERICAL PRECISION FOR ALEXNET. ACCURACY MEASURED FOR TOP-5 ERROR ON IMAGENET. *NOT APPLIED TO FIRST AND/OR LAST LAYERS

<https://github.com/MatthieuCourbariaux/BinaryNet>

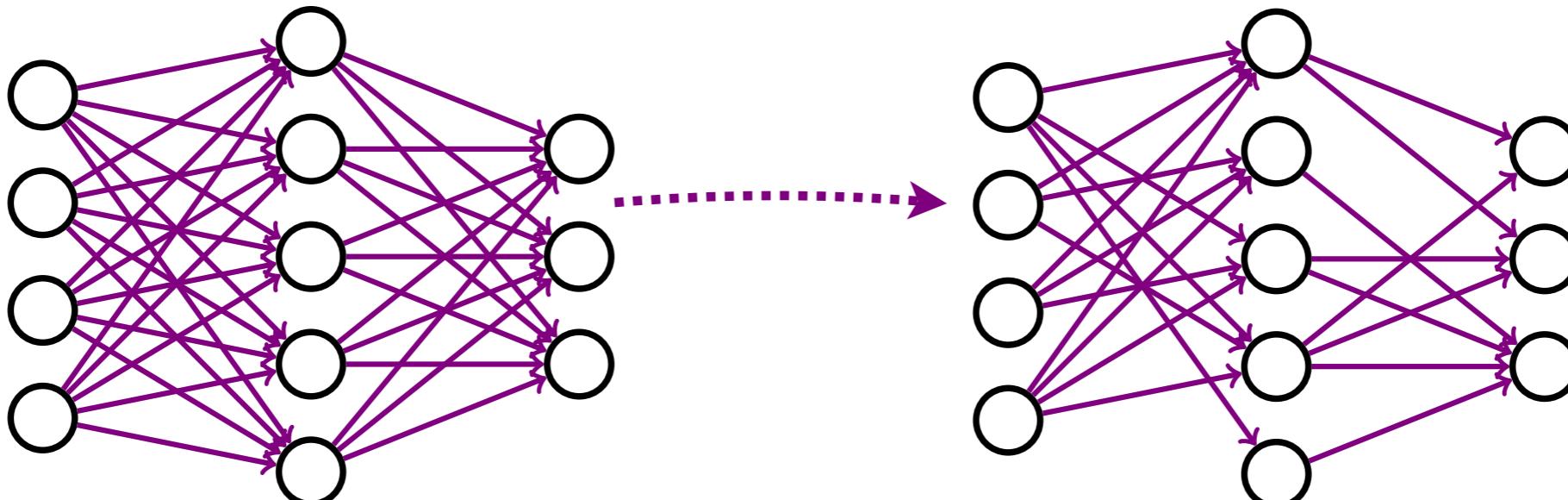
<https://github.com/BertMoons/QuantizedNeuralNetworks-Keras-Tensorflow>

https://github.com/DingKe/nn_playground/tree/master/ternarnet



Summary and Outlook

- Network compression (pruning and quantization) is an important aspect of efficiently computing ML algorithms
 - Especially important for LHC trigger applications on FPGAs
- Many different techniques / implementations
 - Implementations are currently scattered across random GitHub repositories
 - Should become a standard “tool” in our ML toolkit



Backup

