New tools for web-enabled interactive visualizations of electrophysiological data

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Abstract

Electrophysiology datasets in neuroscience are becoming richer and more complex as data is collected on multiple scales, dataset sizes increase, and more sophisticated questions are asked of the data. Visualization is an essential tool for understanding these datasets at all stages of analysis, but current practices in visualization of electrophysiological data are limited in their ability to efficiently compare between visualizations (such as between spike raster plots of neurons or between regression model coefficients and raster plots) and filter complex data (such as comparing only correlations within a brain area versus comparing correlations between brain areas). Such difficulties are only magnified as the amount of data increases.

This paper describes a set of composable, web-enabled interactive visualization tools developed for use in electrophysiological studies. These tools were developed to enhance exploratory data analysis, checking of raw data and statistical modeling assumptions, and data presentation for large, complex and multi-scale neuroscience data. Data from several experiments were used to test to the tools. These visualization tools are viewable in the web browser, making them easily shareable online, and open-source, allowing for modification and development by the neuroscience community.

Introduction

Current theories of brain functioning ascribe different roles to different scales: neurons, cortical layers, brain areas, networks between brain areas. For

example, the Communication-through-Coherence Hypothesis postulates that communication in the brain happens primarily through phase coordination between groups of neurons (Fries, 2005). This phase coordination between groups of neurons may differ between different layers, frequencies, within-brain areas, and between brain areas (Buffalo et al., 2011; Buschman et al., 2012; Gregoriou et al., 2009). Through the use of multiple electrode arrays and laminar probes, we are beginning to collect data at these different scales and understand how they interact (Miller and Wilson, 2008). However, as electrode technology progresses, our understanding of the data is not limited by the amount of data we can collect, but by our ability to efficiently understand and model relationships in the data.

Take, for example, a typical analysis of an electrocorticography dataset in which grids of intracranial electrodes are placed across wide swaths of cortex. These grids span multiple brain areas and can measure both local field potentials and action potentials (Figure 1a). Given enough data, this allows us to ask questions about the properties at different spatial scales (units, multiunits, local field potentials, brain region summaries) and how they relate (e.g. correlation and coherence between local field potentials, local field potentials and neurons, neurons and neurons, see Figure 1b). Moreover, we can ask questions about how these change over time and/or relate to experimental conditions. This results in a dataset with many complex interrelations.

Understanding a dataset such as this becomes even more challenging as we can record from more electrodes, because the number of possible associations between electrodes scales quadratically. For example, 10 electrodes means analyzing 100 relationships between electrodes. Implantation of multielectrode arrays with upwards of 100 electrodes are becoming common (Einevoll et al., 2012; Miller and Wilson, 2008; Siegel et al., 2015) and the number of simultaneously recorded neurons is projected to double every seven years (Stevenson and Kording, 2011).

Visualization of data is one way that we can reduce data complexity—allowing us to make multiple simultaneous comparisons, easing the cognitive burden on working memory by efficiently encoding properties of the data into features salient to the visual system (ref). In addition, visualization is important in the understanding and checking of statistical assumptions—it helps reveal differences between the expected structure of the data and the observed data (Anscombe, 1973; Tukey, 1977). This is important, from

the initial stages of analysis to publication, for revising our assumptions and models and for understanding and communicating where and how often our models fail (Gelman, 2004).

However, current practice with electrophysiology data relies on static visualization — requiring the generation of figures for each particular view. This makes it difficult to explore and check the data efficiently. For example, Liu and Heer (2014) found that even a 500 millisecond delay between visualizations could reduce the amount of the dataset explored and affect the number of hypotheses and observations formed.

Adding interactivity allows the user to change perspectives and modify analyses on demand, facilitating comprehension and hypothesis generation (Liu and Heer, 2014). Neuroimaging studies, which generate large datasets with complex interrelations, make extensive use of interactive visualization tools (e.g. the freeview module in freesurfer, pysurfer, spm), but there are no such tools that exist for electrophysiology studies. One can design user interfaces using MATLAB, but these are hard to share and require commercial software.

We present a set of three tools aimed at providing basic interactive visualizations for electrophysiology studies: SpectraVis is a tool aimed at exploring task-related functional networks over time and frequency; RasterVis is a tool for dynamically displaying and sorting spike raster plots and peri-event histograms; and GLMVis is a a tool for displaying coefficients from generalized linear regressions — which are commonly used to describe the receptive field of neurons. Each visualization allows for examination of the electrophysiological signals (or summary statistic of the signal) over time relative to task-relevant events, comparison of different subjects or recording sessions, and aggregation or filtering of signals. The visualizations can also be easily linked together and static visualizations can be exported for use in papers. Finally, all visualizations are web-based making them easily shareable and operating system independent, and open-source, allowing for modification and repurposing by the neuroscience community. To see working examples of all three tools, please visit http://ericdeno.com/research/.

Related Work

There have been previous attempts to make web-enabled dynamic, interactive visualizations in neuroscience. Here we describe several notable visualizations.

The pycortex webGL MRI viewer is a web-enabled interactive visualization tool that displays the results from Huth et al. (2012). In the study, Huth and colleagues had subjects view two hours of movie trailers. They then categorized objects and actions in the movies, regressed the categories on the BOLD fMRI signals collected on the subjects watching the movies, and performed a principal components dimensionality reduction to recover a "semantic space". The visualization displays a single subject's color-coded 3D cortical surface representation of this semantic space where similar colors indicate similar categorical representations. The visualization also displays a map of the semantic space itself.

The visualization has interactive controls that allow the user to click on a category to see how it is represented throughout the cortical surface. Conversely, the user can click on a voxel on the cortical surface to see the different categories associated with that voxel. The visualization also provides button controls that dynamically transform the view of the cortical surface (e.g. from inflated to superinflated or from superinflated to flat) and sliders that control the thresholding of the surface colors. The cortical surface can be rotated by dragging the cortical surface. A user can also obtain a permanent web link to a particular voxel of interest by clicking a button. Code for the pycortex viewer is available on Github.

The Allen Cell Types Database is a visual interface for a database of neuronal cell types in mouse lateral geniculate nucleus and primary visual cortex. The visualization has several interlinked views including an anatomical cell location view, a parallel coordinate plot of cell features, and a list of cells with more detailed information about the experiment and a brief visual summary of its morphology and electrophysiological response pattern to a step current.

Interactive controls allow the user to filter results for layer type, mouse line, and hemisphere. Clicking on cells in the anatomical cell location view, highlights that cell in the list of cells and in the parallel coordinate plot. The parallel coordinate plot provides a way to visually filter by cell features such as FI curve slope or rheobase. Clicking on cell summary brings the user to

another web page with more detailed information about that neuron such as the cell's response to different types of currents and comparison to common computational models (e.g. leaky integrate and fire) fit to the data.

The Allen Mouse Brain Connectivity Atlas is a similar interface that allows the user to explore the results of 2173 tracer injection experiments on mouse brains. The visualization consists of a 3D cortical surface with labeled injection sites, a brain section image and whole brain projection image corresponding to a specific experiment, and a list of all the projection sites. A user can filter by target or source of the injection or click on an injection site to get the corresponding section and projection image.

Lastly, Freeman and colleagues have incorporated interactive visualizations into their library of distributed computing tools for large scale neuroscience (Freeman et al., 2014). Their tools — Lightning and Thunder — allow for basic chart types such as line graphs, network force diagrams, and heatmaps and custom visualizations to be constructed and updated in real time from data pushed from a server. They demonstrated on whole brain zebrafish recordings how these can be made into interactive visualizations. For example, using tuning curves estimated from moving stimuli in different directions, they visualized the spatial layout of the preferred direction of all neurons in the zebrafish. Mousing over the spatial layout shows the firing rate time course of a neuron in that region. Code for Lightning and Thunder are also available on Github.

Materials and Methods

Design

A set of tools is only as useful as the number of people that can use them. We decided that each visualization should adhere to a set of design principles to make them maximally useful to both the users of the visualizations and developers of visualizations based on our toolkit. To that end, our approach is to create interactive visualizations that are:

1. **Shareable** — so others can easily view the visualizations online or in print.

- 2. **Modular** so the visualizations can be used independently or linked together to provide an integrated view of an electrophysiological dataset.
- 3. **Extendable** so others can implement their own visualization algorithms and modify the visualizations for their own use.
- 4. **Configurable** so visualizations can dynamically display different datasets or be preset to a particular view state.

Shareable

To make the visualizations shareable, the visualizations were written with modern web technologies — HTML, CSS, and Javascript. They can be deployed via a local or remotely hosted webserver and viewed with any modern browsers (Firefox 4+, Chrome 4+, Safari 4+, Opera 9.5+ and IE9+). As a result, the visualizations require no specialized software (beyond a browser) to view.

Users can share a particular state of the visualization using permanent links (permalinks) — each visualization has a button which provides the URL containing the parameters necessary to generate the current view. For example, with SpectraVis, if you wanted to share a snapshot of the correlation network at a specific time (e.g. 100 ms after stimulus onset), clicking on the link button would provide a URL that could then be shared with colleagues.

Additionally, static visualizations can be saved for publication purposes. Each visualization includes a button to download the current view of the visualization in scalable vector graphics (SVG) format. This format has the advantage that it can be resized without loss of resolution — making it useful for both presentations and publications — and can be imported into a graphics program of choice such as Inkscape or Illustrator for further modification. The New York Times, which frequently uses interactive graphics online and in print, has used this workflow successfully.

Modular and Extendable

Each visualization is self-contained and works independently of the other visualizations. The visualizations can be selectively linked together by using the permalinks — which allow specification of a particular state of the linked visualization. For example, GLMVis might display a neuron's receptive field

response to several experimental stimuli. By a simple modification of the code, this can be linked to the neuron's raster plot in RasterVis — showing the spiking response of the neuron to each experimental stimuli.

The visualizations' internal code is also constructed modularly — separating the internal visualization modules from data loading modules and from user interface elements such as buttons. Developers can import and export these modules selectively or make their own modules, making the visualization customizable to the developers' needs. For example, in SpectraVis, a developer might want to customize the layout of the correlation networks, spatially grouping nodes by brain area or another desired metric. Constructing the code modularly allows a developer to implement this new layout without interring with the rest of the code internals.

Finally, each visualization has its own online software repository. The repositories are hosted on Github and can be downloaded and installed — including all software dependencies — using the node package manager (npm). This ensures the development tools, such as deploying a local webserver (allowing the user to view the visualization on their own computer without having to host it remotely), are included. This helps developers extending the visualizations to get started developing as quickly as possible. These repositories are also open-sourced under the GNU General Public License (version 2), meaning the code is available to anyone to use and develop as long as the code remains open-source.

Configurable

The visualizations are configurable in three ways: parameters can be passed through the URL, parameters can be preset using Javascript via the init function for each visualization, and data and data labels can be loaded using the JSON file format.

The JSON file format is a readable, XML-like format allows the visualization to display different datasets — the visualization dynamically adjusts the axes, labels, and the display for each dataset based on the JSON file. In order for this to work, the JSON files must be in the specified format for the visualization, details of which are documented on the wiki for each visualization (Include figure with an example here?).

Importantly, JSON files can be exported from MATLAB structures (using, for example, the open-source toolbox JSONlab) and Python — providing an important bridge between commonly used analysis tools and the visualizations. An example workflow might be to do the analysis in MATLAB, format the data into MATLAB structures that correspond with the visualization, use JSONlab to export the MATLAB structures to the JSON format, and use the visualization tools to explore the dataset. Example MATLAB scripts for exporting JSON in the correct format are included in the Github repositories to make it easier for the user to get started.

Results

Here we describe the functionality and interface for the visualizations and explain why they are useful for analyzing electrophysiological data.

SpectraVis

Functional network analysis is a growing area of neuroscience research, driven in part by technological improvements allowing us to record from more sensors simultaneously. However, as researchers record from more sensors, network analyses can become unwieldy and hard to interpret, because the number of possible network connections scales quadratically with the number of sensors (e.g. electrodes). Further, we expect neural processes to form dynamic networks that vary over time, frequency, and spatial scales (e.g. within and between brain regions), adding numerous dimensions to network analyses.

SpectraVis is an interactive visualization aimed at enhancing exploratory analysis of networks by allowing the user to efficiently: (1) compare task-related functional networks over time and frequency, (2) compare individual and associative measures on all sensor pairs (e.g. spectra, coherences), (3) compare different measures of association (e.g. correlation vs. coherence, binary vs. weighted networks), and (4) view networks at two spatial scales (sensor- and region-of-interest-level). The different views of SpectraVis are dynamically linked, highlighting relationships between the metrics in response to user interaction.

Figure 1 shows a typical view of SpectraVis. The network view shows the anatomical location of the sensors (circles with sensor number) and

edges (lines) weighted by the edge statistic (color of the line, measure of association between the sensors). In this example, the edges are binary, representing significant changes in local field potential coherence between Speech — subjects reading aloud the words of the Gettysburg Address — and Silence at a particular frequency (10 Hz) and time (187.5 ms after speech onset). The network has dense connectivity within and between primary motor and primary somatosensory cortices (M1 and S1). Users can compare between binary edge statistics, which categorically declare associations between sensors, and weighted edge statistics, which use continuous measures such as the raw coherence difference and z-scored coherence difference, via the edge statistic dropdown.

The controls can also be used to examine the evolution of the network over time using either the time slider, which can be dragged to a time of interest, or the play button, which will automatically move the time step forward. The user can compare networks at different frequency bands (for example, the network in the 8-13 Hz alpha band versus the 20-40 Hz gamma band) using the frequency slider.

One difficulty of analyzing networks is interpreting the edges between sensors, particularly if the network is a weighted network and there are many sensors. There often is not enough room in a visualization to display all the edges without much overlap. To solve this problem, we use two strategies: layout and filtering.

The network layout toggle controls where nodes are positioned (and consequently the edges between nodes). Because the networks are dynamic and may change based on time or frequency, SpectraVis offers a topological layout—which models the nodes and edges as a physical system to limit the number of overlapping edges. There is also an anatomical layout which places the nodes according to the anatomical position defined in the JSON files.

Filtering edges and sensors allow the user to isolate subsets of the network — reducing the number of comparisons needed to be made in any one view. Using the edge filter dropdown, the user can isolate the edges between sensors that reside within the same brain area (e.g. only auditory cortex - auditory cortex sensor pairs) or between sensors that have non-matching brain areas (e.g. only auditory cortex - motor cortex sensor pairs).

Once the desired network view has been obtained, users can get further detail

by clicking on a pair of sensors. This loads a sensor view (1, dotted box) which depicts the relationship (spectra, coherences) between a selected pair of sensors (circled in black, network view, sensors 85 and 90) at all times and frequencies. Here, the edge between M1 (sensor 90) and S1 (sensor 85) represents a 10 Hz increase in speech coherence relative to silence. The increase co-occurs with higher frequency beta (15-25Hz) power suppression on the M1 sensor. The user can investigate the relationship between the sensor pair and the network view by mousing over a time-frequency bin in the sensor view, which correspondingly updates the network view to the time-frequency bin under the cursor.

RasterVis

RasterVis incorporates two canonical visualizations for single and multiunit spiking data — the raster plot and peri-event time histogram. The raster plot describes spike times for each trial relative to a trial event. The peri-event time histogram is a simple but useful summary of how, over a series of trials, the spike times are distributed across time bins relative to the time of a trial event. Because these two types of visualizations are familiar and represent the "raw" spiking data, they are an ideal building-block visualization. Furthermore, they can also be used to compare raw spiking data to model-generated data in order to check statistical modeling assumptions (posterior predictive checks) — so they can be useful in understanding how models reflect the data.

RasterVis uses interactivity and animation to supplement the raster plot and peri-event time histogram in order to make it easier for the user to accomplish typical tasks in the analysis of spiking data (See Figure 2 for a screenshot of the RasterVis interface).

For example, RasterVis allows for dynamic alignment of spike times and "on-the-fly" computation of peri-event histograms relative to experimental trial events (e.g. visual stimuli, timing of rewards, presentation of fixation points). Animated transitions emphasize how spike timing relative to trial event relates to another. This helps a user quickly compare the timing of individual spikes and aggregate spiking (via histogram) to different cues and conditions. Different levels of aggregation (Gaussian smoothing) for the histogram can be compared as well.

RasterVis also allows for dynamic sorting by experimental task factors. This

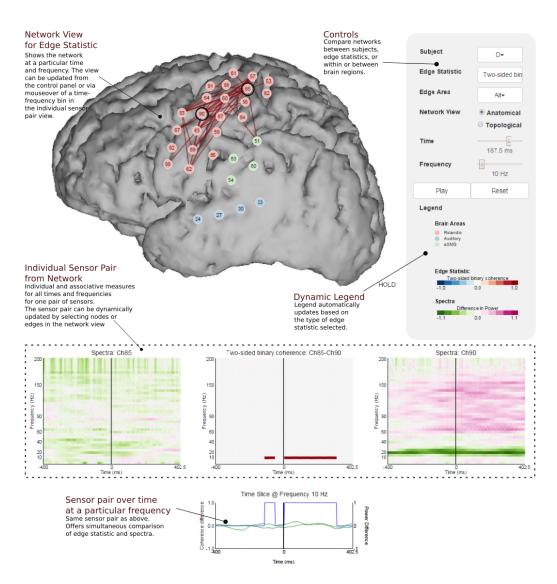


Figure 1: A static screenshot of the SpectraVis interface with the ECOG overt reading data.

feature creates on-demand plots for each condition within the task factor. For example, if a task factor is a visual cue with two experimental conditions — the color cue and the orientation cue — sorting by the visual cue creates two plots for the color condition and the orientation condition. This is essential for multidimensional analysis which may compare several different factors and conditions.

Finally, RasterVis allows users to find and select neurons by subject, recording session, or name. This is useful for fast comparison between neurons, linking to other visualizations (other visualizations can directly link to a specific neuron by name via a parameter passed via the URL), and general exploratory analysis of the dataset.

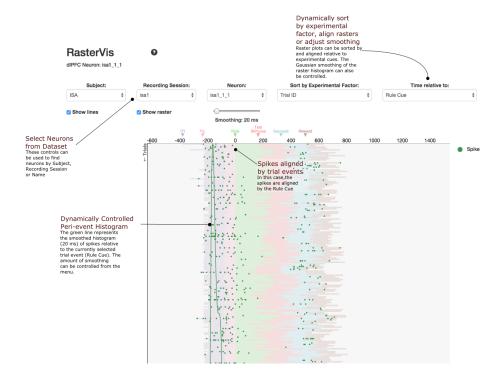


Figure 2: A static screenshot of the RasterVis interface.

GLMVis

A common analysis framework for characterizing the spiking response of neurons is the generalized linear model (GLM) (Fernandes et al., 2014; Harris

et al., 2003; Mayo et al., 2015; Park et al., 2014; Pillow et al., 2008). GLMs can simultaneously estimate effects of experimental conditions, spike history (refractory period, bursting), non-linear firing rate changes over time, and dependence on other neurons (Truccolo, 2004) — making them useful for analyzing a wide range of experiments.

One consequence of being able to estimate many covariates simultaneously is the relationship of the effects becomes hard to understand because of the number of dimensions — particularly if the covariates change over time and there are many neurons. Moreover, understanding the relationship between multiple covariates may be important to understanding *mixed selectivity* neurons (Rigotti et al., 2013). These neurons are sensitive to a combination of sensory, motor and cognitive processes, appear in higher-order association brain regions such as parietal and prefrontal cortex (Park et al., 2014; Rigotti et al., 2013), and may underlie the computation of complex behavior (Rigotti et al., 2010).

Therefore, we built GLMVis, an interactive visualization for GLMs, that: (1) shows the relationship between the multiple dimensions of the model fit over time, (2) allows filtering of neurons by effect size, brain area, and experimental subject, and (3) can be used to compare estimates from different models. To show the relationship between multiple dimensions, we use the parallel coordinate plots (Inselberg, 1985; Wegman, 1990) — a compact representation of multivariate data that links each dimension on parallel axes by a line.

Figure 3 shows a typical view of RasterVis. Each axis is a black horizontal line that corresponds to a dimension of the GLM. Non-parallel lines connect the dimensions and represent a single neuron. The intersection of the axes and non-parallel lines is the computed value of the neuron at that dimension. Dropdown menus allow the user to filter the neurons by their brain area or subject. The user can also filter by effect size by "brushing" along a desired axis — holding and dragging the mouse to select neurons in the range of values. Multiple axes can be selected in order to investigate the associations between values in different dimensions.

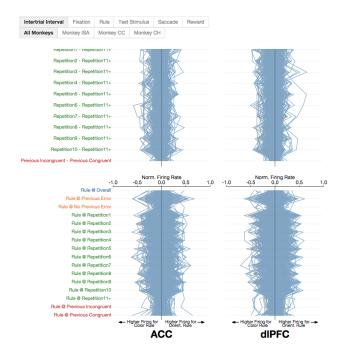


Figure 3: A static screenshot of the GLMVis interface.

Discussion

We developed an interactive visualization toolkit for investigating electrophysiological data. This toolkit is built to be

Importance of Visualization for Open Neuroscience

Sharing datasets is important for ensuring the reproducibility of results, metaanalyses, as benchmarks for computational models, and getting the greatest utility out of datasets (Poldrack and Gorgolewski, 2014) — particularly for datasets that are hard to collect such as those from non-human primates.

One challenge for the sharing of datasets is providing users with a way to find the datasets they want. Datasets provided in numerical form in non-standardized formats are hard to navigate and limit the usefulness of sharing the data. As electrophysiology dataset sharing becomes more common, it will be important to have tools to do preliminary investigations of these open datasets. Online interactive visualization tools such as ours may provide a

way for quick exploration of datasets online — enabling users to understand the datasets before performing more in-depth analyses. Indeed, the Allen Brain Institute — which shares massive neuroscience datasets online — makes extensive use of online visualizations to enable users to find the appropriate datasets. Because our tools encompass many common types of analysis for electrophysiological data, we hope our tools and future extensions can be used in a similar manner.

Future Directions

References

Anscombe, F. J. (1973). Graphs in statistical analysis. The American Statistician 27, 17–21.

Buffalo, E. A., Fries, P., Landman, R., Buschman, T. J., and Desimone, R. (2011). Laminar differences in gamma and alpha coherence in the ventral stream. *PNAS* 108, 11262–11267. doi:10.1073/pnas.1011284108.

Buschman, T., Denovellis, E., Diogo, C., Bullock, D., and Miller, E. (2012). Synchronous Oscillatory Neural Ensembles for Rules in the Prefrontal Cortex. *Neuron* 76, 838–846. doi:10.1016/j.neuron.2012.09.029.

Einevoll, G. T., Franke, F., Hagen, E., Pouzat, C., and Harris, K. D. (2012). Towards reliable spike-train recordings from thousands of neurons with multielectrodes. *Current Opinion in Neurobiology* 22, 11–17. doi:10.1016/j.conb.2011.10.001.

Fernandes, H. L., Stevenson, I. H., Phillips, A. N., Segraves, M. A., and Kording, K. P. (2014). Saliency and Saccade Encoding in the Frontal Eye Field During Natural Scene Search. *Cerebral Cortex* 24, 3232–3245. doi:10.1093/cercor/bht179.

Freeman, J., Vladimirov, N., Kawashima, T., Mu, Y., Sofroniew, N. J., Bennett, D. V., et al. (2014). Mapping brain activity at scale with cluster computing. *Nature Methods* 11, 941–950. doi:10.1038/nmeth.3041.

Fries, P. (2005). A mechanism for cognitive dynamics: neuronal communication through neuronal coherence. *Trends in Cognitive Sciences* 9, 474–480.

- doi:10.1016/j.tics.2005.08.011.
- Gelman, A. (2004). Exploratory Data Analysis for Complex Models. *Journal of Computational and Graphical Statistics* 13, 755–779. doi:10.1198/106186004X11435.
- Gregoriou, G. G., Gotts, S. J., Zhou, H., and Desimone, R. (2009). High-Frequency, Long-Range Coupling Between Prefrontal and Visual Cortex During Attention. *Science* 324, 1207–1210. doi:10.1126/science.1171402.
- Harris, K. D., Csicsvari, J., Hirase, H., Dragoi, G., and Buzsáki, G. (2003). Organization of cell assemblies in the hippocampus. *Nature* 424, 552–556.
- Huth, A., Nishimoto, S., Vu, A., and Gallant, J. (2012). A Continuous Semantic Space Describes the Representation of Thousands of Object and Action Categories across the Human Brain. *Neuron* 76, 1210–1224. doi:10.1016/j.neuron.2012.10.014.
- Inselberg, A. (1985). The plane with parallel coordinates. *The Visual Computer* 1, 69–91. Available at: http://link.springer.com/article/10.1007/BF01898350 [Accessed January 25, 2016].
- Liu, Z., and Heer, J. (2014). The effects of interactive latency on exploratory visual analysis. *Visualization and Computer Graphics, IEEE Transactions on* 20, 2122–2131. Available at: http://ieeexplore.ieee.org/xpls/abs_all.jsp?arnumber=6876022 [Accessed June 29, 2015].
- Mayo, J. P., DiTomasso, A. R., Sommer, M. A., and Smith, M. A. (2015). Dynamics of visual receptive fields in the macaque frontal eye field. *Journal of Neurophysiology* 114, 3201–3210. doi:10.1152/jn.00746.2015.
- Miller, E. K., and Wilson, M. A. (2008). All My Circuits: Using Multiple Electrodes to Understand Functioning Neural Networks. *Neuron* 60, 483–488. doi:10.1016/j.neuron.2008.10.033.
- Park, I. M., Meister, M. L. R., Huk, A. C., and Pillow, J. W. (2014). Encoding and decoding in parietal cortex during sensorimotor decision-making. *Nature Neuroscience* 17, 1395–1403. doi:10.1038/nn.3800.
- Pillow, J. W., Shlens, J., Paninski, L., Sher, A., Litke, A. M., Chichilnisky, E. J., et al. (2008). Spatio-temporal correlations and visual signalling in a com-

plete neuronal population. Nature 454, 995–999. doi:10.1038/nature07140.

Poldrack, R. A., and Gorgolewski, K. J. (2014). Making big data open: data sharing in neuroimaging. *Nature Neuroscience* 17, 1510–1517. doi:10.1038/nn.3818.

Rigotti, M., Barak, O., Warden, M. R., Wang, X.-J., Daw, N. D., Miller, E. K., et al. (2013). The importance of mixed selectivity in complex cognitive tasks. *Nature* advance online publication. doi:10.1038/nature12160.

Rigotti, M., Rubin, D. B. D., Wang, X.-J., and Fusi, S. (2010). Internal representation of task rules by recurrent dynamics: the importance of the diversity of neural responses. *Frontiers in Computational Neuroscience* 4. doi:10.3389/fncom.2010.00024.

Siegel, M., Buschman, T. J., and Miller, E. K. (2015). Cortical information flow during flexible sensorimotor decisions. *Science* 348, 1352–1355. Available at: http://www.sciencemag.org/content/348/6241/1352.short [Accessed August 5, 2015].

Stevenson, I. H., and Kording, K. P. (2011). How advances in neural recording affect data analysis. *Nature Neuroscience* 14, 139–142. doi:10.1038/nn.2731.

Truccolo, W. (2004). A Point Process Framework for Relating Neural Spiking Activity to Spiking History, Neural Ensemble, and Extrinsic Covariate Effects. *Journal of Neurophysiology* 93, 1074–1089. doi:10.1152/jn.00697.2004.

Tukey, J. W. (1977). Exploratory data analysis.

Wegman, E. J. (1990). Hyperdimensional data analysis using parallel coordinates. *Journal of the American Statistical Association* 85, 664–675.